

# Light KK modes in Custodially Symmetric Randall-Sundrum

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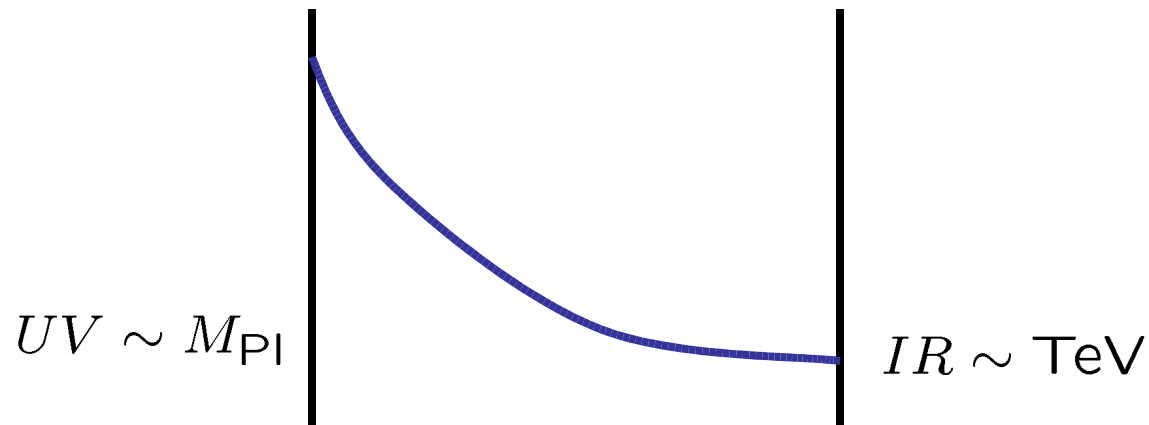
hep-ph/0607106, with M. Carena (FNAL), E. Pontón (Columbia) and C. Wagner (ANL)

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# Motivation

- Randall-Sundrum like models offer a nice solution to the gauge hierarchy problem



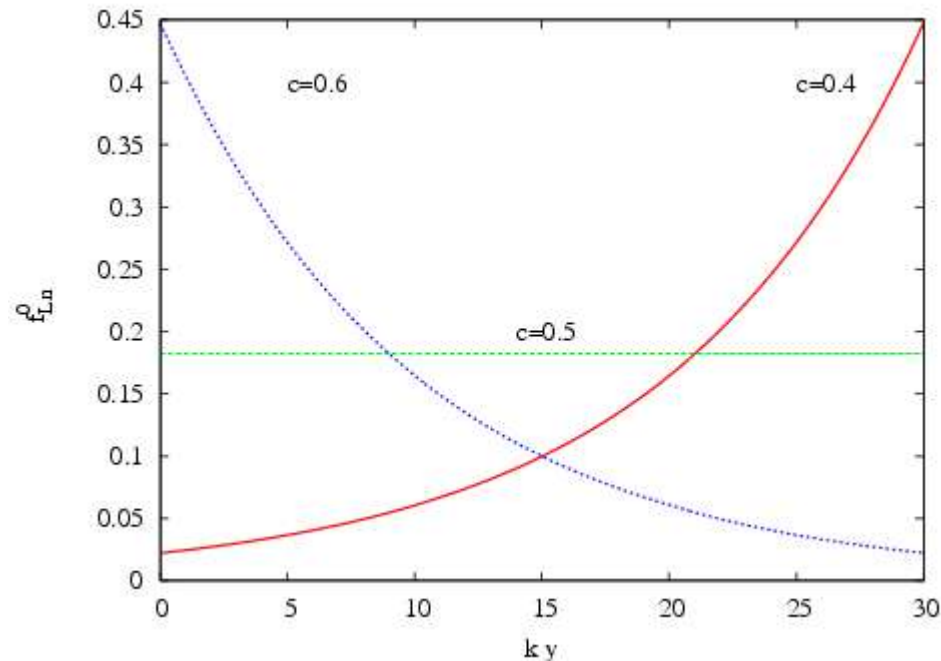
- Bulk fermions give a rationale for fermion mass hierarchies



# Fermions in Randall-Sundrum

- Bulk fermions can have a **mass term** that determines the **zero mode localization** properties (and the mass of the first KK modes)

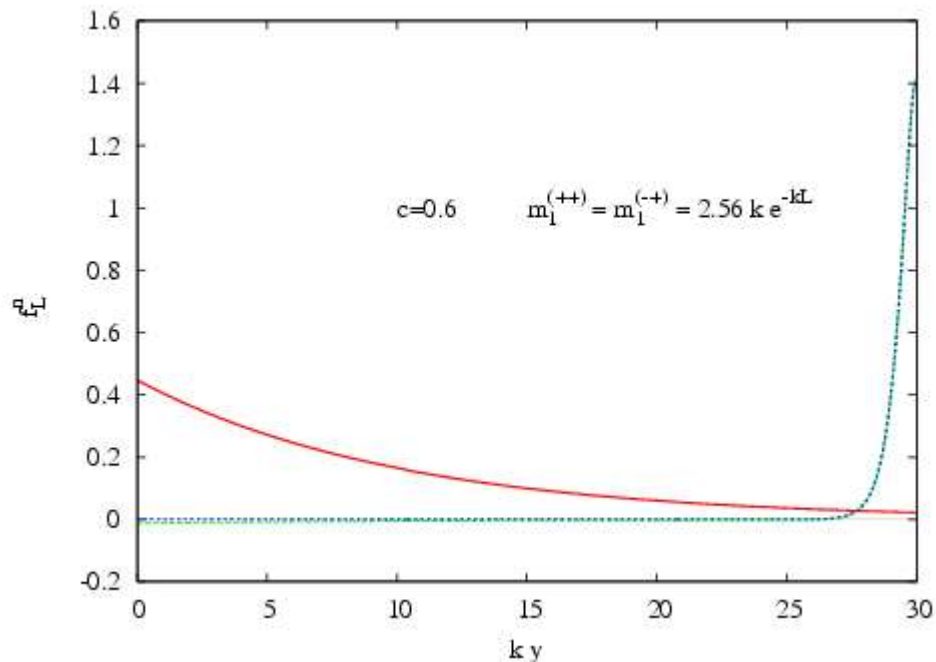
$$\mathcal{L}_m = c_\psi k \bar{\Psi} \Psi$$



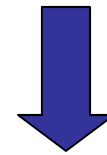


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- Non-trivial ( $- +$ ) boundary conditions can produce **ultralight** KK modes (depending on the bulk mass) Agashe, Servant JCAP (05)



$- +$  b.c.

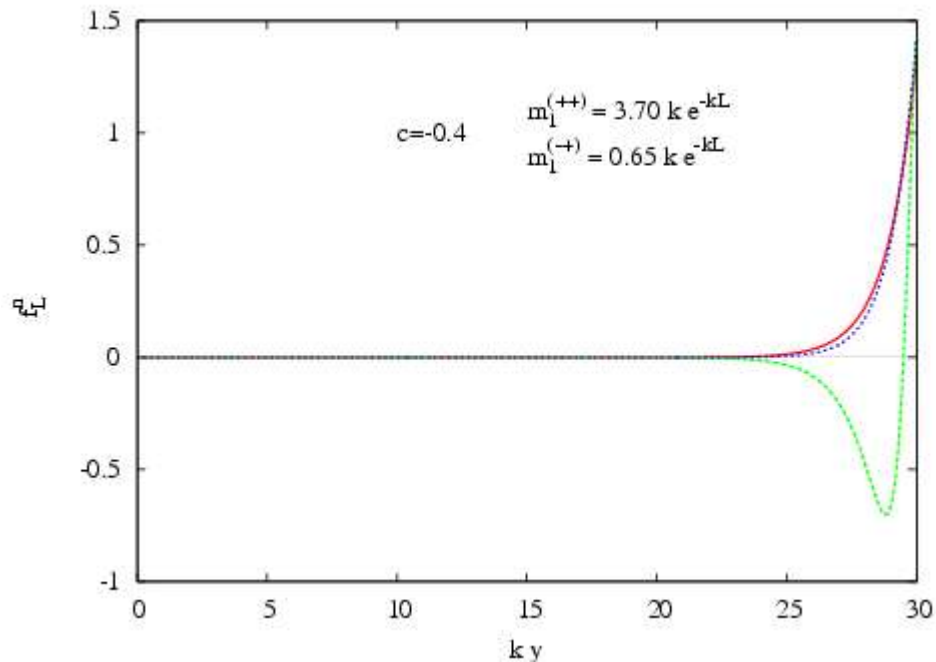


~~zero mode~~

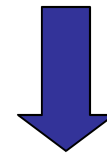


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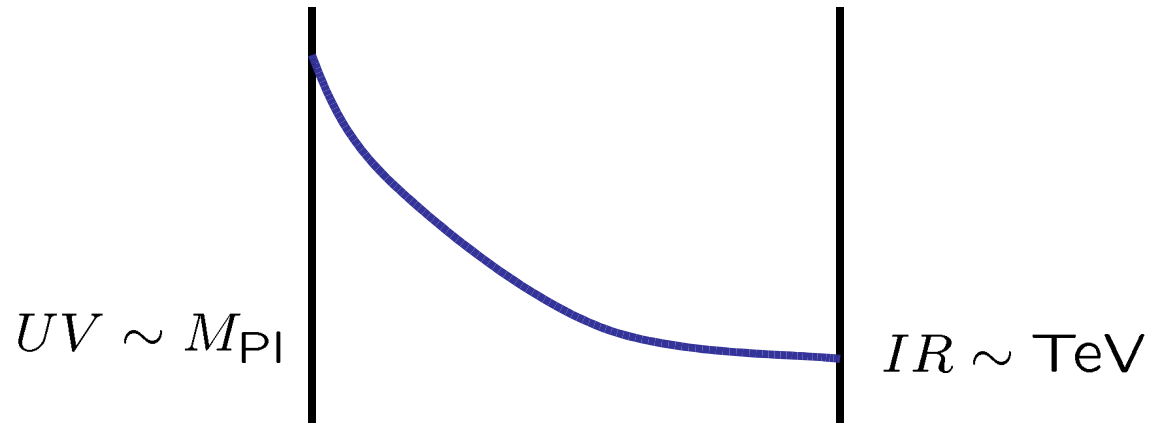


~~zero mode~~



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- Randall-Sundrum like models offer a nice solution to the gauge hierarchy problem



- Bulk fermions give a rationale for fermion mass hierarchies
- **Large contributions** to the  $T$  parameter and  $Zb\bar{b}$  force the KK modes to be **too heavy to be observable at the LHC** unless custodial symmetry is implemented





# Outline

- Custodially symmetric Randall-Sundrum models
- Low energy effects of KK modes
- Custodial Symmetry at work: tree-level protection of  $T$  and  $Zbb$
- One loop contribution to the oblique parameters
- Models of gauge-Higgs unification in warped space
- Realistic RS models with light KK modes: phenomenology
- Summary



# $SU(2)_L \times SU(2)_R$ Randall-Sundrum Models

- Bulk gauge symmetry is  $SU(2)_L \times SU(2)_R \times U(1)_X$  broken by boundary conditions on the UV brane

Agashe, Delgado, May,  
Sundrum JHEP (03)

$$SU(2)_R \times U(1)_X \rightarrow U(1)_Y$$

$$W_{L\mu}^{1,2,3} \sim (+, +), \quad B_\mu \sim (+, +),$$
$$W_{R\mu}^{1,2} \sim (-, +), \quad Z'_\mu \sim (-, +),$$

where

$$B_\mu = \frac{g_{5X} W_{R\mu}^3 + g_{5R} X_\mu}{\sqrt{g_{5R}^2 + g_{5X}^2}}, \quad Z'_\mu = \frac{g_{5R} W_{R\mu}^3 - g_{5X} X_\mu}{\sqrt{g_{5R}^2 + g_{5X}^2}},$$





# Low energy effects

- We can **integrate out the gauge KK modes** in terms of the 5D propagators, with the zero mode subtracted Carena, Delgado, Pontón, Tait, Wagner PRD(03)

$$\tilde{G}_{p=0}^{++}(y, y') = \frac{1}{4k(kL)} \left\{ \frac{1 - e^{2kL}}{kL} + e^{2ky_{<}}(1 - 2ky_{<}) + e^{2ky_{>}} [1 + 2k(L - y_{>})] \right\} ,$$

$$\tilde{G}_{p=0}^{-+}(y, y') = -\frac{1}{2k} [e^{2ky_{<}} - 1] .$$

- We will define **corrections** in terms of convolutions

$$\delta_{++}^2 = \frac{Lv^2}{2} \int_0^L dy dy' e^{-2ky} f_H(y)^2 \tilde{G}_{p=0}^{++}(y, y') e^{-2ky'} f_H(y')^2 .$$

$$G_{++}^\psi = \frac{v^2}{2} \int_0^L dy dy' |f_\psi^0(y)|^2 \tilde{G}_{p=0}^{++}(y, y') e^{-2ky'} f_H(y')^2 ,$$



# Low energy effects

➤ The SM gauge boson masses are

$$m_Z^2 = \frac{e^2 v^2}{2s^2 c^2} \left\{ 1 + \frac{e^2}{s^2 c^2} \left[ \delta_{++}^2 + \left( \frac{g_R^2}{g_L^2} c^2 - s^2 \right) \delta_{-+}^2 \right] + \dots \right\},$$

$$m_W^2 = \frac{e^2 v^2}{2s^2} \left\{ 1 + \frac{e^2}{s^2} \left[ \delta_{++}^2 + \frac{g_R^2}{g_L^2} \delta_{-+}^2 \right] + \dots \right\},$$

and their coupling to the SM fermions

$$J_Z^\mu = \bar{\psi}^0 \gamma^\mu (T_L^3 - s^2 Q) \psi^0 \left[ 1 + \frac{e^2}{s^2 c^2} \left( G_{++}^\psi - \frac{g_R^2/g_L^2 c^2 T_R^3 + s^2 T_L^3 - s^2 Q}{T_L^3 - s^2 Q} G_{-+}^\psi \right) \right]$$

$$J_+^\mu = \left\{ \bar{\psi}^0 \gamma^\mu T_L^+ \psi^0 \left[ 1 + \frac{e^2}{s^2} G_{++}^\psi \right] + \frac{g_R^2}{g_L^2} \frac{e^2}{s^2} \bar{\psi}^0 \gamma^\mu T_R^+ \psi^0 G_{-+}^\psi \right\}$$



# Low energy effects

- If the **light fermions** are all near the UV brane we can cast the most important corrections in terms of effective **oblique parameters**

Carena, Delgado, Pontón,  
Tait, Wagner PRD(03)

$$S_{\text{eff}} = 32\pi G_{++}^f,$$

$$T_{\text{eff}} = \frac{8\pi}{c^2} G_{++}^f - \frac{4\pi}{c^2} [\delta_{++}^2 - \delta_{-+}^2] + \frac{2\pi v^2}{s^2} G_{++}^{\mu\mu},$$

$$U_{\text{eff}} = -8\pi v^2 G_{++}^{\mu\mu}.$$

$G_{++}^{\mu\mu}$  encodes the effects of gauge KK modes on  **$\mu$  decay**. In practice these effects can be neglected.



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$$U = 0,$$

and the  $Z\bar{b}_L b_L$  anomalous coupling

$$\frac{\delta g_{b_L}}{g_{b_L}} = \frac{e^2}{s^2 c^2} \left[ G_{++}^{b_L} - \frac{c^2 T_R^3 g_R^2 / g_L^2 + s^2 T_L^3 - s^2 Q}{T_L^3 - s^2 Q} G_{-+}^{b_L} - G_{++}^f \right]$$



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- If **light fermions** are not near the UV brane, then there are extra corrections that can be **non-universal** and therefore **cannot be absorbed into oblique** effects (more on this latter)

# Custodial symmetry at work: T and Zbb

- The relevant EW observables are then the S and T oblique parameters:

$$S = 32\pi G_{++}^f \quad \text{Tend to cancel}$$

$$T = \frac{8\pi}{c^2} G_{++}^f - \frac{4\pi}{c^2} [\delta_{++}^2 - \delta_{-+}^2]$$

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and the  $Z\bar{b}_L b_L$  anomalous coupling

$$\frac{\delta g_{b_L}}{g_{b_L}} = \frac{e^2}{s^2 c^2} [G_{++}^{b_L} - 0.09 G_{-+}^{b_L} - G_{++}^f]$$

**Bad** cancellation

$$T_R^3(b_L) = 0$$

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$$\frac{\delta g_{b_L}}{g_{b_L}} = \frac{e^2}{s^2 c^2} [G_{++}^{b_L} - G_{-+}^{b_L} - G_{++}^f]$$

Good cancellation

$$T_R^3(b_L) = T_L^3(b_L) \\ (g_R = g_L)$$

$SU(2)_L \times SU(2)_R \times P_{LR}$  can protect  $Z\bar{b}\bar{b}$

Agashe, Contino, Da Rold,  
Pomarol ph/0605341



# Quantum Numbers

$$T_R^3(b_L) = 0$$

$$\begin{pmatrix} t_L(+, +) \\ b_L(+, +) \end{pmatrix} \sim (2, 1) \quad \begin{pmatrix} t_R(+, +) \\ b'_R(-, +) \end{pmatrix}, \begin{pmatrix} t'_R(-, +) \\ b_R(+, +) \end{pmatrix} \sim (1, 2)$$

$$\begin{aligned} T_R^3(b_L) &= T_L^3(b_L) \\ (g_R &= g_L) \end{aligned}$$

$$\begin{pmatrix} \chi_L^u(-+) & t_L(+, +) \\ \chi_L^d(-+) & b_L(+, +) \end{pmatrix} \sim (2, 2)$$

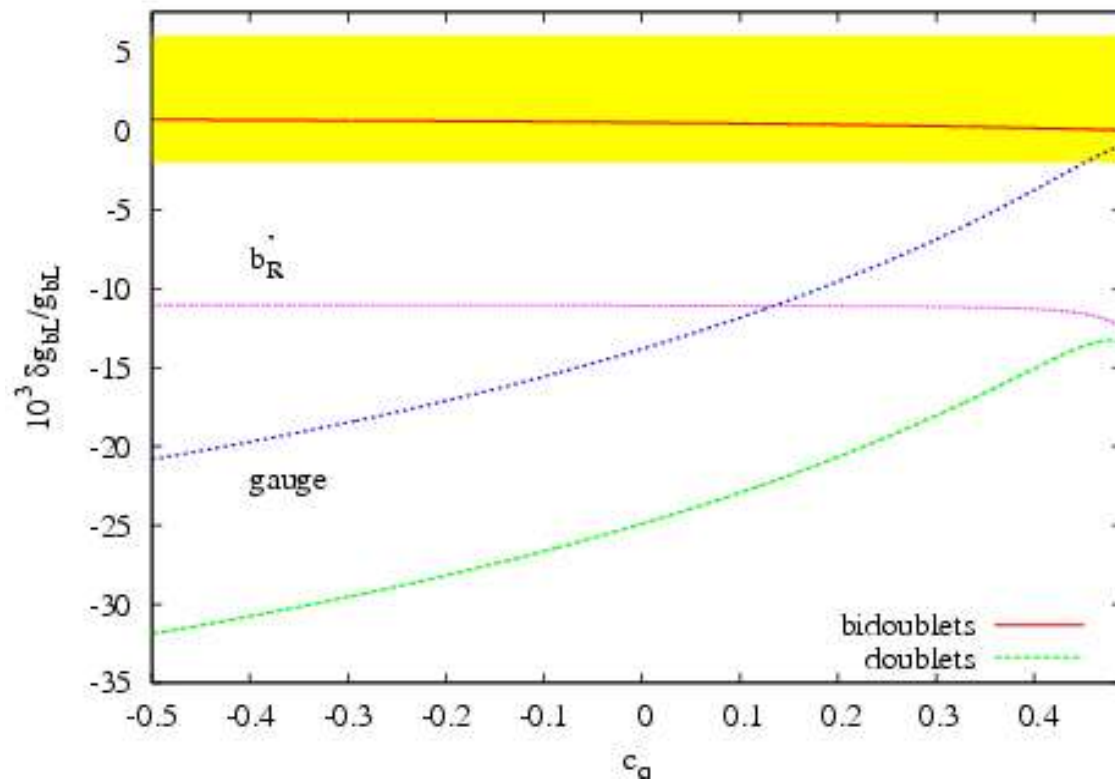
$$t_R(+, +) \sim (1, 1)$$

or

$$\begin{pmatrix} \psi'_R(-, +) \\ t'_R(-, +) \\ b'_R(-, +) \end{pmatrix} \sim (3, 1) \oplus \begin{pmatrix} \psi''_R(-, +) \\ t_R(+, +) \\ b''_R(-, +) \end{pmatrix} \sim (1, 3)$$



$$M_{KK} \approx 3.75 \text{ TeV}$$



Custodial protection of  $Zb\bar{b}$  (and therefore **bidoublets**) is crucial to have light KK excitations



# Bidoublets and oblique corrections

- The new states give a one loop contribution to the  $T$  parameter that is **finite** due to the **non-local** breaking of EW and  $SU(2)_R$
- Typical results for  $T$  (very sensitive to the parameters of the model and not necessarily small):

- **Bidoublets** contribute **negatively**

$$\Delta T = -T_{\text{top}} \frac{4m_{\chi^{d,t}}^2}{M_q^2} \left[ 2(\eta_m + \eta_\lambda) \ln \frac{M_q^2}{m_{\text{top}}^2} - 5\eta_m - 3\eta_\lambda + \dots \right]$$

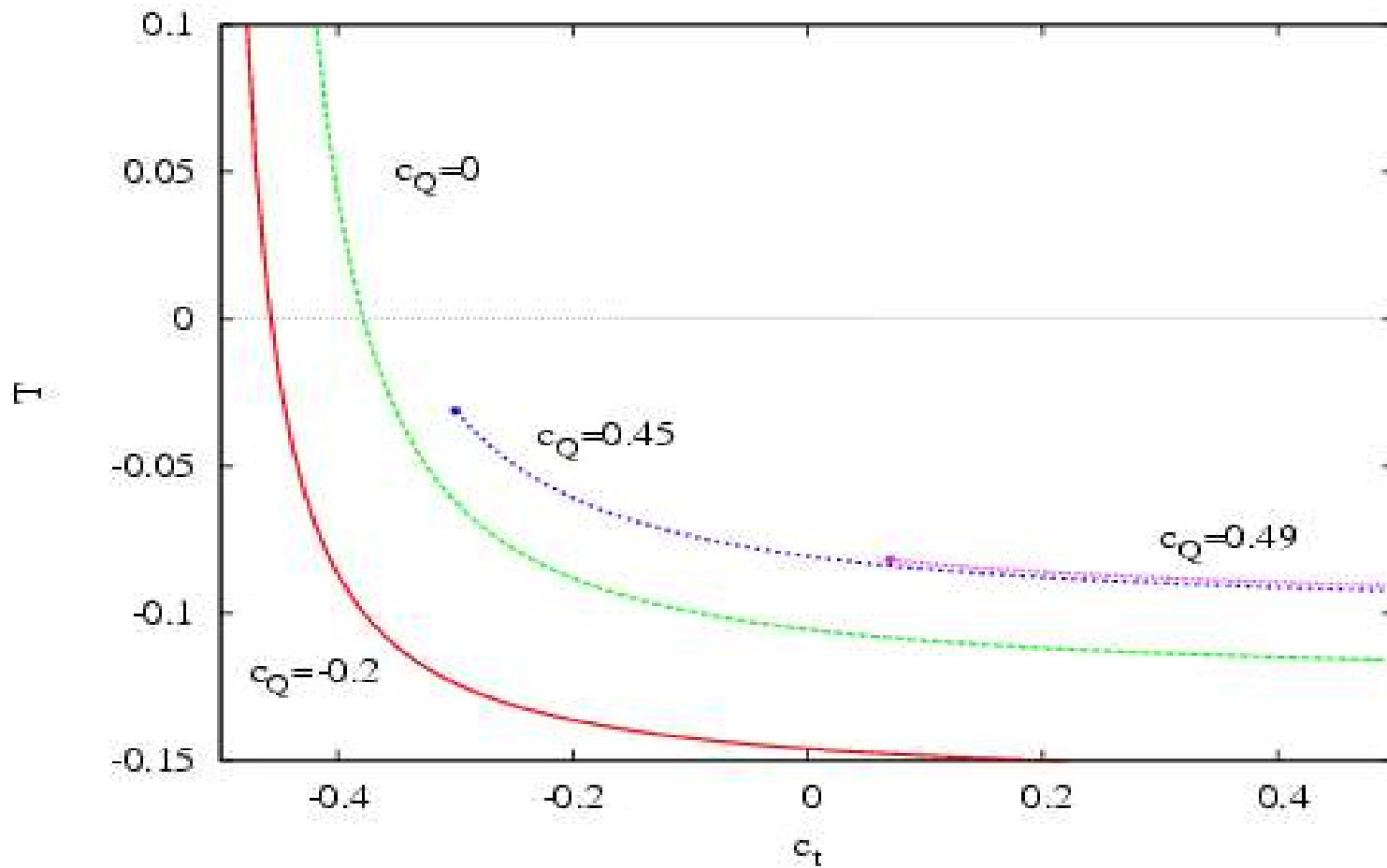
- **Singlets and triplets** contribute **positively**

$$\Delta T = T_{\text{top}} \frac{2m_{q_0,t}^2}{M_t^2} \left( \ln \frac{M_t^2}{m_{\text{top}}^2} - 1 + \frac{m_{q_0,t}^2}{2m_{\text{top}}^2} \right),$$

- $S$  is small and quite insensitive to the parameters of the model.



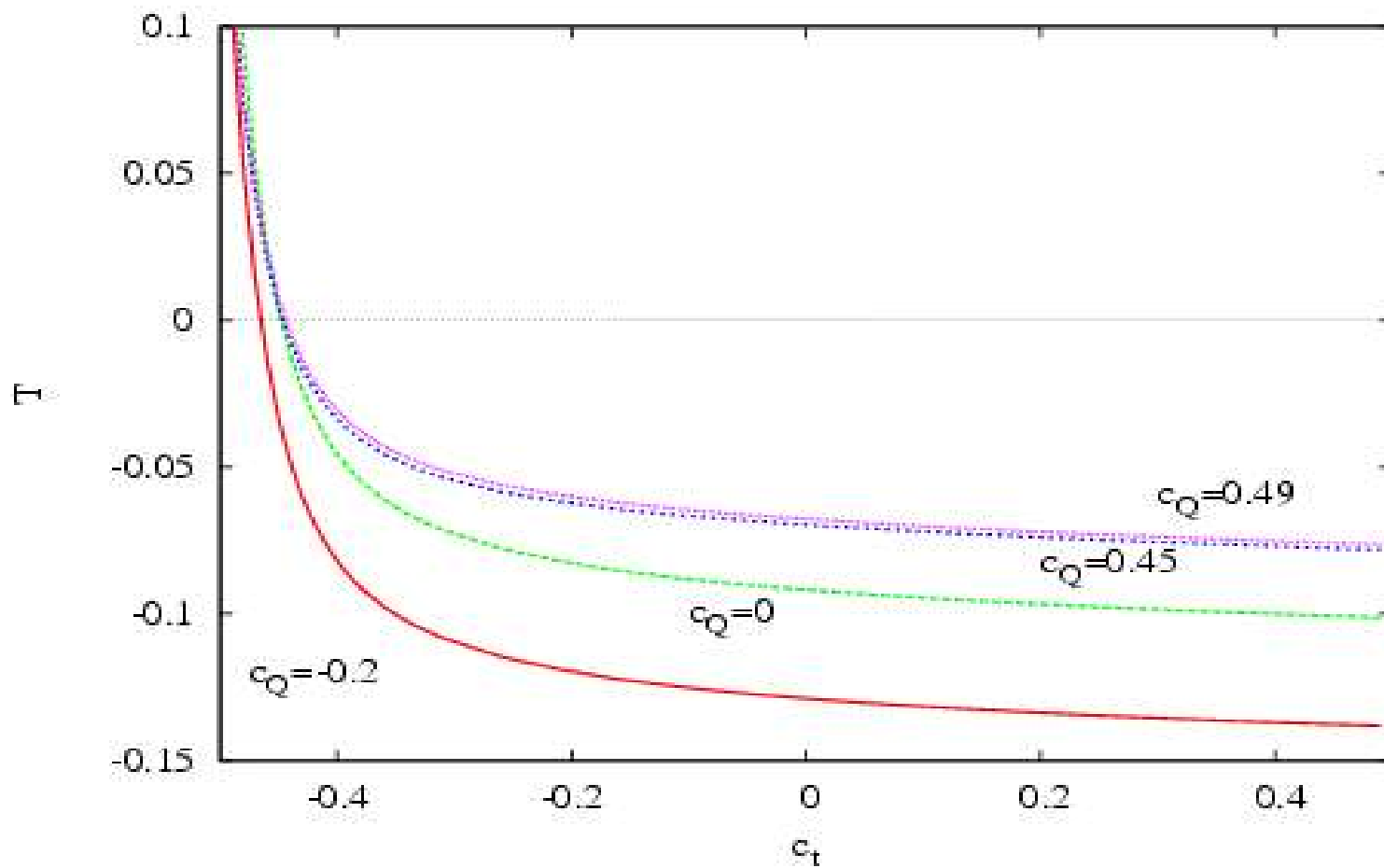
Brane Higgs  $t_R \sim (1, 1)$





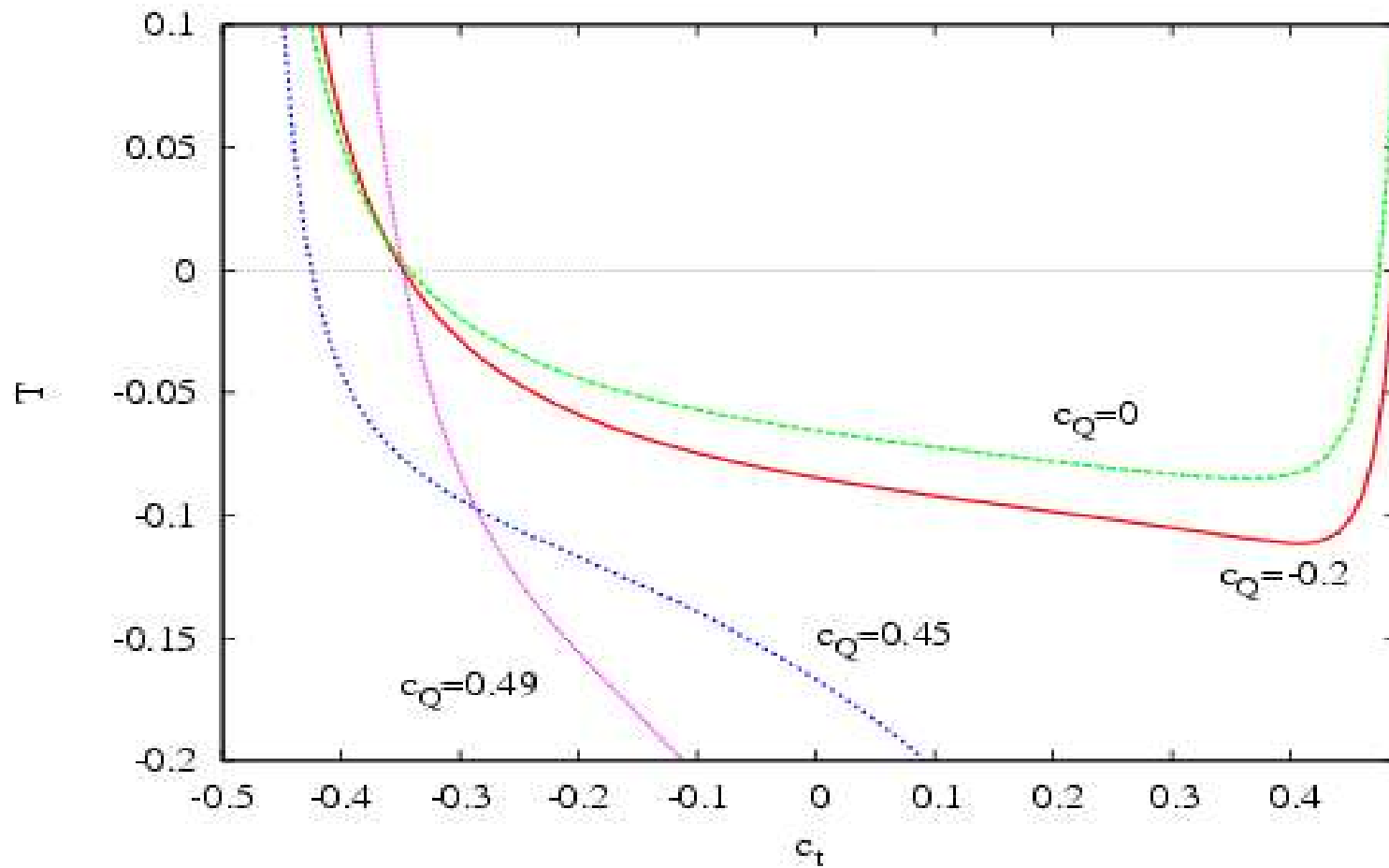


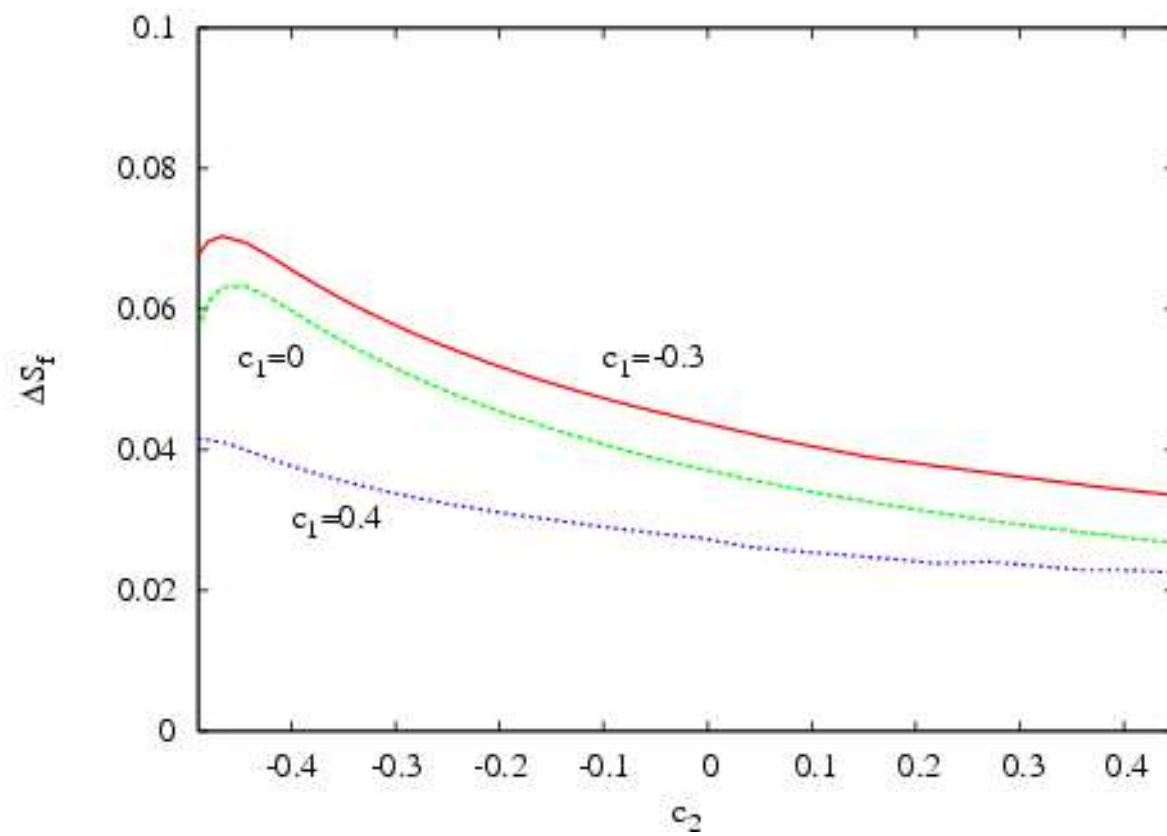
Bulk Higgs  $t_R \sim (1, 1)$





Bulk Higgs  $t_R \sim (1, 3)$

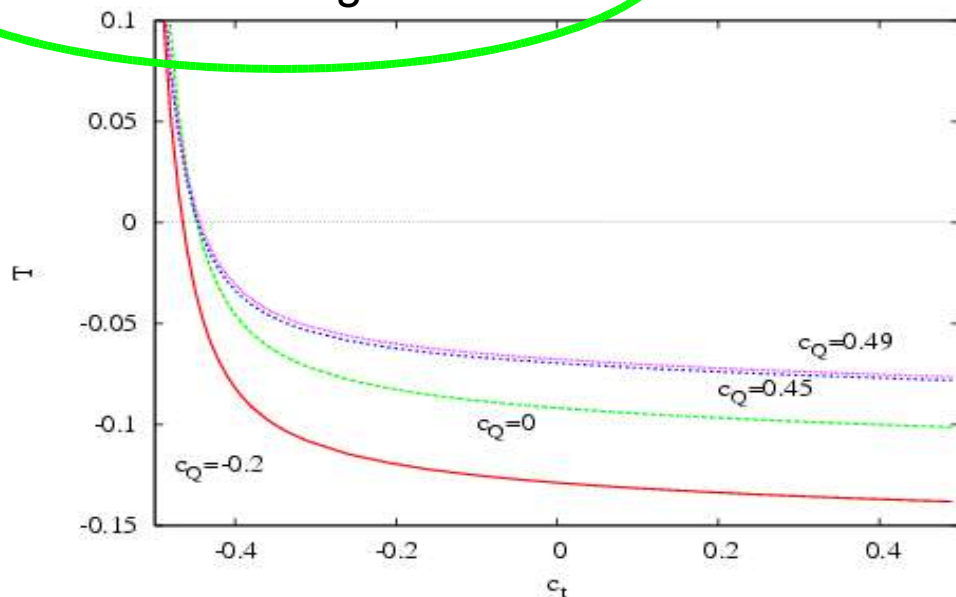






- There are regions of parameter space with a well-defined value of  $T$ :
  - Negative for  $t_R$  close to the IR brane, positive for  $t_R$  far from the IR brane (compatible with  $m_t$ )

$t_R^{(1)}$  light,  $\lambda^5$  large  $\Rightarrow$  large effect from singlets



$t_R^{(1)}$  heavy,  $\lambda^5$  small  $\Rightarrow$  small effect from singlets



# Gauge-Higgs unification

Agashe, Contino, Pomarol NPB(05)

- We can **enlarge the bulk symmetry** to  $SO(5)$  broken by boundary conditions to  $SU(2)_L \times SU(2)_R$  on the IR brane and to the SM on the UV brane.
- The Higgs can arise then as the  $A_5$  along the broken direction  $SO(5)/SU(2)_L \times SU(2)_R$

$$A_5^{\hat{a}}(x, y) = a_H e^{2ky} A_5^{\hat{a}(0)}(x) + \dots$$

- 5D gauge symmetry ensures that the **Higgs potential is finite**  $\Rightarrow$   
Little hierarchy
- Yukawa couplings come from gauge couplings. **Non-trivial flavor can be obtained by mixing at the boundary.**



# Gauge-Higgs unification

- Fermions must come in **full representations** of  $SO(5)$

$$5 \sim (2, 2) \oplus 1, \quad 10 \sim (2, 2) \oplus (3, 1) \oplus (1, 3)$$

- We focus on the simplest realistic choice of boundary conditions and quantum numbers

$$\xi_1 \sim Q_{1L} = \left( \begin{array}{cc} \chi_{1L}^u(-, +) & q_L^u(+, +) \\ \chi_{1L}^d(-, +) & q_L^d(+, +) \end{array} \right) \oplus u'_L(-, +)$$

$$\xi_2 \sim Q_{2R} = \left( \begin{array}{cc} \chi_{2R}^u(+, -) & q_R^u(+, -) \\ \chi_{2R}^d(+, -) & q_R^d(+, -) \end{array} \right) \oplus u_R(+, +)$$

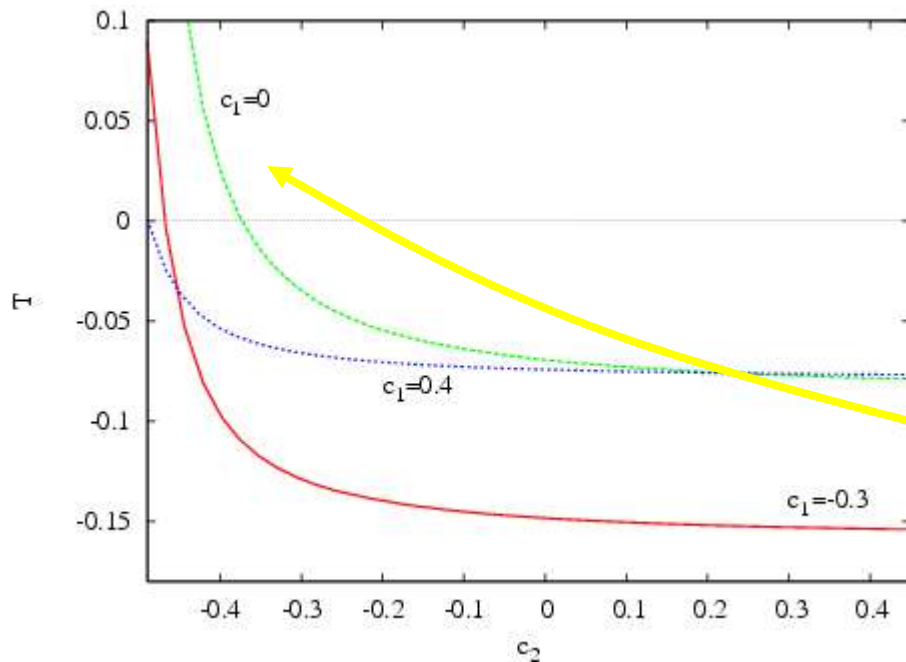
- With mixing

$$\mathcal{L}_m = \delta(y - L)[\widehat{M}_u \bar{u}'_L u_R + \text{h.c.}]$$



# Gauge-Higgs unification

- Localized masses can make the light KK modes even **lighter**
  - Enhances the positive contribution of the singlet
  - Would enhance the negative contribution of the bidoublet
- The final result is similar to models with fundamental Higgs



$t_R$  far from the IR brane forces  $\widehat{M}_u$  to be larger (to generate  $m_t$ ) and that makes  $t_R^{(1)}$  lighter and therefore its positive contribution more important



➤ A realistic example:

- For  $c_2 \sim -0.5$  we can get any value of  $T$ , thus the **bound comes from the  $S$  parameter**.
- For  $m_H = 115$  GeV, the EW fit requires, at the two sigma level,

$$S \lesssim 0.3$$

- This imposes a bound  $\tilde{k} \equiv ke^{-kL} \gtrsim 1.2$  TeV  $\Rightarrow M_{KK} \gtrsim 3$  TeV

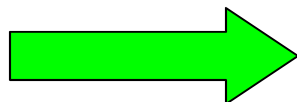
➤ These values can be obtained with the following parameters

$$\tilde{k} = 1.2 \text{ TeV}$$

$$c_1 = 0$$

$$c_2 = -0.468$$

$$\hat{M}_u = 2.91$$



$$S \approx T \approx 0.3$$

$$\delta g_{b_L}/g_{b_L} \approx 0.8 \times 10^{-3}$$

$$U \approx 0.005$$



# Phenomenology

➤ Fermionic spectrum:

- Three light quarks (with charge 5/3, 2/3 and -1/3) that **do not mix**

$$M_{\chi_2^u} = M_{q_1} = M_{q'd} \approx 470 \text{ GeV} .$$

- Two **charge 2/3 quarks** that **mix (strongly) with the top**

$$M_{q_2} \approx 495 \text{ GeV} , \quad M_{u_2} \approx 742 \text{ GeV} .$$

- Heavier modes with masses  $\gtrsim 1.9 \text{ TeV}$

➤ **Top** mixing with vector-like quarks induces **anomalous couplings**

$$\frac{\delta g_{Ztt}^L}{g_{Ztt}^L} \sim -0.2 - 0.04 \quad \frac{\delta g_{Wtb}^L}{g_{Wtb}^L} \sim -0.07 - 0.015$$



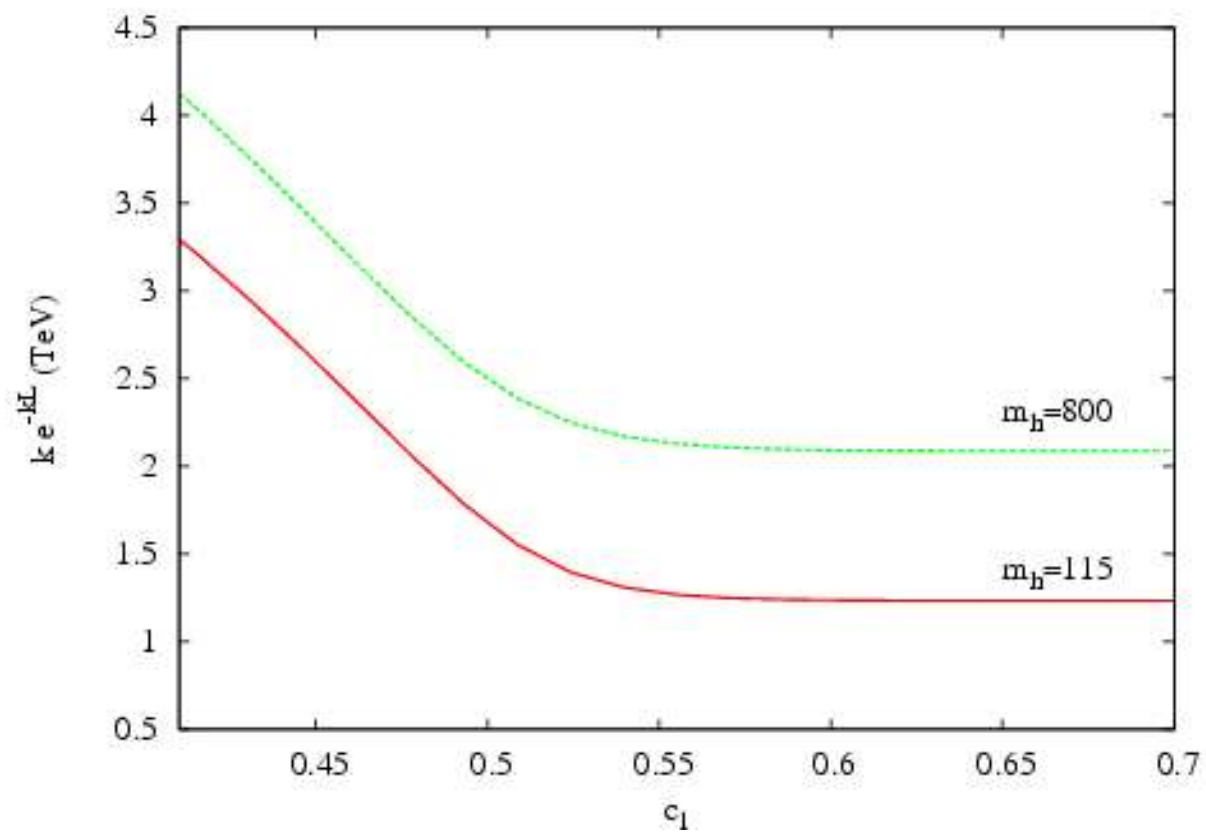
# Moving the light generations

- The S,T analysis we have performed is valid when the **light quarks and leptons are near the UV brane**
- The couplings to the  $Z$  become **non-universal** if they get closer to the IR

$$\frac{\delta g_{fL}}{g_{fL}} = \frac{e^2}{s^2 c^2} \left[ G_{++}^{fL} - \frac{c^2 T_R^3 + s^2 T_L^3 - s^2 Q}{T_L^3 - s^2 Q} G_{-+}^{fL} \right]$$

- A **global fit** is necessary in that case

Han, Skiba PRD(05); Han PRD(06); Cacciapaglia, Csaki, Marandella, Strumia ph/0604111





# Conclusions

- Randall-Sundrum models with custodial symmetry can have small tree-level corrections to the T parameter and the  $Zb\bar{b}$  coupling.
- One loop contributions to the T parameter are finite (therefore calculable) and generically large:
  - Bidoublets give a negative contribution
  - Singlets and triplets give a positive contribution
- Realistic models with  $M_{KK}^{\text{gauge}} \sim 3 \text{ TeV}$  can be constructed and typically have light quarks that mix strongly with the top.
- Exciting phenomenology at the LHC
  - Light new fermions and gauge bosons
  - Anomalous top couplings