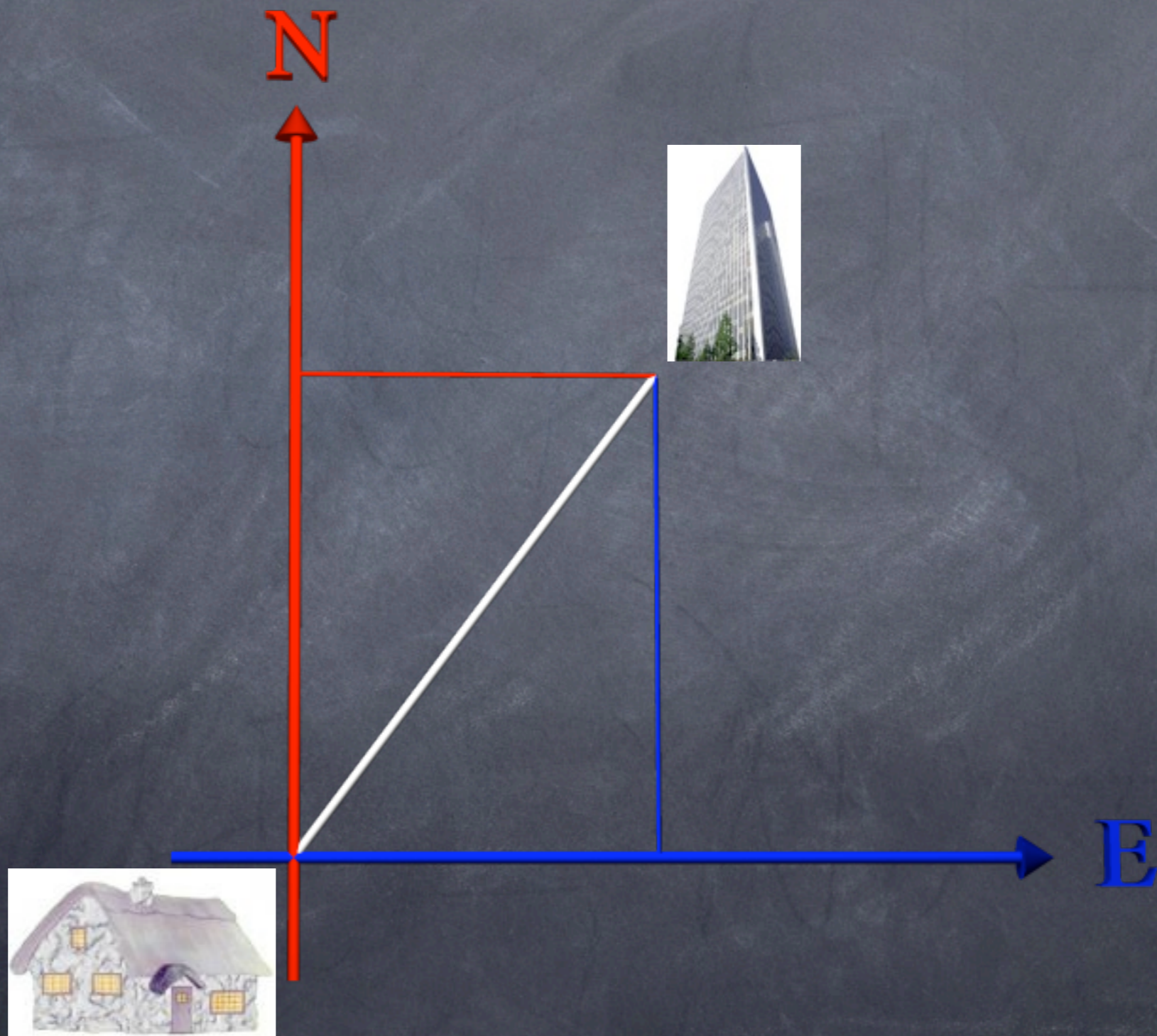
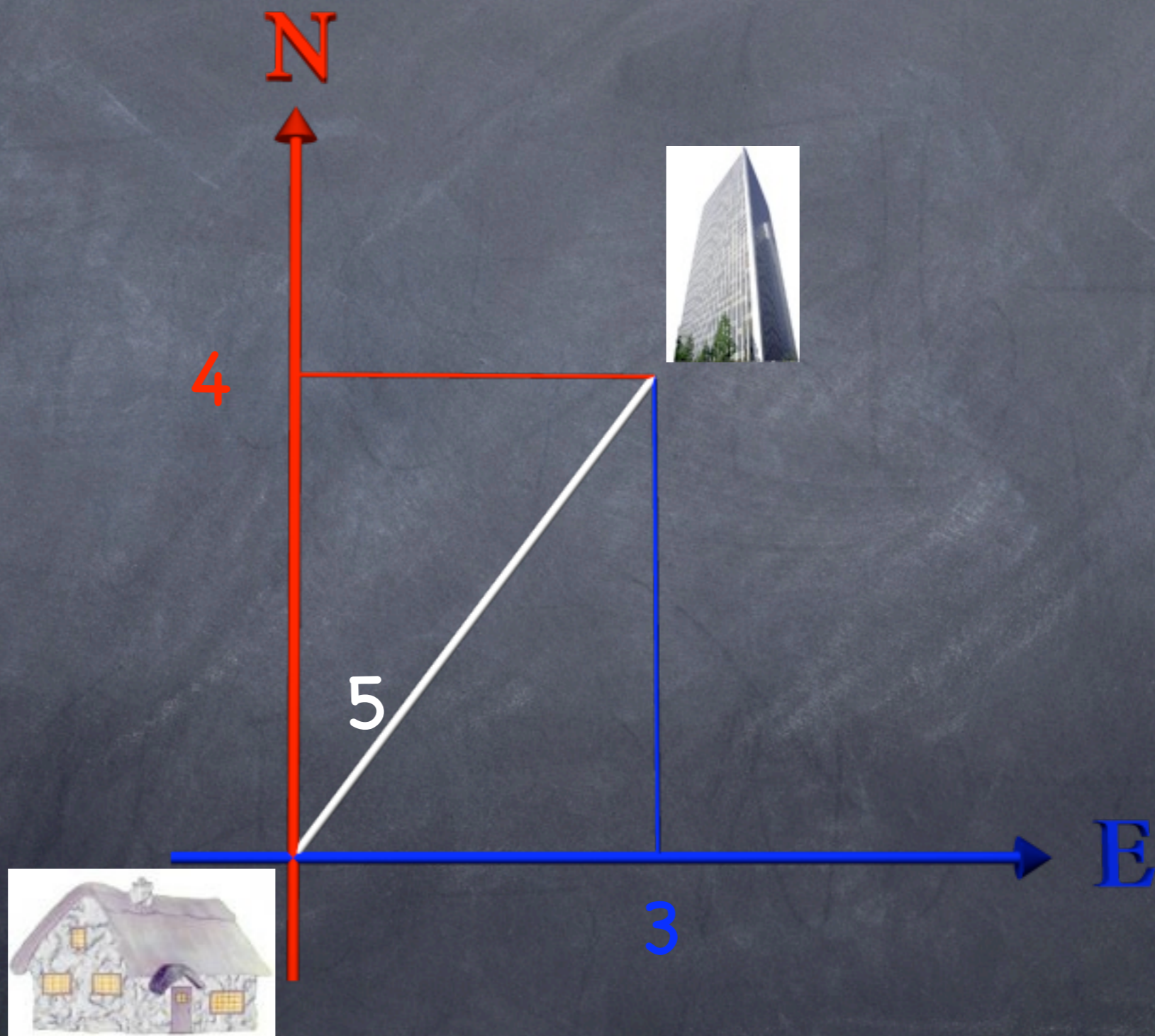


Chapter 9: Symmetry

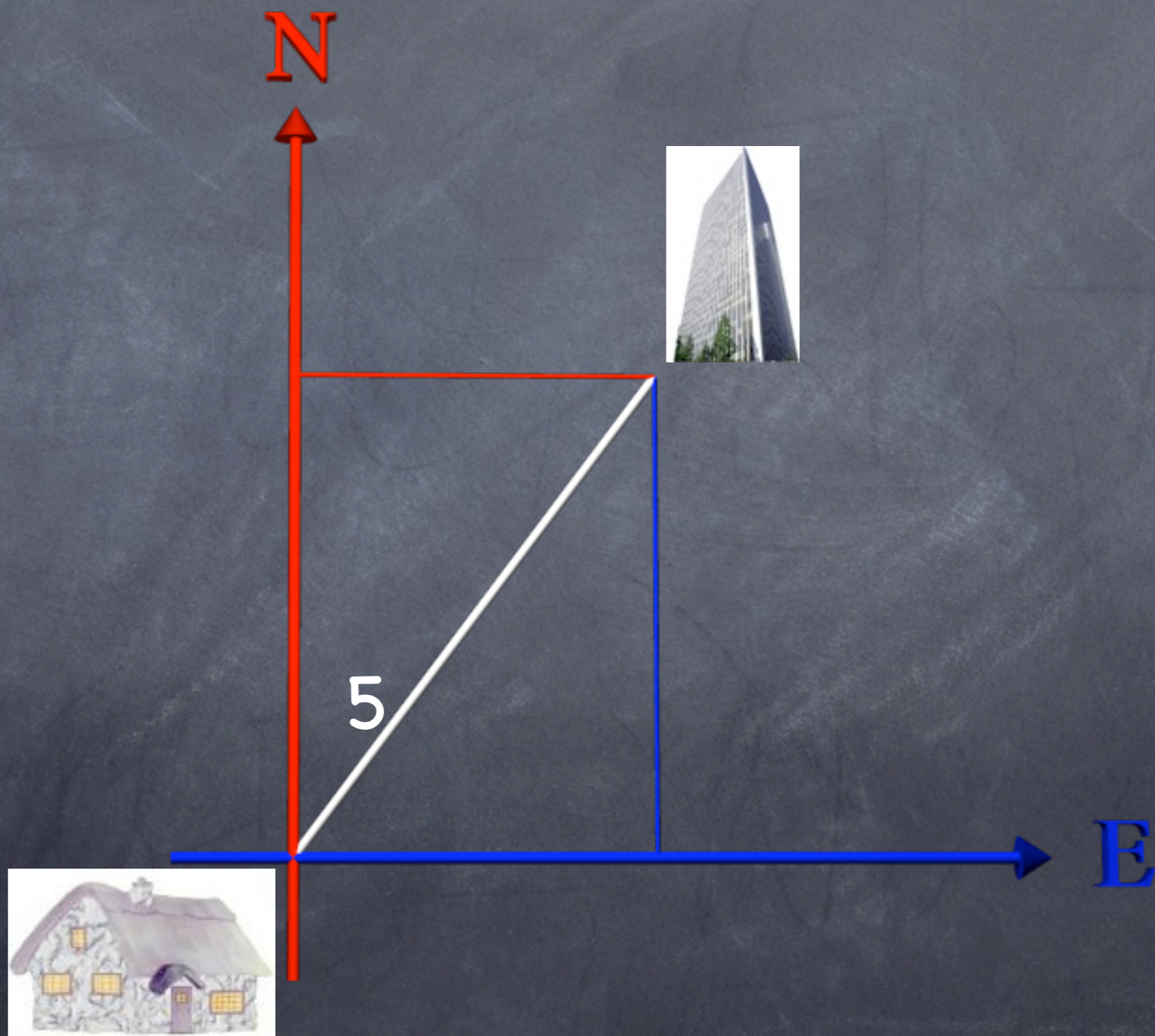
Rotations



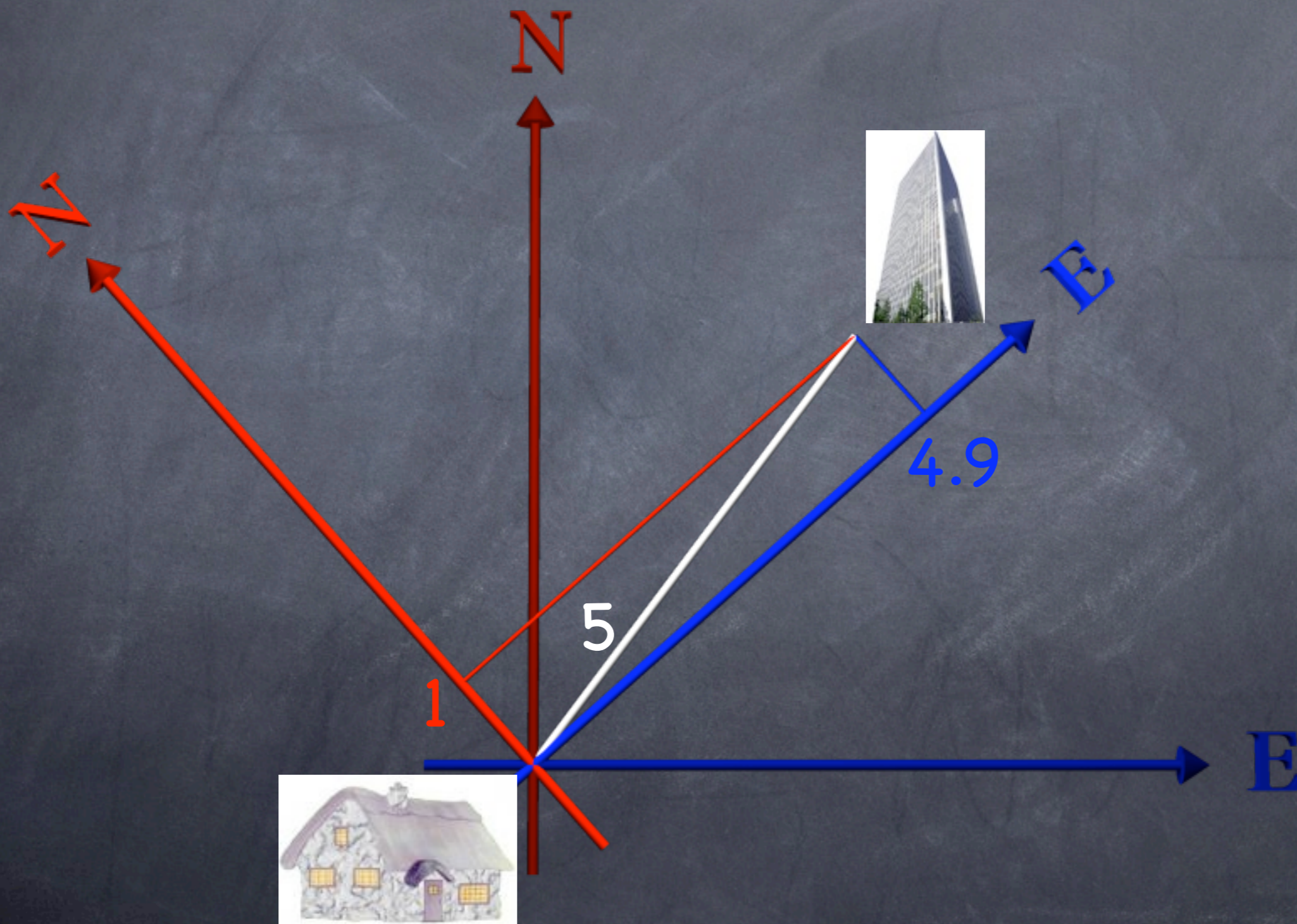
Rotations



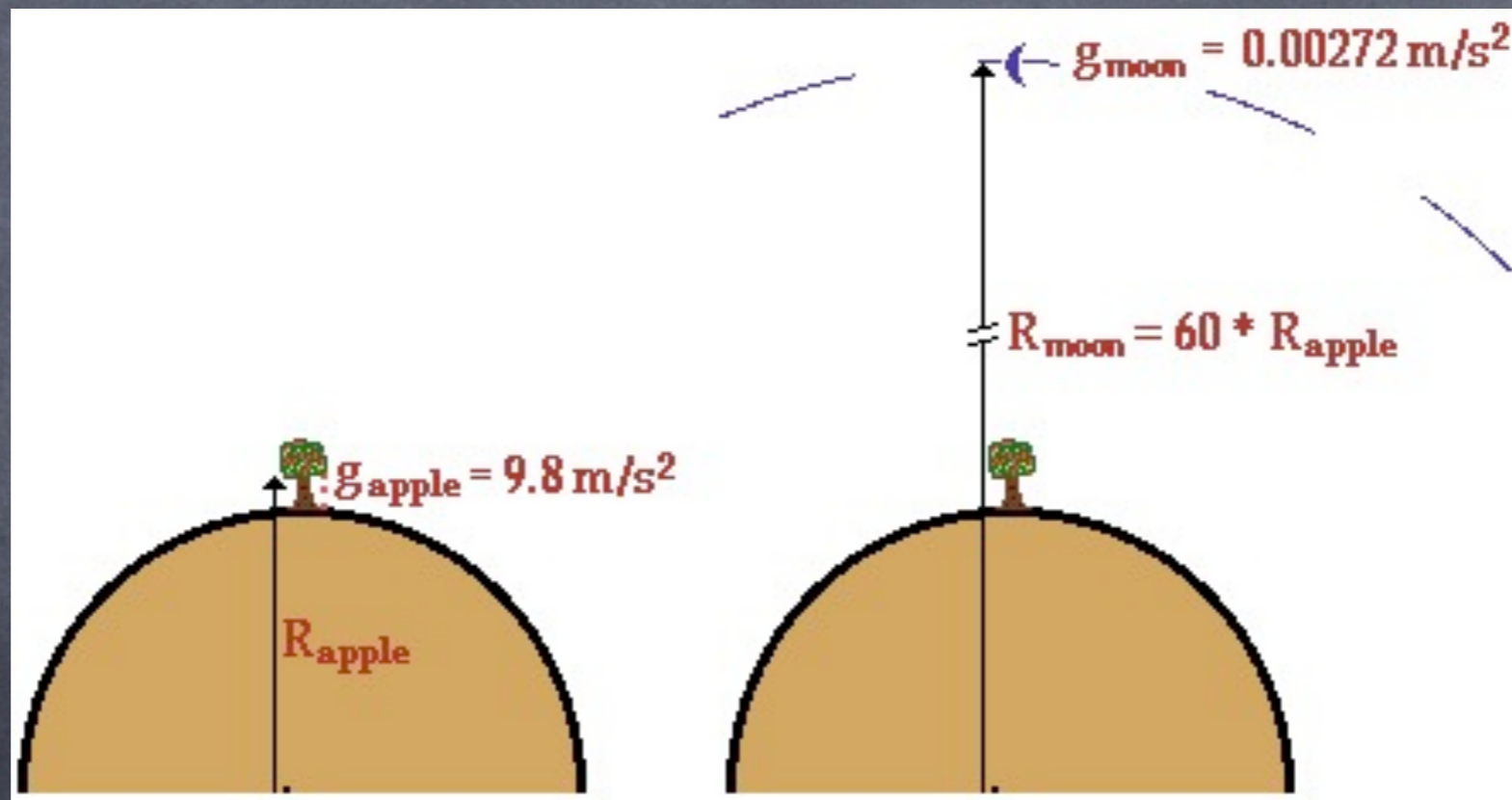
Rotations



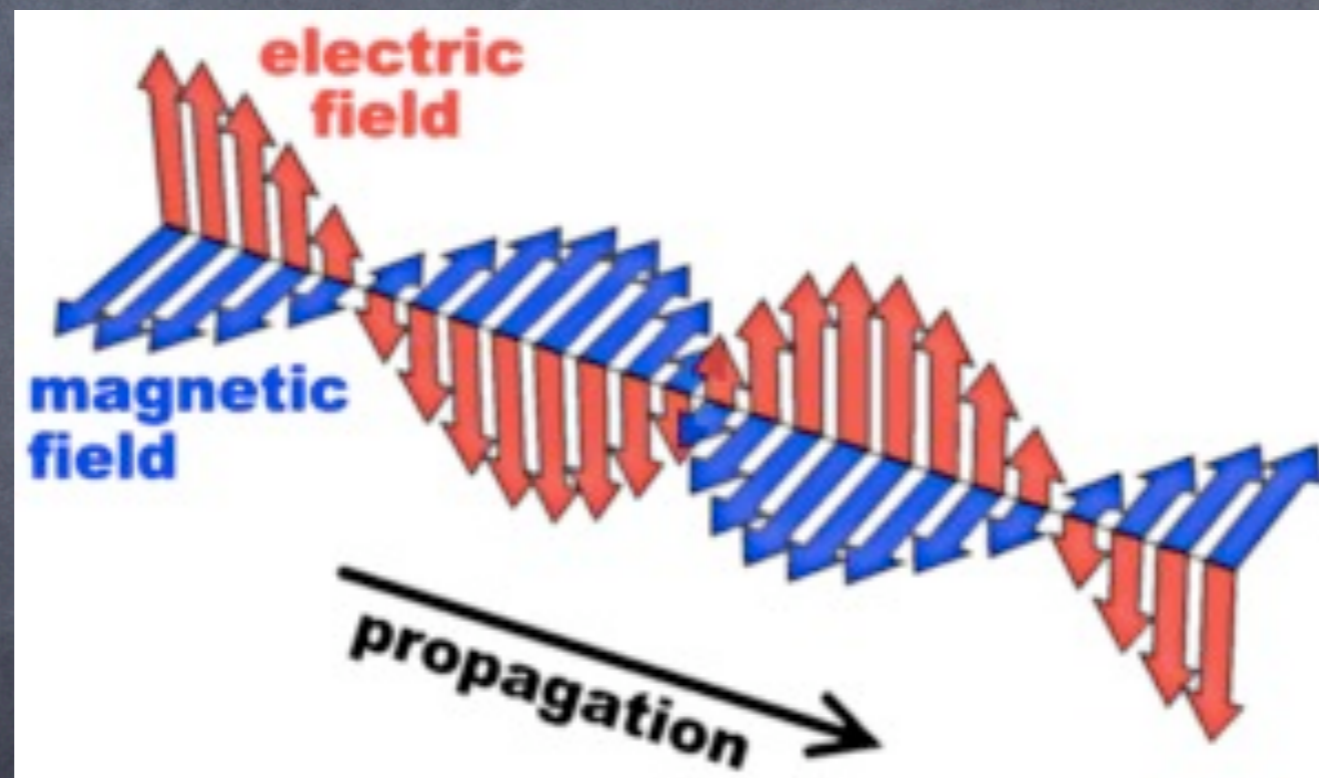
Rotations



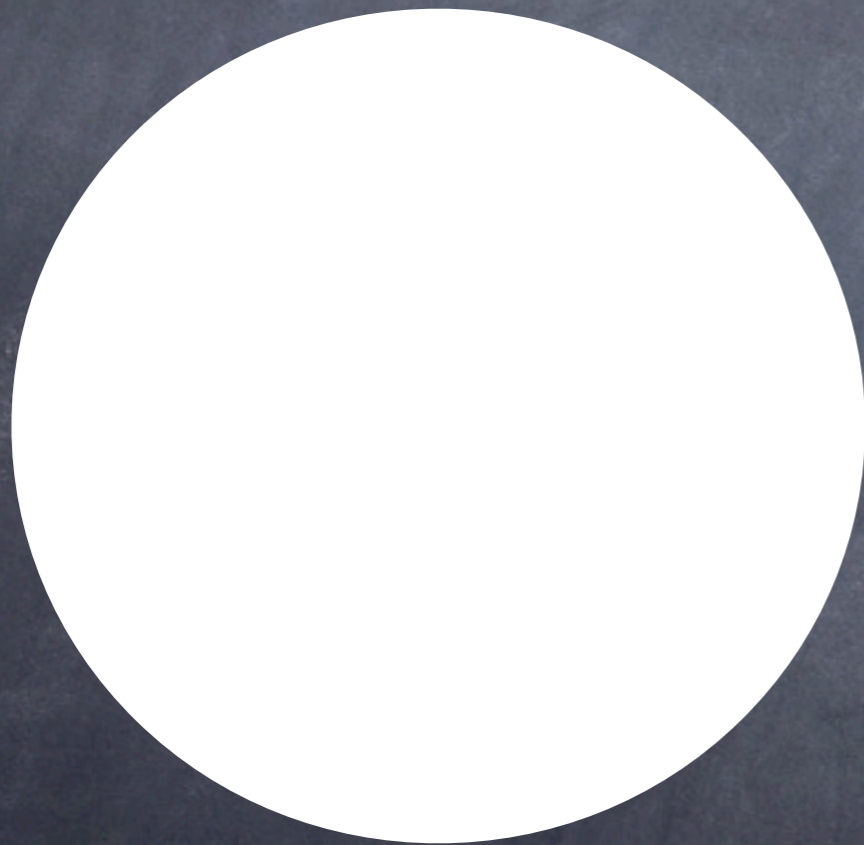
Translational and Rotational Symmetry



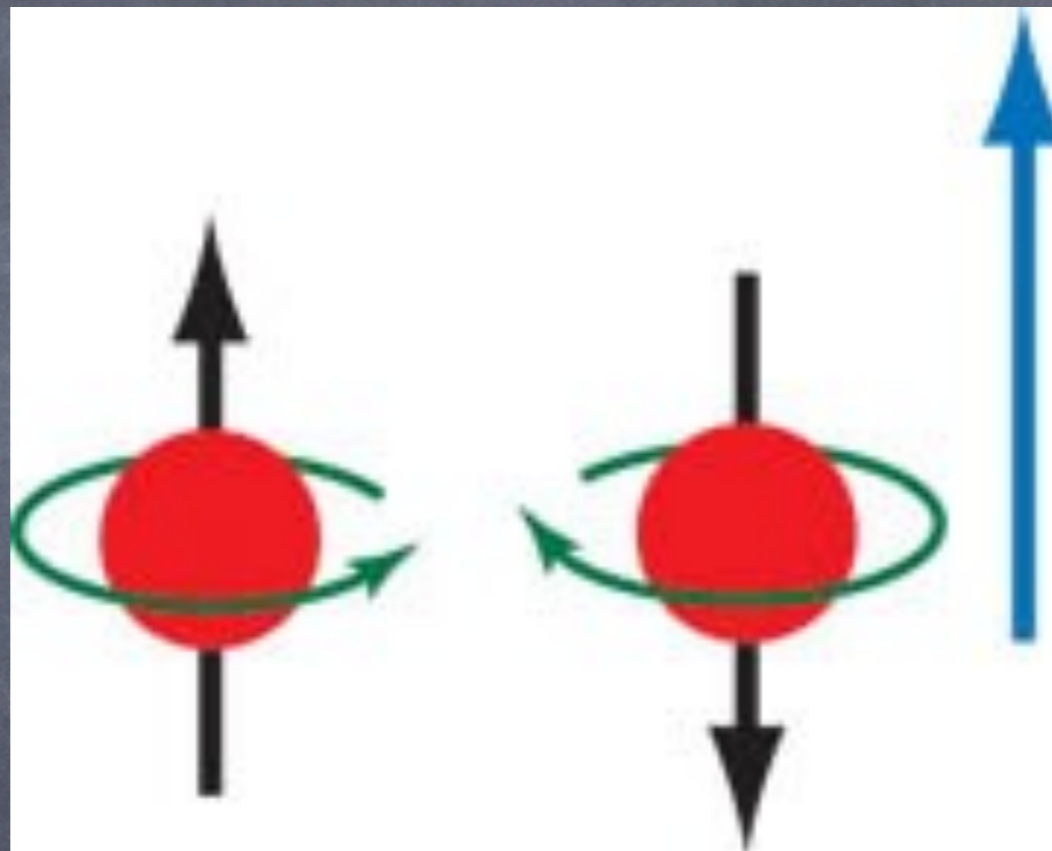
Light Wave



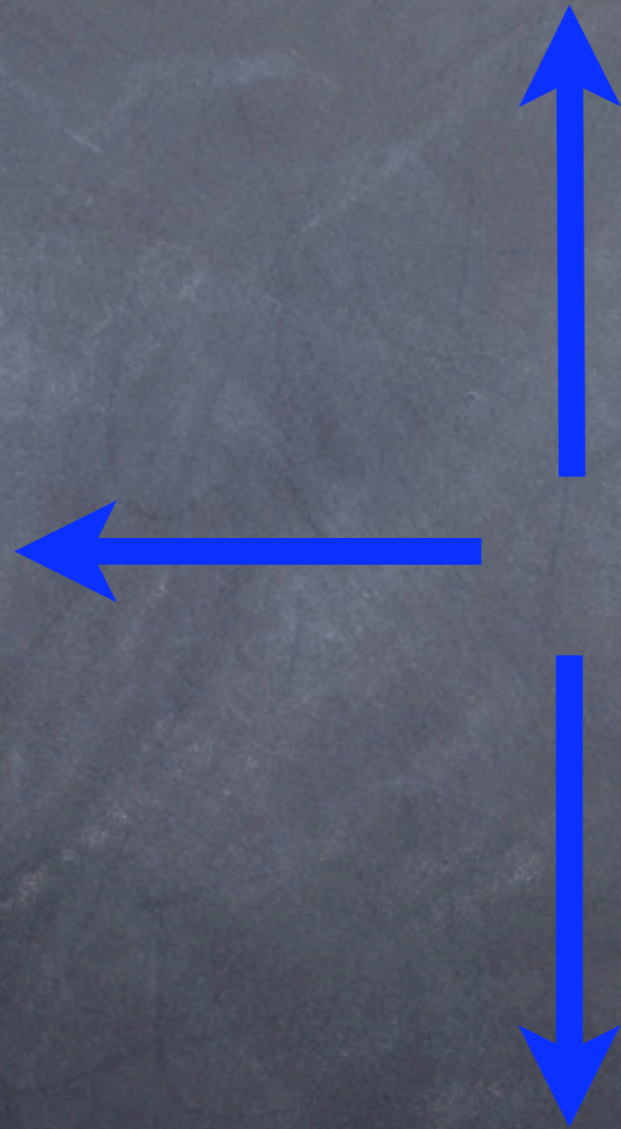
Quantum Spin



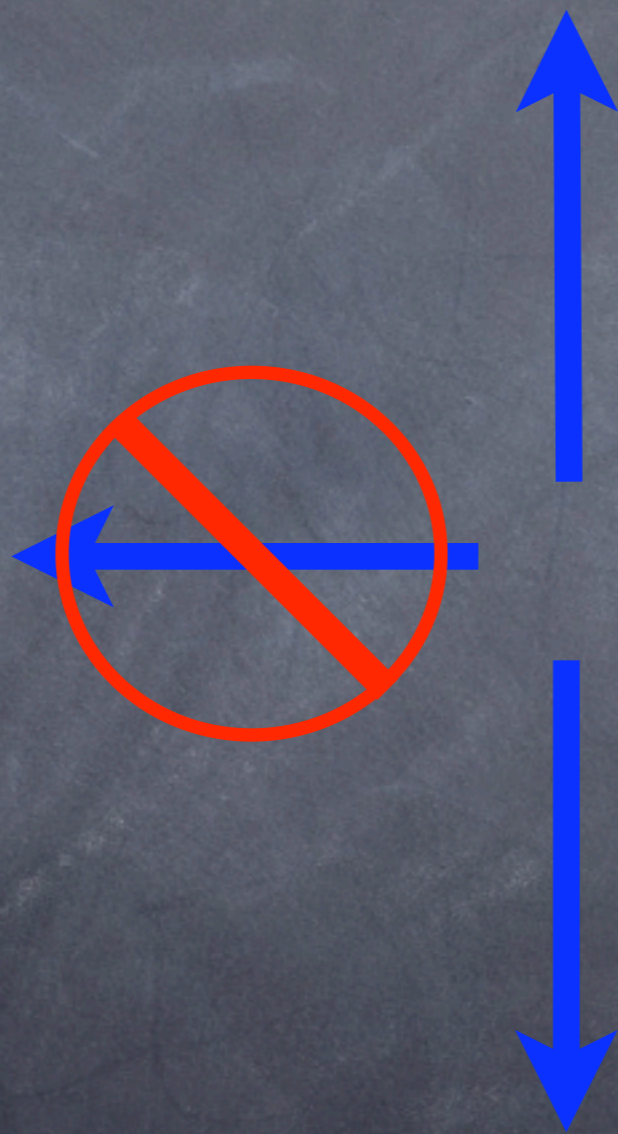
Photon Spin



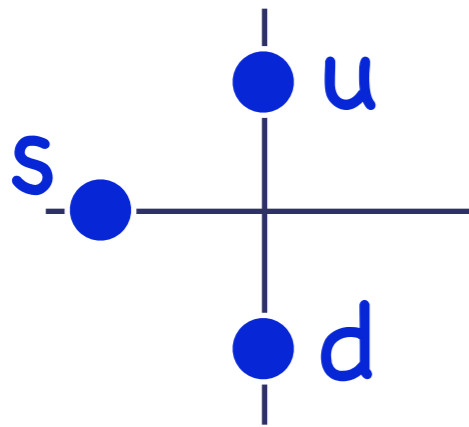
Massive Spin 1 at Rest



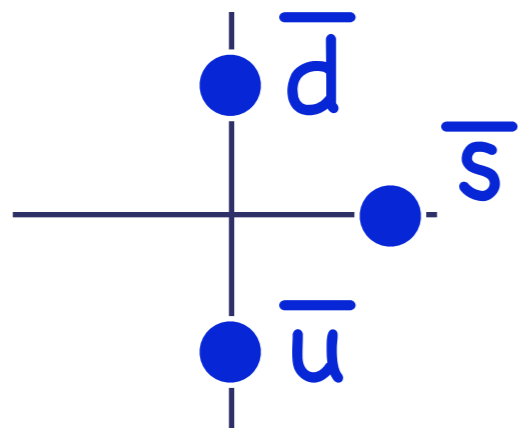
Gauge Symmetry



SU(3) Flavor

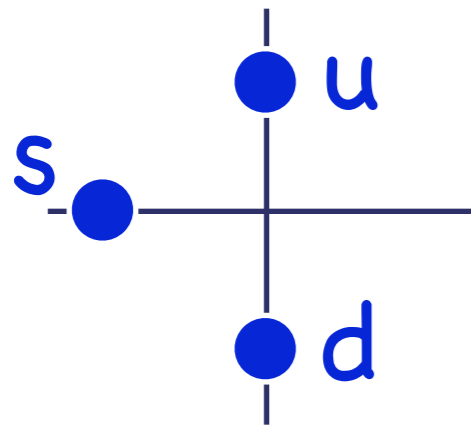


quarks

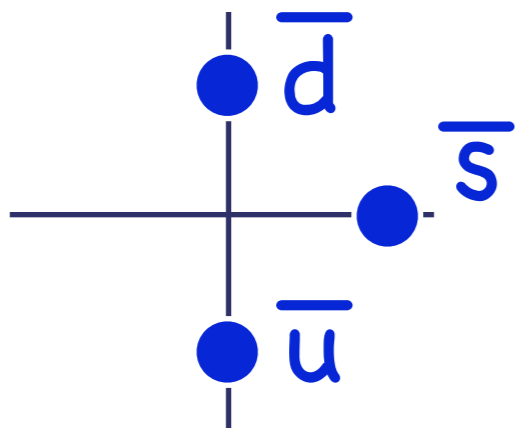


antiquarks

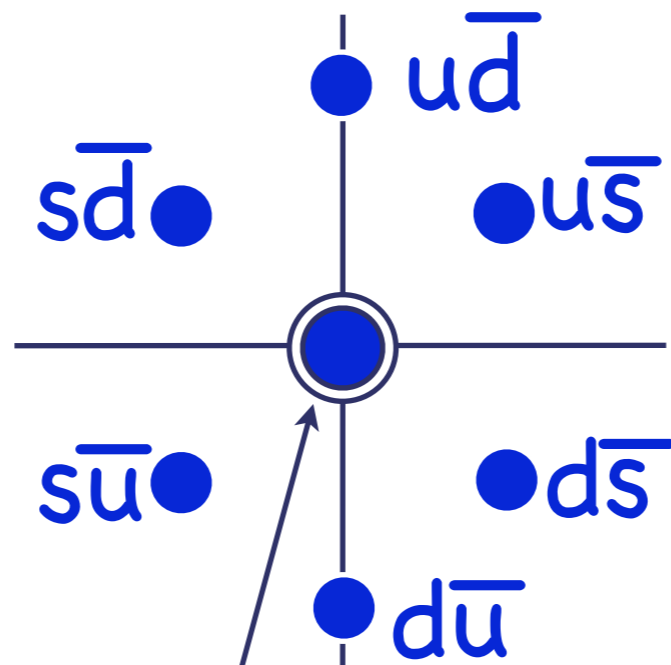
SU(3) Flavor



quarks



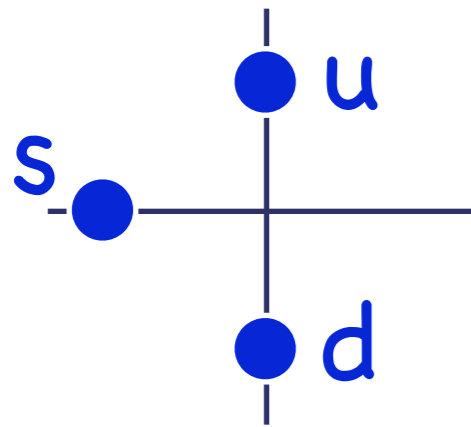
antiquarks



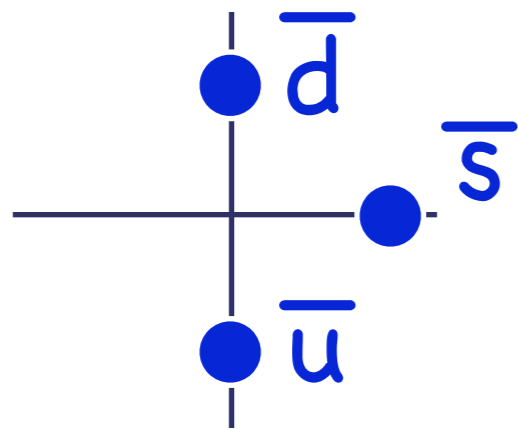
$$u\bar{u} - d\bar{d}$$

$$u\bar{u} + d\bar{d} - 2s\bar{s}$$

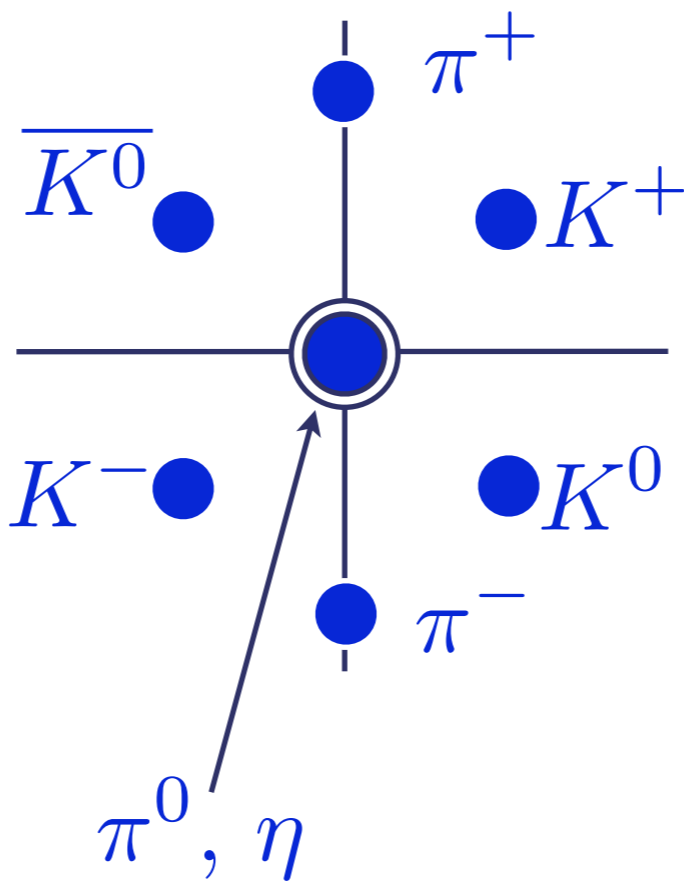
SU(3) Flavor



quarks

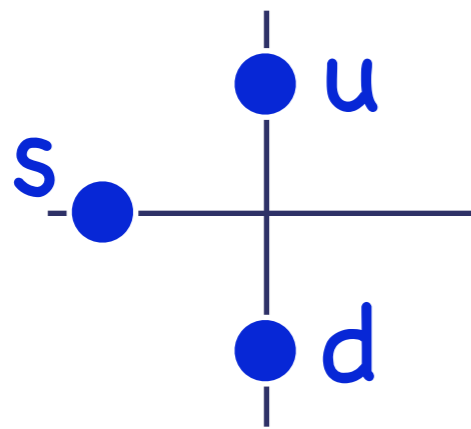


antiquarks

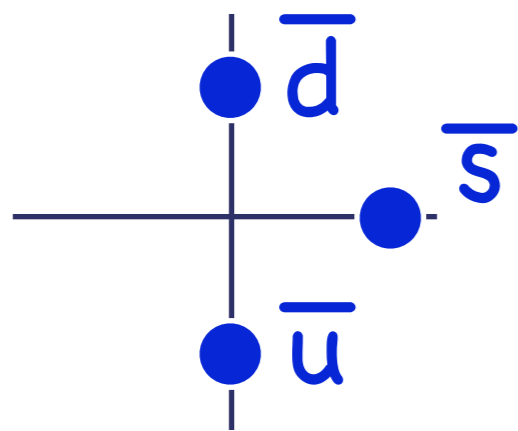


mesons

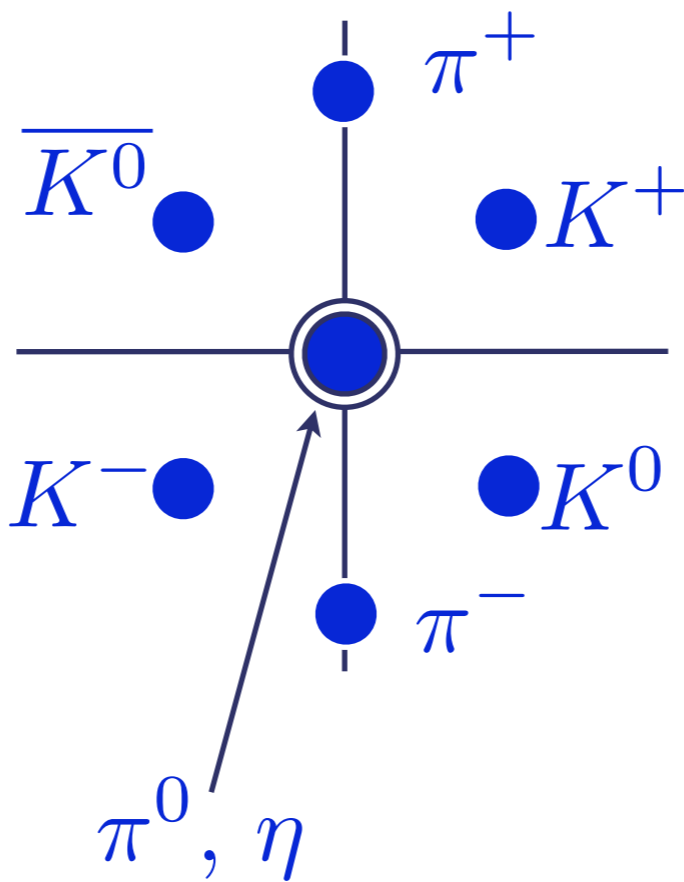
SU(3) Flavor



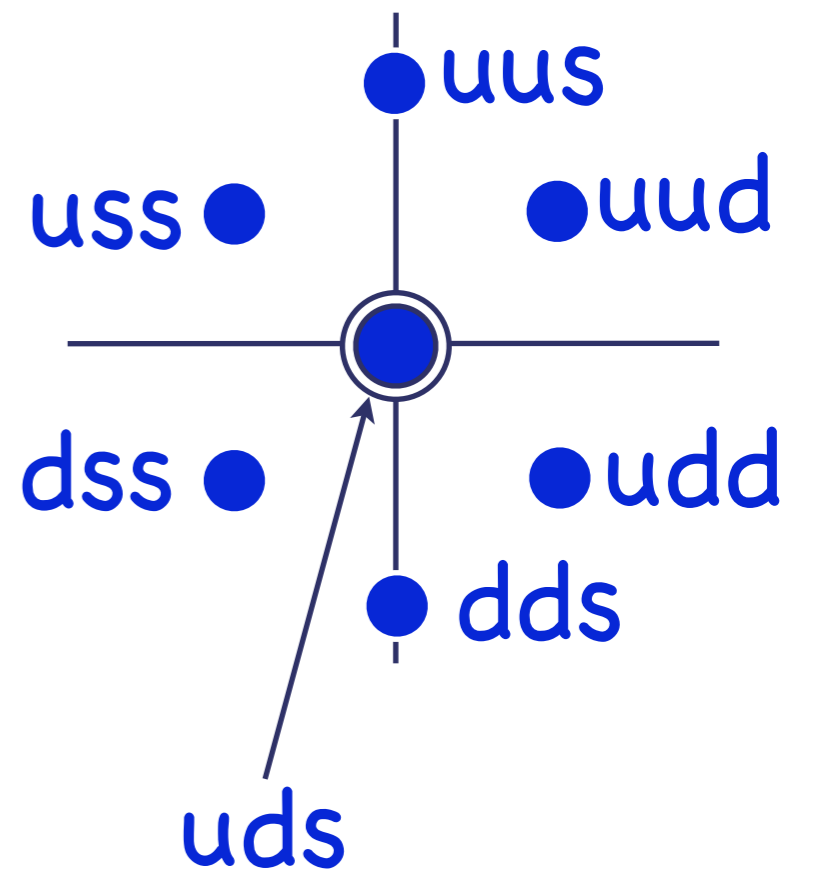
quarks



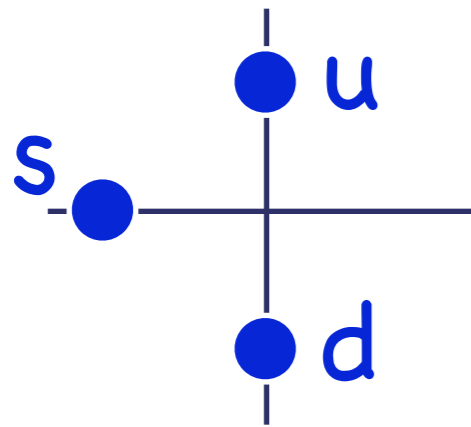
antiquarks



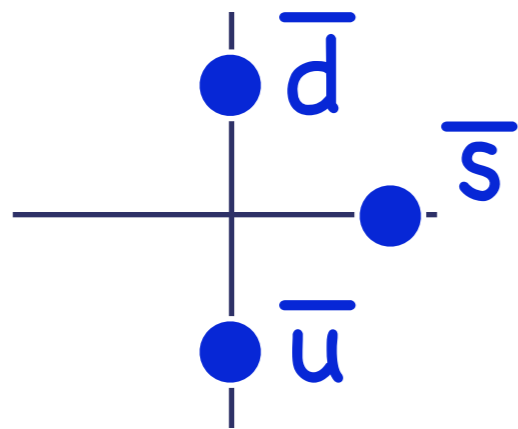
mesons



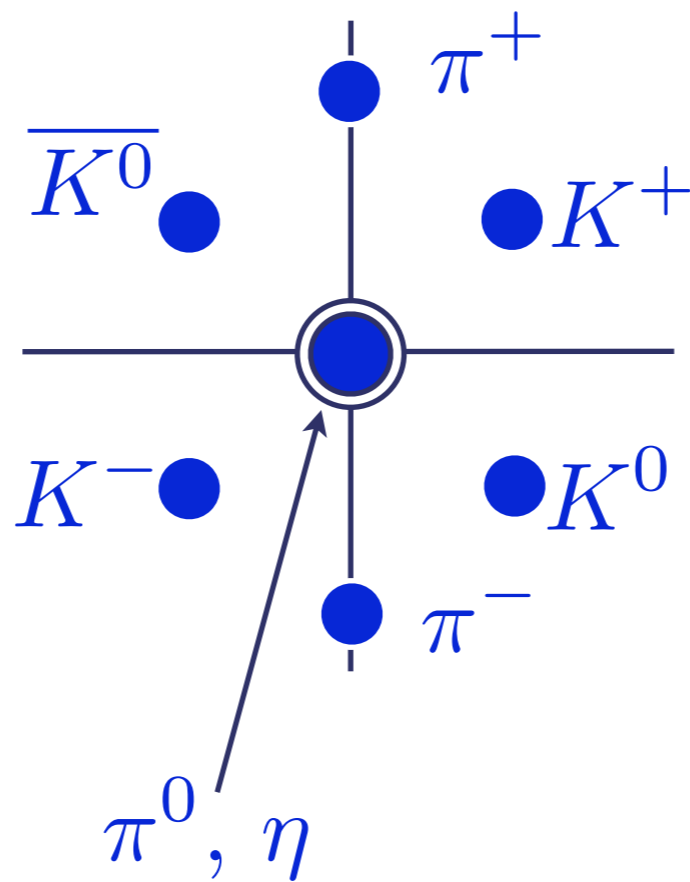
SU(3) Flavor



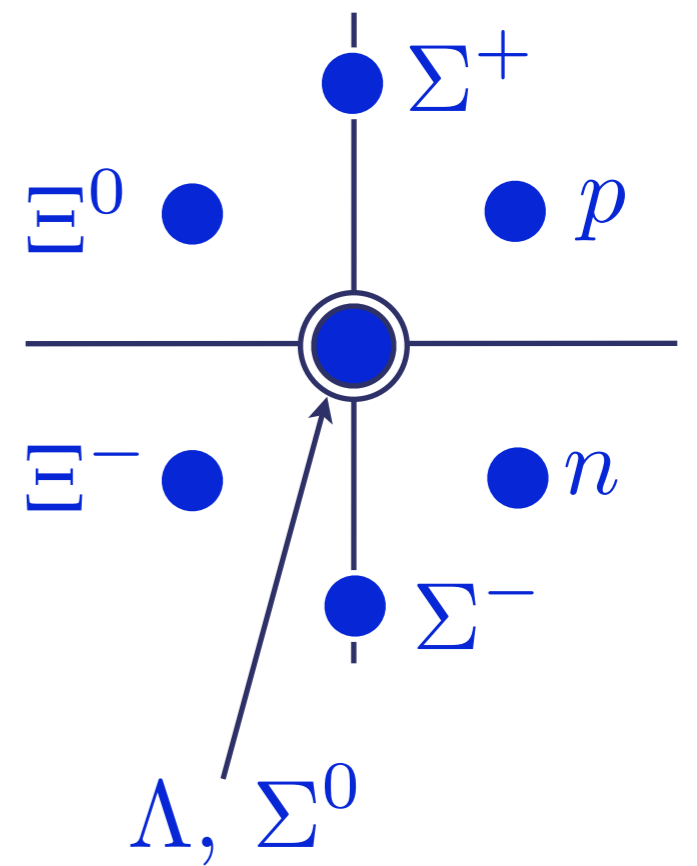
quarks



antiquarks

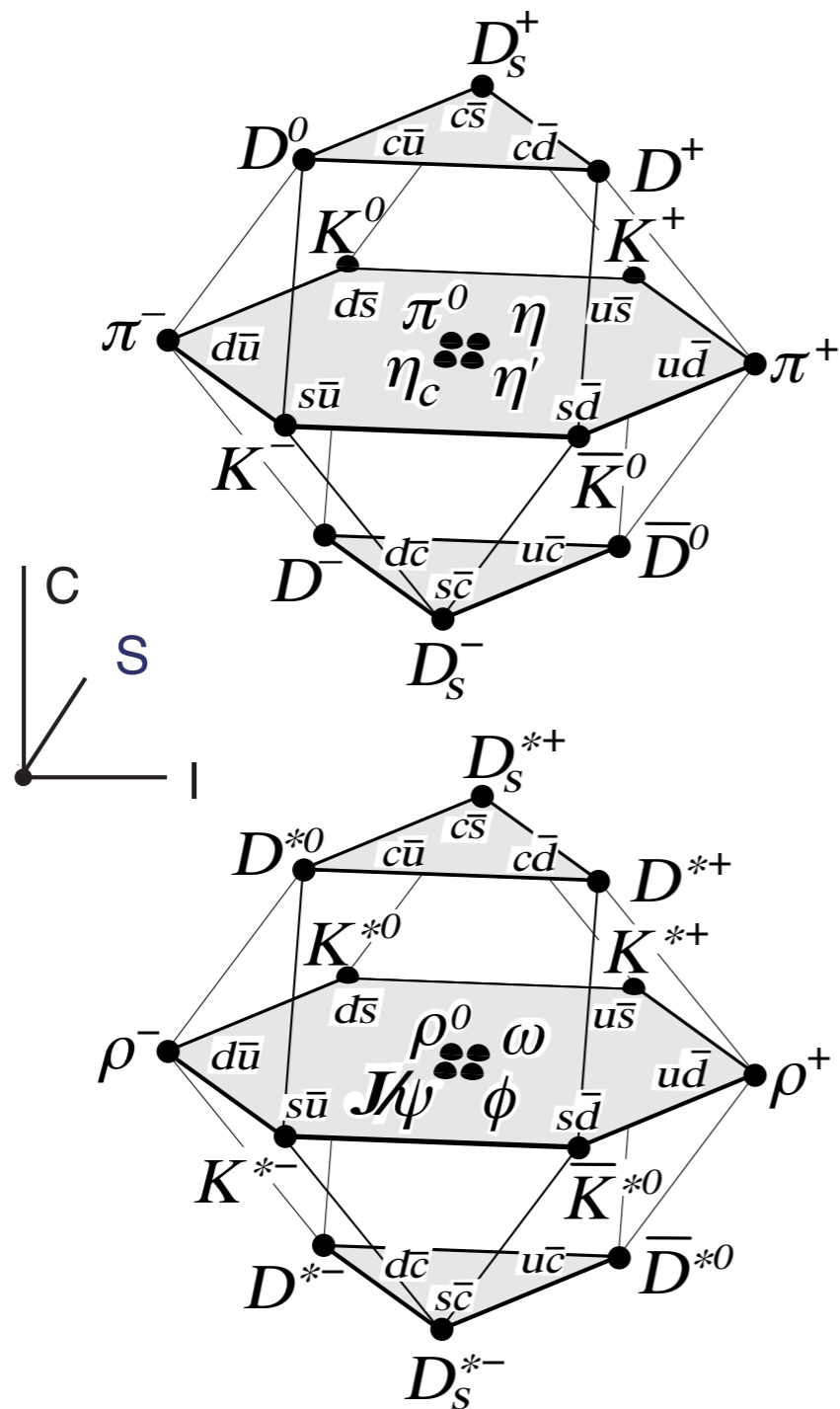


mesons

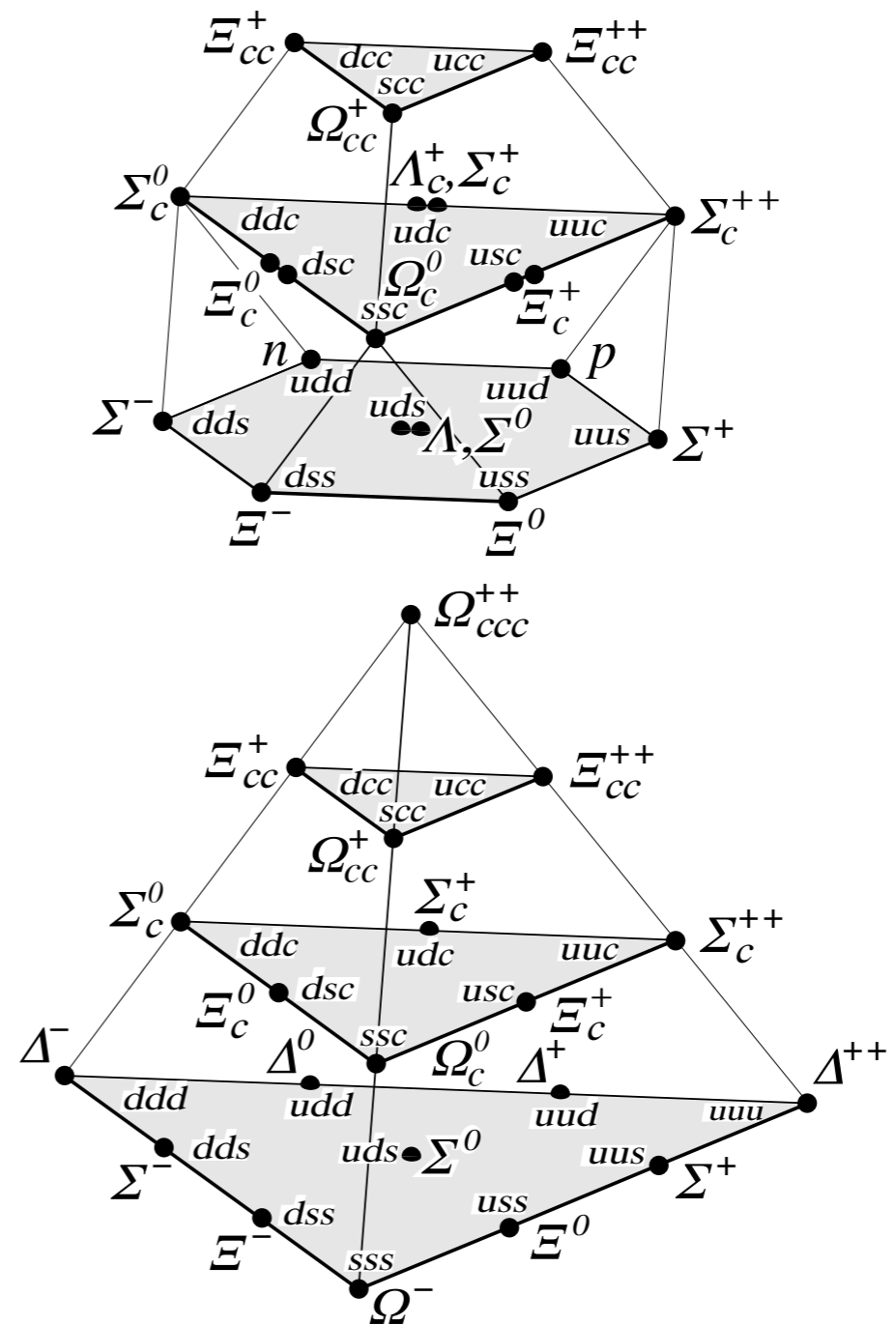


baryons

4 Flavours



mesons



baryons

QED Potential

1/r potential:

Fourier
Transform

$$J^\mu(x) \frac{e^2}{|x-y|} J_\mu(y)$$



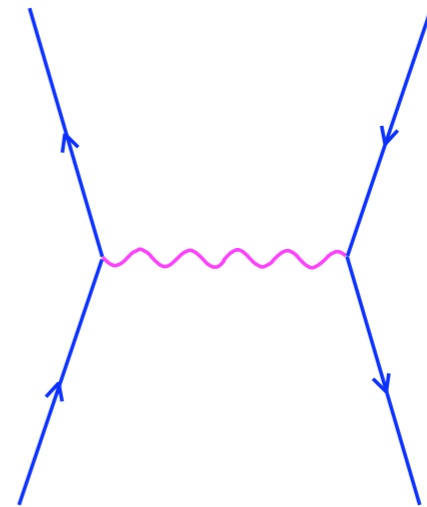
$$J^\mu \frac{e^2}{q^2} J_\mu$$

QED Potential

1/r potential:

$$J^\mu(x) \frac{e^2}{|x-y|} J_\mu(y) \quad \longleftrightarrow \quad J^\mu \frac{e^2}{q^2} J_\mu$$

Fourier Transform



elastic scattering amplitude

QED Potential

1/r potential:

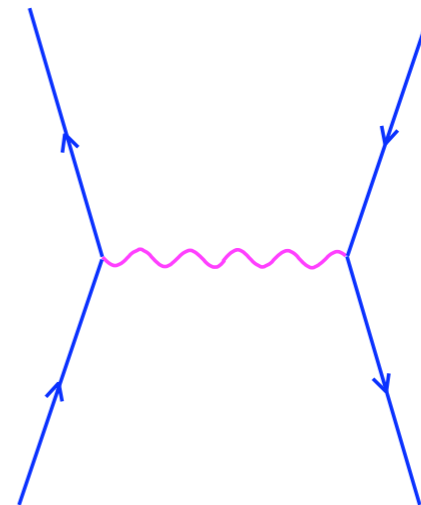
Fourier
Transform

$$J^\mu(x) \frac{e^2}{|x-y|} J_\mu(y)$$



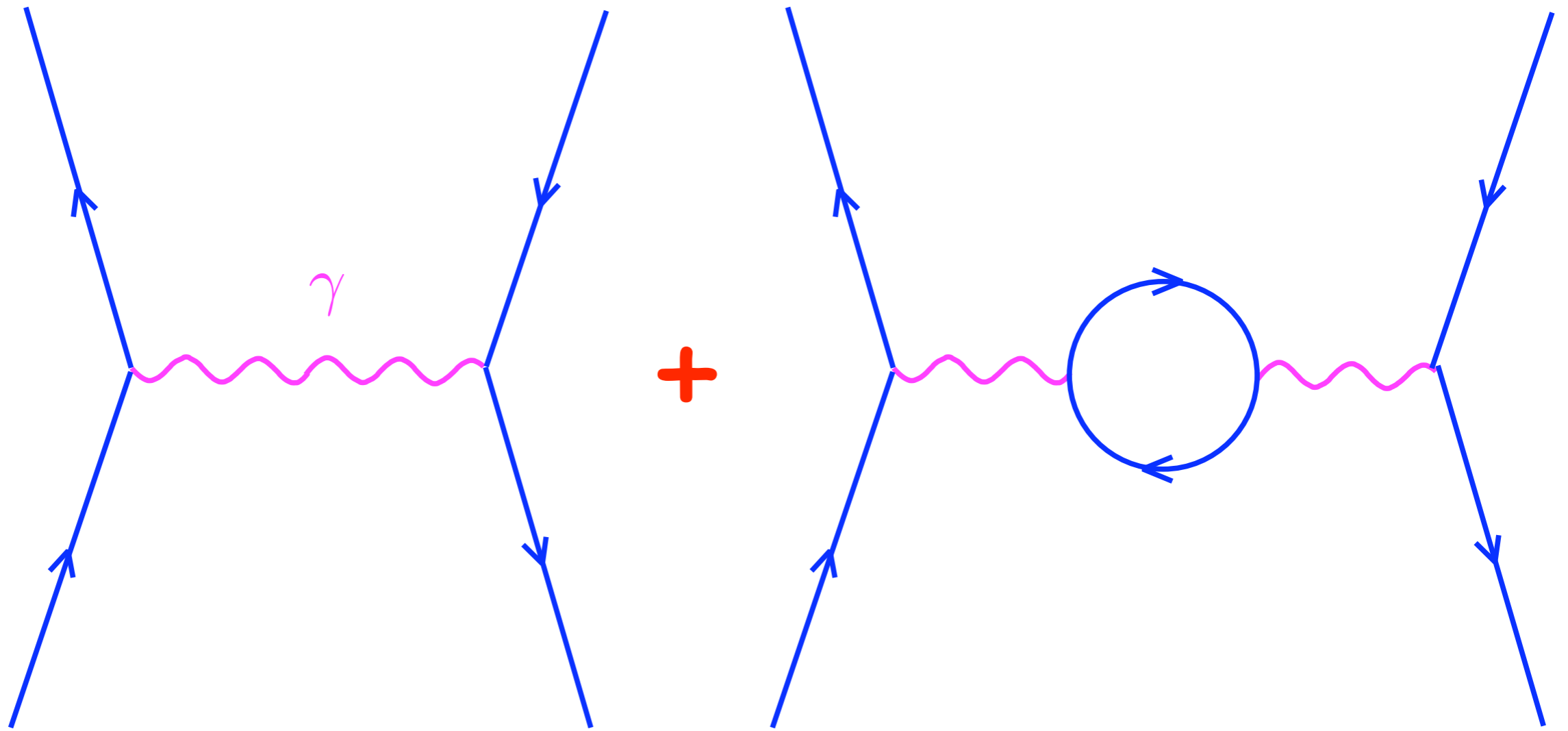
$$J^\mu \frac{e^2}{q^2} J_\mu$$

$$\alpha = \frac{e^2}{4\pi} \approx \frac{1}{137}$$



elastic scattering amplitude

Quantum Corrections

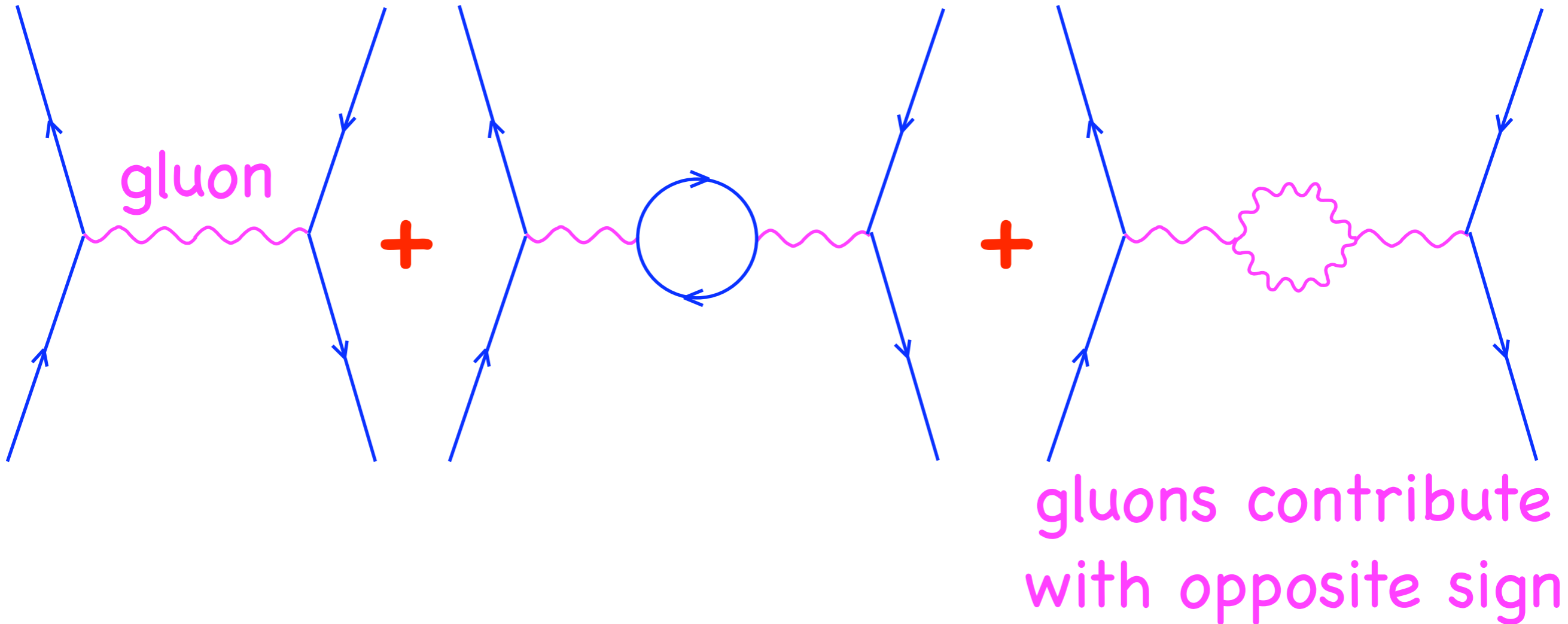


coupling is distance dependent

$$\alpha(10^{-10} \text{ m}) \approx \frac{1}{137}$$

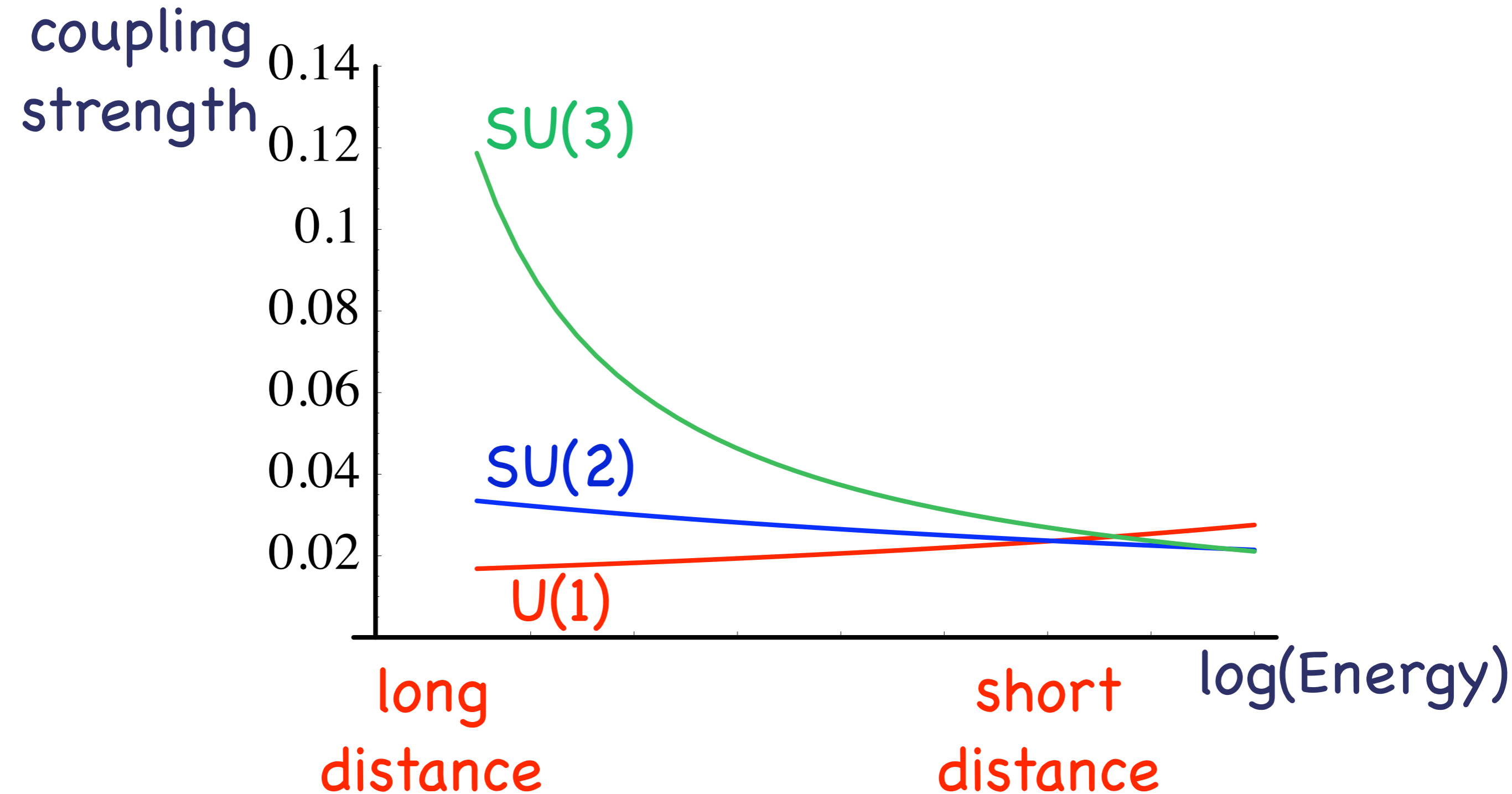
$$\alpha(10^{-17} \text{ m}) \approx \frac{1}{128}$$

Quantum Corrections

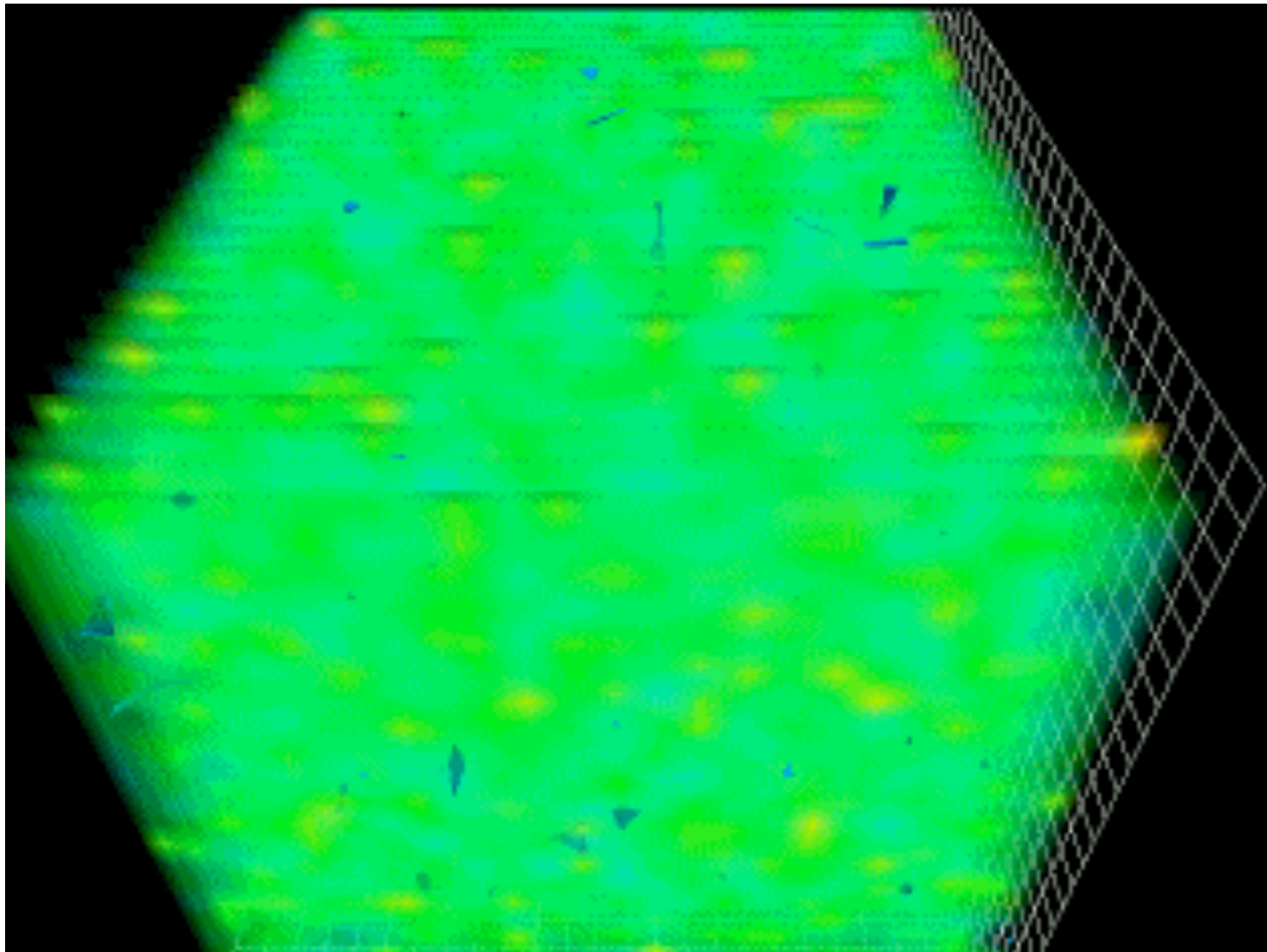


QCD coupling gets stronger at larger distances

Running Coupling

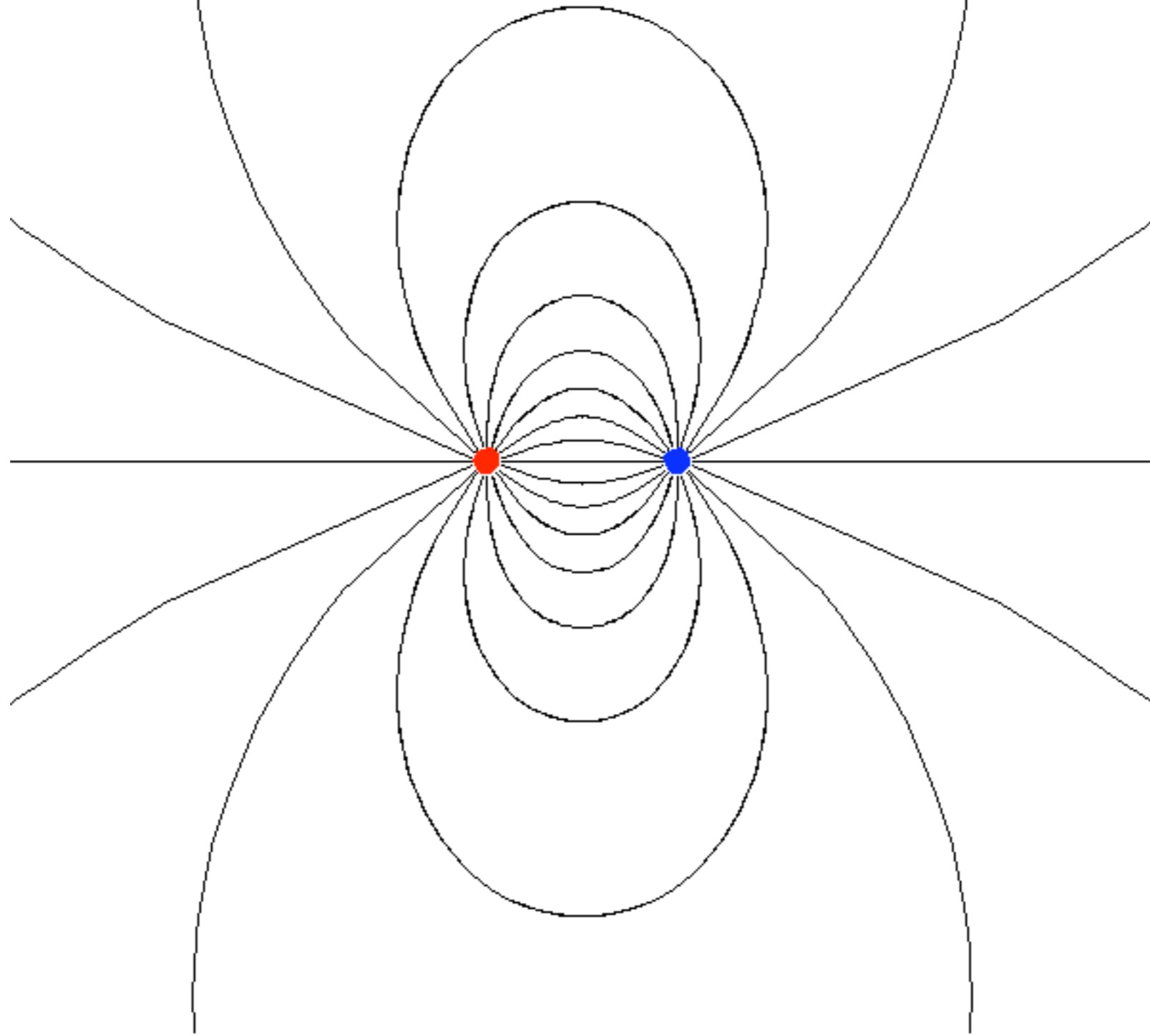


Strong Coupling

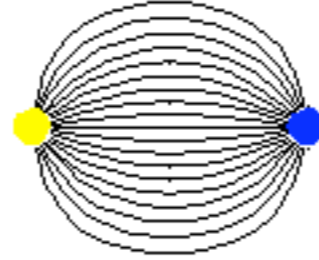


<http://bit.ly/qcdvac>

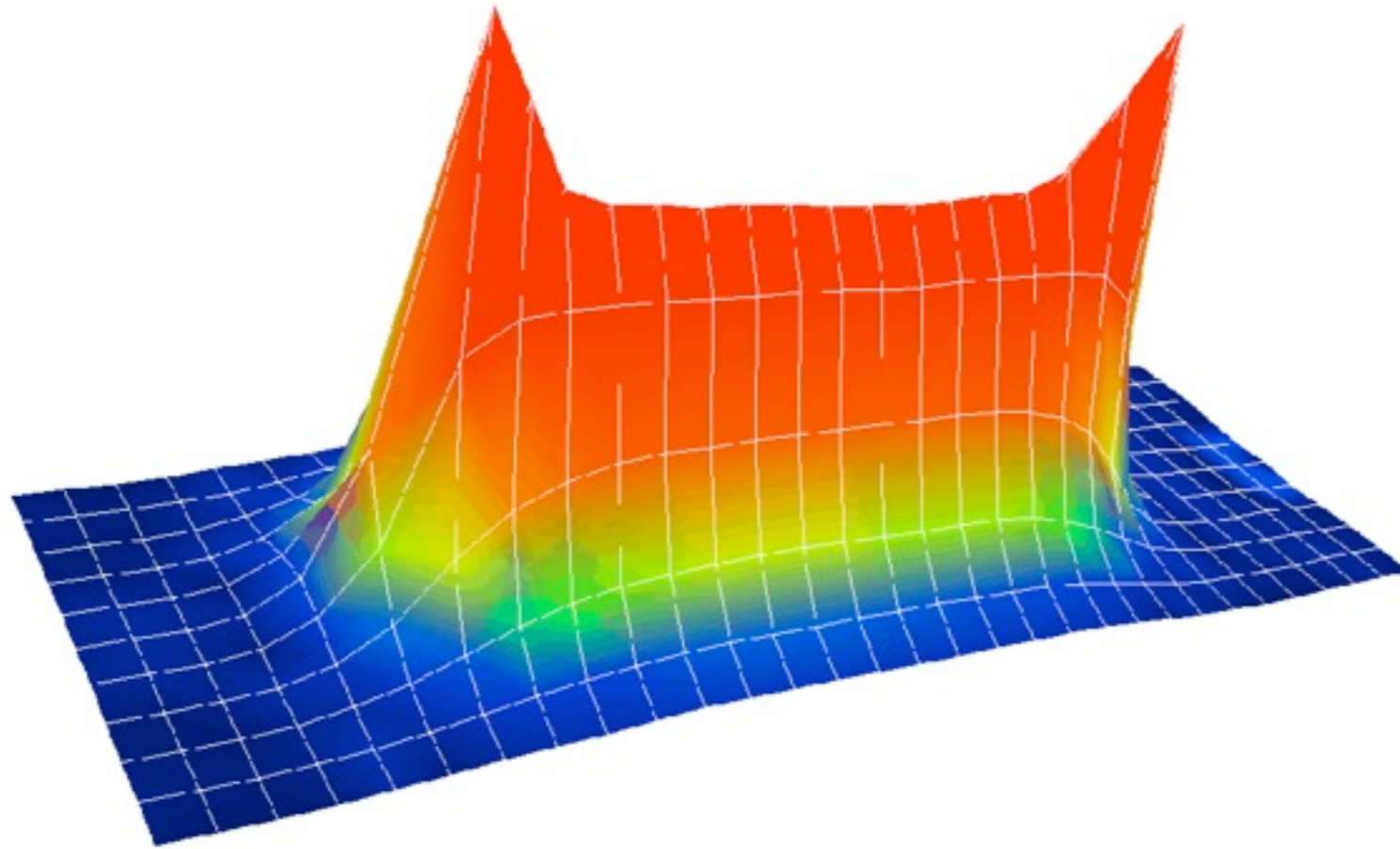
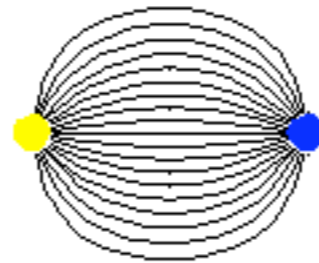
Electric Fields



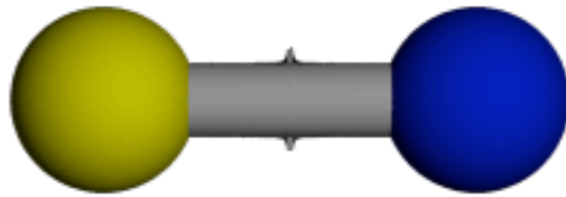
"Color" Fields



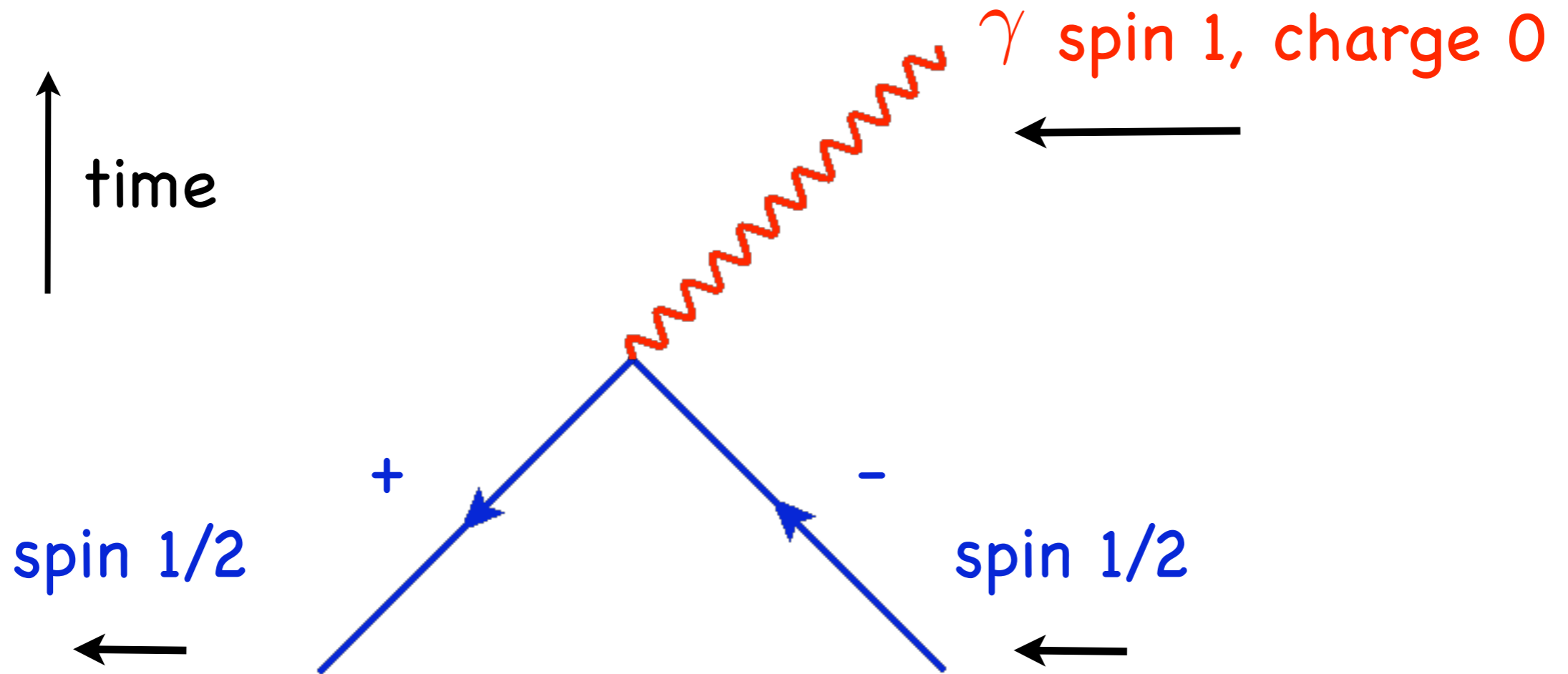
"Color" Fields



Flux Tube \rightarrow Meson

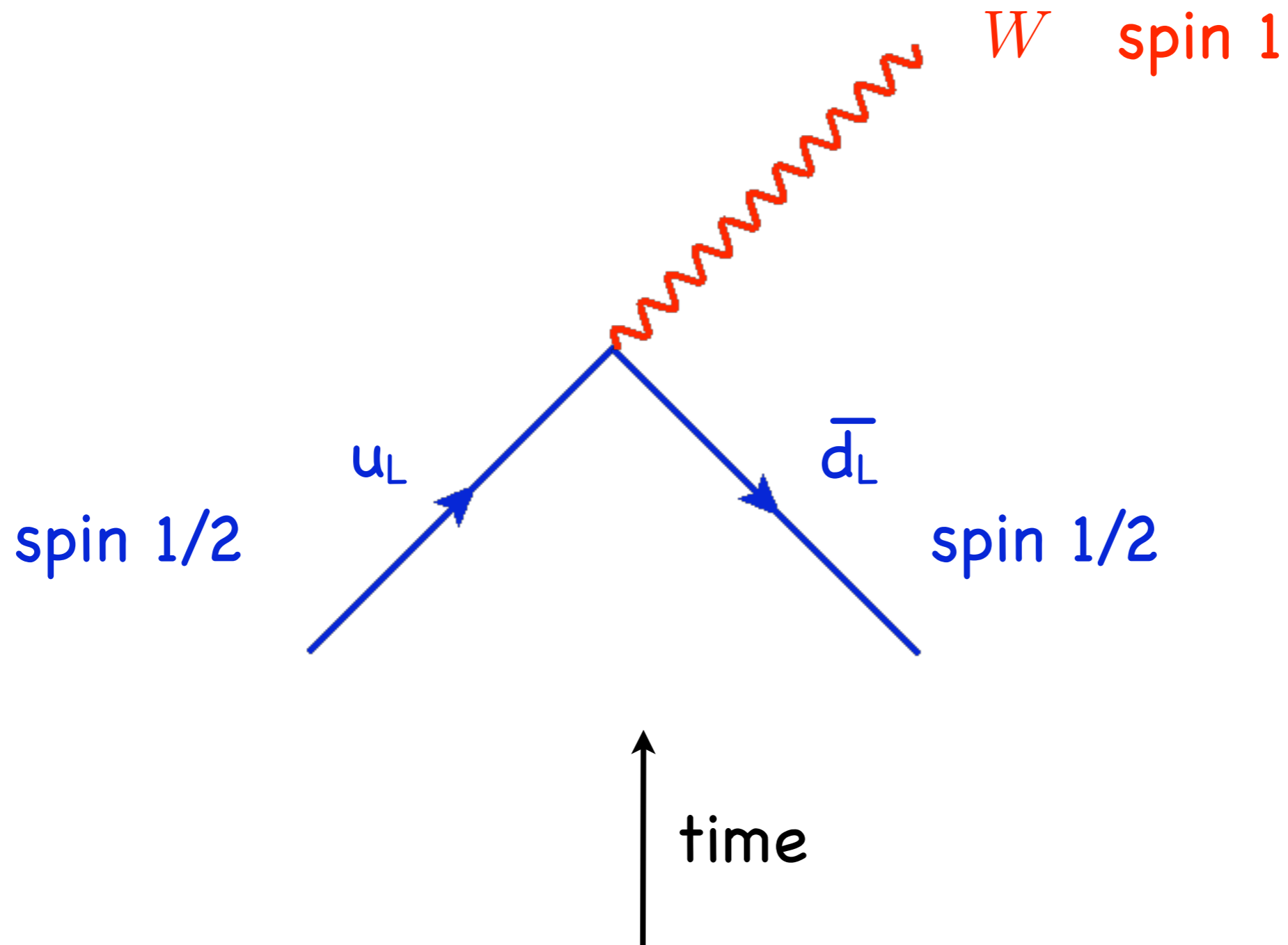


$U(1)$



spin and charge must add up

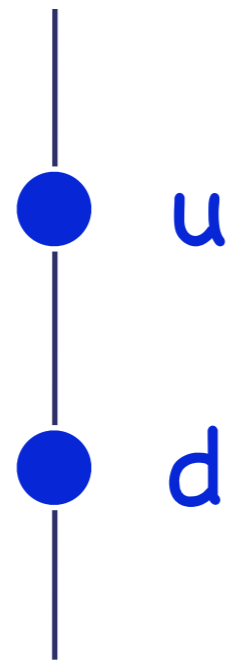
$SU(2)_L$



SU(2) Gauge Bosons

adding SU(2) charges
works just like spin:

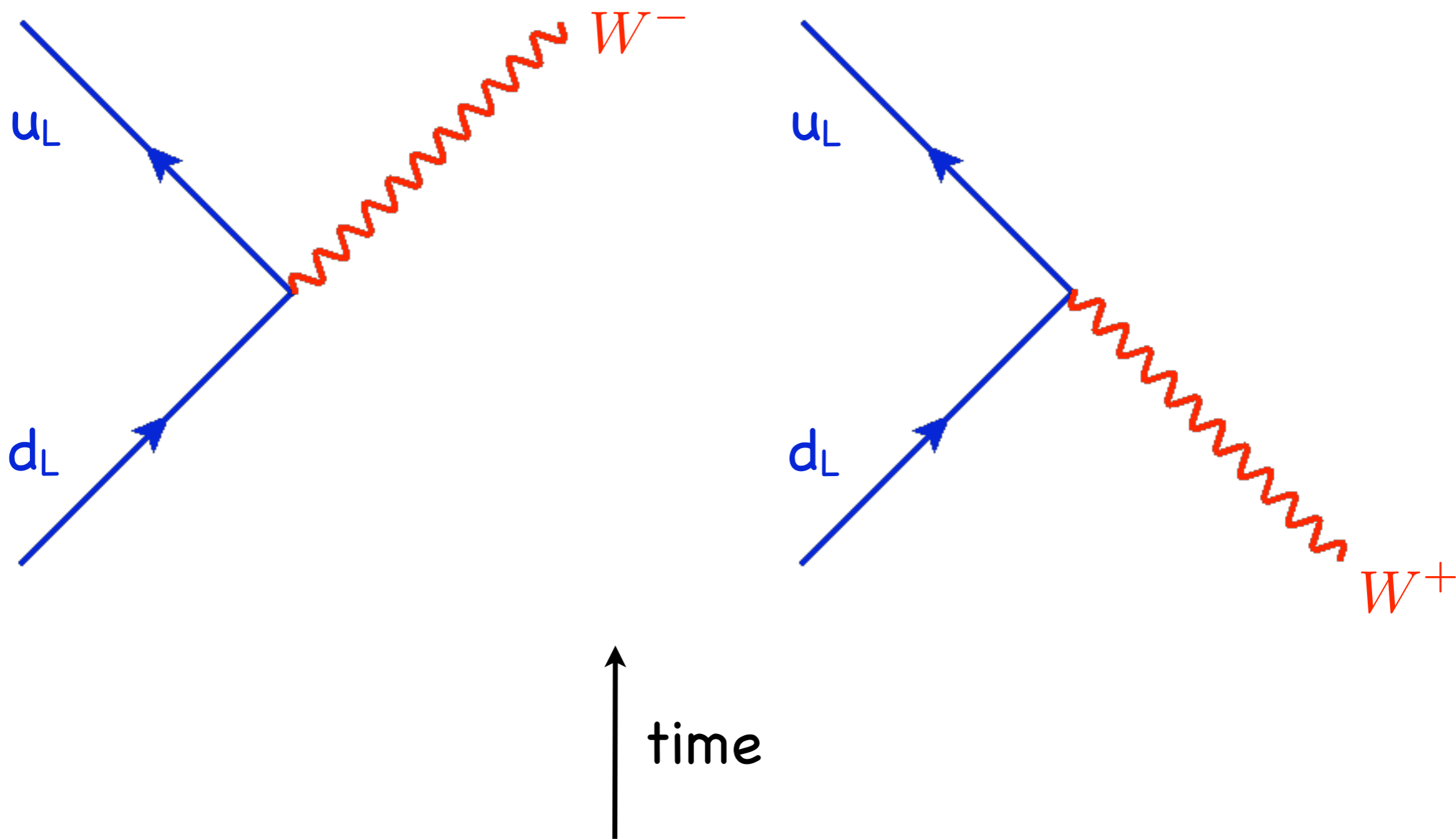
$$\pm\frac{1}{2} \pm \frac{1}{2} = -1, 0, 1$$



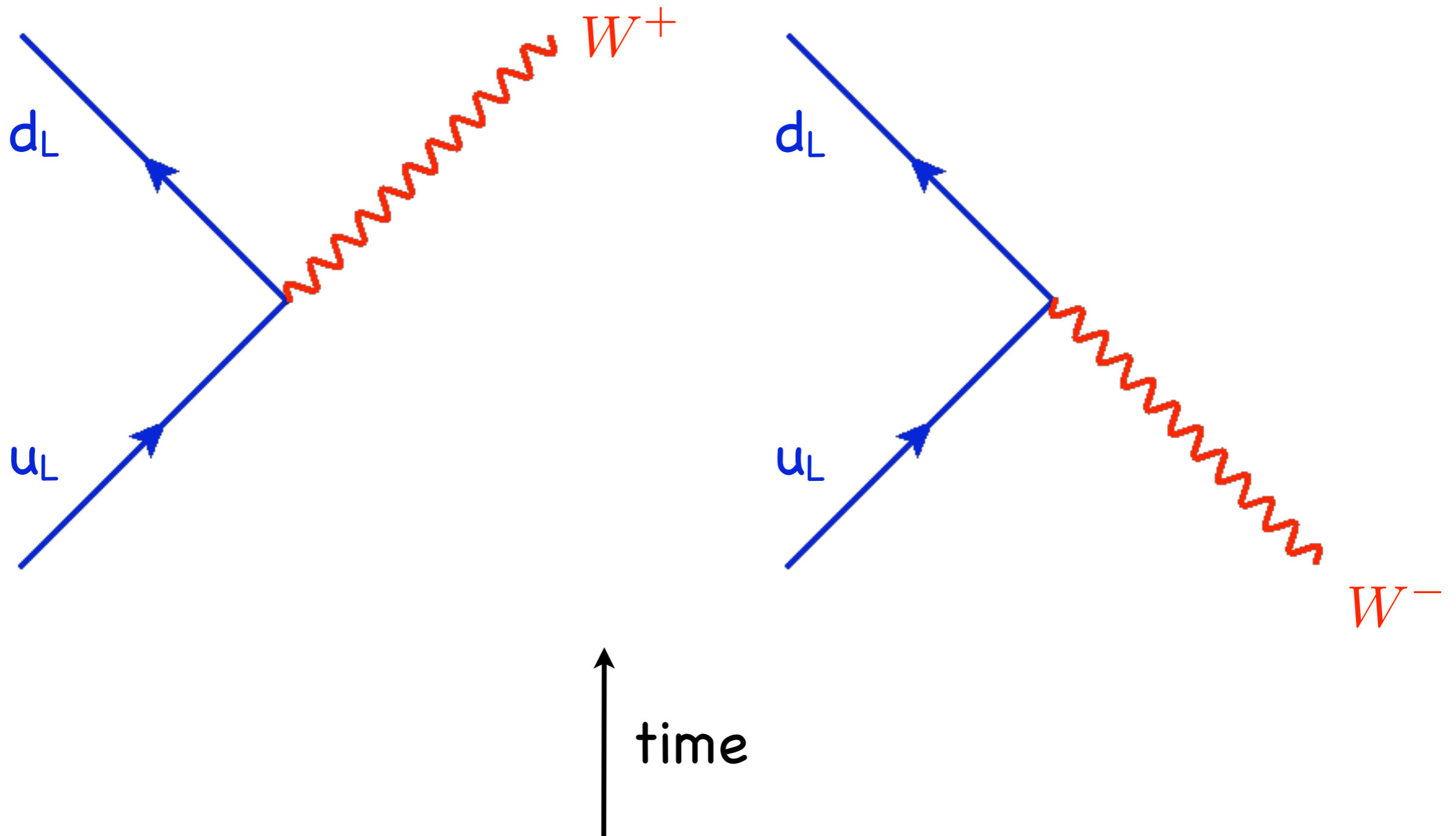
← symmetry
 $u\bar{u}-d\bar{d}$

three weak gauge bosons

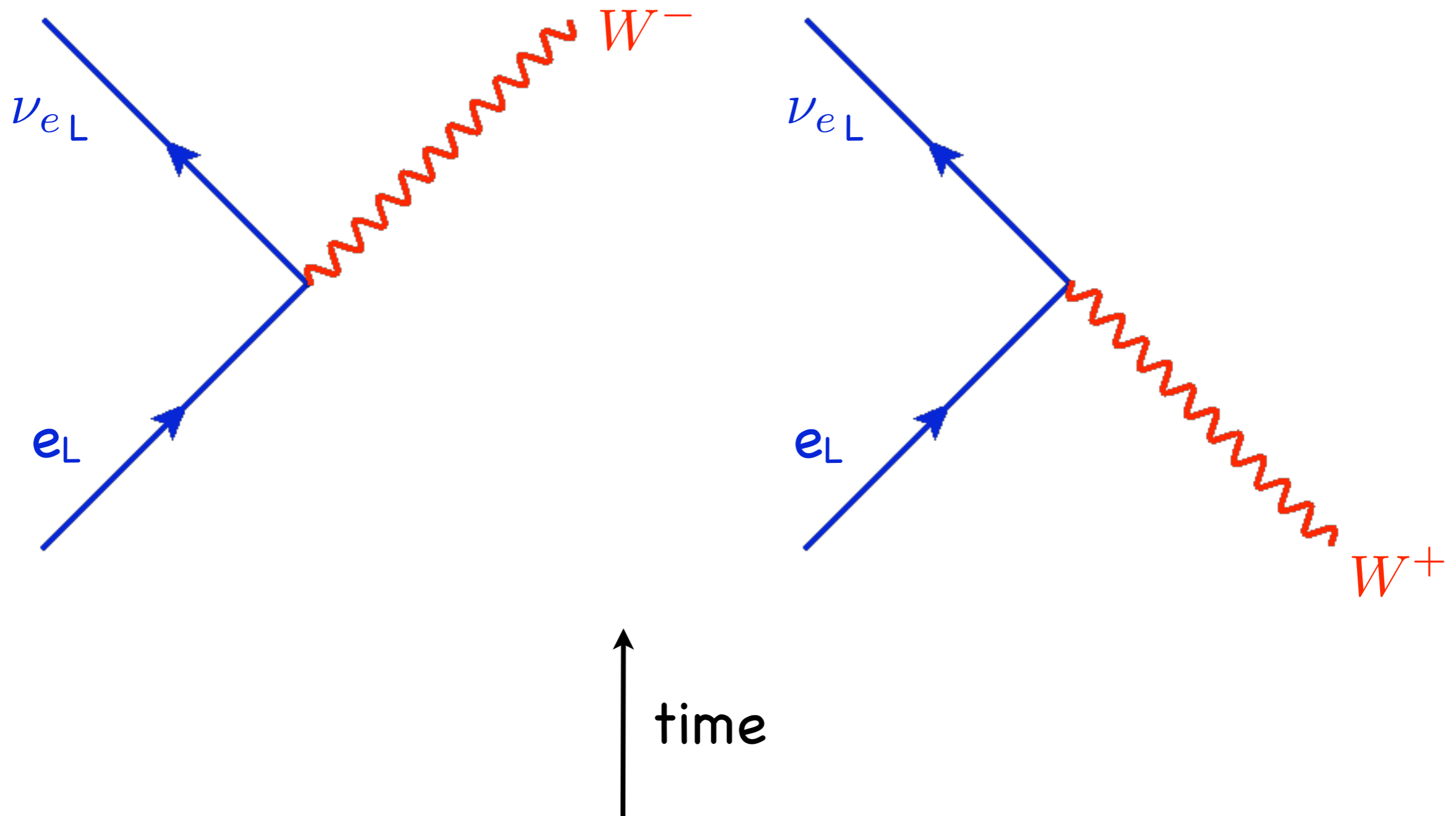
$SU(2)_L$ Weak Interactions



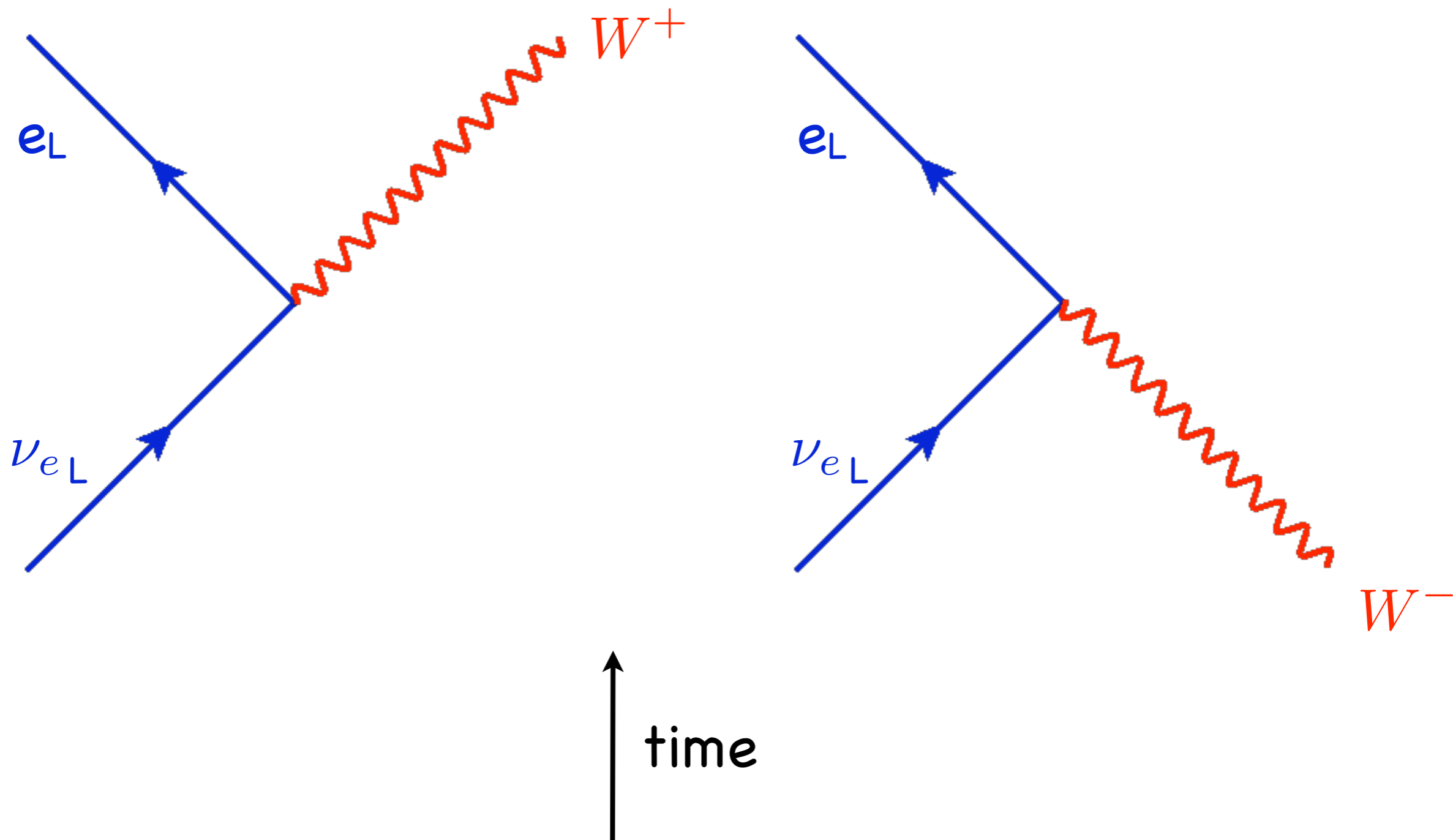
$SU(2)_L$ Weak Interactions



$SU(2)_L$ Weak Interactions



$SU(2)_L$ Weak Interactions



Standard Model

THREE GENERATIONS OF MATTER

MATTER CONSTITUENTS: FERMIONS

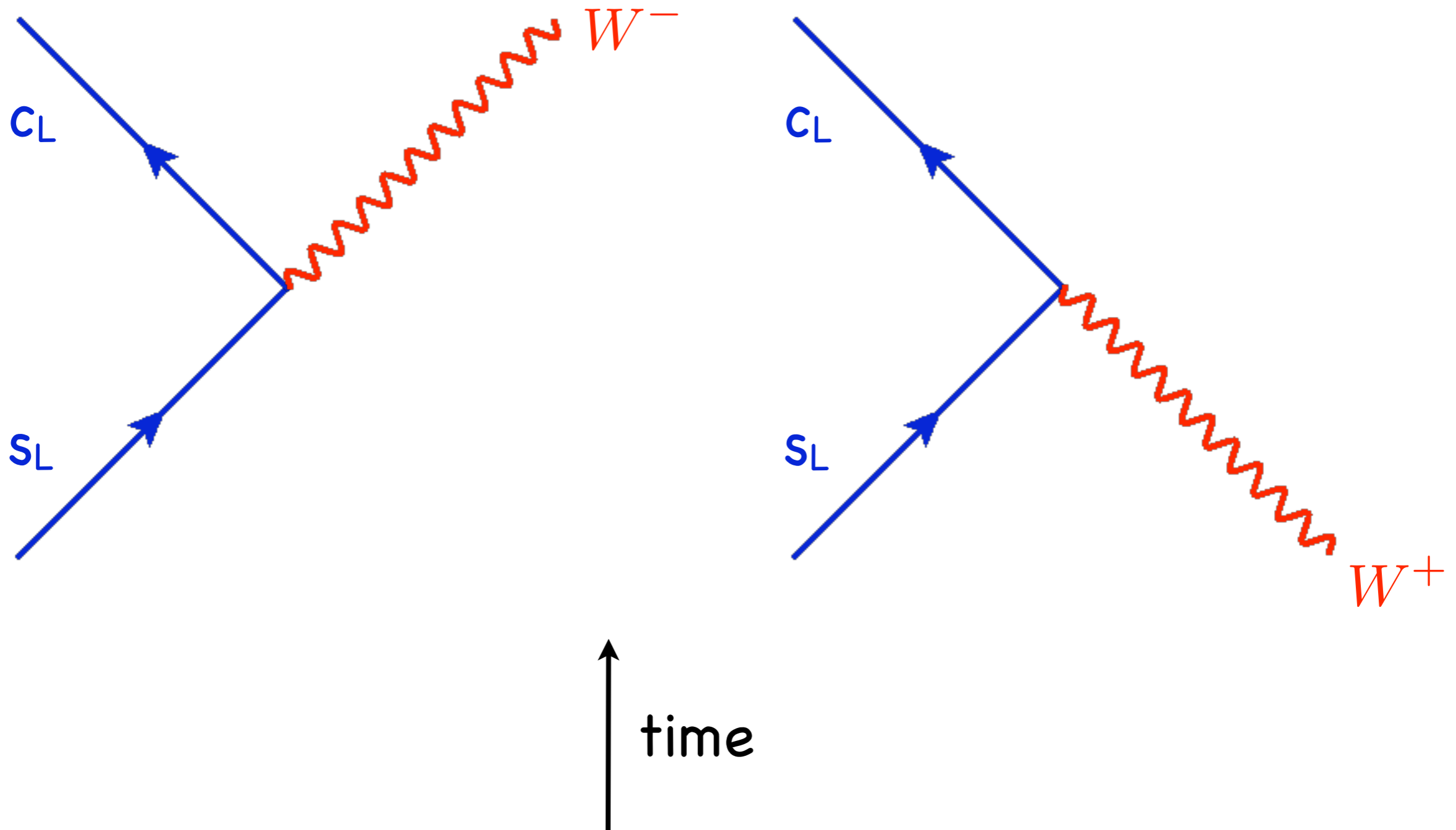
QUARKS

LEPTONS

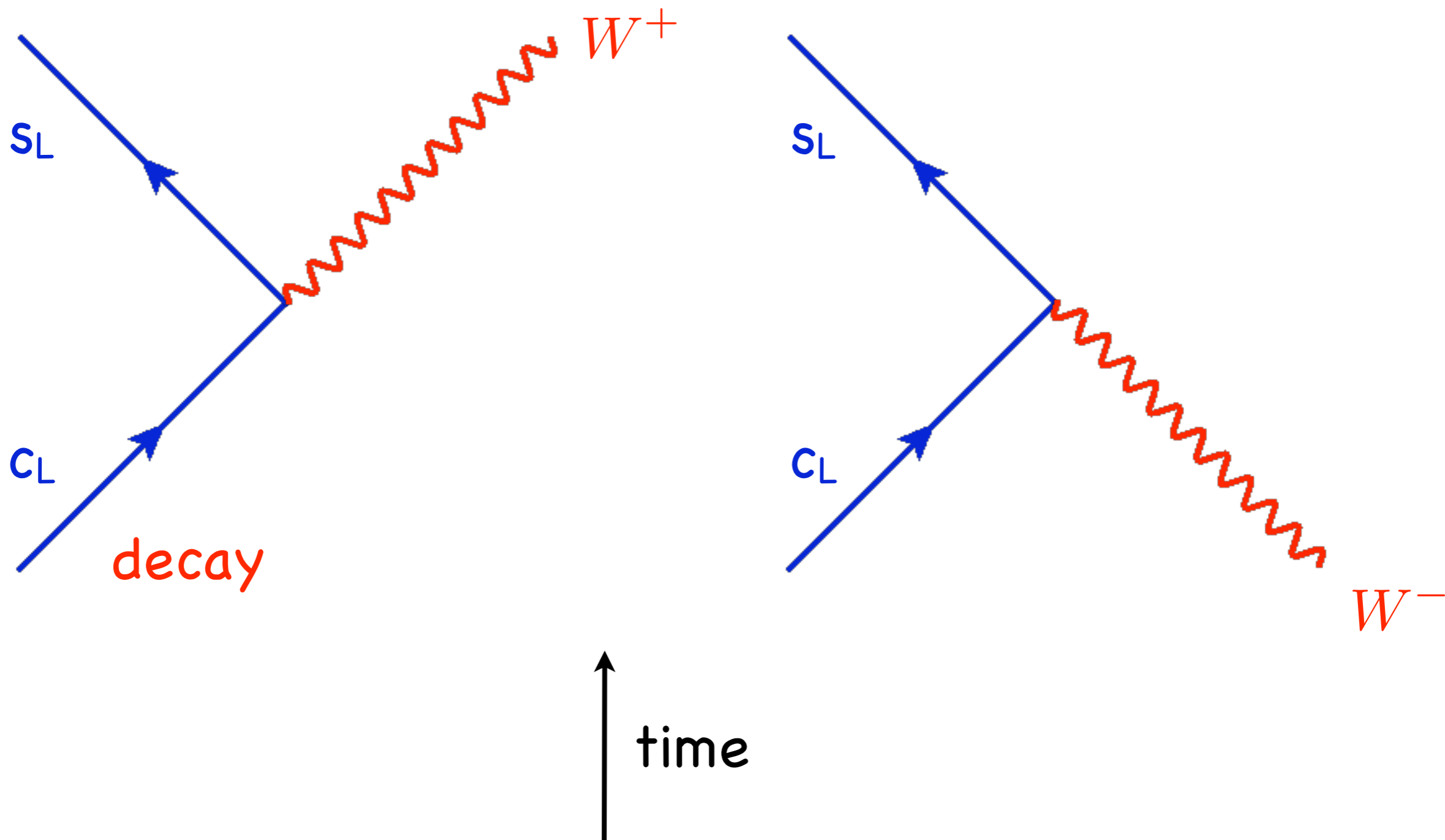
	I	II	III	CHARGE:	
UP	 2.75	 1300	 178000	$\leftarrow \frac{2}{3}$	 91188 Z^0
DOWN	 6	 110	 4500	$\leftarrow -\frac{1}{3}$	 80430 W^+/W^-
ELECTRON	 0.511	 105.7	 1777	$\leftarrow -1$	 $< 10^{-23}$ PHOTON
NEUTRINO	 $< 3 \cdot 10^{-6}$ e	 < 0.19 μ	 < 18.2 τ	$\leftarrow 0$	 theory: 0 GLUON

FORCE CARRIERS: BOSONS

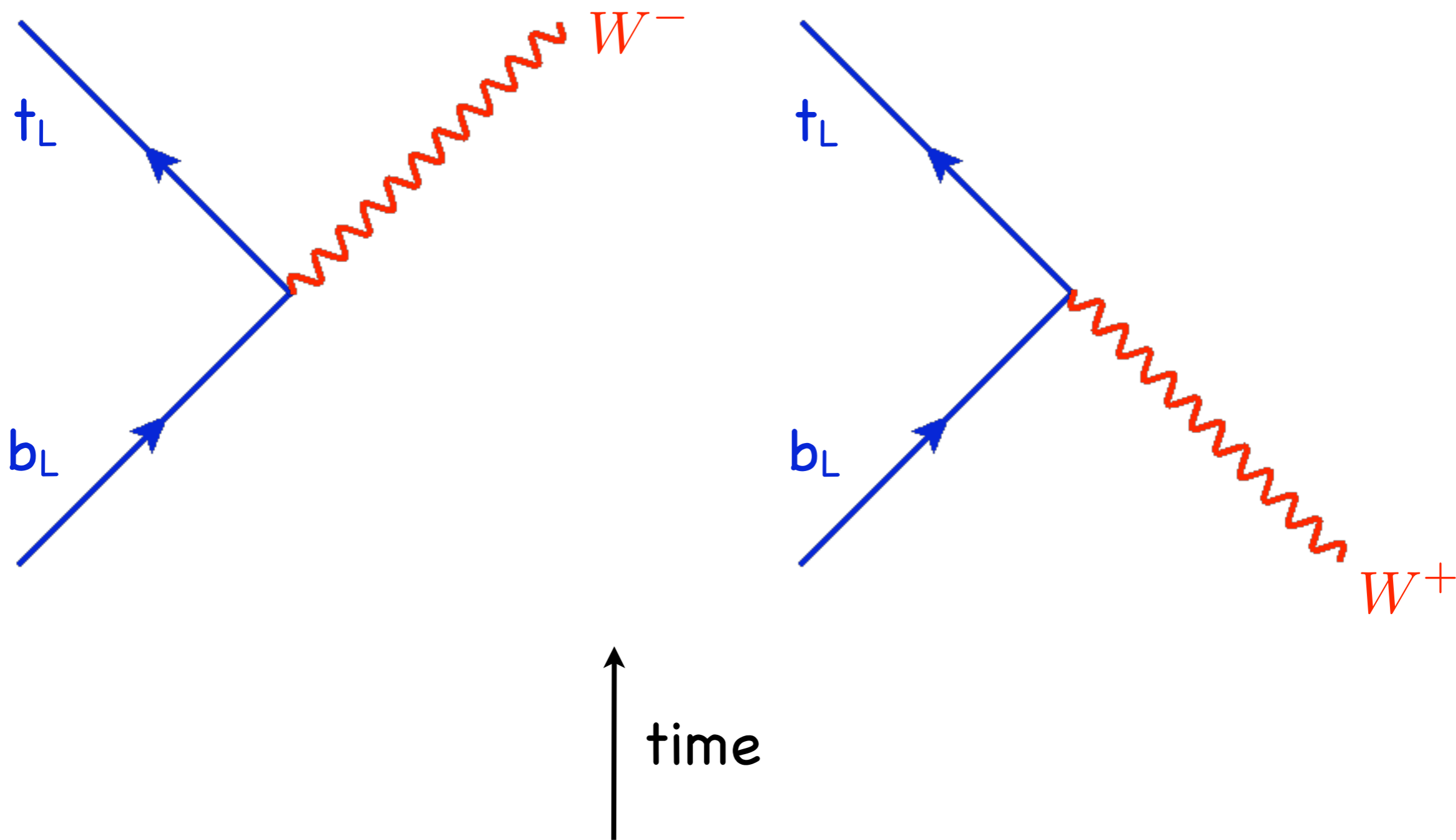
$SU(2)_L$ Weak Interactions



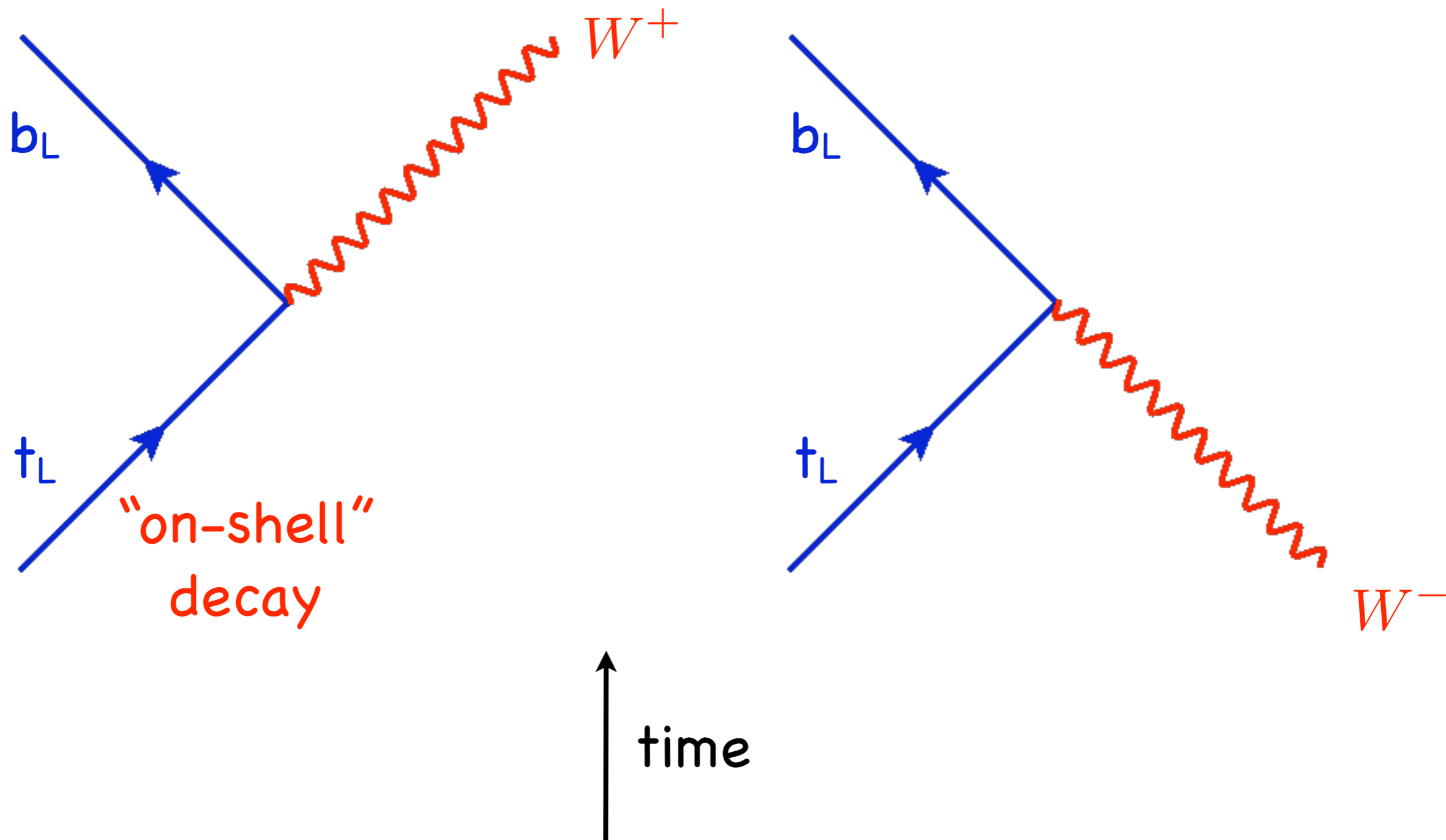
$SU(2)_L$ Weak Interactions



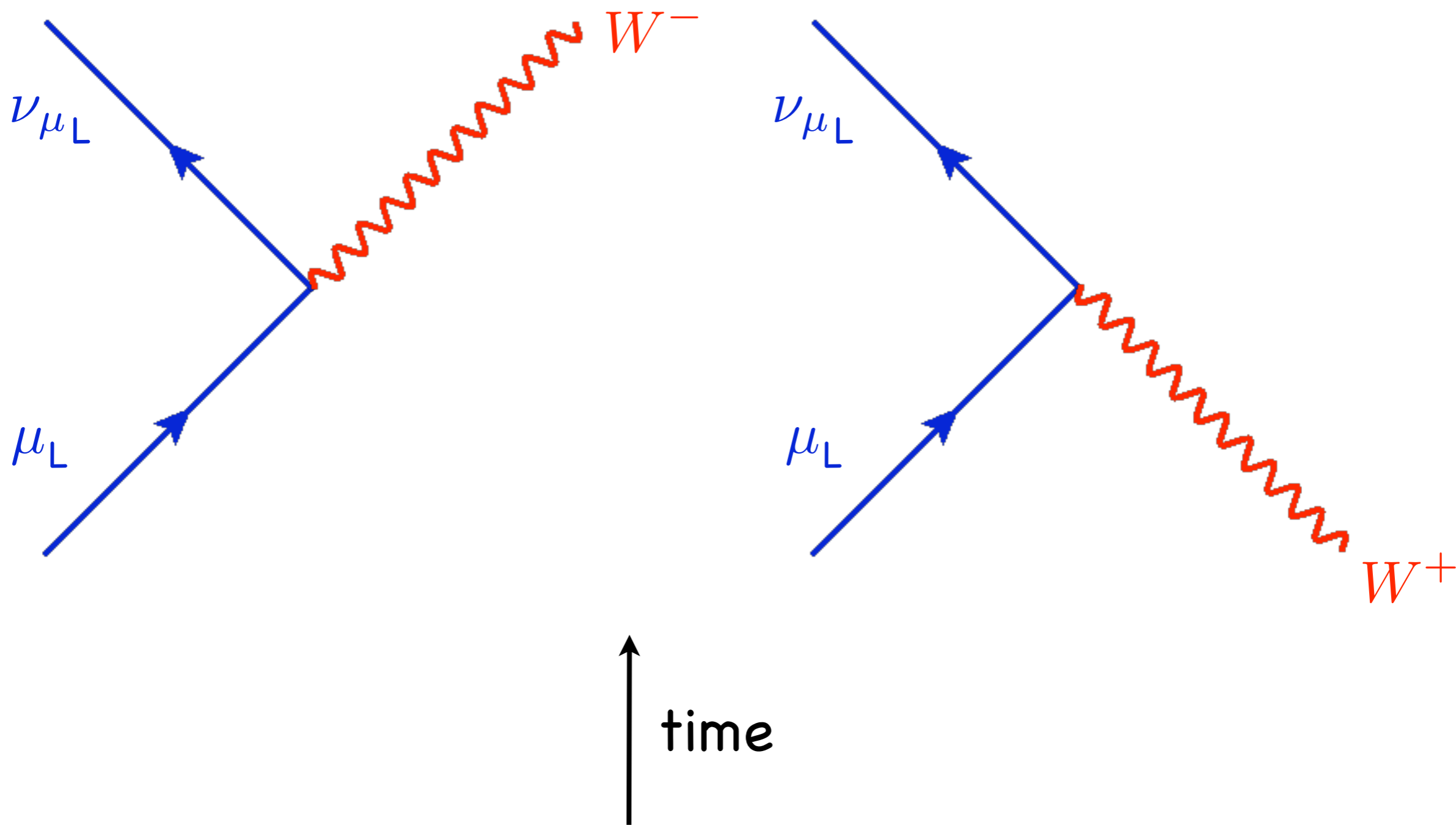
$SU(2)_L$ Weak Interactions



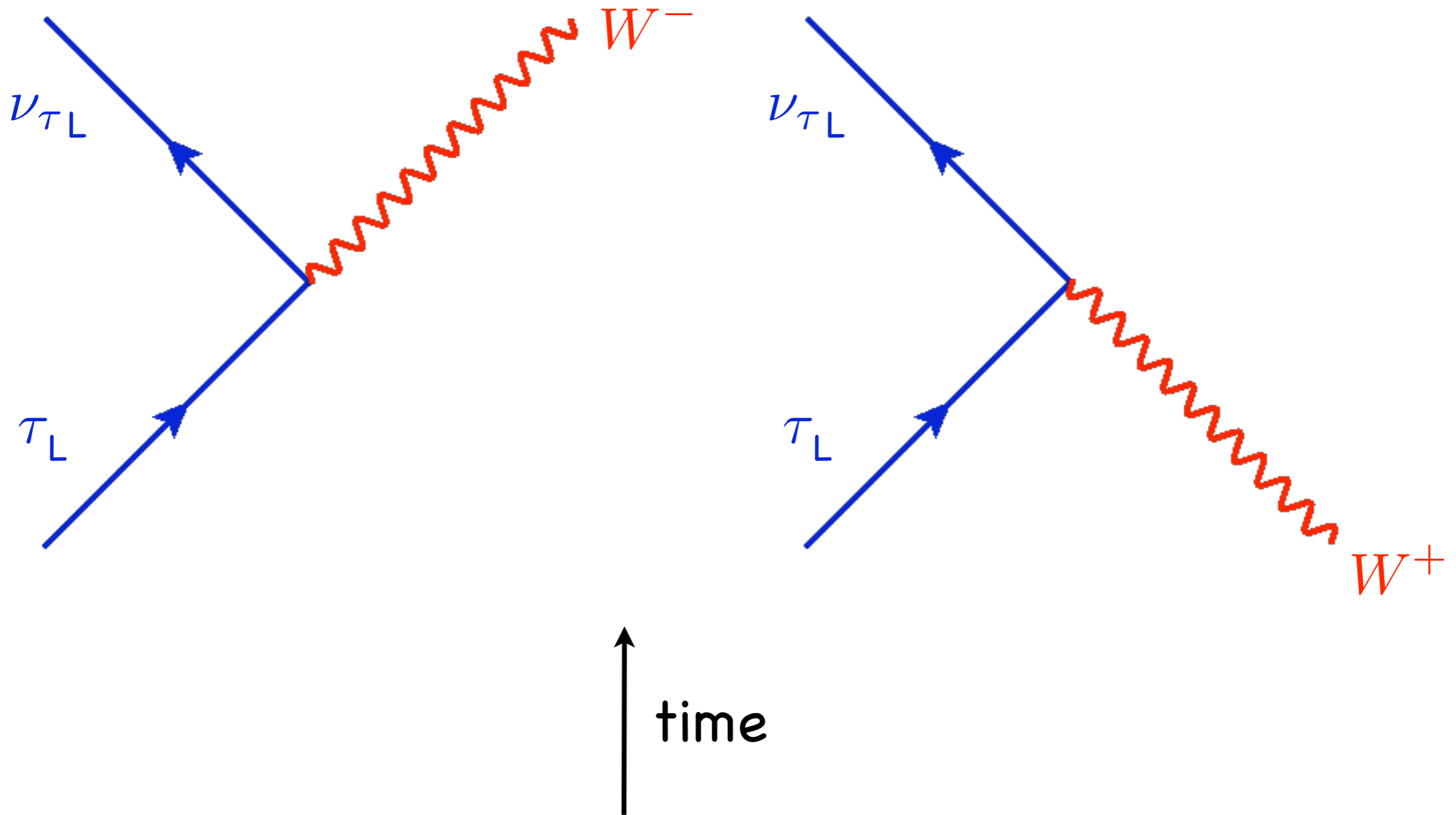
$SU(2)_L$ Weak Interactions



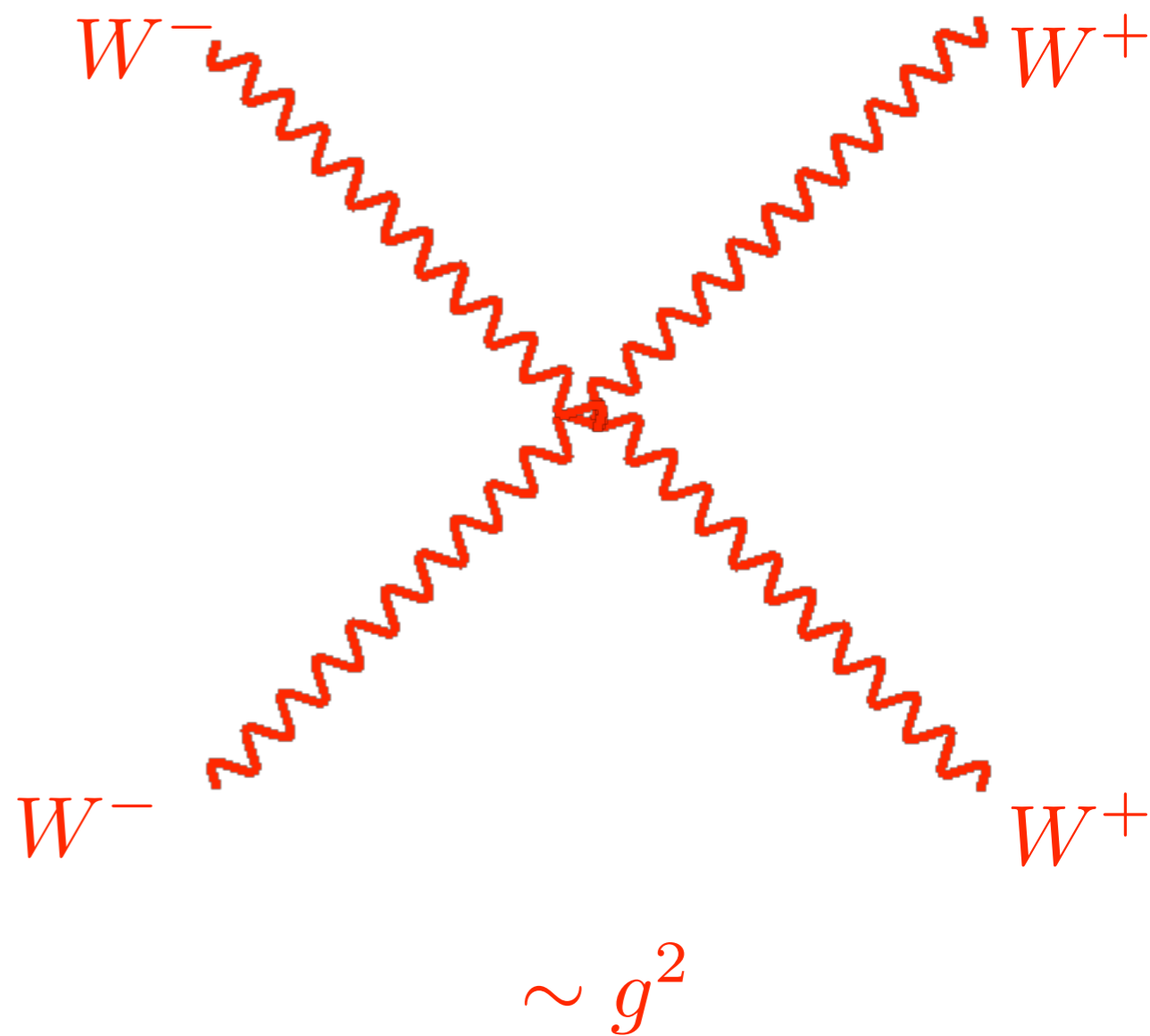
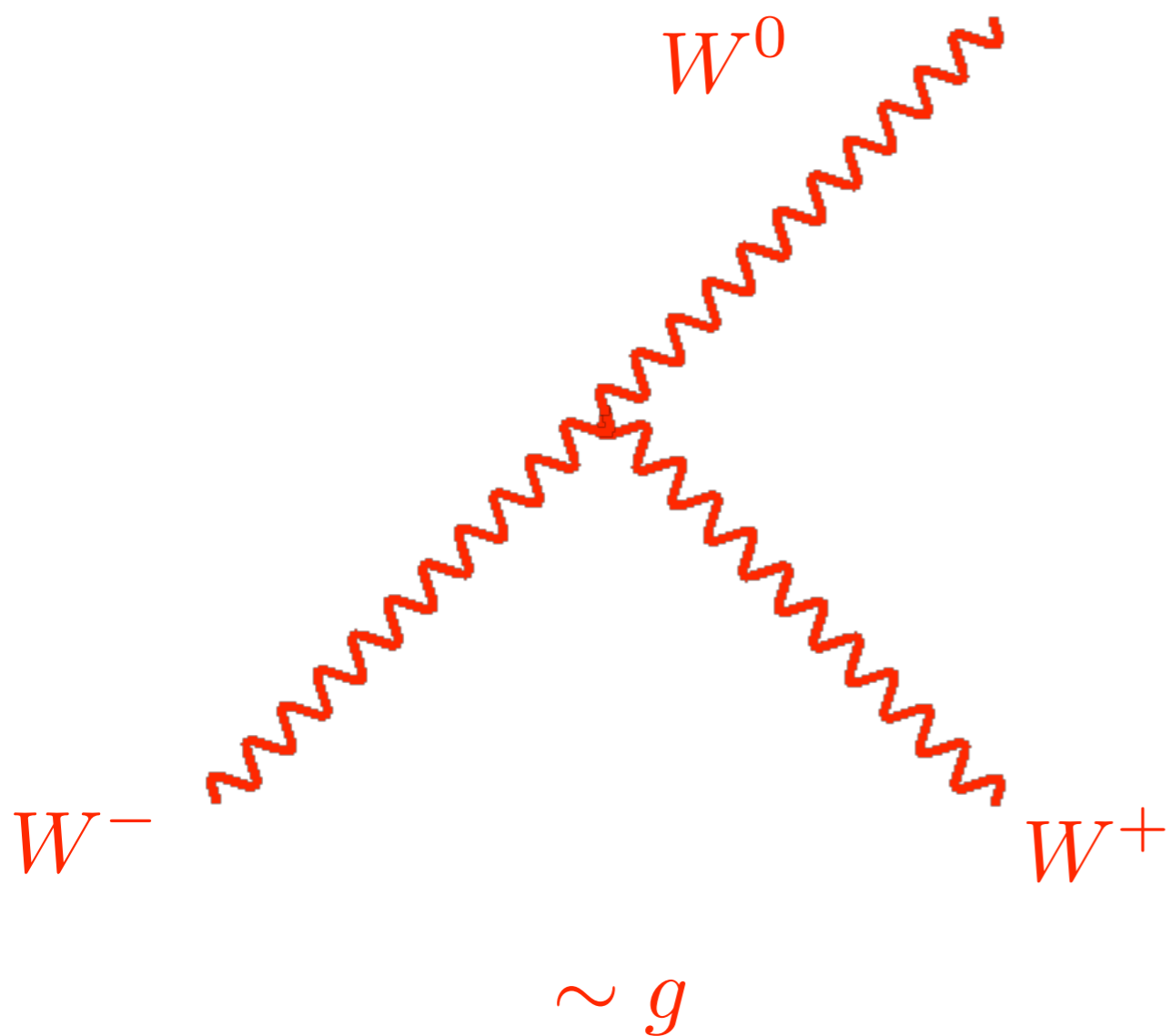
$SU(2)_L$ Weak Interactions



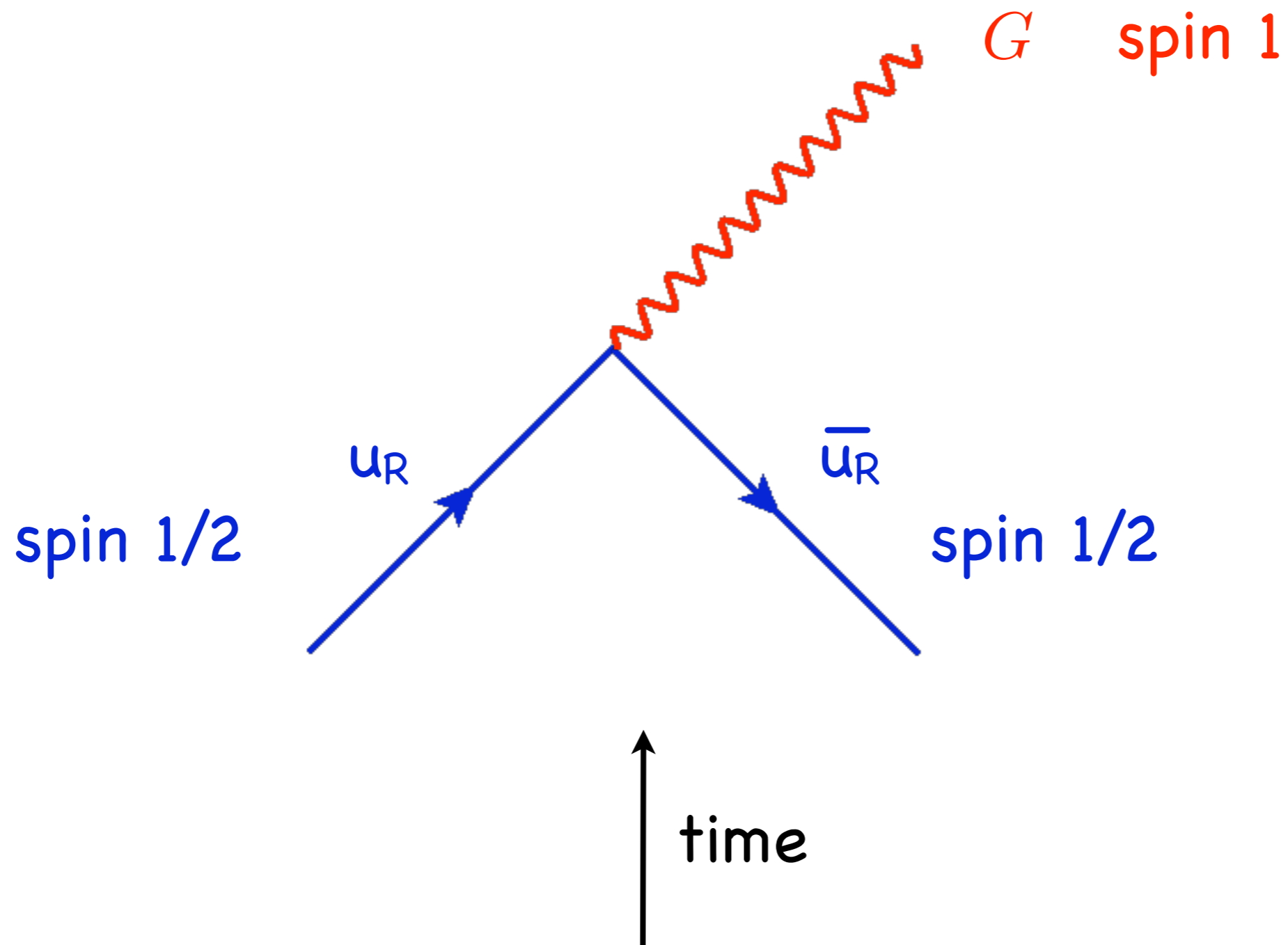
$SU(2)_L$ Weak Interactions



$SU(2)_L$ Weak Interactions

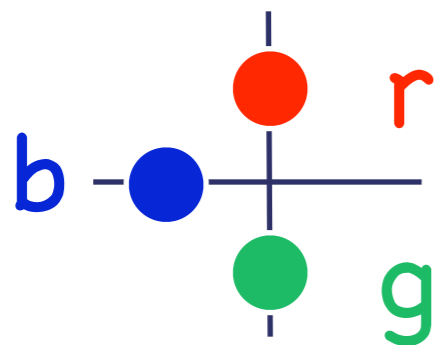


$SU(3)_c$

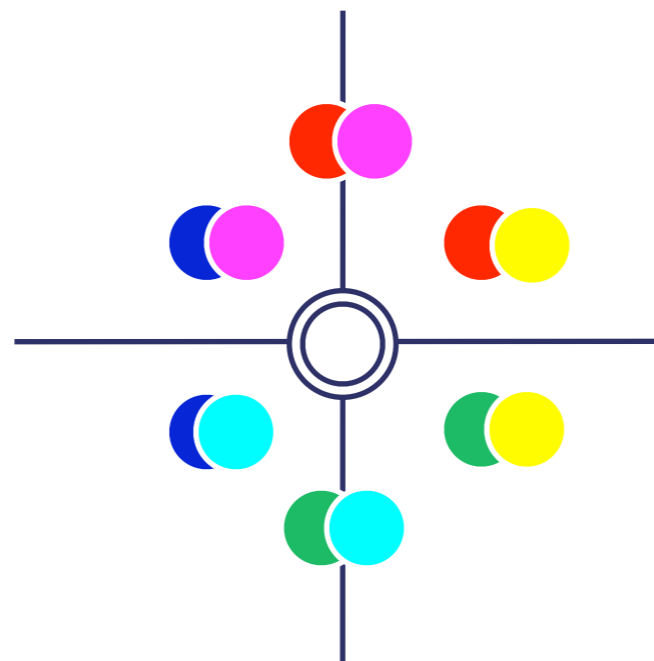


$SU(3)_c$ Gauge Bosons

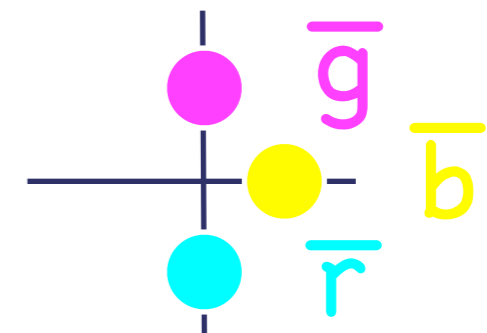
adding $SU(3)$ charges:



three quarks

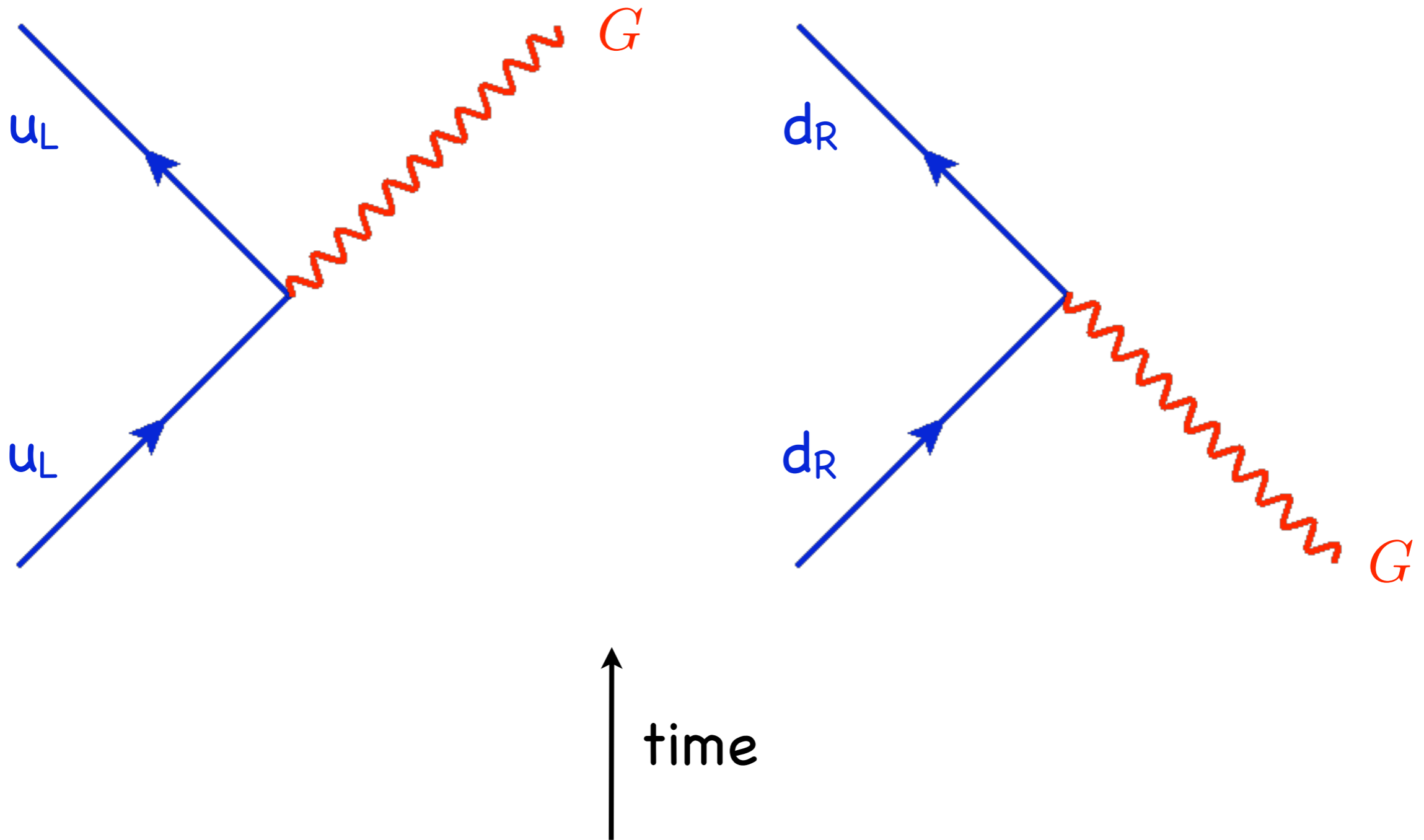


eight gluons



three antiquarks

SU(3) Color Interactions

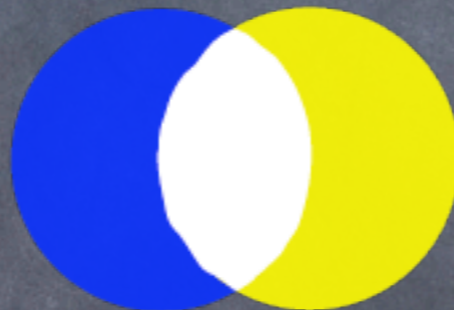


Colors



R

\bar{R}



B

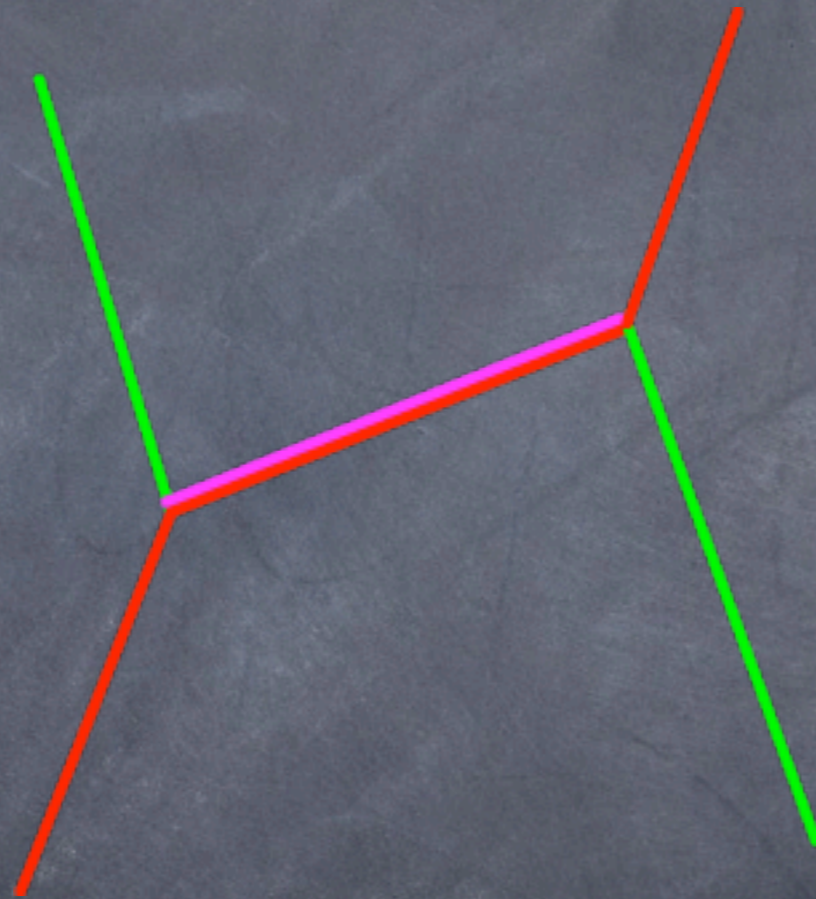
\bar{B}



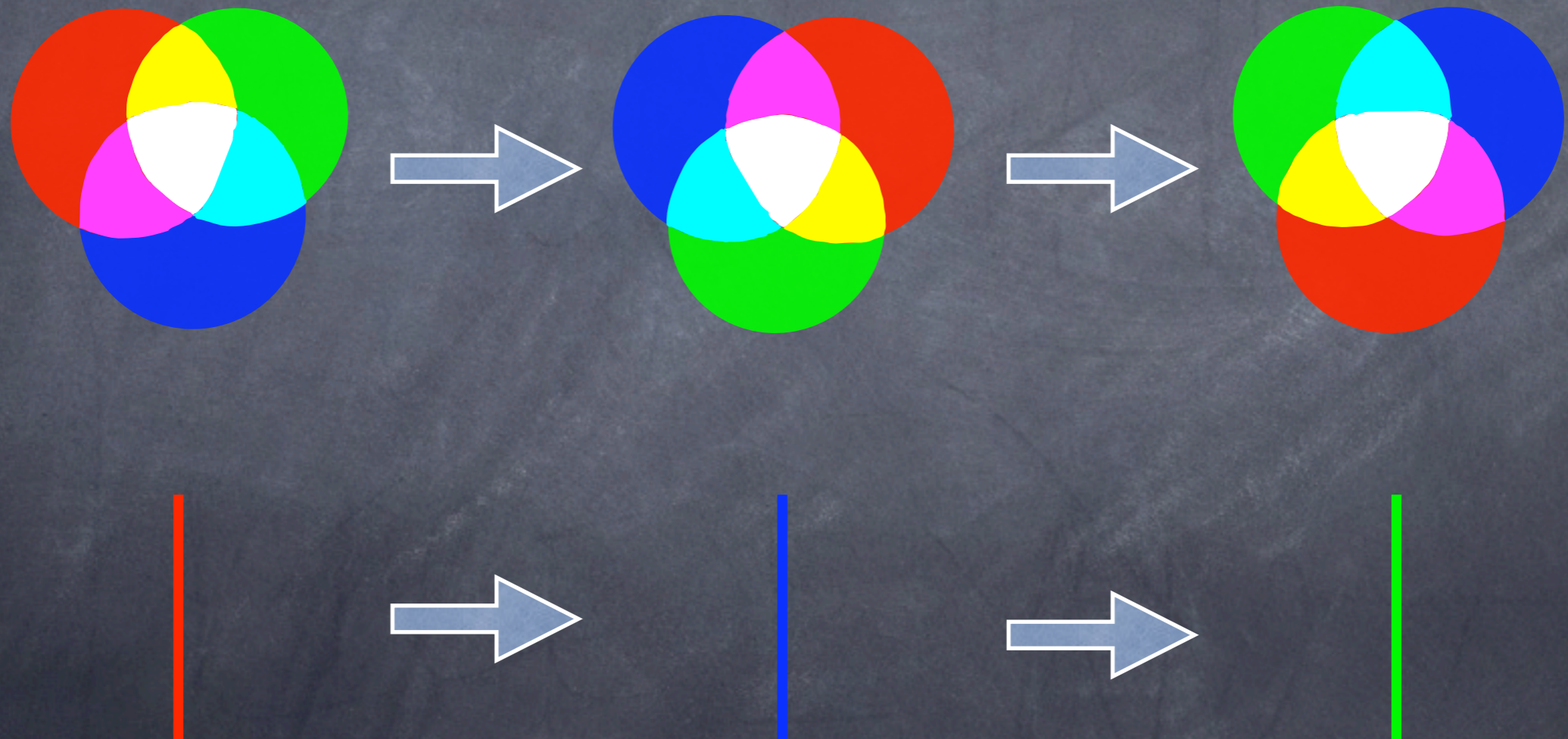
G

\bar{G}

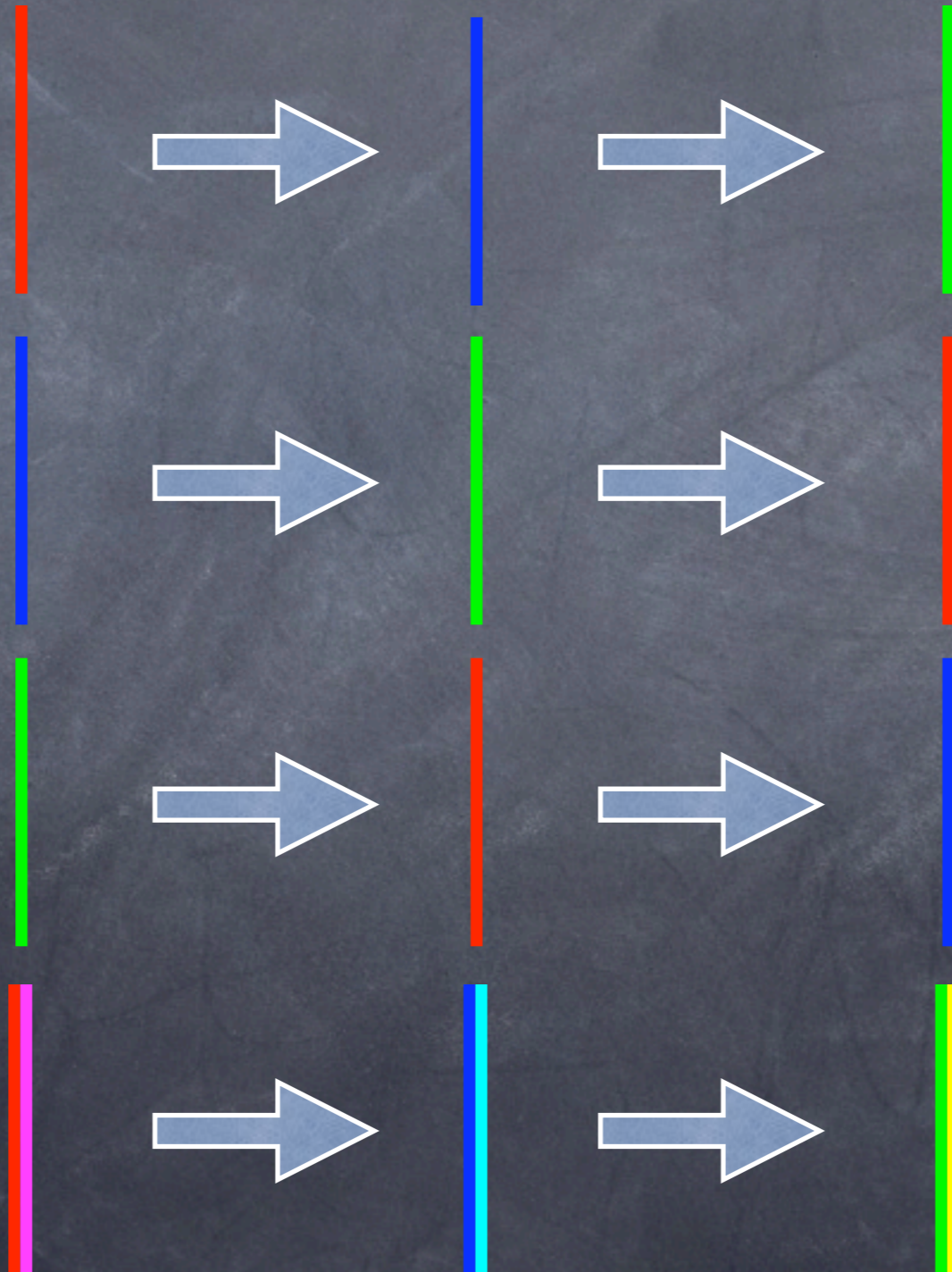
Color Exchange



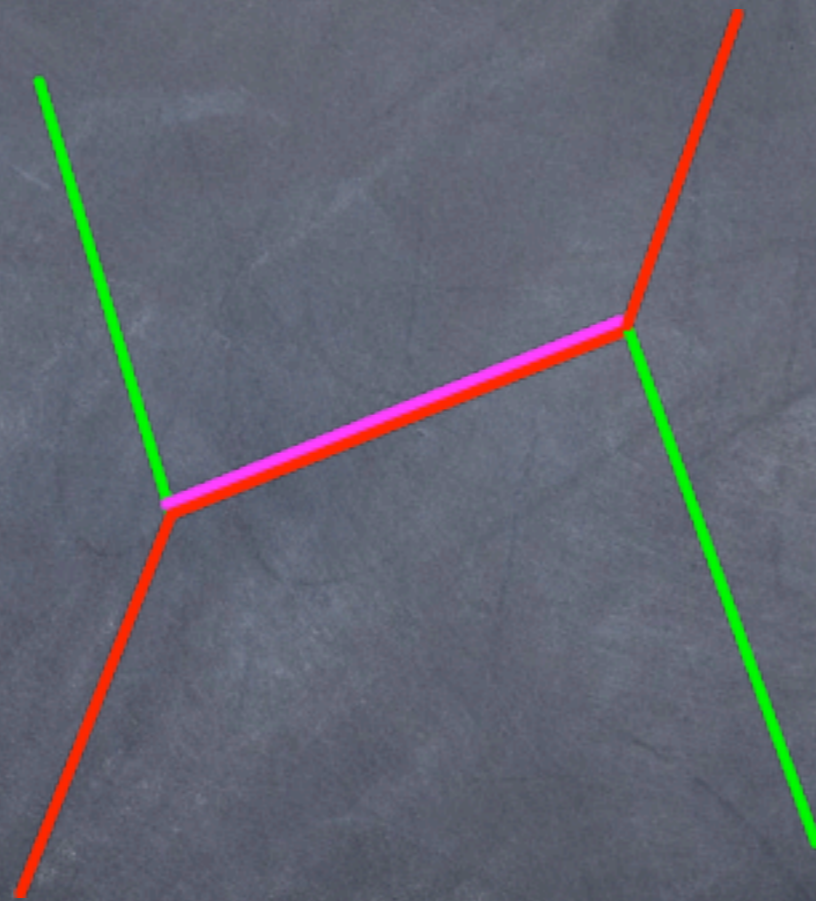
Color Gauge Symmetry



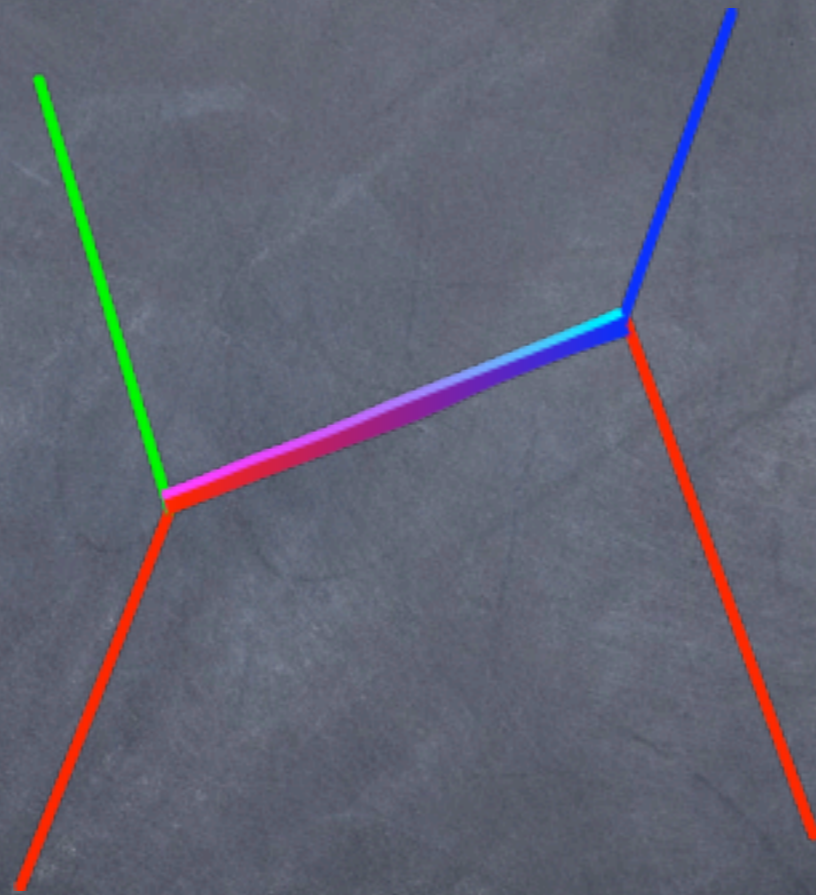
Color Gauge Symmetry



Color Exchange



Local Color Symmetry



Local Color Symmetry

