

The Hidden Geometry of Particle Collisions

Jesse Thaler



Joint Theory Seminar, UC Davis — November 16, 2020

Wearing my New Hat...

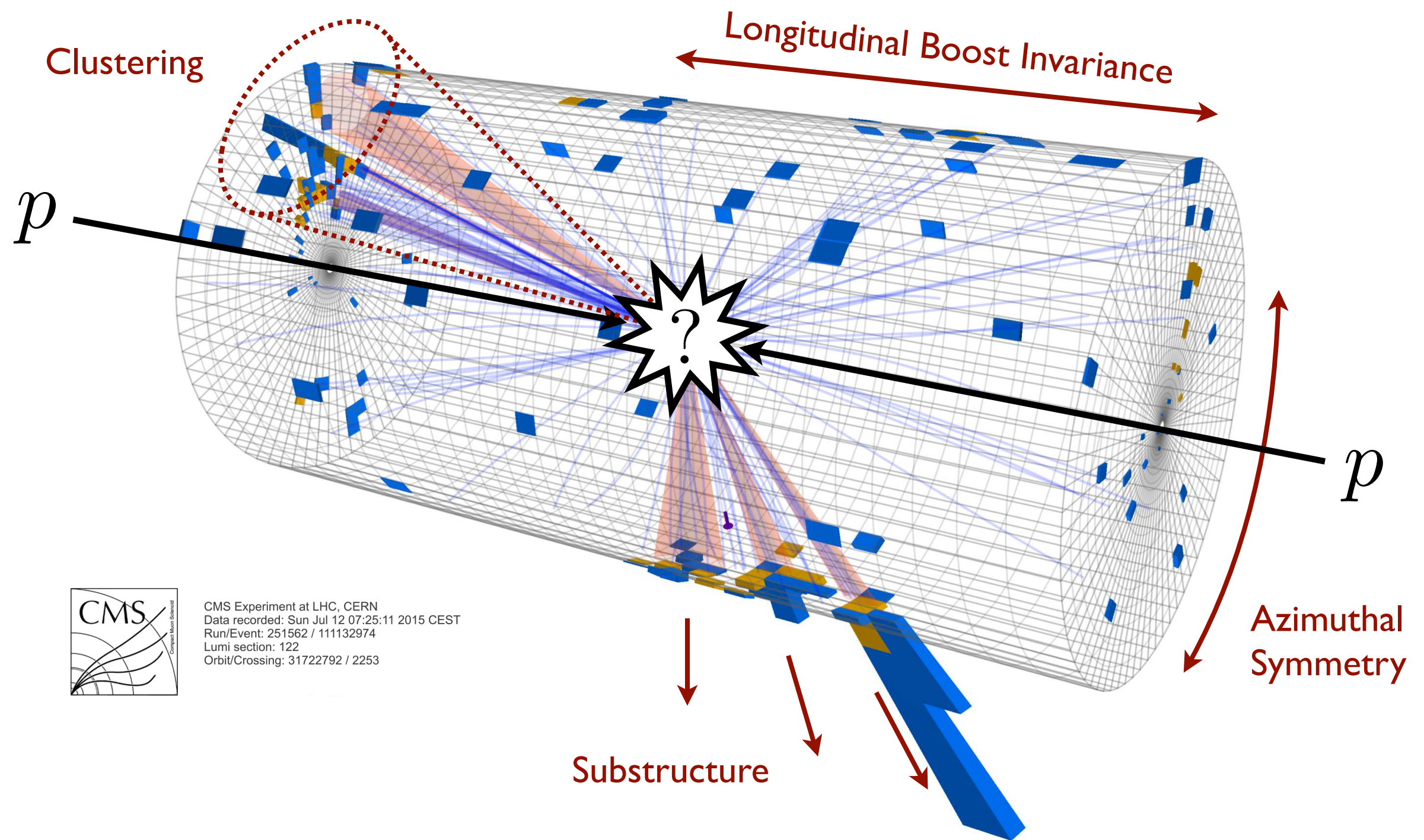


The NSF AI Institute for Artificial Intelligence and Fundamental Interactions



<http://iaifi.org/>

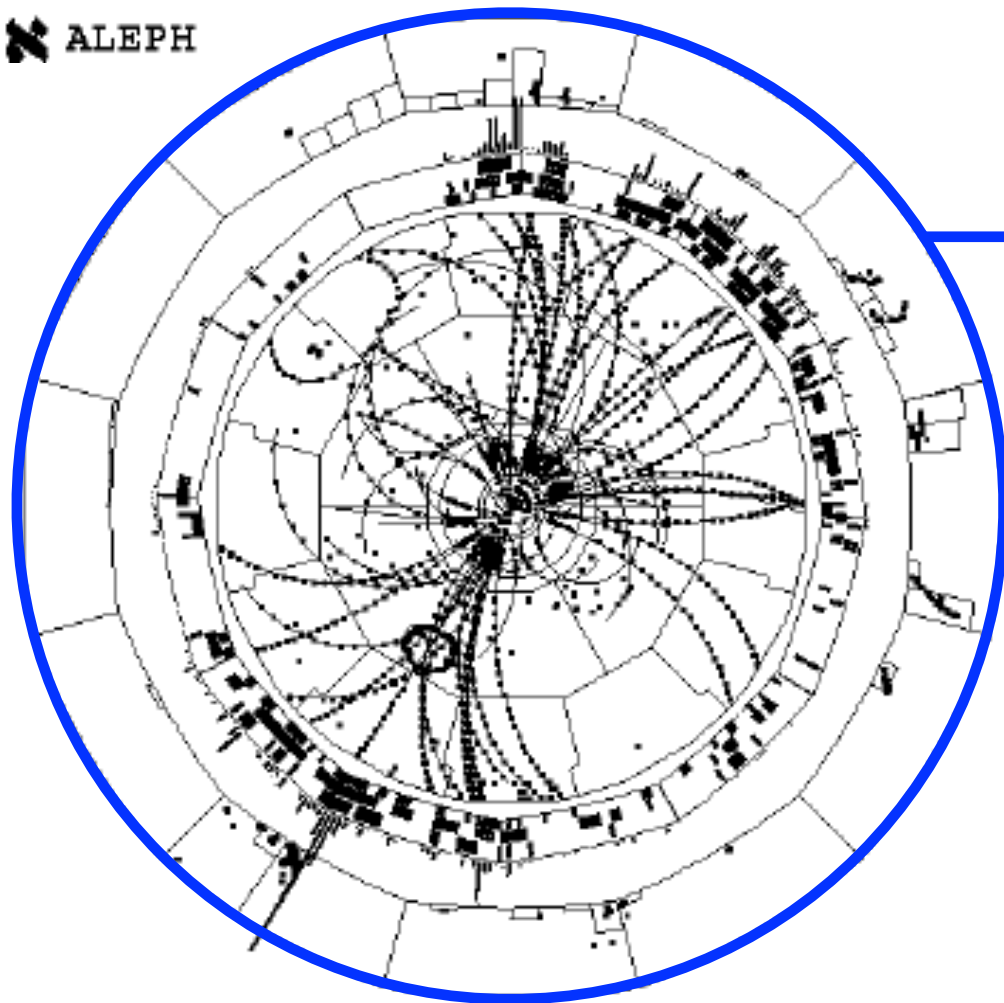
The Manifest Geometry of One Collision



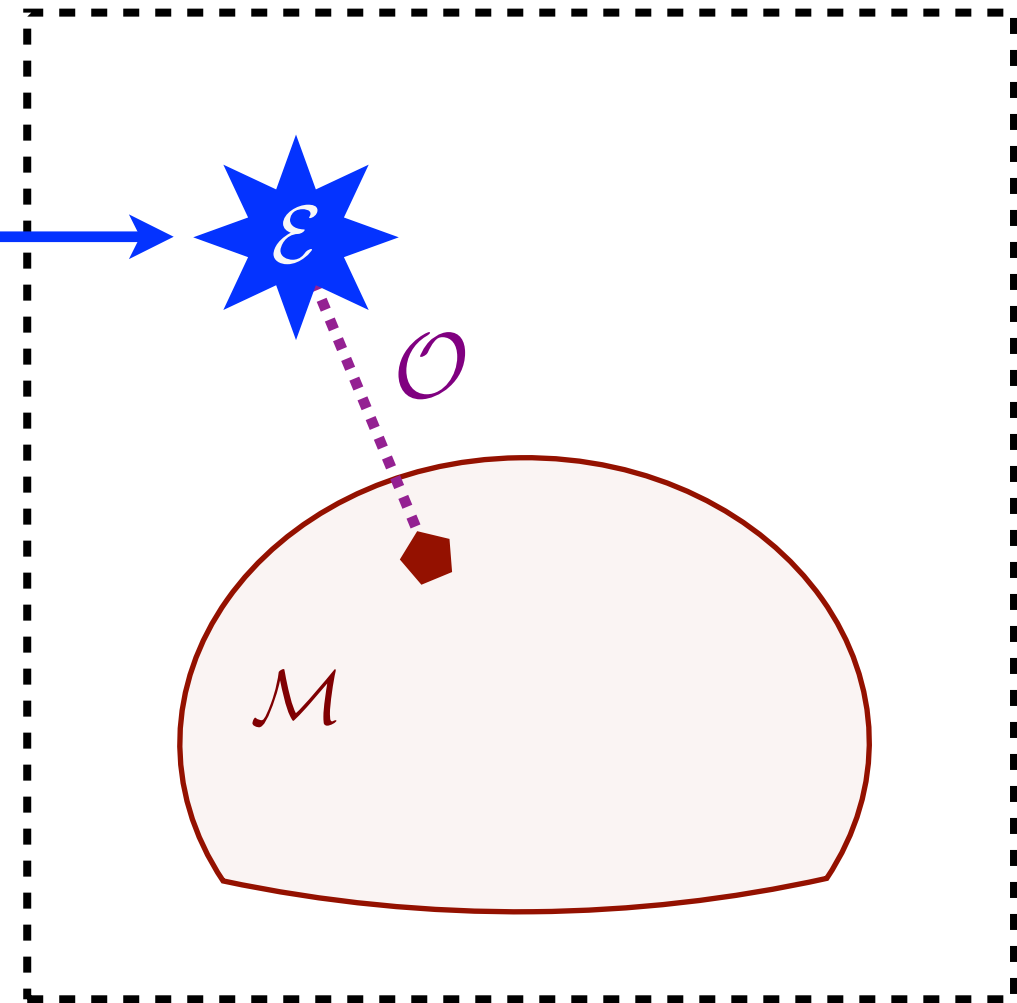
The Hidden Geometry of Particle Collisions

E.g. Classic QCD Event Shapes

ALEPH



One Electron-Positron Event

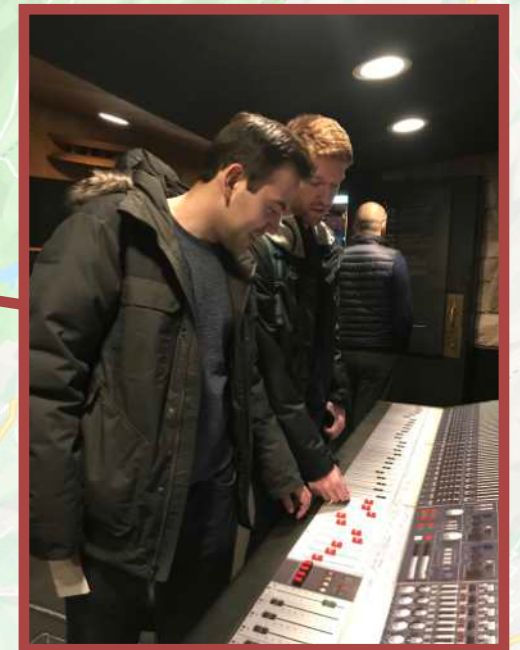


Distance to a Manifold in Event Space

[Komiske, Metodiev, JDT, JHEP 2020]

[Brandt, Peyrou, Sosnowski, Wroblewski, PL 1964; Farhi, PRL 1977]

Scenes from My Sabbatical



Eric Methodiev

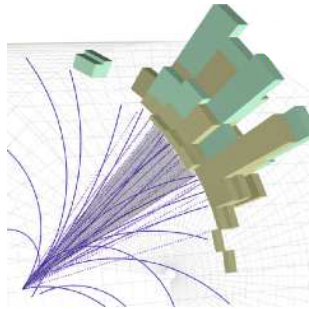
Patrick Komiske

[February 2019;
Simons Sabbatical Fellowship]

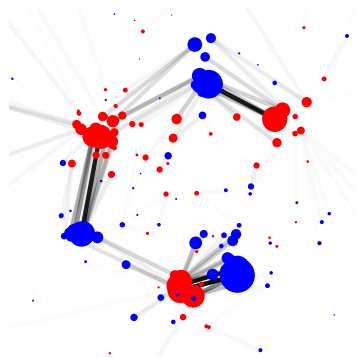


Grand Combin

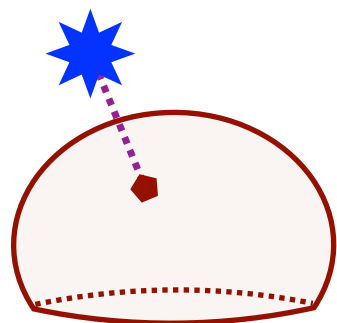
Outline



What is a Collider Event?



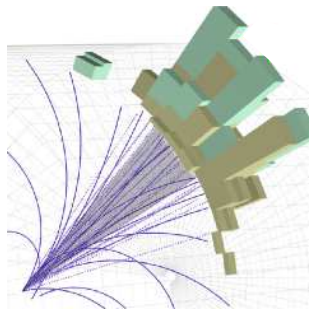
When are Events Similar?



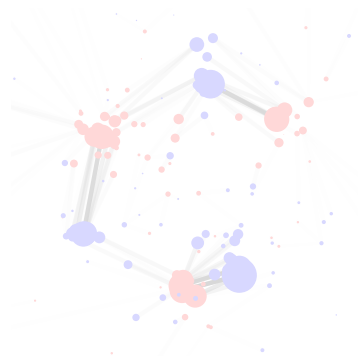
What can be Geometrized?

Pause

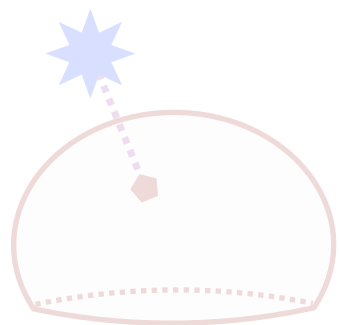
Interrupt me or drop questions in the chat, and I'll try to answer them as I go



What is a Collider Event?



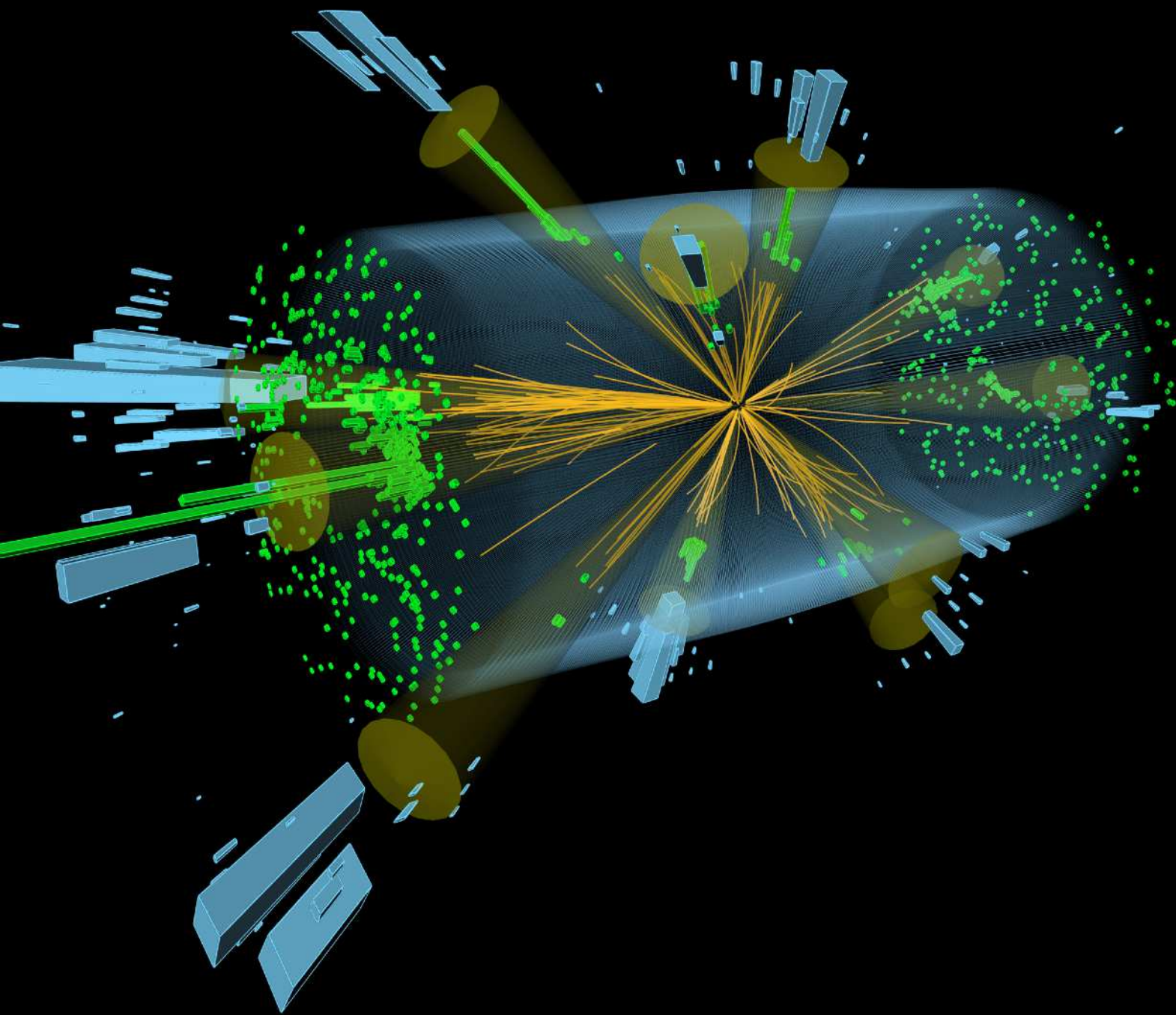
When are Events Similar?



What can be Geometrized?

Collider Event

Collection of points in (momentum) space



T E H M

	●	γ	photon	elementary	
●	●	e^{\pm}	electron		
●	●	●	μ^{\pm}		muon
●	●	●	π^{\pm}	pion	composite
●	●	●	K^{\pm}	kaon	
	●	●	K_L^0	K-long	
●	●	●	p/\bar{p}	proton	
	●	●	n/\bar{n}	neutron	

elementary

composite

Point Cloud

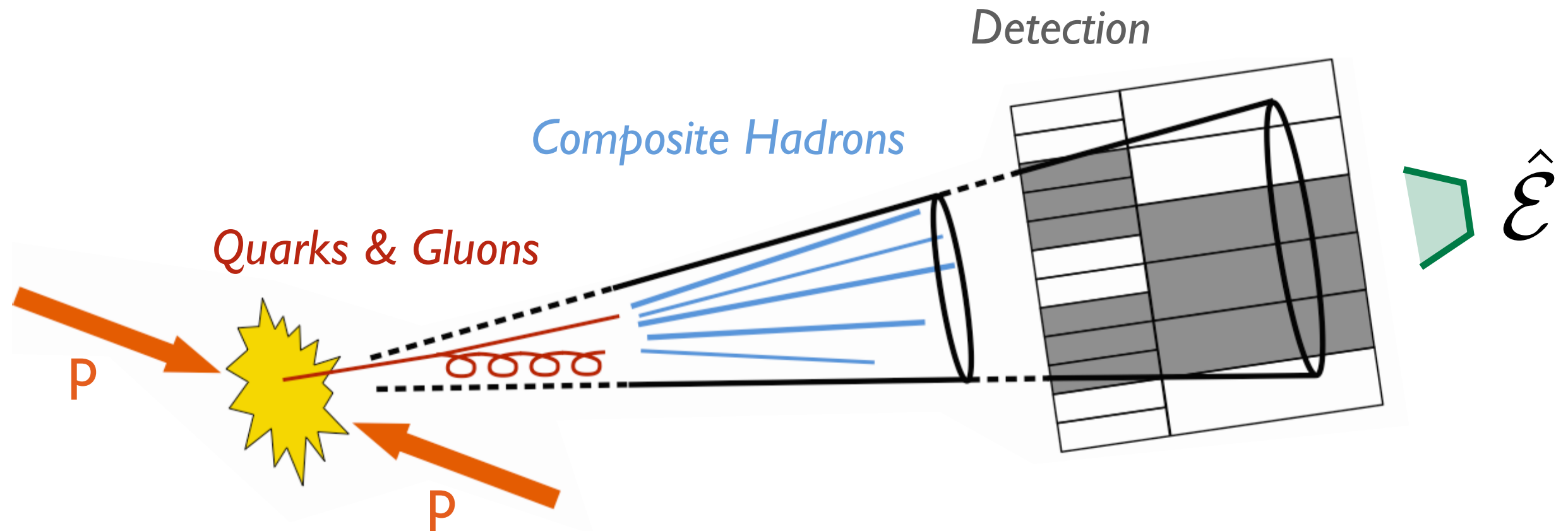
Collection of points in (position) space



[Popular Science, 2013]

Jet Formation from QCD

Theory



Energy Flow:

Robust to hadronization and detector effects
Well-defined for massless gauge theories

$$\hat{\mathcal{E}} \simeq \lim_{t \rightarrow \infty} \hat{n}_i T^{0i}(t, vt\hat{n})$$

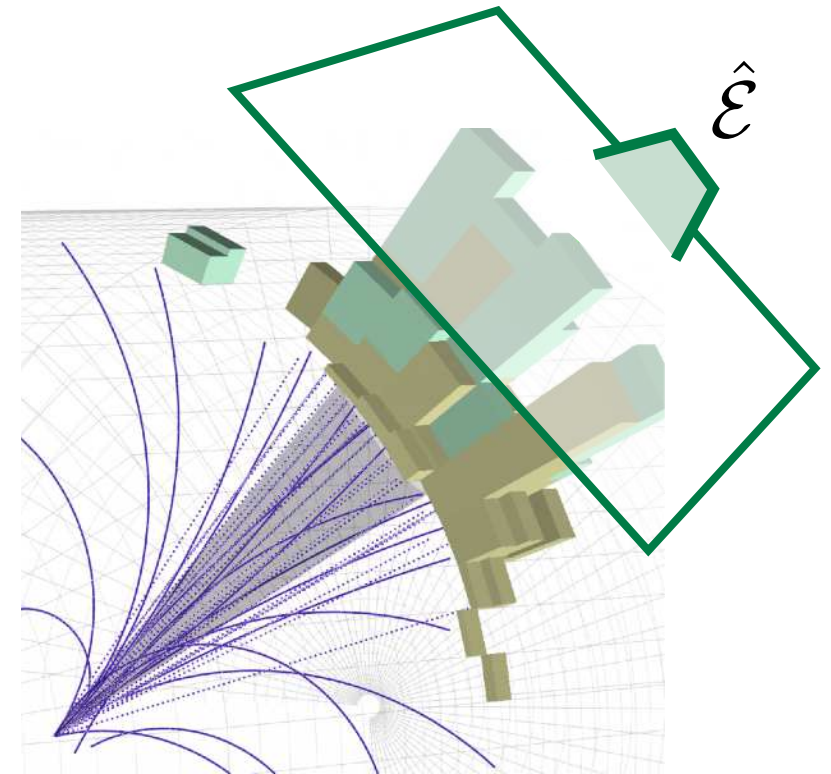
[see e.g. Sveshnikov, Tkachov, [PLB 1996](#); Hofman, Maldacena, [JHEP 2008](#); Mateu, Stewart, [JDT, PRD 2013](#); Belitsky, Hohenegger, Korchemsky, Sokatchev, Zhiboedov, [PRL 2014](#); Chen, Mout, Zhang, Zhu, [PRD 2020](#)]

Jets as **Weighted Point Clouds**

- **Energy-Weighted Directions**

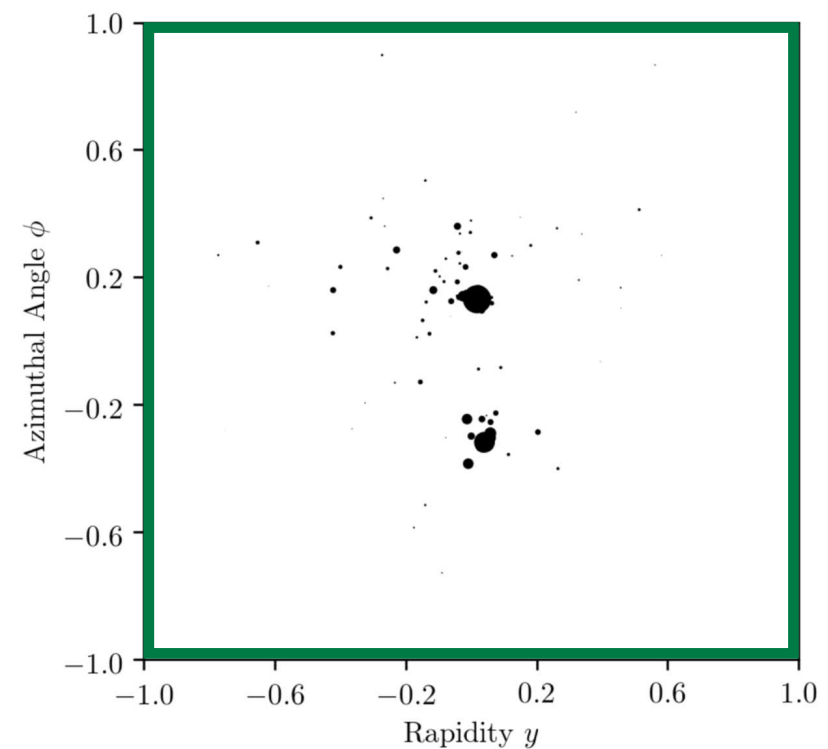
$$\vec{p} = \left\{ \underset{\substack{\uparrow \\ \text{Energy}}}{E}, \underbrace{\hat{n}_x, \hat{n}_y, \hat{n}_z}_{\text{Direction}} \right\}$$

(suppressing “unsafe” charge/flavor information)



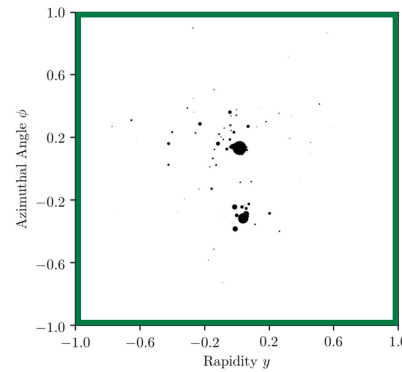
- Equivalently: **Energy Density**

$$\rho(\hat{n}) = \sum_{i \in \mathcal{J}} \underset{\substack{\uparrow \\ \text{Energy}}}{E_i} \delta^{(2)}(\hat{n} - \underset{\substack{\uparrow \\ \text{Direction}}}{\hat{n}_i})$$



Pause

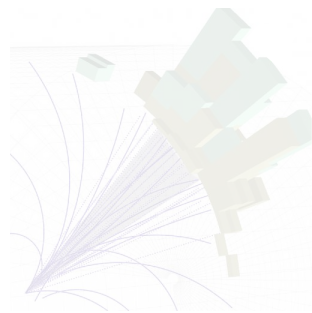
What is a Collider Event?



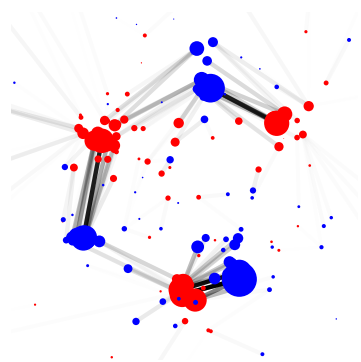
“Calo” Energy Density

$$\mathcal{E}(\hat{n}) = \sum_i E_i \delta(\hat{n} - \hat{n}_i)$$

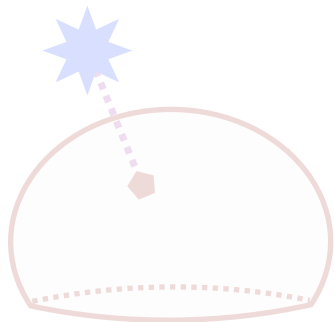
(see backup for relevance to ML and QCD)



What is a Collider Event?



When are Events Similar?

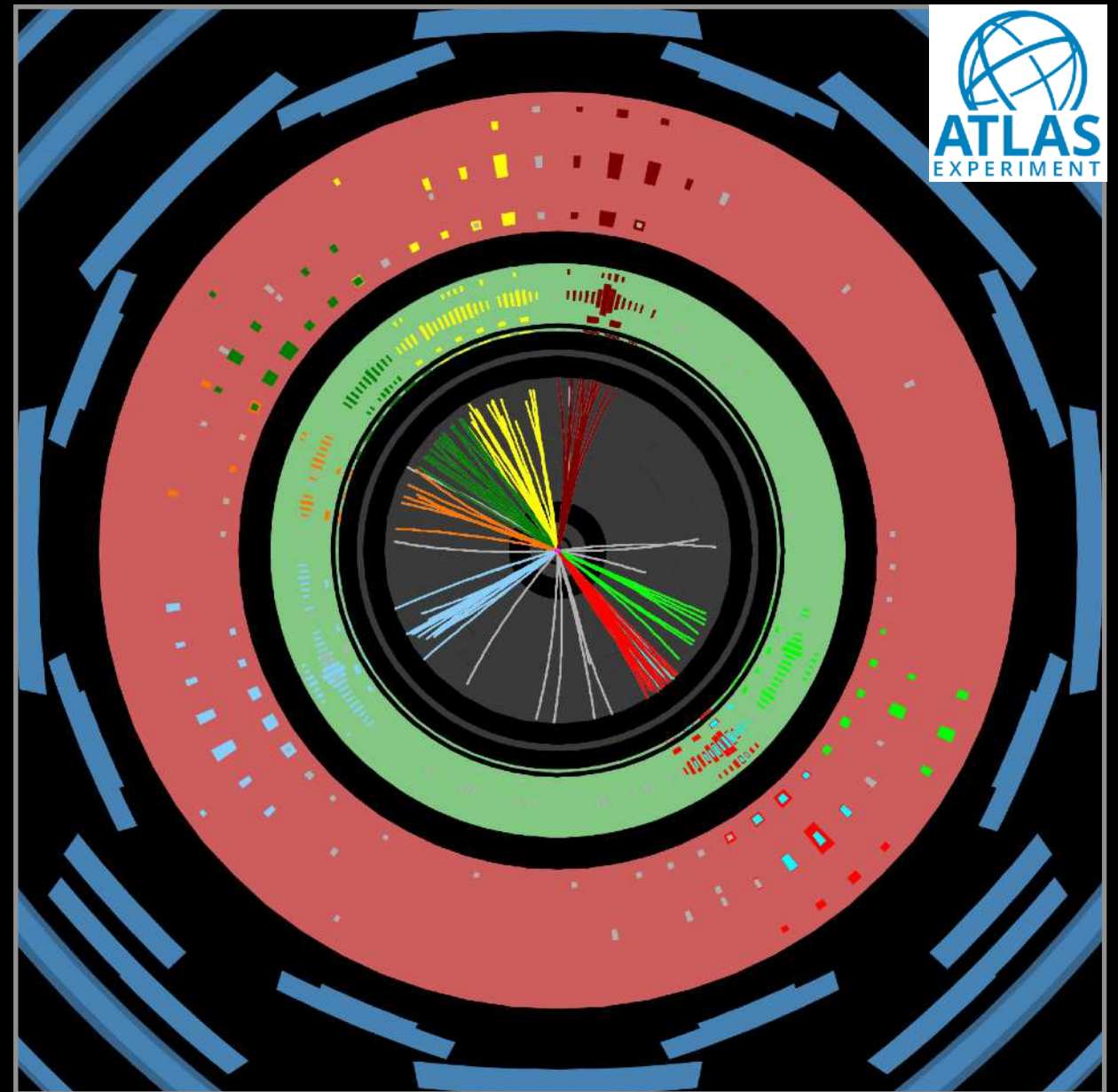
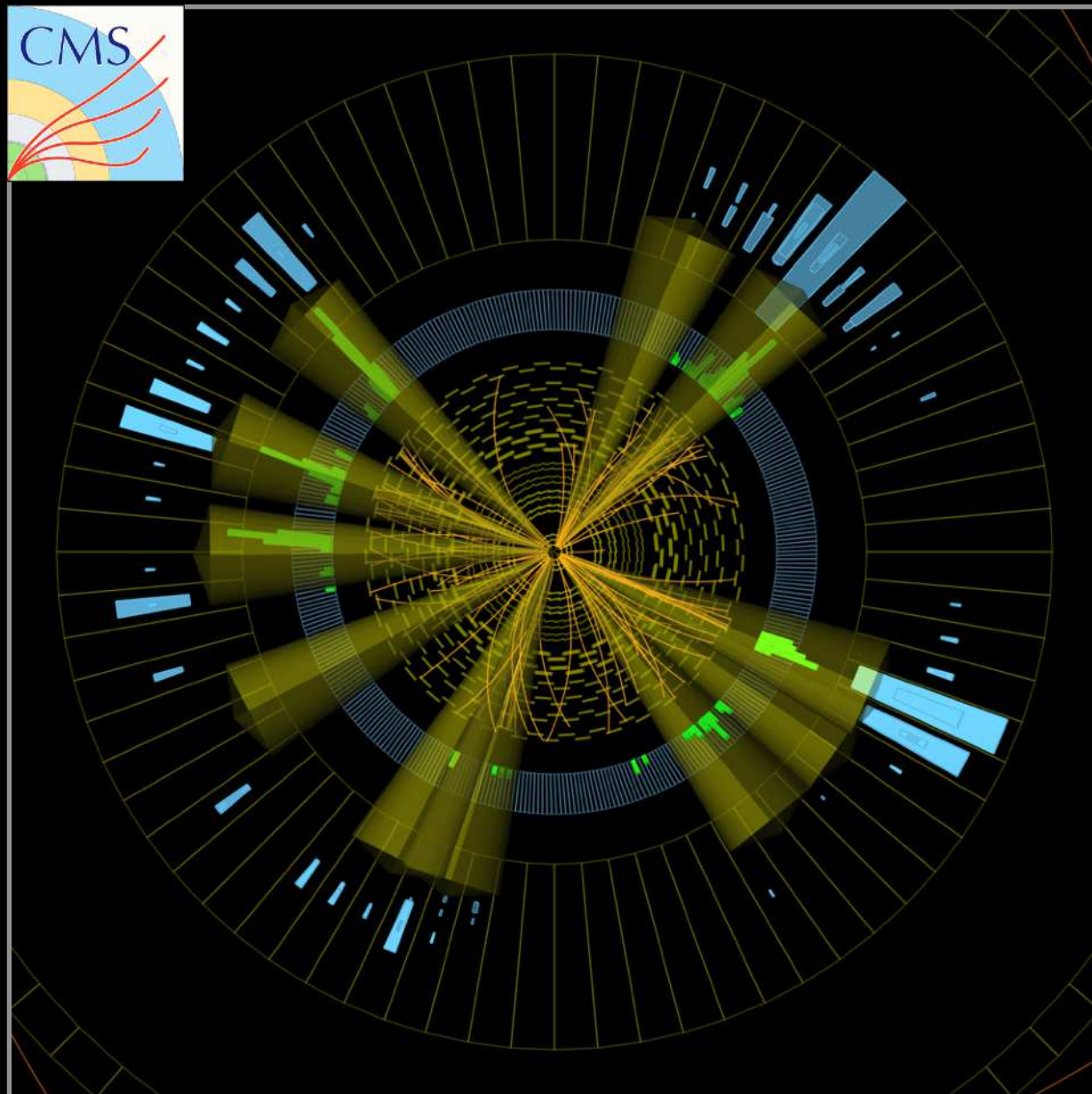
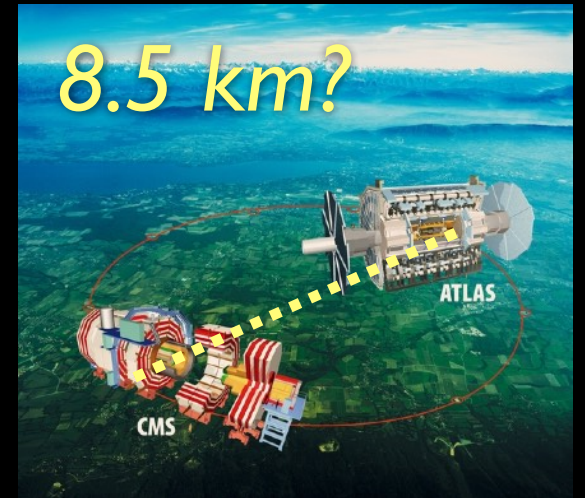


What can be Geometrized?

Two Collider Events

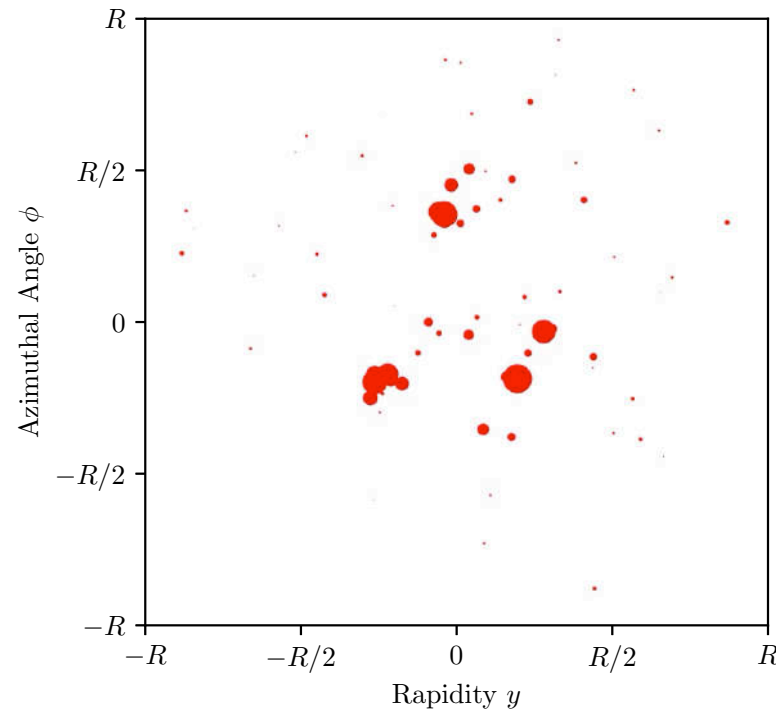
Two collections of points in (momentum) space

How “close” are these?



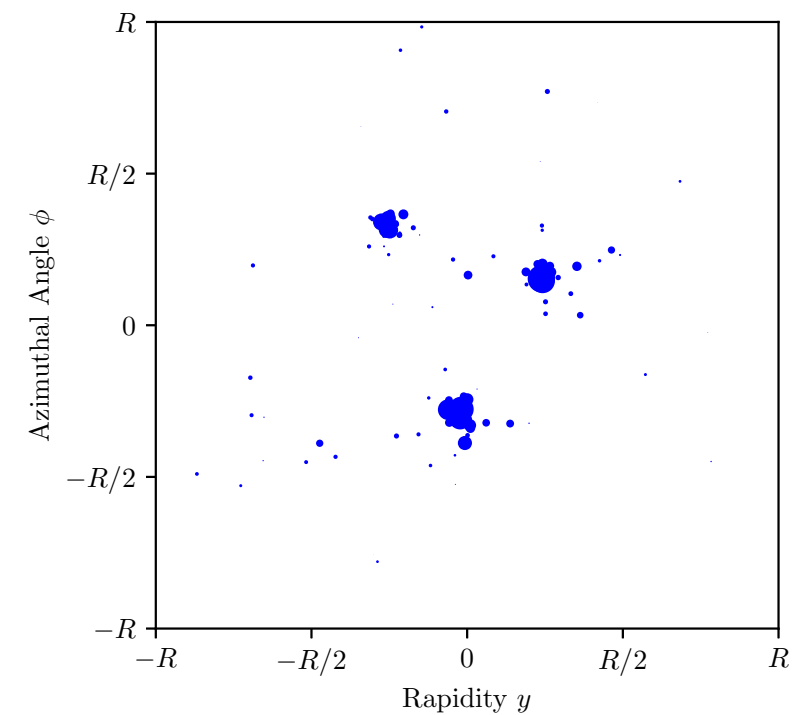
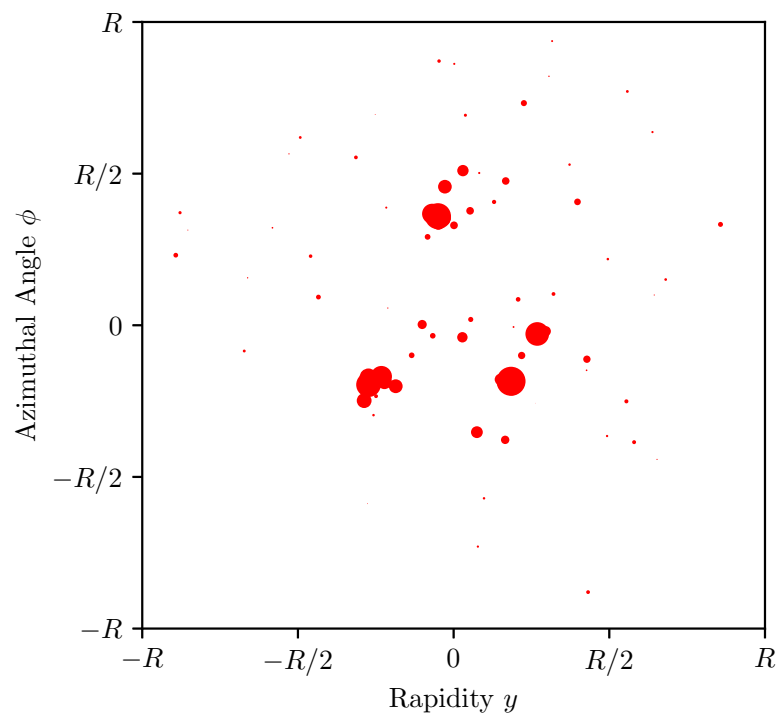
Similarity of Two Energy Flows?

$$\mathcal{E}(\hat{n}) = \sum_i E_i \delta(\hat{n} - \hat{n}_i)$$



Optimal Transport:

Earth Mover's Distance
a.k.a. *1-Wasserstein metric*



[Komiske, Metodiev, JDT, [PRL 2019](#); code at Komiske, Metodiev, JDT, [energyflow.network](#)]

The Earth Mover's Distance

Optimal Transport:

[Peleg, Werman, Rom, [IEEE 1989](#);
Rubner, Tomasi, Guibas, [ICCV 1998](#), [ICJV 2000](#);
Pele, Werman, [ECCV 2008](#); Pele Taskar, [GSI 2013](#)]

Minimum “work” (stuff x distance) to make one distribution look like another distribution



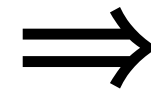
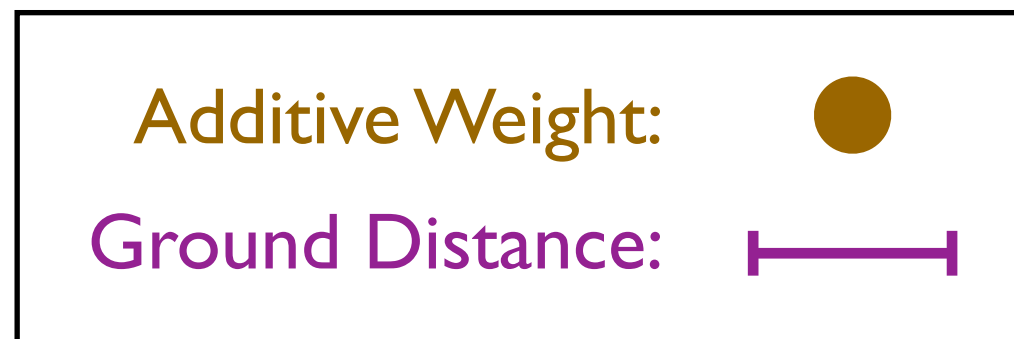
[h/t Niles-Weed, [ML4jets 2020](#); Monge, 1781; Vaserštejn, 1969; [Wikipedia](#)]

The Earth Mover's Distance

Optimal Transport:

[Peleg, Werman, Rom, [IEEE 1989](#);
Rubner, Tomasi, Guibas, [ICCV 1998](#), [ICJV 2000](#);
Pele, Werman, [ECCV 2008](#); Pele Taskar, [GSI 2013](#)]

Minimum “work” (stuff x distance) to make
one distribution look like another distribution

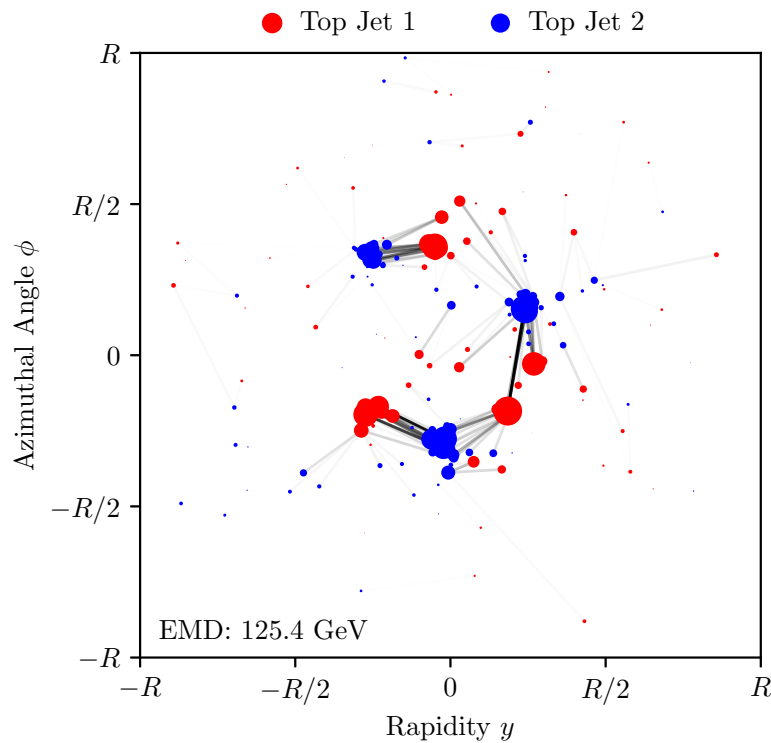
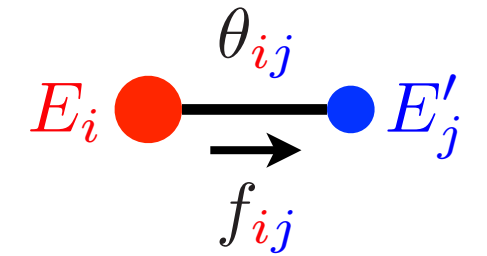


Distance Between
Distributions



[h/t Niles-Weed, [ML4jets 2020](#); Monge, 1781; Vaserštejn, 1969; [Wikipedia](#)]

The Energy Mover's Distance



Optimal transport between energy flows...

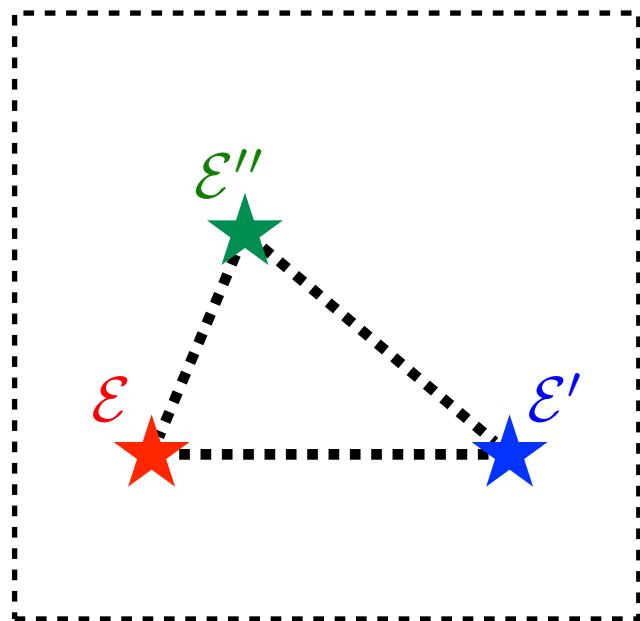
$$\text{EMD}(\mathcal{E}, \mathcal{E}') = \min_{\{f\}} \underbrace{\sum_i \sum_j f_{ij} \frac{\theta_{ij}}{R}}_{\text{Cost to move energy}} + \underbrace{\left| \sum_i E_i - \sum_j E'_j \right|}_{\text{Cost to create energy}}$$

↑
in GeV

...defines a metric on the space of events

$$0 \leq \text{EMD}(\mathcal{E}, \mathcal{E}') \leq \text{EMD}(\mathcal{E}, \mathcal{E}'') + \text{EMD}(\mathcal{E}', \mathcal{E}'')$$

(assuming $R \geq \theta_{\max}/2$, i.e. $R \geq$ jet radius for conical jets)



[Komiske, Metodiev, JDT, PRL 2019;

see also Pele, Werman, ECCV 2008; Pele, Taskar, GSI 2013;

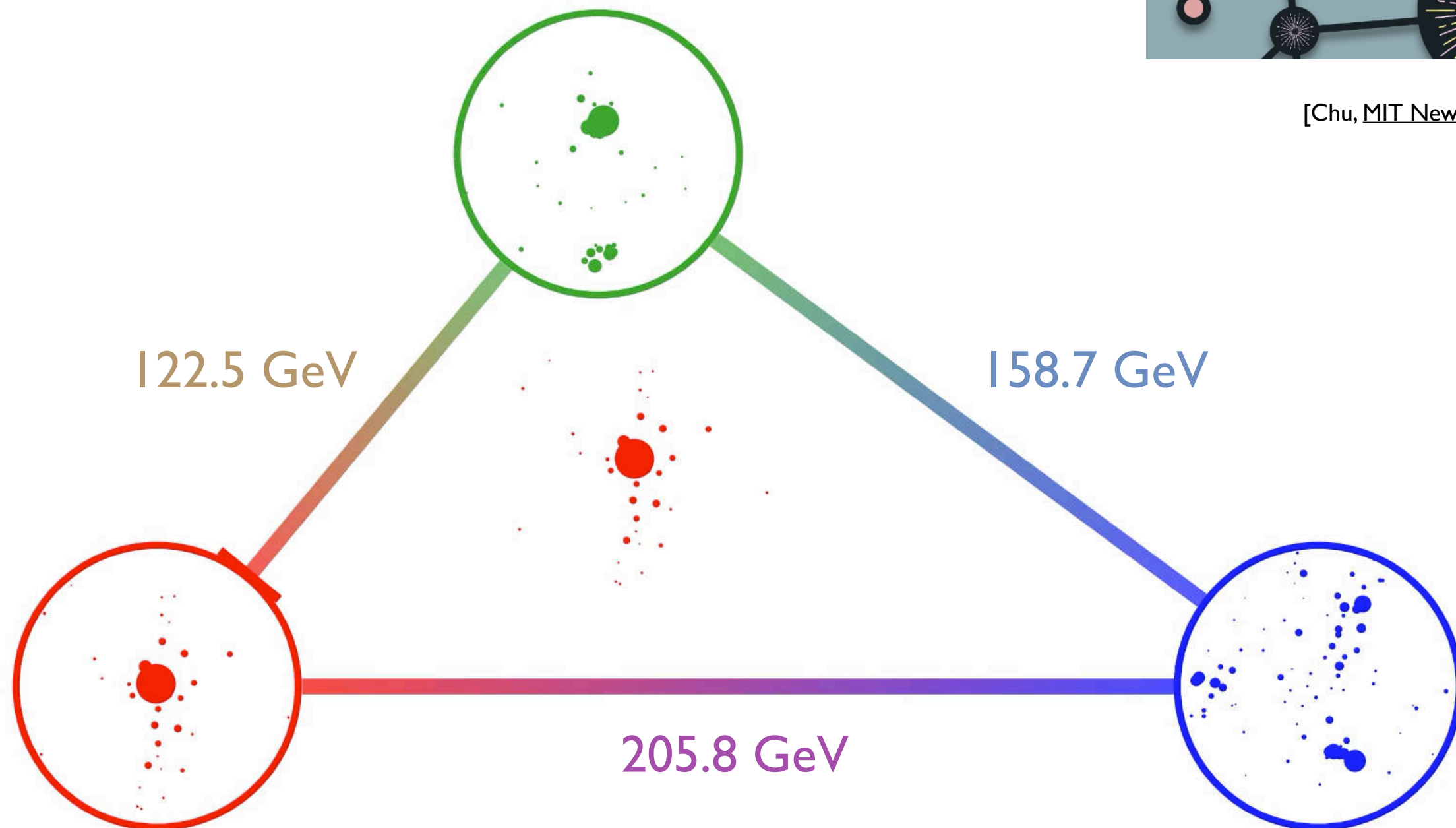
[see flavored variant in Crispim Romão, Castro, Milhano, Pedro, Vale, arXiv 2020]

[see computational speed up in Cai, Cheng, Craig, Craig, arXiv 2020]

Similarity of Three Energy Flows?



[Chu, [MIT News July 2019](#)]



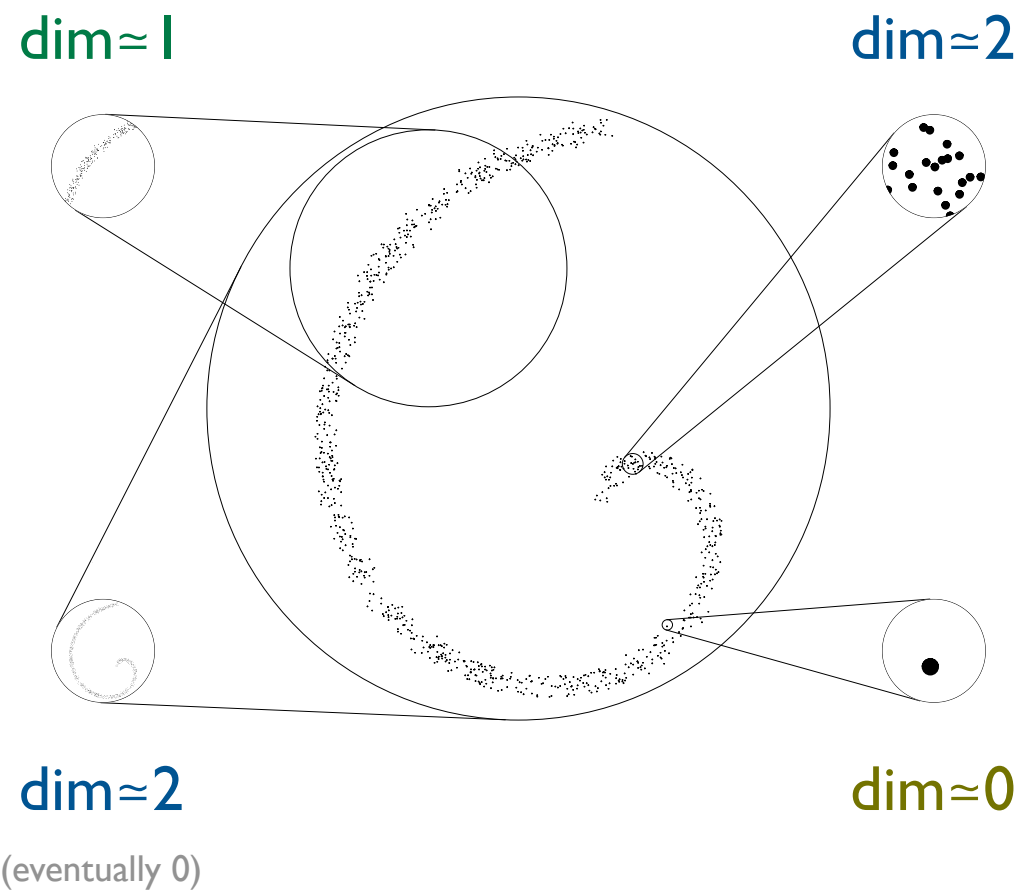
[Komiske, Metodiev, JDT, [PRL 2019](#); code at Komiske, Metodiev, JDT, [energyflow.network](#);
see alternative graph network approach in Mullin, Pacey, Parker, White, Williams, [arXiv 2019](#)]

Dimensionality of Space of Jets

$$N_{\text{neighbors}}(r) \sim r^{\text{dim}}$$

$$\Rightarrow \text{dim}(r) \sim r \frac{\partial}{\partial r} \ln N_{\text{neighbors}}(r)$$

[Grassberger, Procaccia, PRL 1983; Kégl, NIPS 2002]



Dimensionality of Space of Jets



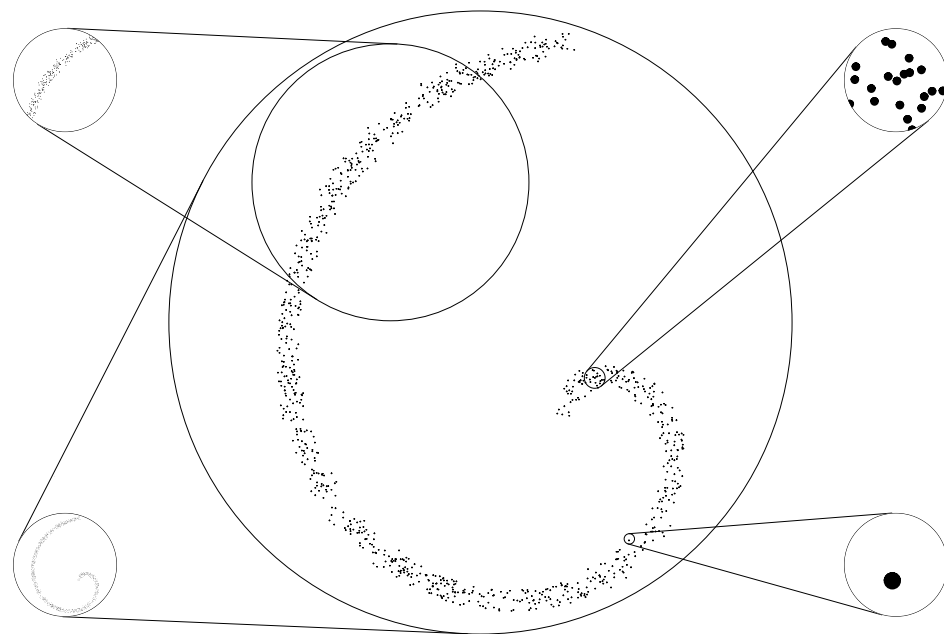
$$N_{\text{neighbors}}(r) \sim r^{\text{dim}}$$

$$\Rightarrow \text{dim}(r) \sim r \frac{\partial}{\partial r} \ln N_{\text{neighbors}}(r)$$

[Grassberger, Procaccia, PRL 1983; Kégl, NIPS 2002]

dim ≈ 1

dim ≈ 2

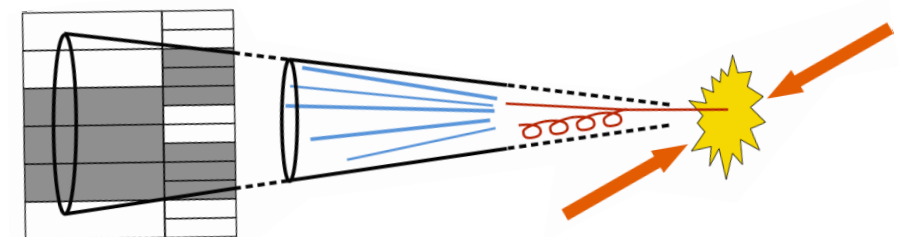
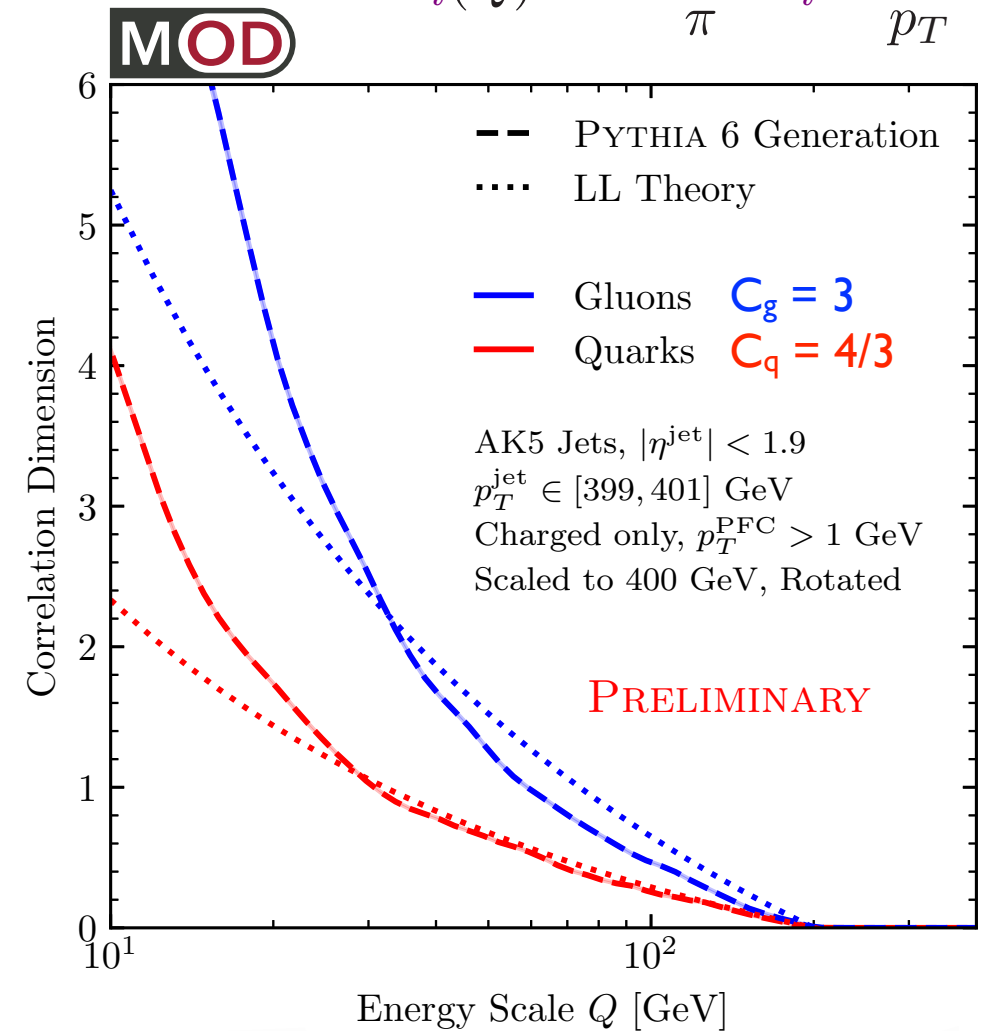


dim ≈ 2

dim ≈ 0

(eventually 0)

$$\text{dim}_i(Q) \simeq -\frac{8\alpha_s}{\pi} C_i \ln \frac{Q}{p_T}$$



Dimensionality of Space of Jets

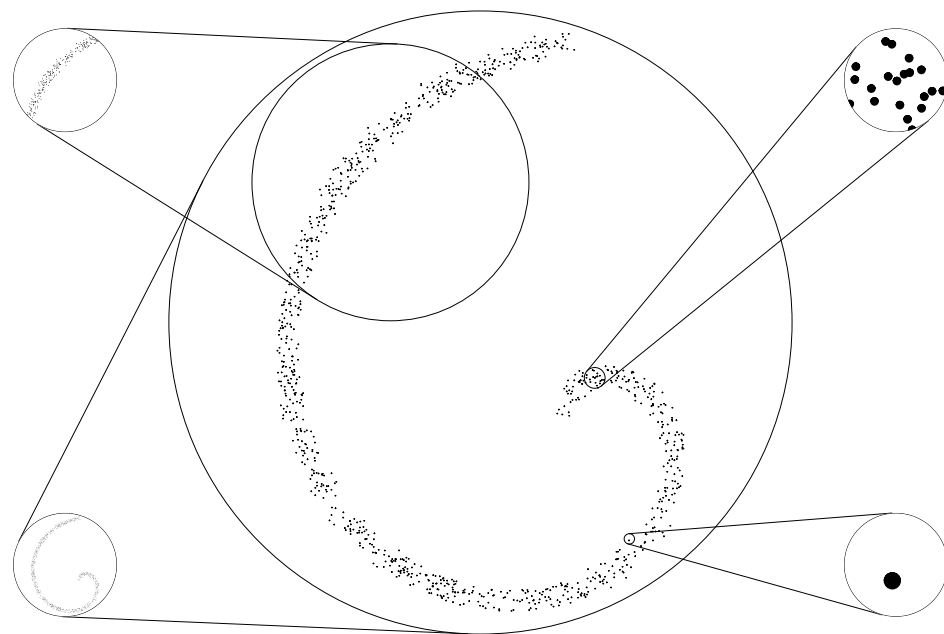
$$N_{\text{neighbors}}(r) \sim r^{\text{dim}}$$

$$\Rightarrow \text{dim}(r) \sim r \frac{\partial}{\partial r} \ln N_{\text{neighbors}}(r)$$

[Grassberger, Procaccia, PRL 1983; Kégl, NIPS 2002]

dim ≈ 1

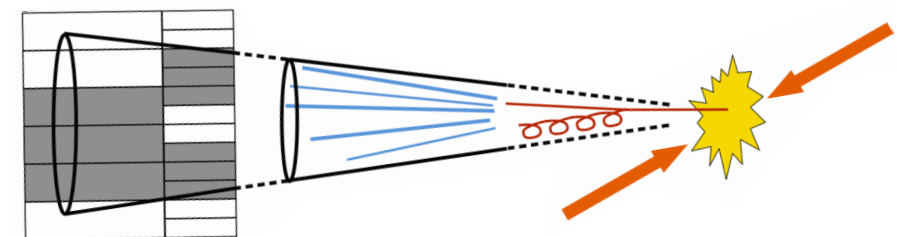
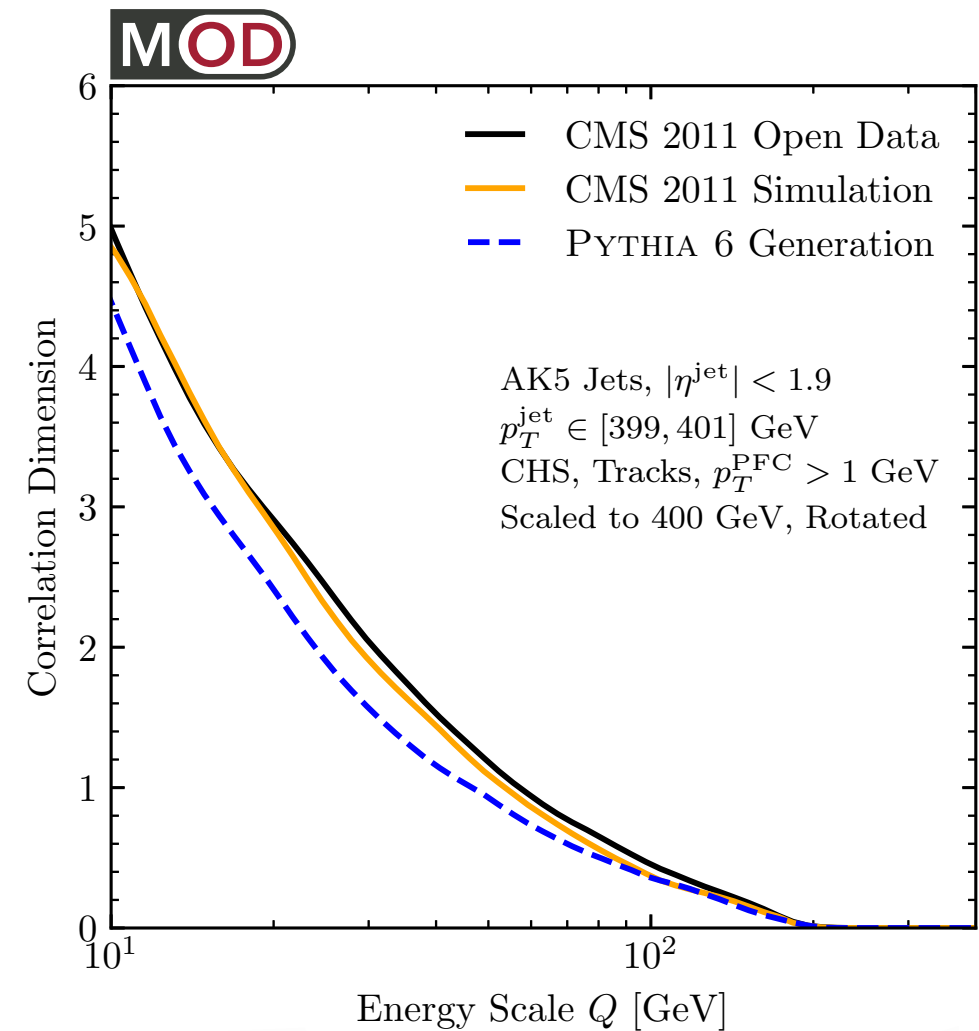
dim ≈ 2



dim ≈ 2

dim ≈ 0

(eventually 0)

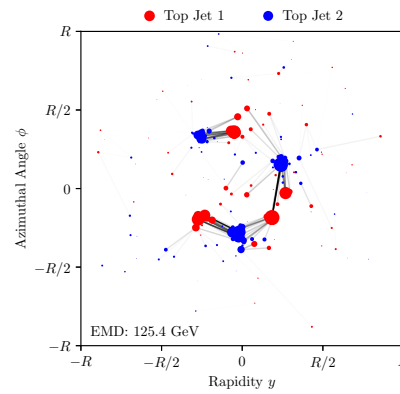


[Komiske, Mastandrea, Metodiev, Naik, JDT, PRD 2020; using CMS Open Data]



Pause

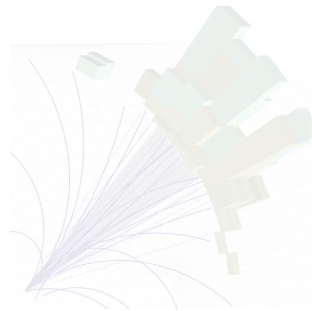
When are Events Similar?



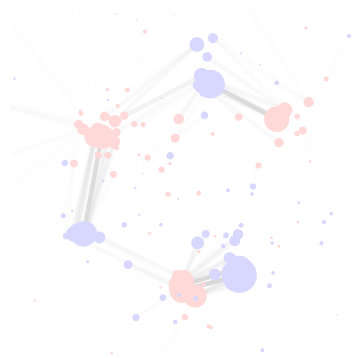
Small Energy Mover's Distance

$$\text{EMD}(\mathcal{E}, \mathcal{E}') = \min_{\{f\}} \sum_i \sum_j f_{ij} \frac{\theta_{ij}}{R} + \left| \sum_i E_i - \sum_j E'_j \right|$$

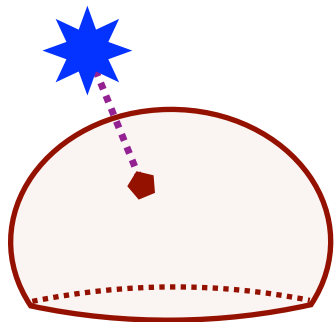
(see backup for more applications)



What is a Collider Event?



When are Events Similar?

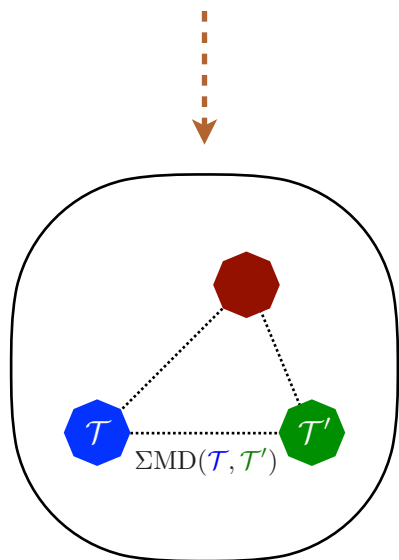


What can be Geometrized?

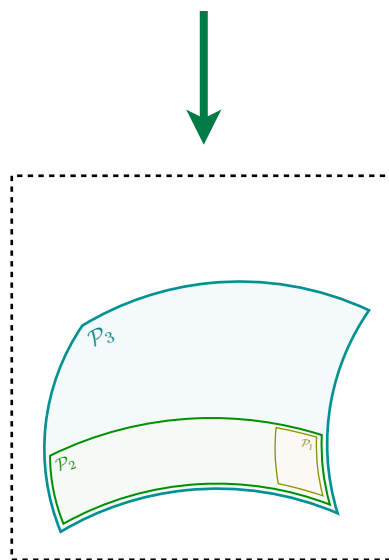
Master Formula for Collider Physics

$$\sigma_{\text{obs}} \simeq \frac{1}{2E_{\text{CM}}^2} \sum_{n=2}^{\infty} \int d\Phi_n |\mathcal{M}_{AB \rightarrow 12\dots n}|^2 f_{\text{obs}}(\Phi_n)$$

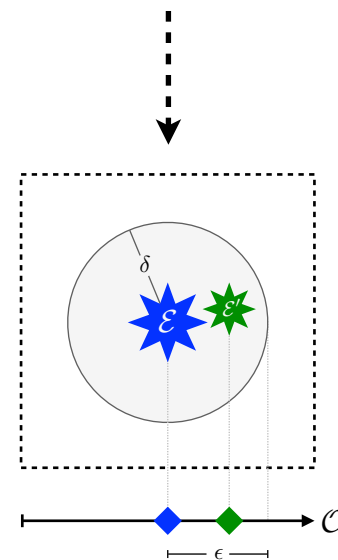
cross section



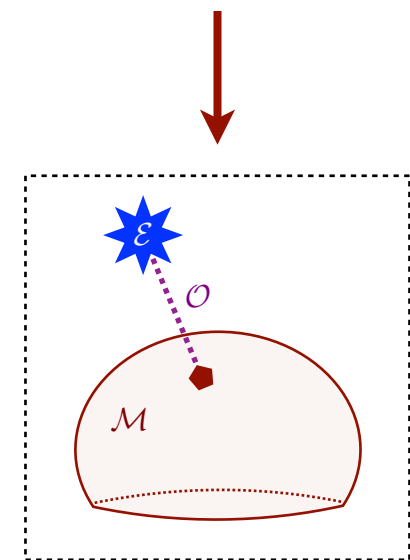
phase space



amplitude



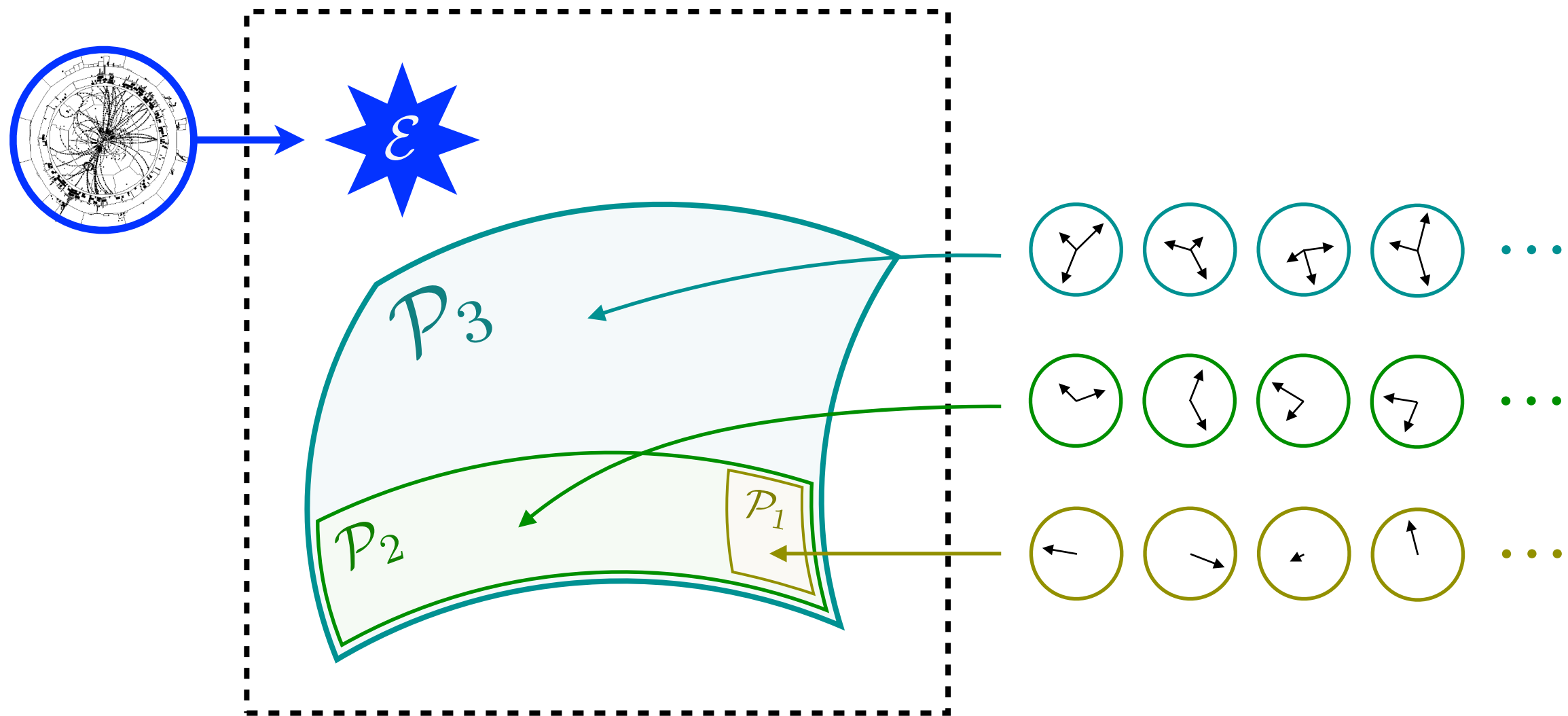
observable



Introducing N-particle Manifolds

$$\sum_{n=2}^{\infty} \int d\Phi_n$$

\mathcal{P}_N = set of all N-particle configurations

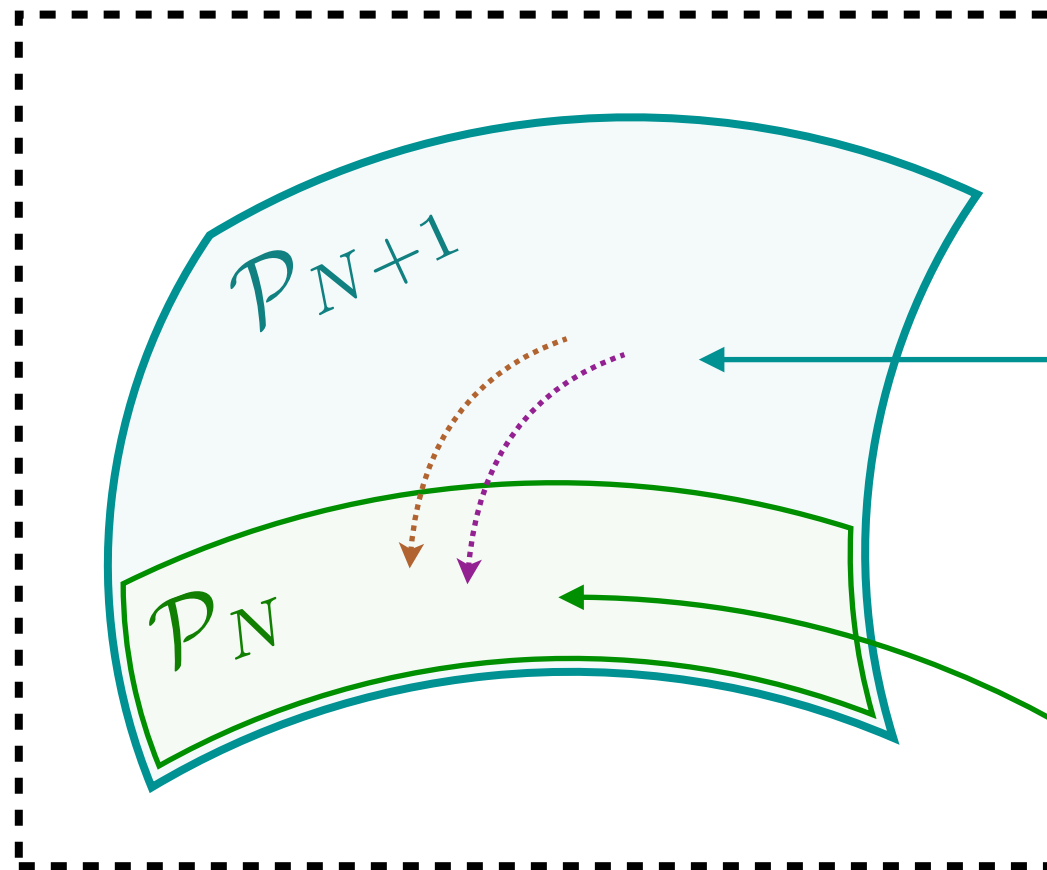
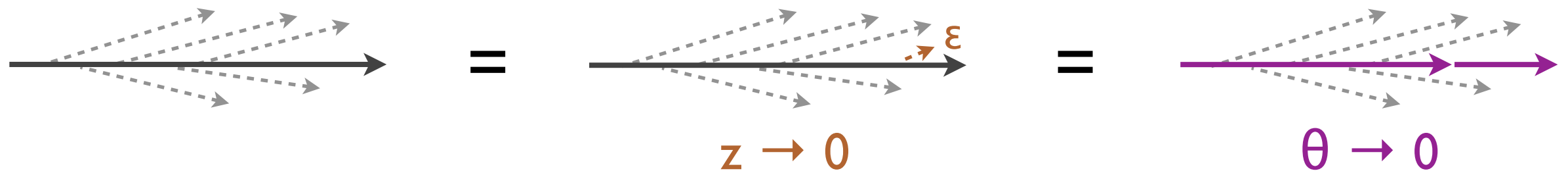


$\mathcal{P}_N \supset \mathcal{P}_{N-1} \supset \dots \supset \mathcal{P}_2 \supset \mathcal{P}_1$ by **soft/collinear** limits

When are Two Events **the Same**?

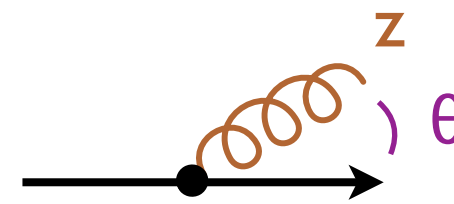
$$\mathcal{E}(\hat{n}) = \sum_i E_i \delta(\hat{n} - \hat{n}_i)$$

Energy Flow unchanged by infinitesimal **soft/collinear** emissions



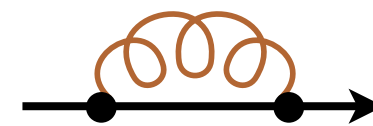
Infrared divergences “live” together!

Real:



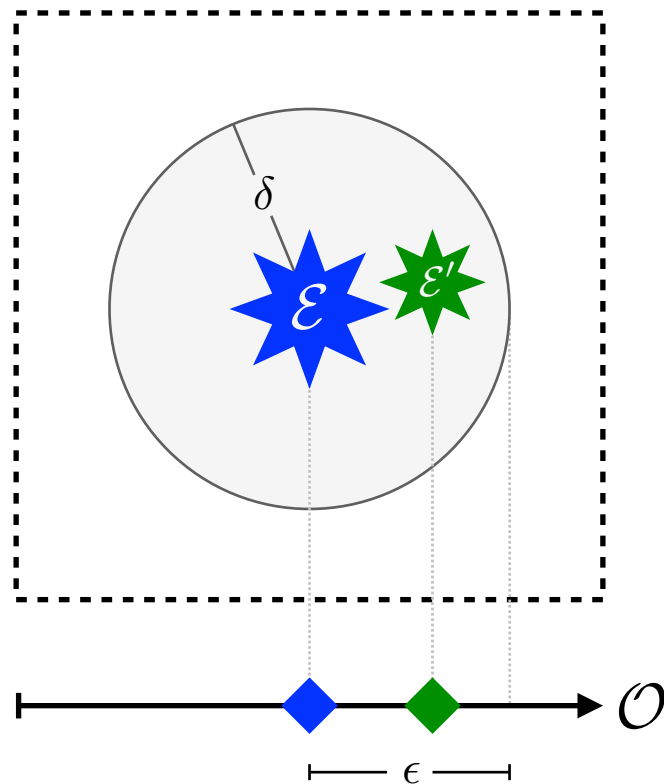
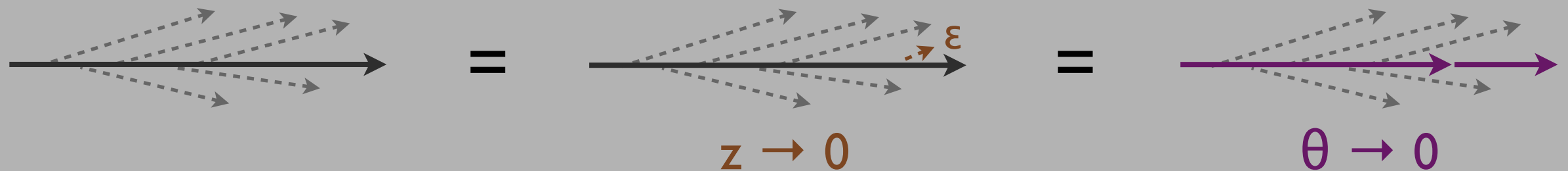
$$dP_{i \rightarrow ig} \simeq \frac{2\alpha_s}{\pi} C_i \frac{dz}{z} \frac{d\theta}{\theta}$$

Virtual:



When are Two Events the Same?

Energy Flow unchanged by infinitesimal *soft/collinear* emissions



Infrared & Collinear Safety

\approx calculable in perturbative quantum field theory

iS^*

Continuity in EMD Space

[Komiske, Metodiev, JDT, [JHEP 2020](#)]
[Sterman, Weinberg, [PRL 1977](#); Sterman, [PRD 1979](#)]
[see also Banfi, Salam, Zanderighi, [JHEP 2005](#)]

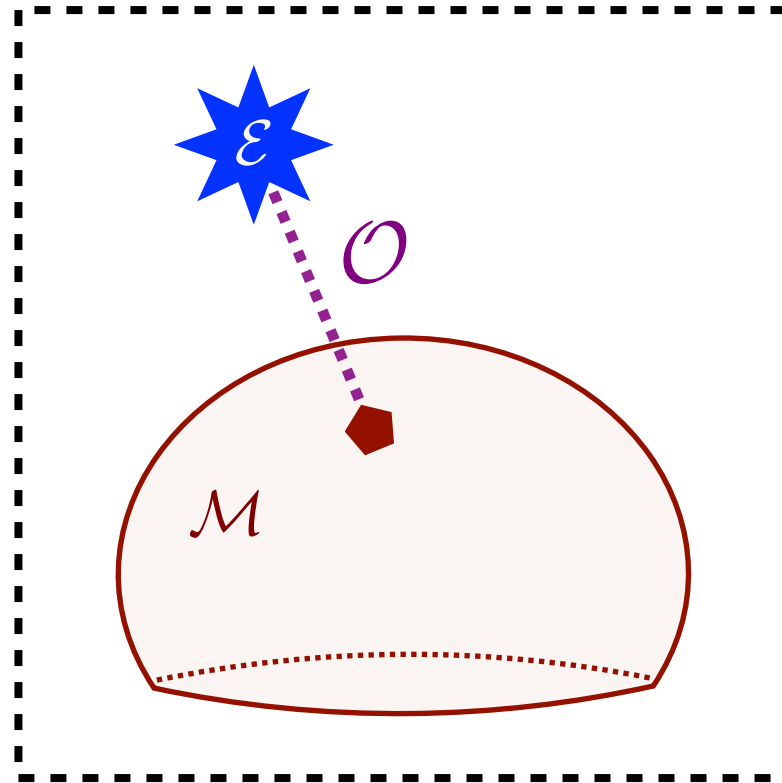
*EMD seems to define the “natural”
geometry for massless gauge theories*

Open question: Can you define $|\mathcal{M}_{AB \rightarrow 12 \dots n}|^2$ directly in this space?

Manifolds for Observables

$$f_{\text{obs}}(\Phi_n)$$

One Event



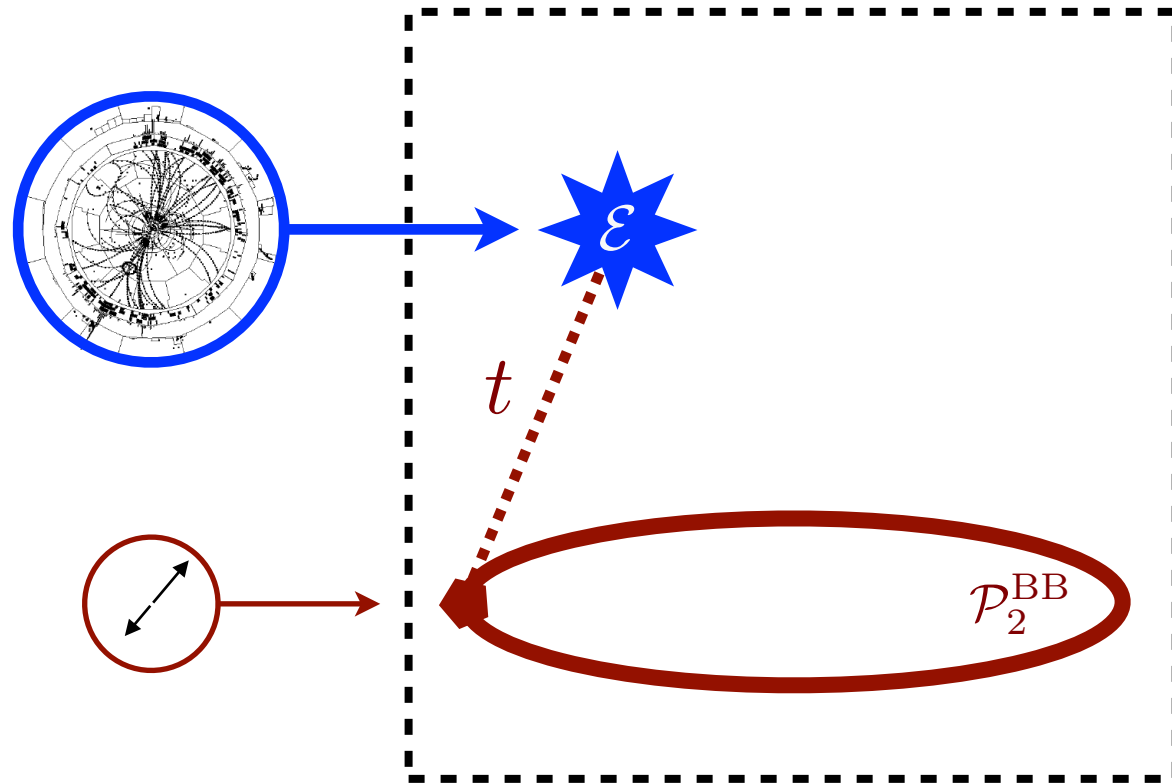
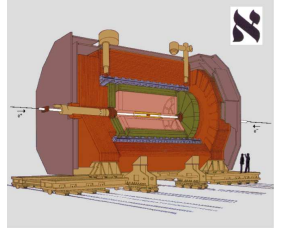
Set of Events

Distance of Closest Approach \Rightarrow Observable

$$\mathcal{O}(\mathcal{E}) = \min_{\mathcal{E}' \in \mathcal{M}} \text{EMD}(\mathcal{E}, \mathcal{E}')$$

E.g. Thrust

How dijet-like is an event?

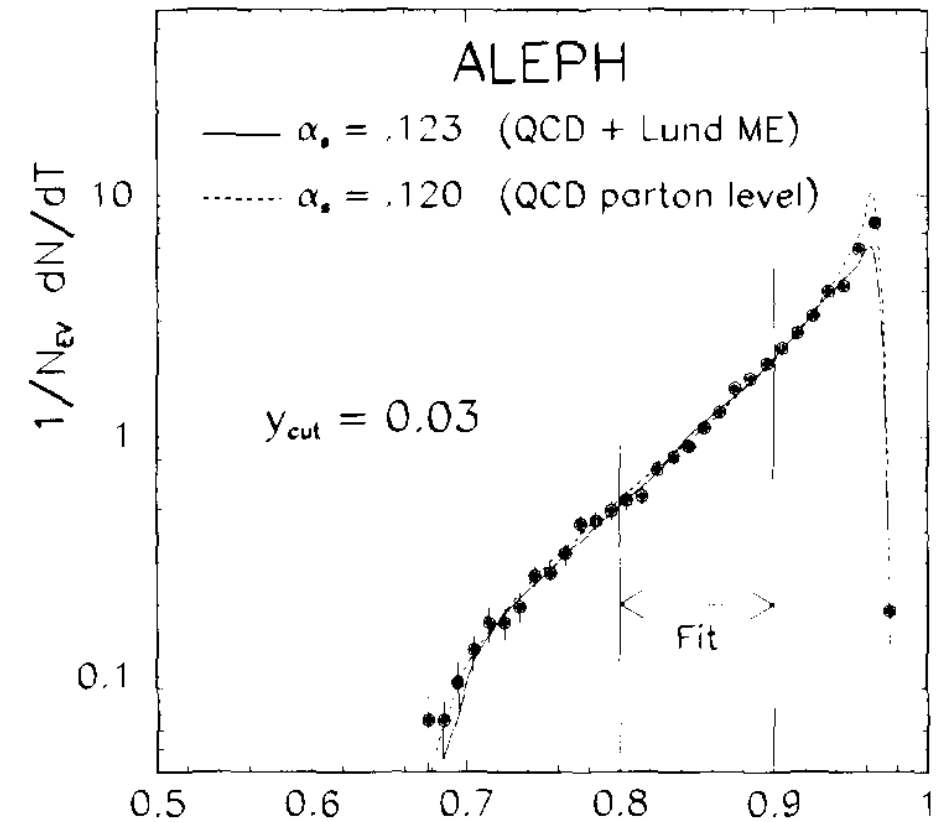


All Back-to-Back Two Particle Configurations

$$\mathcal{P}_2^{\text{BB}} = \left\{ \begin{array}{c} \text{[Diagram of four circles with arrows pointing in various directions]} \dots \end{array} \right\}$$

(using $\beta=2$ EMD variant)

$$t(\mathcal{E}) = \min_{\mathcal{E}' \in \mathcal{P}_2^{\text{BB}}} \text{EMD}_2(\mathcal{E}, \mathcal{E}')$$



$$1 - \frac{t}{2E_{\text{CM}}}$$

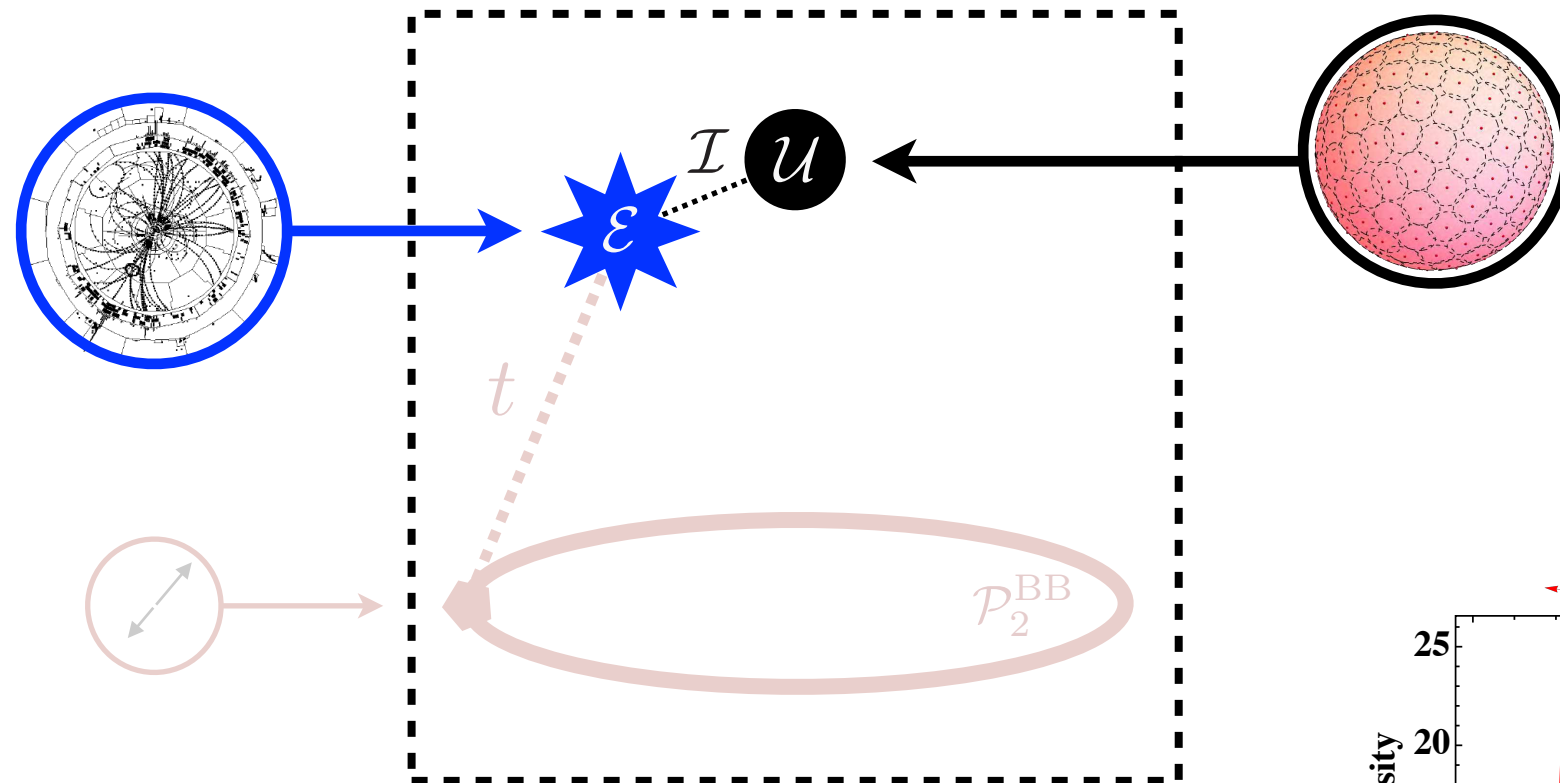
cf. $T(\mathcal{E}) = \max_{\hat{n}} \frac{\sum_i |\vec{p}_i \cdot \hat{n}|}{\sum_j |\vec{p}_j|}$

[Komiske, Metodiev, JDT, JHEP 2020]

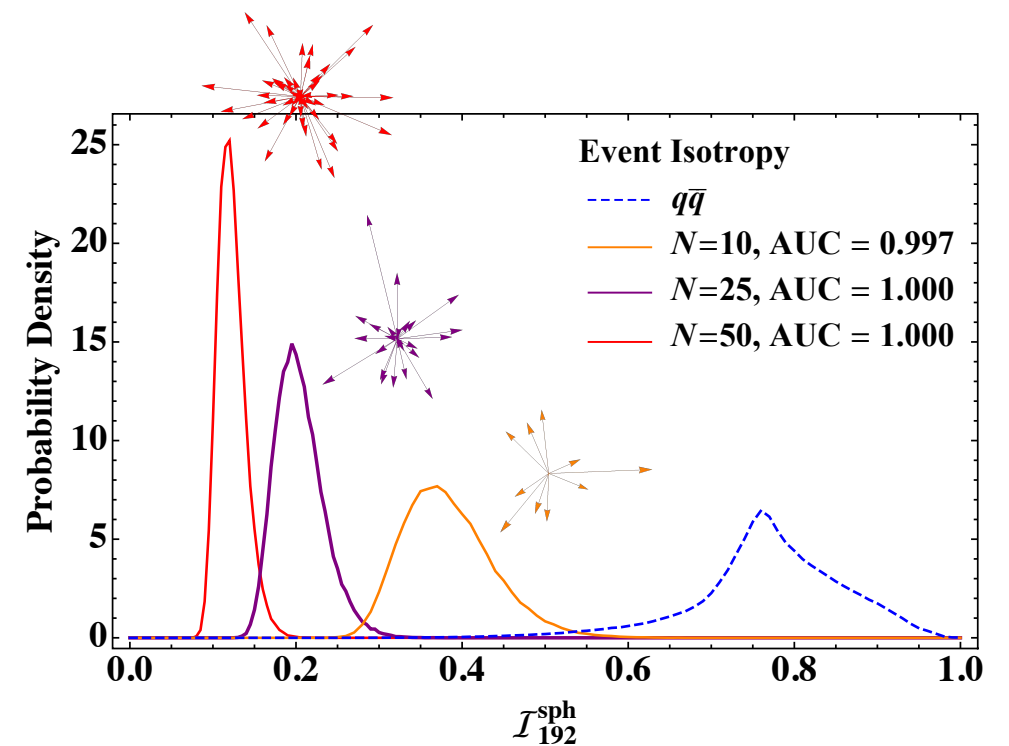
[Brandt, Peyrou, Sosnowski, Wroblewski, PL 1964; Farhi, PRL 1977; ALEPH, PLB 1991]

New! Event Isotropy

How isotropic is an event?



$$\mathcal{I}(\mathcal{E}) = \text{EMD}(\mathcal{E}, \mathcal{U})$$

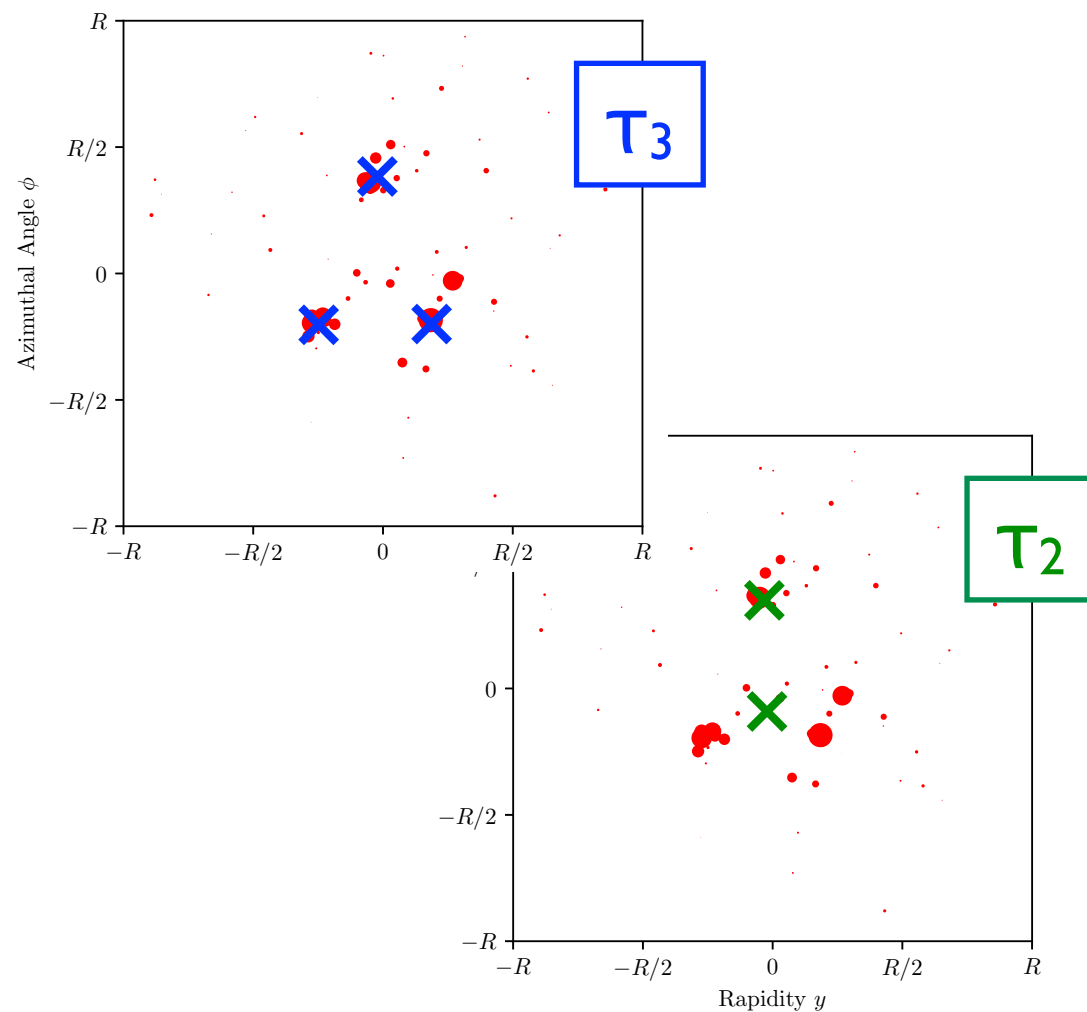


[Cesarotti, JDT, JHEP 2020;
see also Cesarotti, Reece, Strassler, arXiv 2020]

N-subjettiness

Ubiquitous jet substructure observable used for almost a decade...

$$\tau_N(\mathcal{J}) = \min_{N \text{ axes}} \sum_i E_i \min \{ \theta_{1,i}, \theta_{2,i}, \dots, \theta_{N,i} \}$$

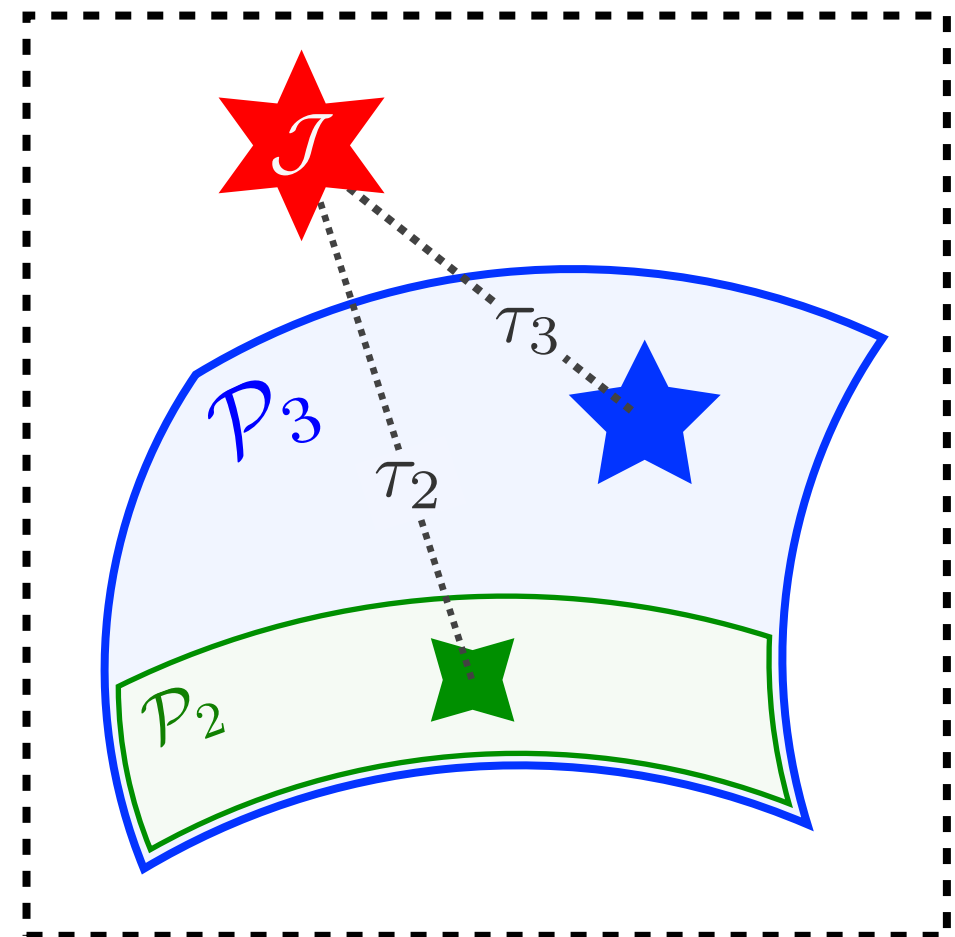
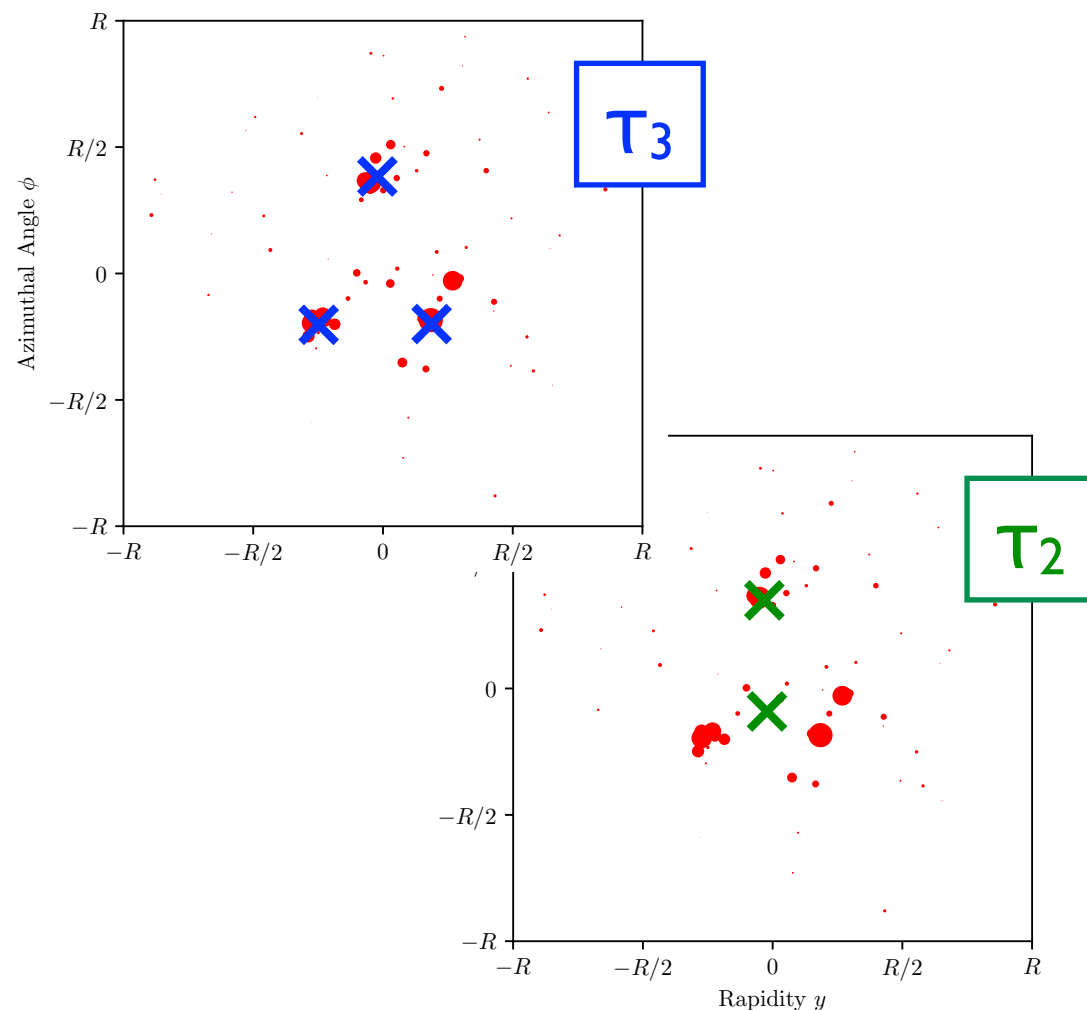


[JDT, Van Tilburg, JHEP 2011, JHEP 2012;
based on Brandt, Dahmen, ZPC 1979; Stewart, Tackmann, Waalewijn, PRL 2010]

N-subjettiness = Point to Manifold EMD

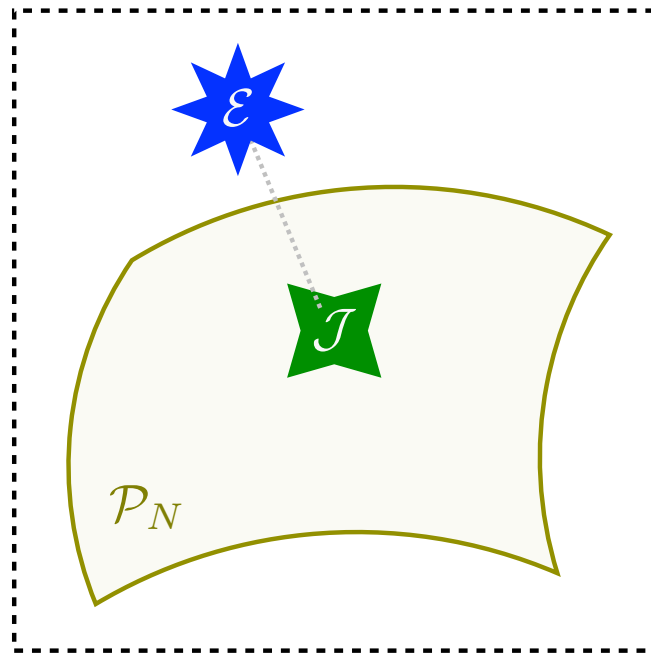
...is secretly an optimal transport problem

$$\tau_N(\mathcal{J}) = \min_{\mathcal{J}' \in \mathcal{P}_N} \text{EMD}(\mathcal{J}, \mathcal{J}')$$



[JDT, Van Tilburg, JHEP 2011, JHEP 2012;
rephrased in the language of Komiske, Metodiev, JDT, PRL 2019]

More Fun with N-particle Manifolds



N-jettiness

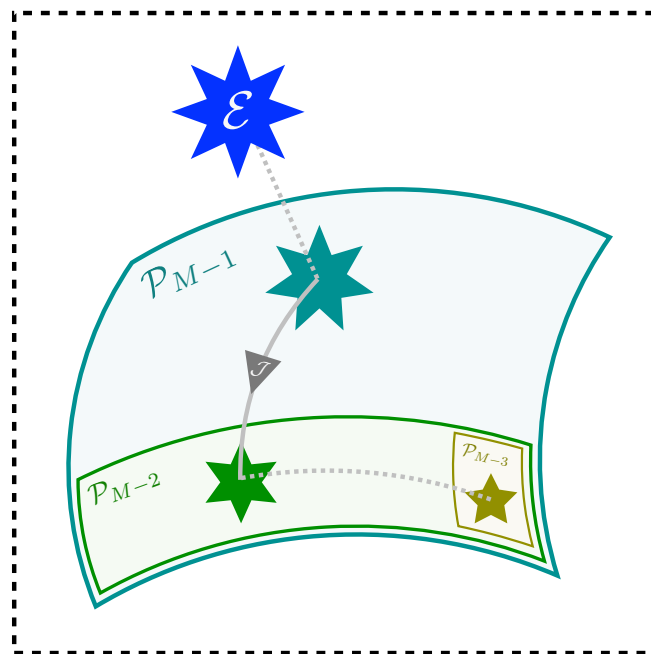
Distance of closest approach to N-particle manifold

[Brandt, Dahmen, ZPC 1979; Stewart, Tackmann, Waalewijn, PRL 2010]

Exclusive Cone Jet Finding

Point of closest approach on N-particle manifold

[Stewart, Tackmann, JDT, Vermilion, Wilkason, JHEP 2015]



Sequential Jet Recombination

Iteratively stepping between various N-particle manifolds

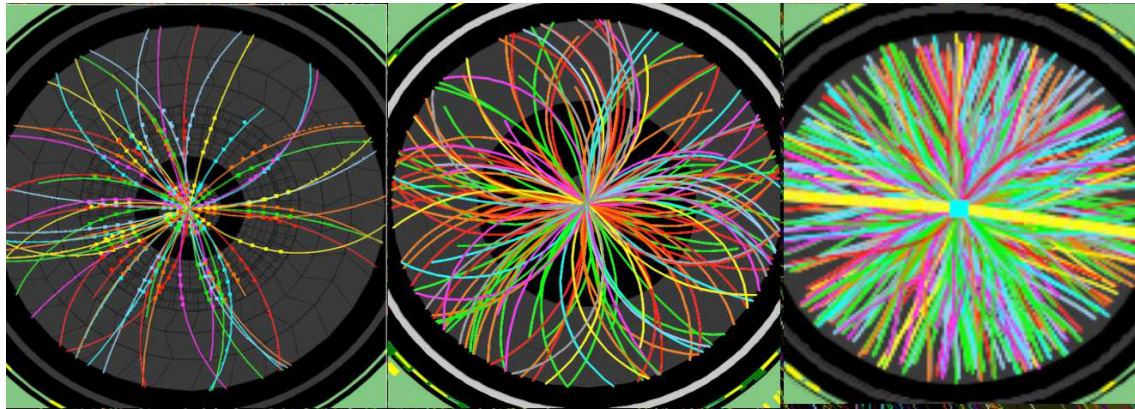
[Catani, Dokshitzer, Seymour, Webber, NPB 1993; Ellis, Soper, PRD 1993]

[Dokshitzer, Leder, Moretti, Webber, JHEP 1997; Wobisch, Wengler, arXiv 1999]

[Butterworth, Couchman, Cox, Waugh, CPC 2003; Larkoski, Neill, JDT, JHEP 2014]

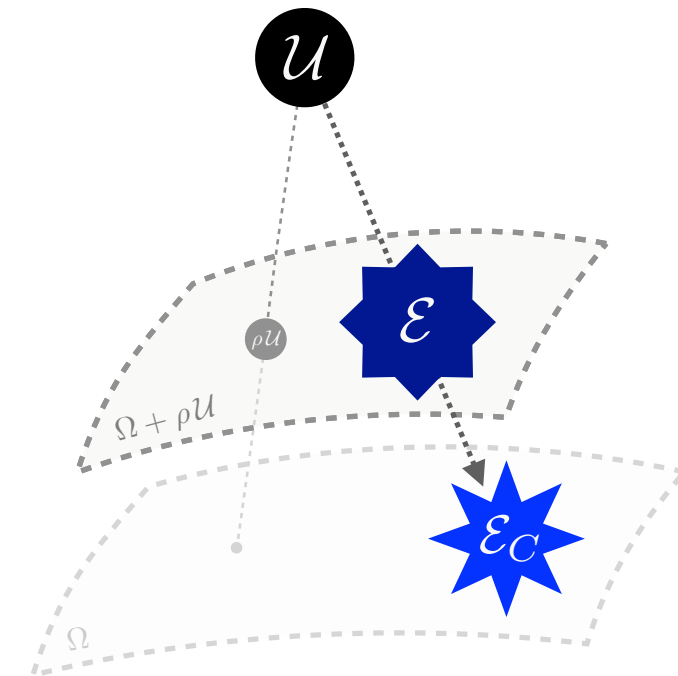
[Komiske, Metodiev, JDT, JHEP 2020]

Pileup Mitigation



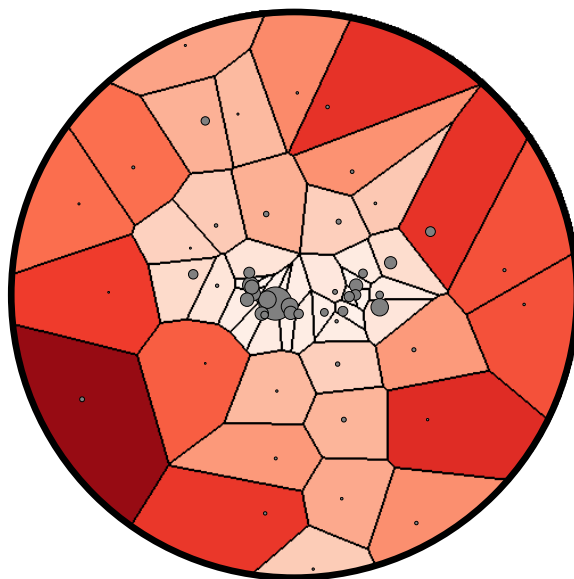
[see review in Soyez, PR 2019]

Uniform event contamination from overlapping proton-proton collisions



Pileup Mitigation:
“Move away” from uniform event

Voronoi



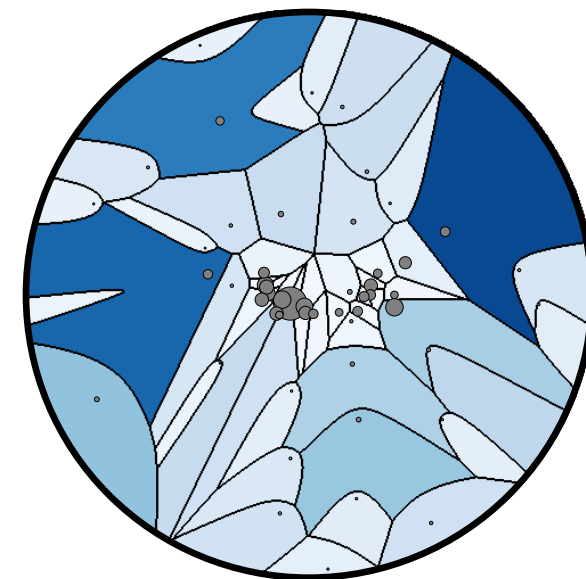
[Cacciari, Salam, Soyez, JHEP 2008]

Constituent Subtraction



[Berta, Spousta, Miller, Leitner, JHEP 2014]

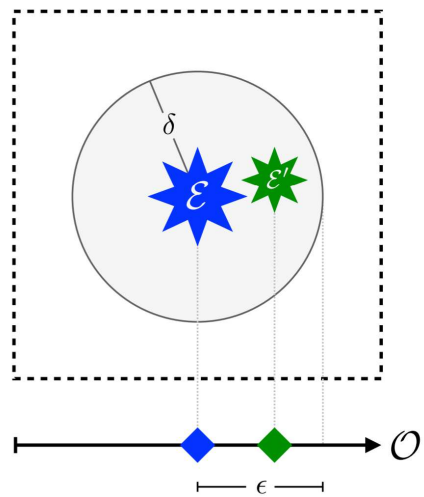
Apollonius



[Komiske, Metodiev, JDT, JHEP 2020]

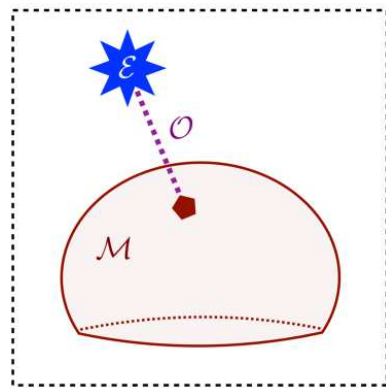
Six Decades of Collider Physics Translated into a New Geometric Language!

IRC Safety is smoothness in the space of events



Taming infinities

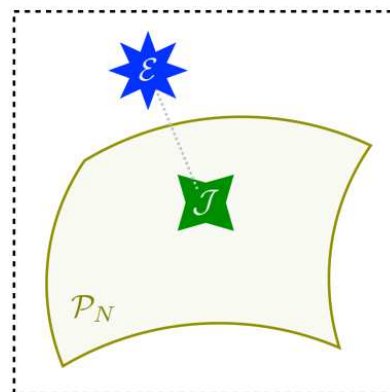
Event shapes are distances from events to manifolds.



$$O(\mathcal{E}) = \min_{\mathcal{E}' \in \mathcal{M}} \text{EMD}_{\beta, R}(\mathcal{E}, \mathcal{E}')$$

Event Shapes

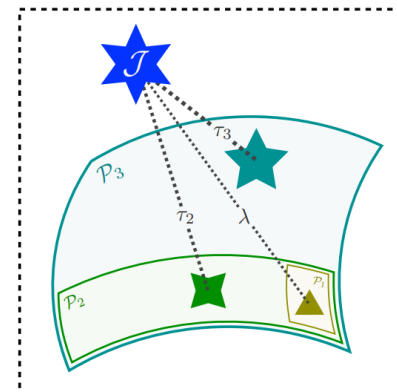
Jets are projections to few-particle manifolds.



$$J = \operatorname{argmin}_{\mathcal{E}' \in \mathcal{P}_N} \text{EMD}_{\beta, R}(\mathcal{E}, \mathcal{E}')$$

Jet Algorithms

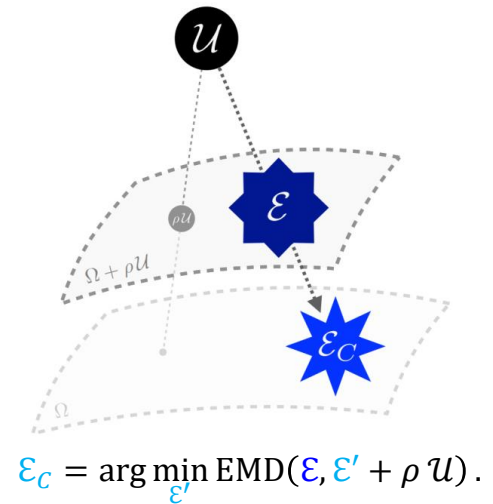
Substructure resolves emissions within the jet.



$$\tau(J) = \min_{\mathcal{E}' \in \mathcal{P}_N} \text{EMD}_{\beta}(\mathcal{J}, \mathcal{E}')$$

Jet Substructure

Pileup mitigation moves away from uniform radiation.



$$\mathcal{E}_C = \operatorname{argmin}_{\mathcal{E}'} \text{EMD}(\mathcal{E}, \mathcal{E}' + \rho \mathcal{U}).$$

Pileup

1960

1962-1964

Infrared Safety

[Kinoshita, JMP 1962]
[Lee, Nauenberg, PR 1964]

1977

Thrust, Sphericity

[Farhi, PRL 1977]
[Georgi, Machacek, PRL 1977]

1993

k_T jet clustering

[Ellis, Soper, PRD 1993]
[Catani, Dokshitzer, Seymour, Webber, NPB 1993]

1997-1998

C/A jet clustering

[Wobisch, Wengler, 1998]
[Dokshitzer, Leder, Moretti, Webber, JHEP 1997]

2010-2015

N-(sub)jettiness, X Cone

[Stewart, Tackmann, Waalewijn, PRL 2010]
[Thaler, Van Tilburg, JHEP 2011]
[Stewart, Tackmann, Thaler, Vermilion, Wilkason, JHEP 2015]

2014-2019

Constituent Subtraction

[Berta, Spousta, Miller, Leitner, JHEP 2014]
[Berta, Masetti, Miller, Spousta, JHEP 2019]

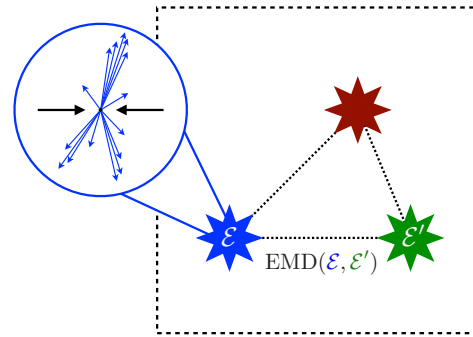
And many more!

2020

[timeline from Eric Metodiev]

Pause

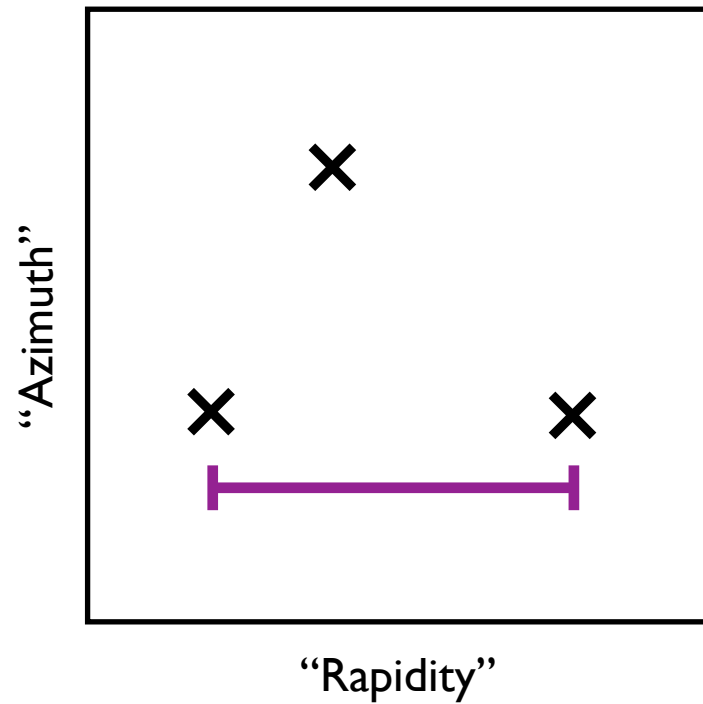
What can be Geometrized?



IRC Safety, Observables,
Jet Algorithms, Pileup Mitigation

How far down does this rabbit hole go?

Direction Space



x = Direction

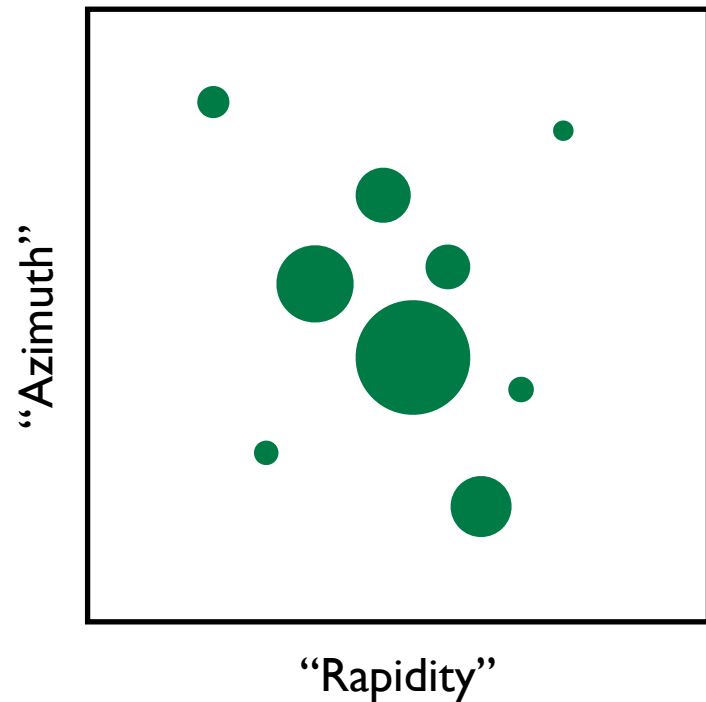
— = Angular Distance

$$n_i^\mu = \frac{p_i^\mu}{E_i} = (1, \hat{n})^\mu$$

$$\theta_{ij} = \sqrt{2n_i^\mu n_{j\mu}}$$

(for massless particles)

Direction Space Distribution



● = Weighted Direction

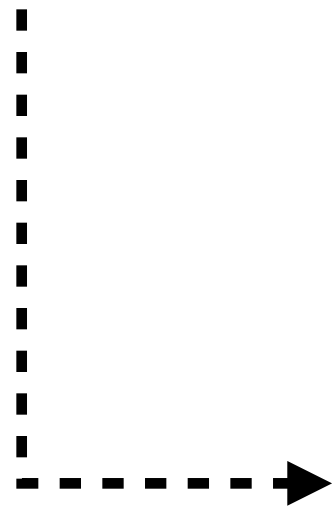
— = Angular Distance

$$n_i^\mu = \frac{p_i^\mu}{E_i} = (1, \hat{n})^\mu$$

$$w_i = E_i$$

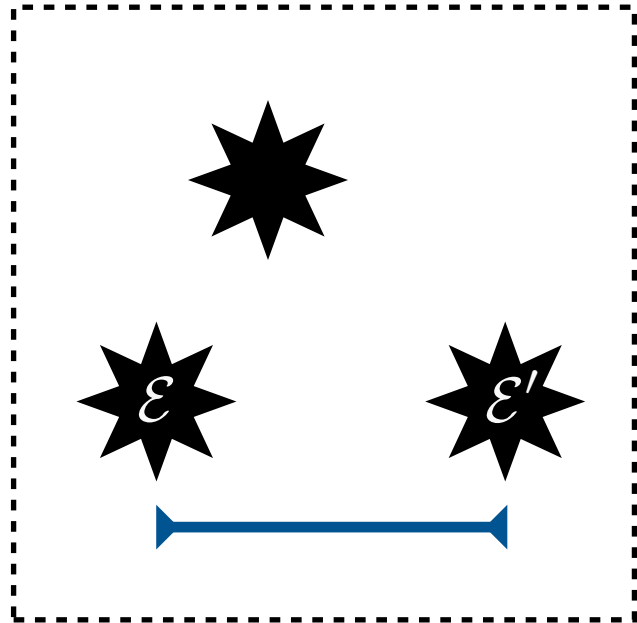
$$\theta_{ij} = \sqrt{2n_i^\mu n_{j\mu}}$$

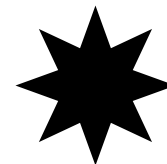
(for massless particles)



★ = Event

Event Space



 = Event

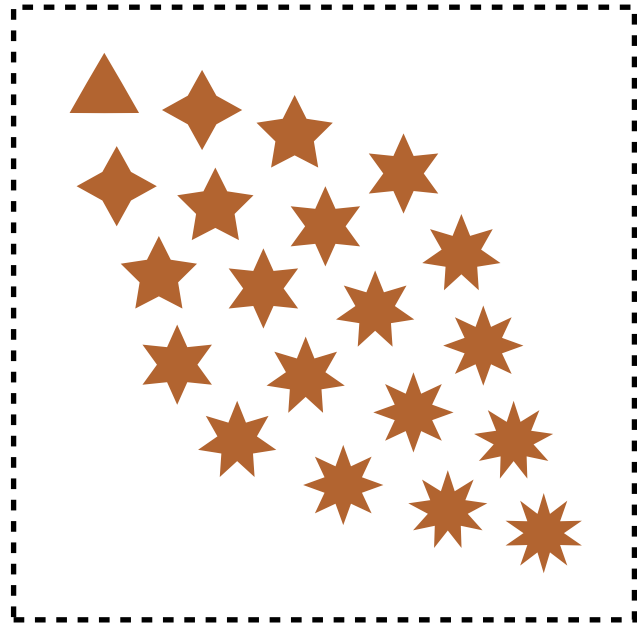
 = EMD
Energy
Mover's Distance


$$\mathcal{E}(\hat{n}) = \sum_i E_i \delta(\hat{n} - \hat{n}_i)$$

$$\text{EMD}(\mathcal{E}, \mathcal{E}') = \min_{\{f\}} \sum_i \sum_j f_{ij} \theta_{ij}$$

(for equal total energy)

Event Space Distribution



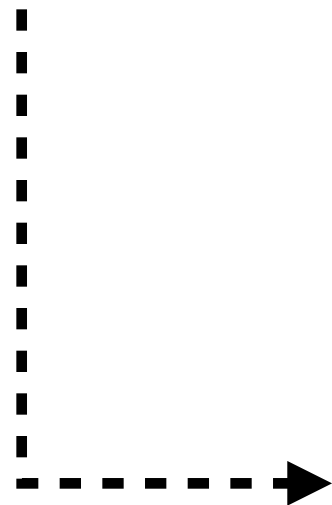
 = **Weighted Event**

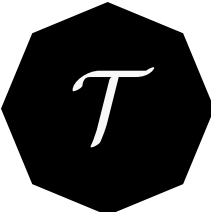
$$\mathcal{E}(\hat{n}) = \sum_i E_i \delta(\hat{n} - \hat{n}_i)$$

$$w_a = \sigma_a$$

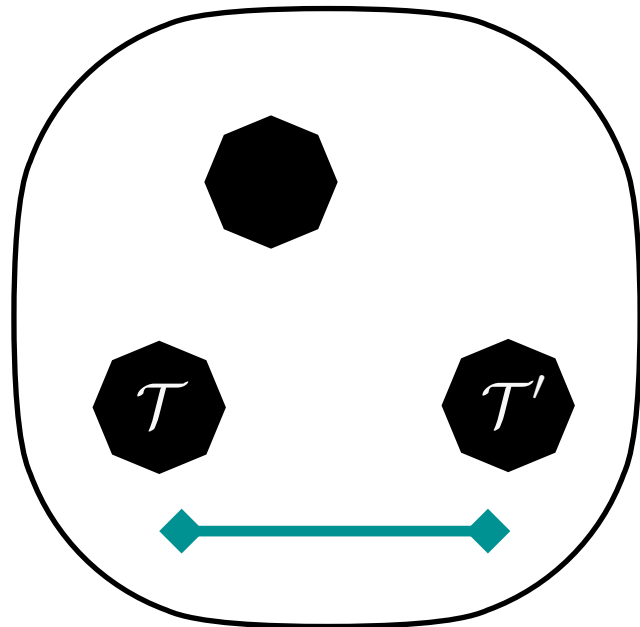
 = **EMD**
 Energy
 Mover's Distance

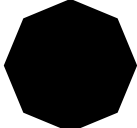
$$\text{EMD}(\mathcal{E}, \mathcal{E}') = \min_{\{f\}} \sum_i \sum_j f_{ij} \theta_{ij}$$
 (for equal total energy)




 = **Theory**

Theory Space



 = Theory

 = ΣMD
Cross-Section
Mover's Distance

$$\mathcal{T}(\mathcal{E}) = \sum_a \sigma_a \delta(\mathcal{E} - \mathcal{E}_a)$$

$$\Sigma\text{MD}(\mathcal{T}, \mathcal{T}') = \min_{\{\mathcal{F}\}} \sum_a \sum_b \mathcal{F}_{ab} \text{EMD}(\mathcal{E}_a, \mathcal{E}'_b)$$

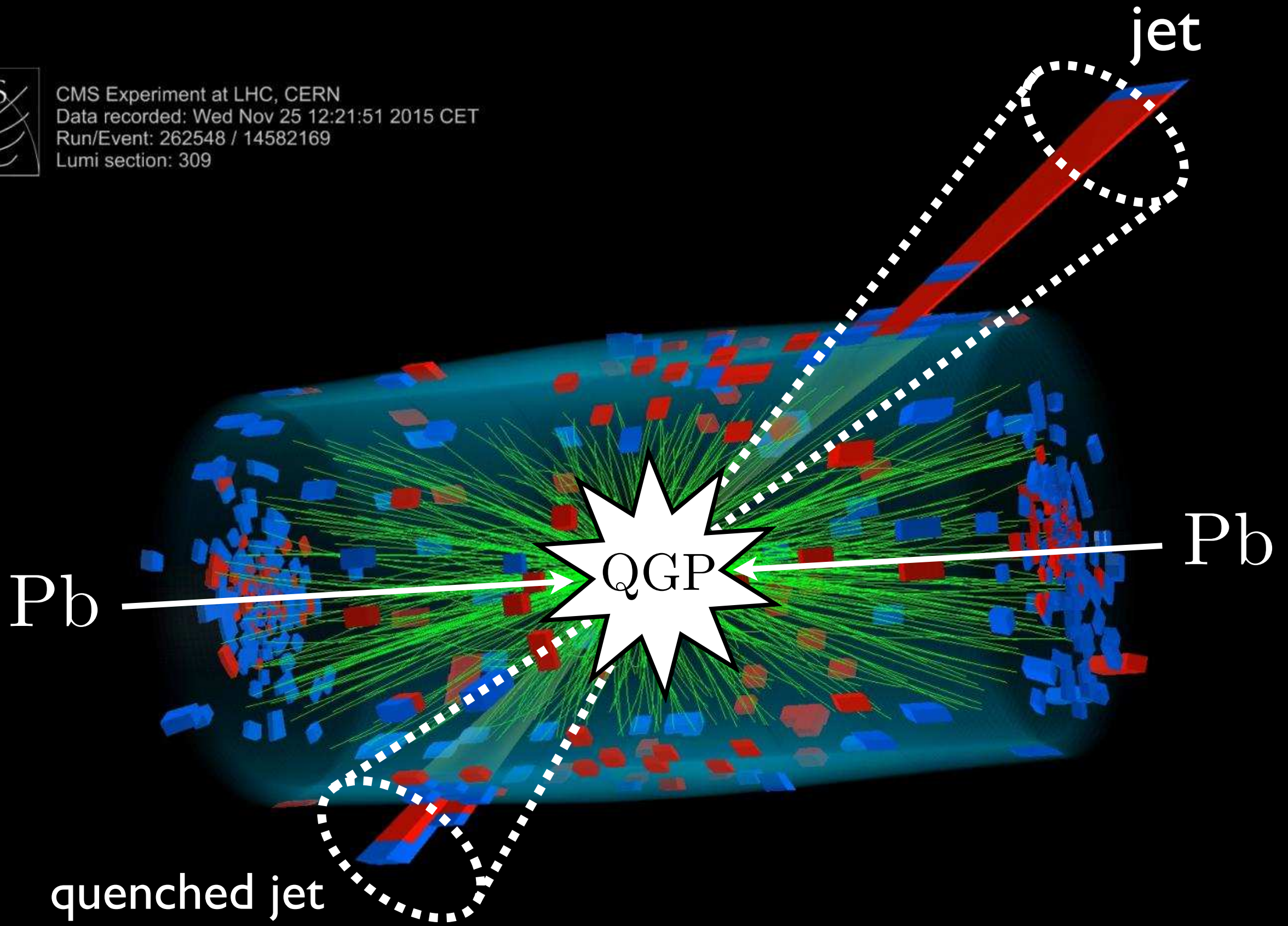
(for equal total xsec)

A distance between theories!

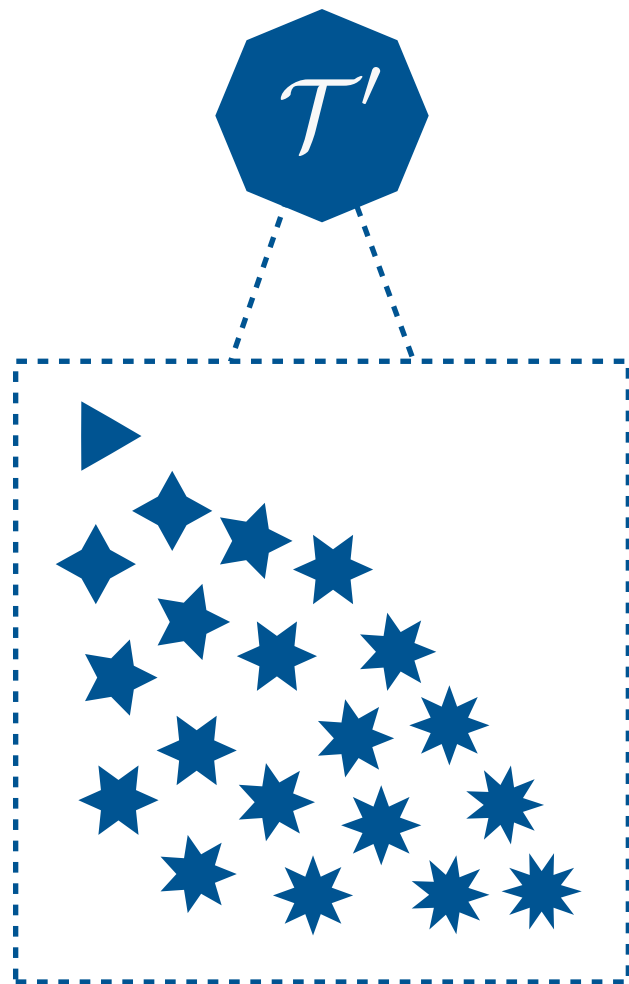
(e.g. EMD : N-jettiness :: ΣMD : k-eventiness)



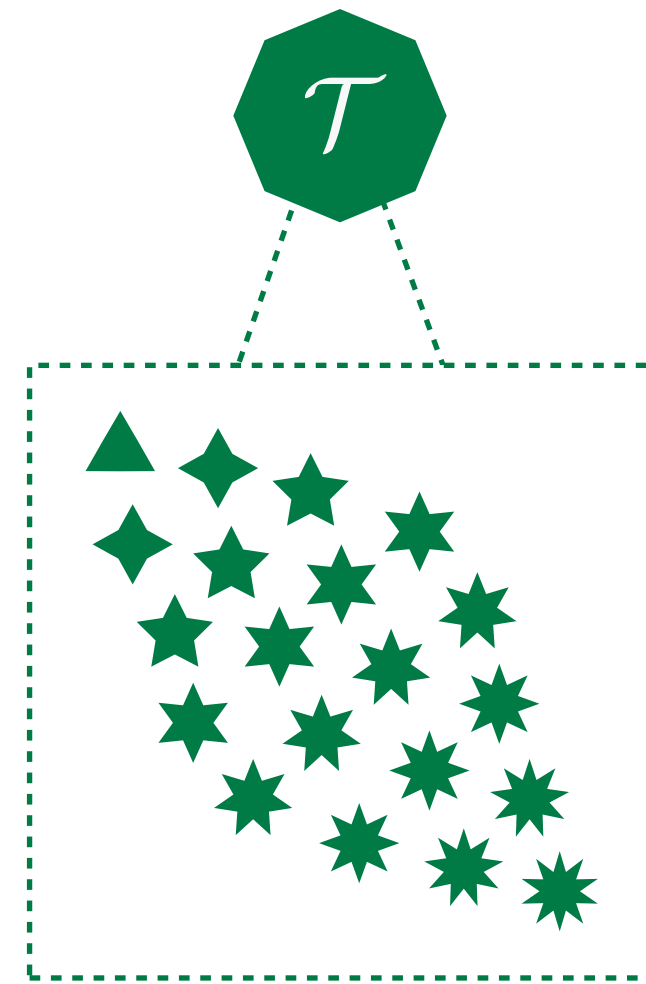
CMS Experiment at LHC, CERN
Data recorded: Wed Nov 25 12:21:51 2015 CET
Run/Event: 262548 / 14582169
Lumi section: 309



Theory Prime: In-Medium QCD



Theory: Vacuum QCD



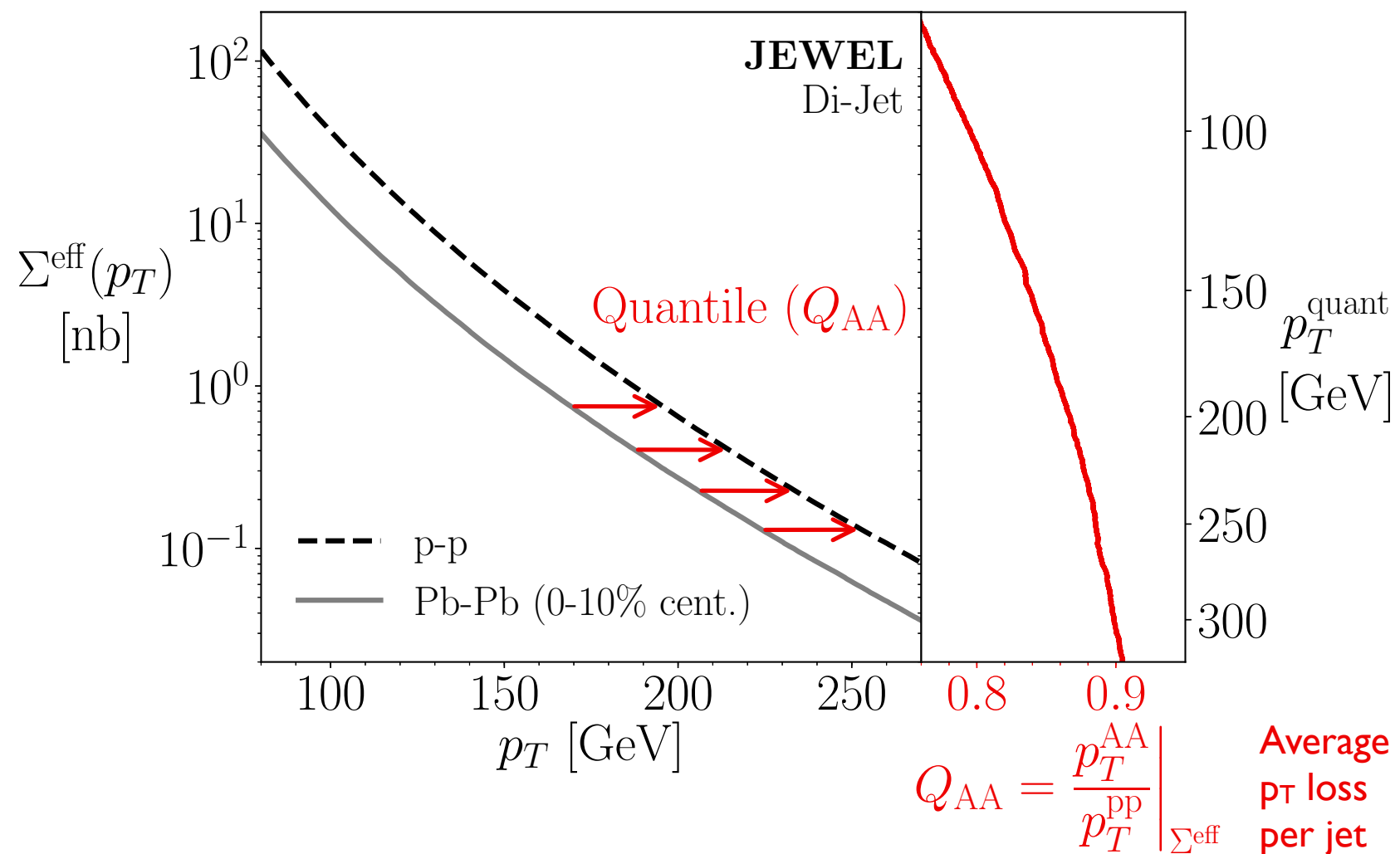
Σ MMD



*Optimal transportation plan defines mapping
between in-medium jets and vacuum jets!*

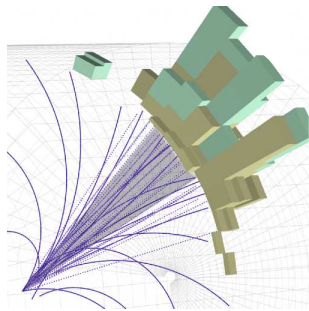
Jet Quenching via Quantile Matching

Equivalent to following a geodesic in theory space (!)



[Brewer, Milhano, JDT, PRL 2019]

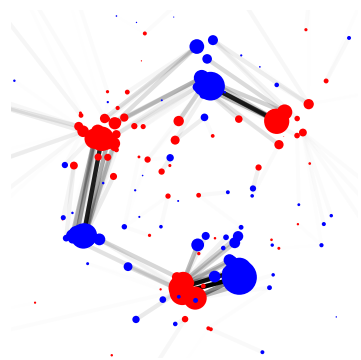
Summary



What is a Collider Event?

An unordered set of particles that describes the energy flow away from the collision point

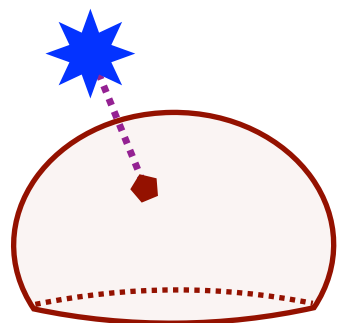
(ask me about ML & QCD)



When are Events Similar?

When they are close in the geometric space triangulated by the energy mover's distance

(ask me more about EMD)



What can be Geometrized?

Many concepts/techniques in quantum field theory and collider physics from the last half century

Fin

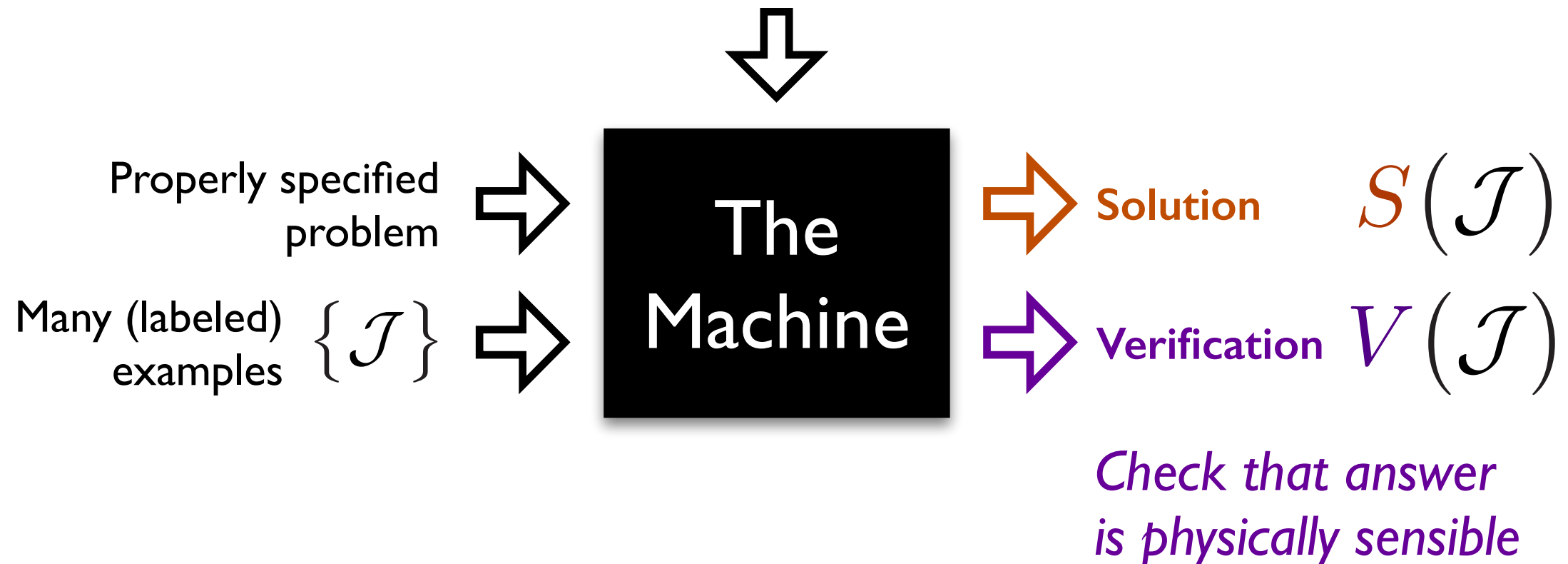
Backup Slides

Aside: Machine Learning for Jets

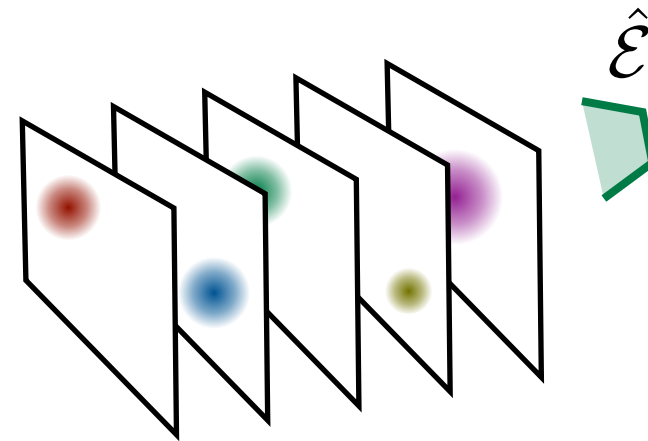
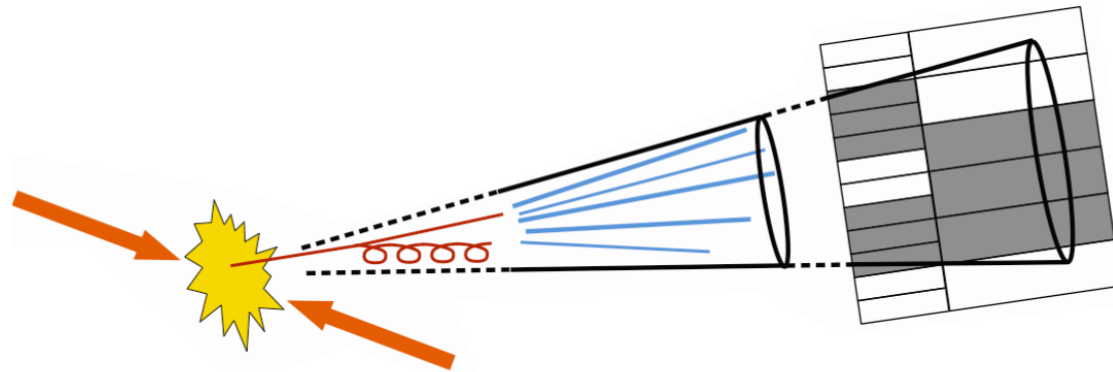
“ML4jets”
NYU, January 2020

Symmetry: $\mathcal{J} = \{ \vec{p}_1, \vec{p}_2, \vec{p}_3, \dots, \vec{p}_N \}$
Unordered, Variable Length Set (QM!)

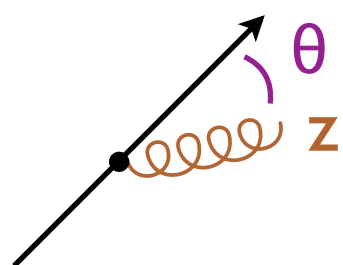
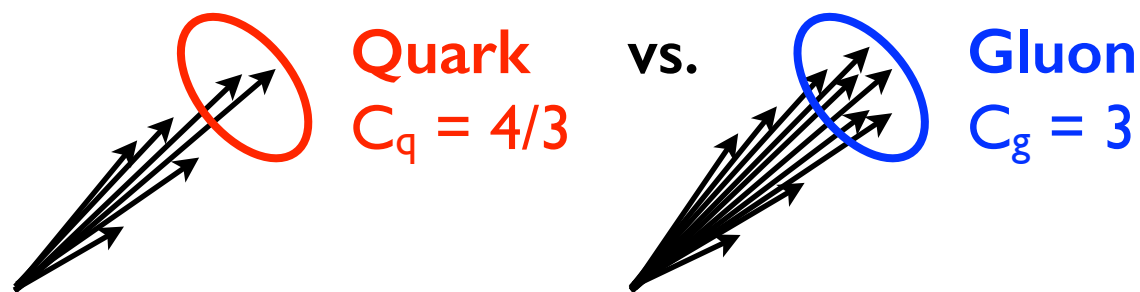
Safety: $\vec{p} = \{ E, \hat{n}_x, \hat{n}_y, \hat{n}_z \}$
Energy weighting (QFT!)



E.g. Energy Flow Networks

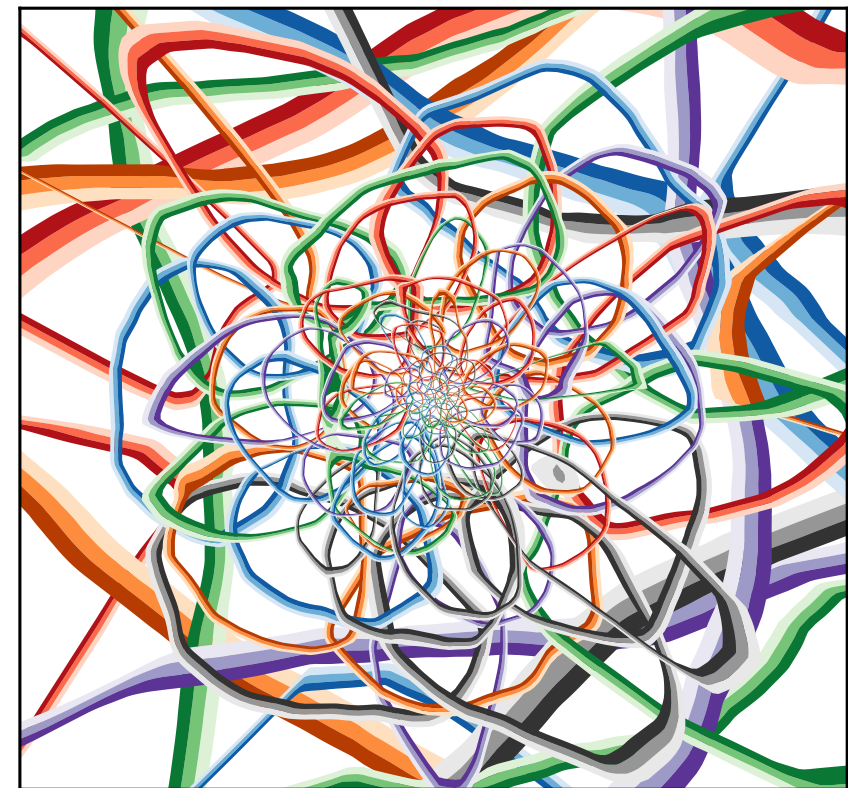


Learning QCD singularities!



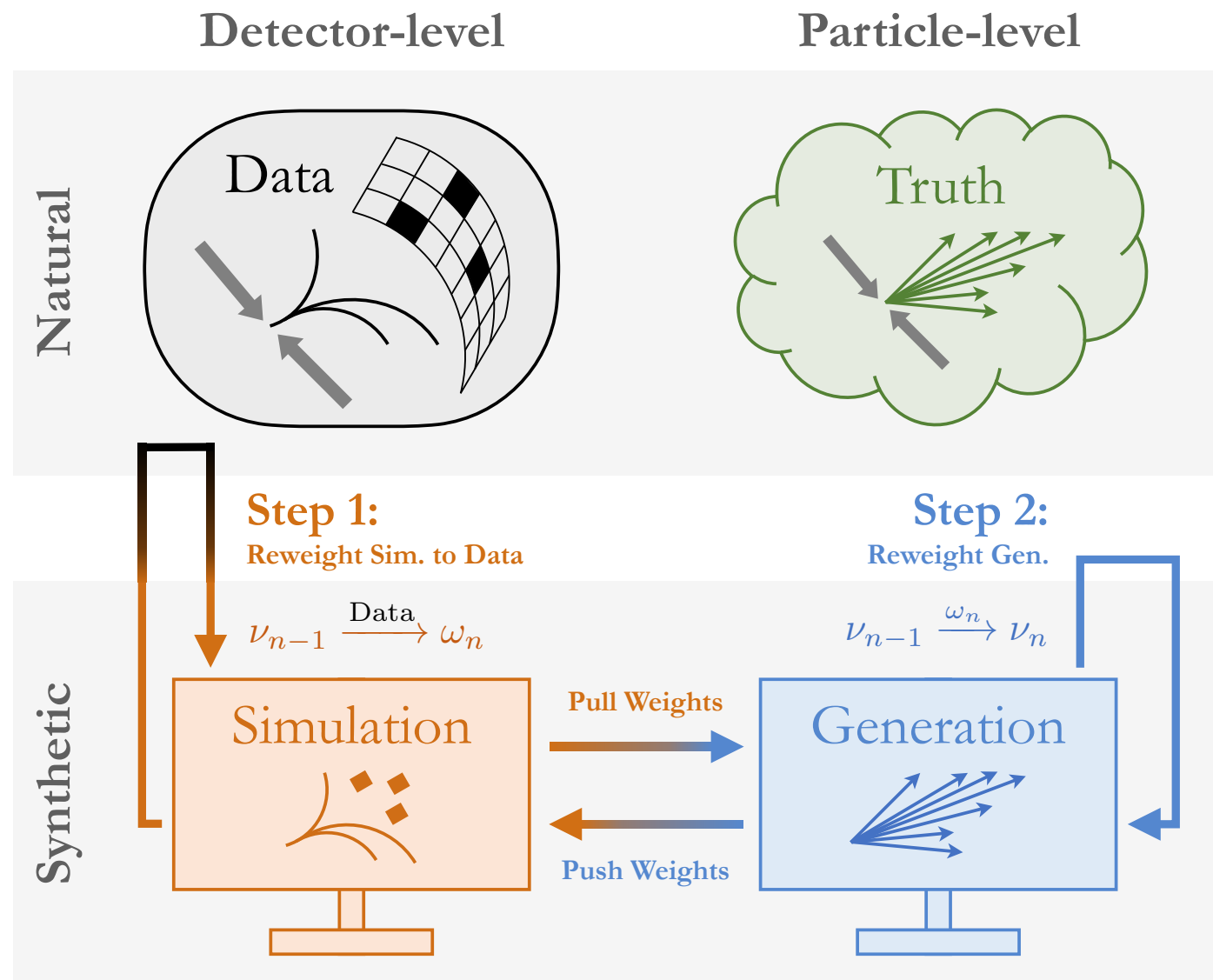
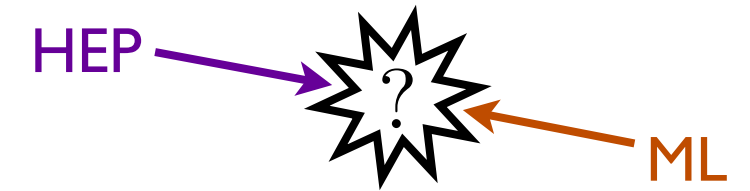
AP splitting probability:

$$dP_{i \rightarrow ig} \simeq \frac{2\alpha_s}{\pi} C_i \frac{d\theta}{\theta} \frac{dz}{z}$$



[Komiske, Metodiev, JDT, JHEP 2019; see also Komiske, Metodiev, JDT, JHEP 2018, PRD 2020; special case of Zaheer, Kottur, Ravanbakhsh, Poczos, Salakhutdinov, Smola, NIPS 2017]

OmniFold



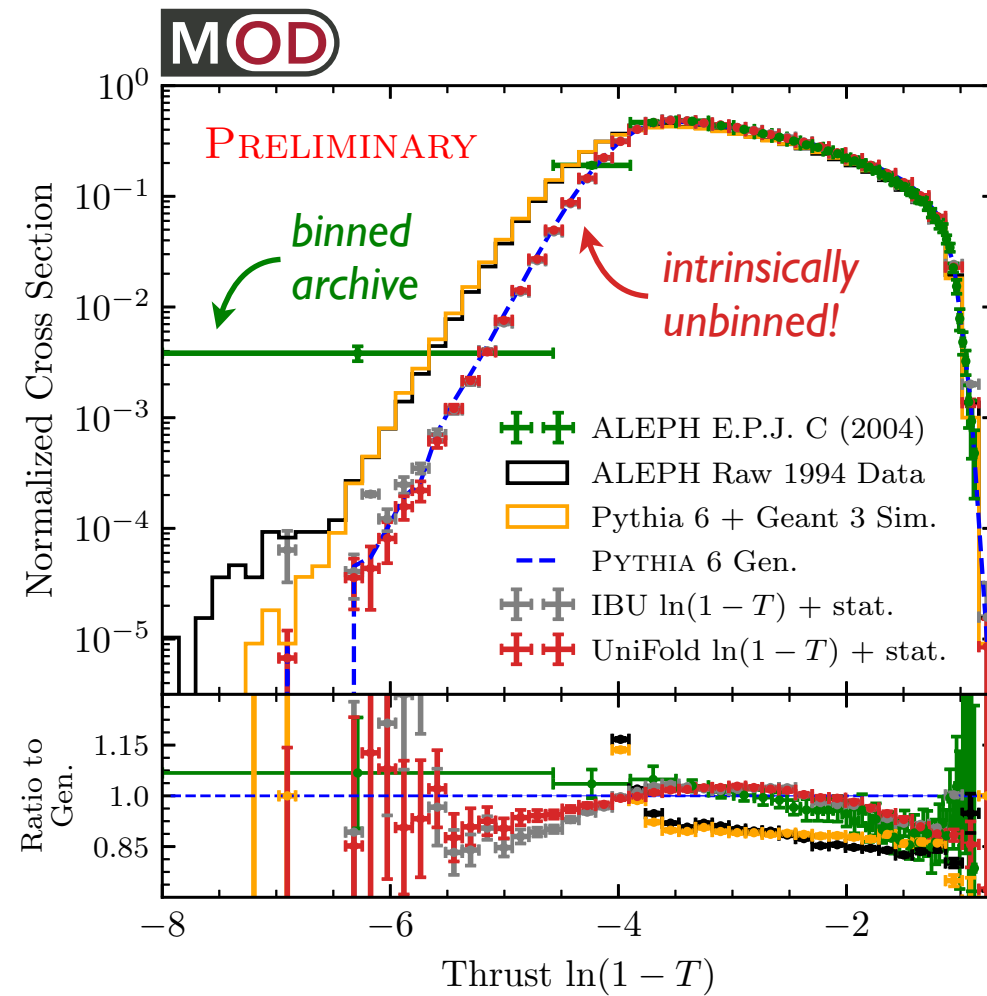
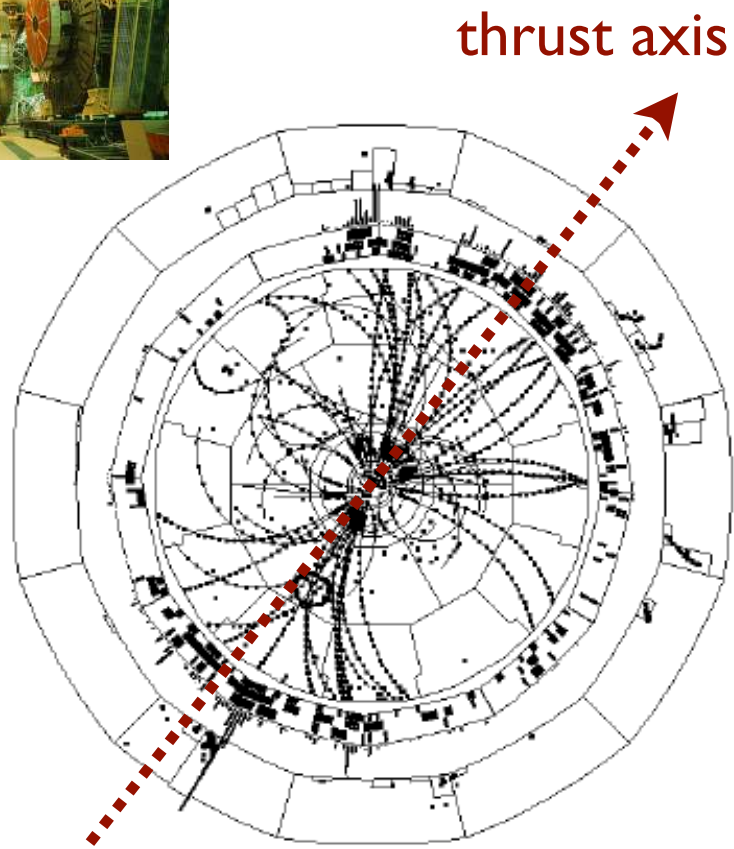
Using, e.g.,
Energy Flow
Networks

Multi-dimensional unbinned detector corrections via iterated binary classification

[Andreassen, Komiske, Metodiev, Nachman, JDT, PRL 2020]



Back to the Future with ALEPH Archival Data

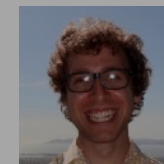


[talk by Badea, [ICHEP 2020](#); cf. ALEPH, [EPJ C 2004](#)]

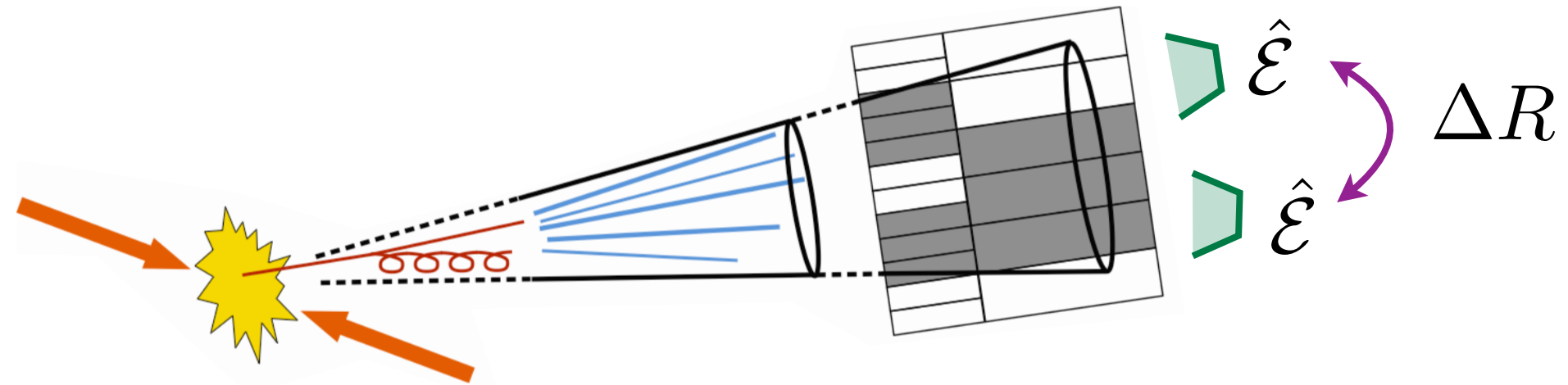
[see also Badea, Baty, Chang, Innocenti, Maggi, McGinn, Peters, Sheng, [JDT, Lee, PRL 2019](#)]



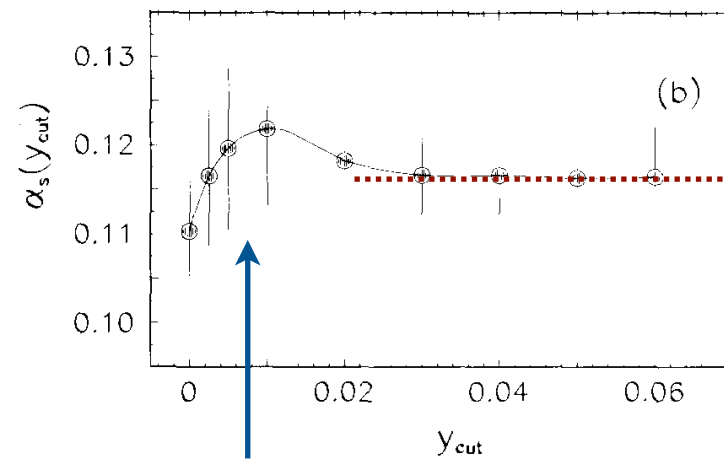
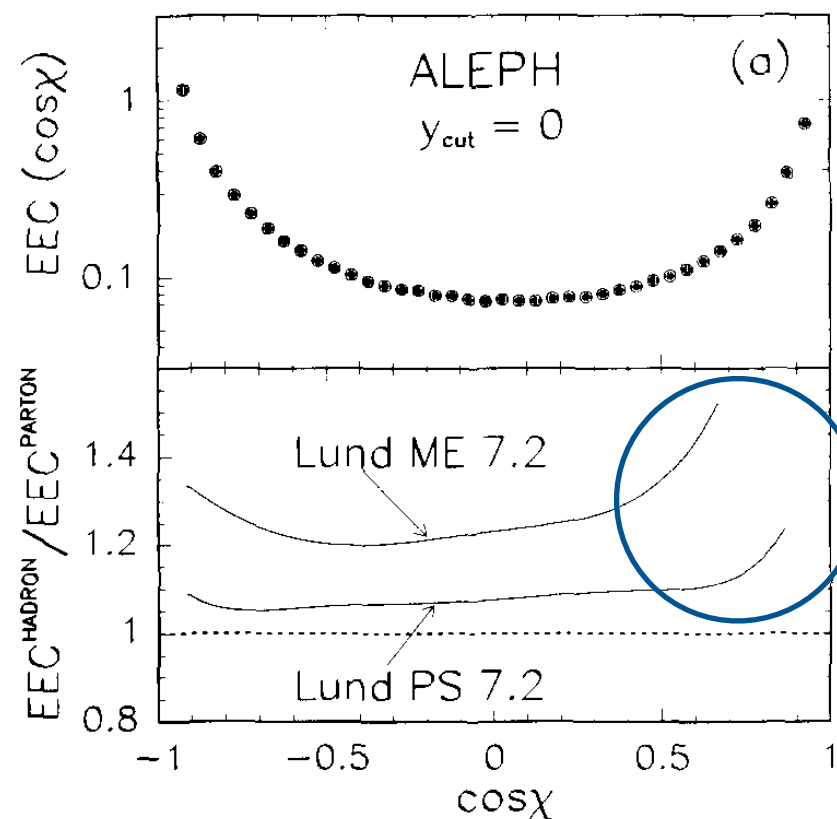
[Andreassen, Komiske, Metodiev, Nachman, [JDT, PRL 2020](#)]



Energy-Energy Correlators



A long history in probing collinear dynamics of QCD

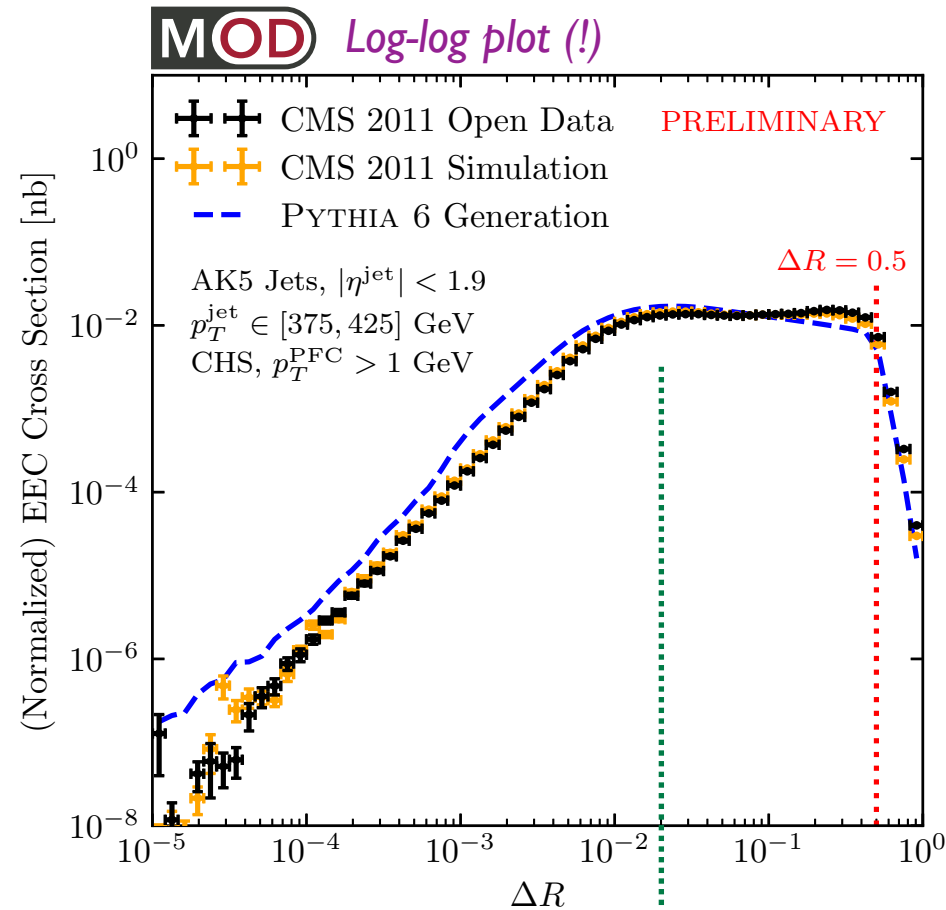


Extracting the strong coupling constant

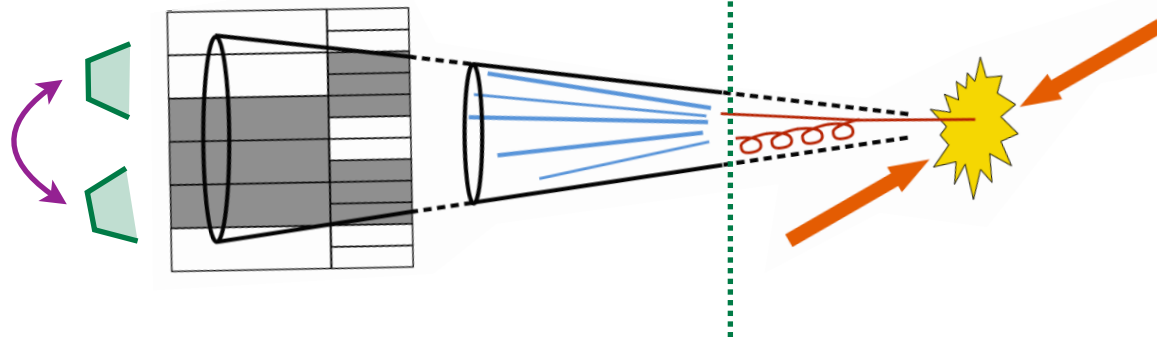
Theoretical challenges with small angle (collinear) limit

[Basham, Brown, Ellis, Love, *PRL* 1978; ALEPH, *PLB* 1991; see Chen, Mout, Zhang, Zhu, *PRD* 2020]

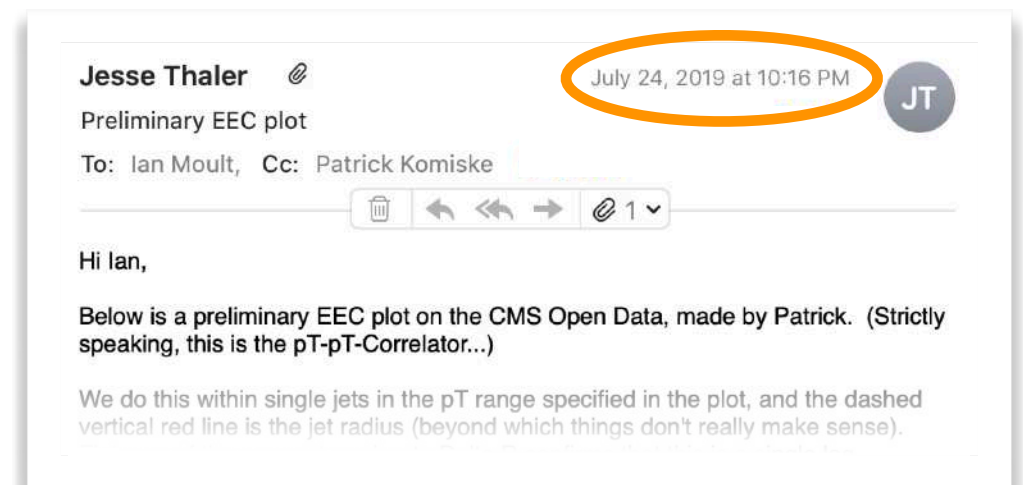
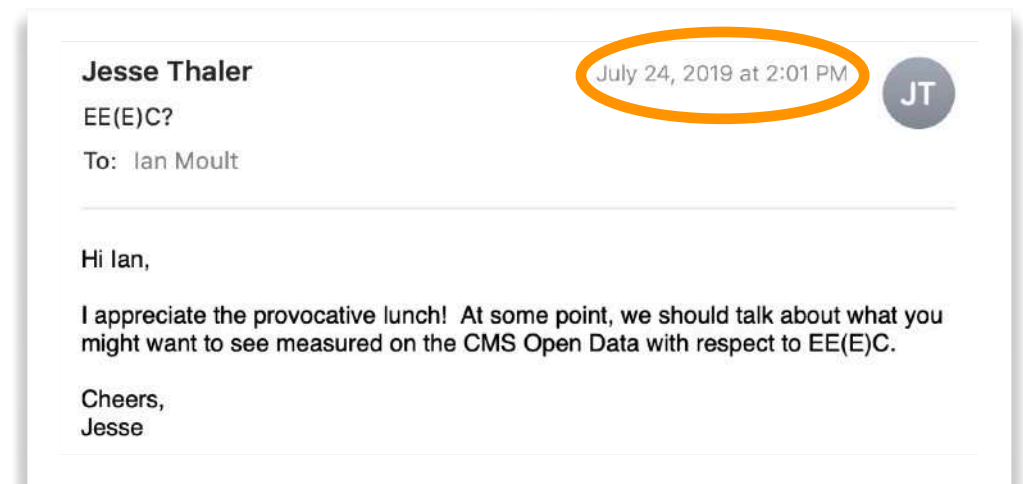
QCD Phase Transition in Jets?



← **Hadronic Phase** **Partonic Phase** →



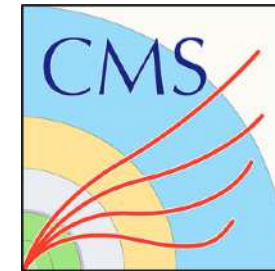
Behind the scenes at **BOOSTON 2019**



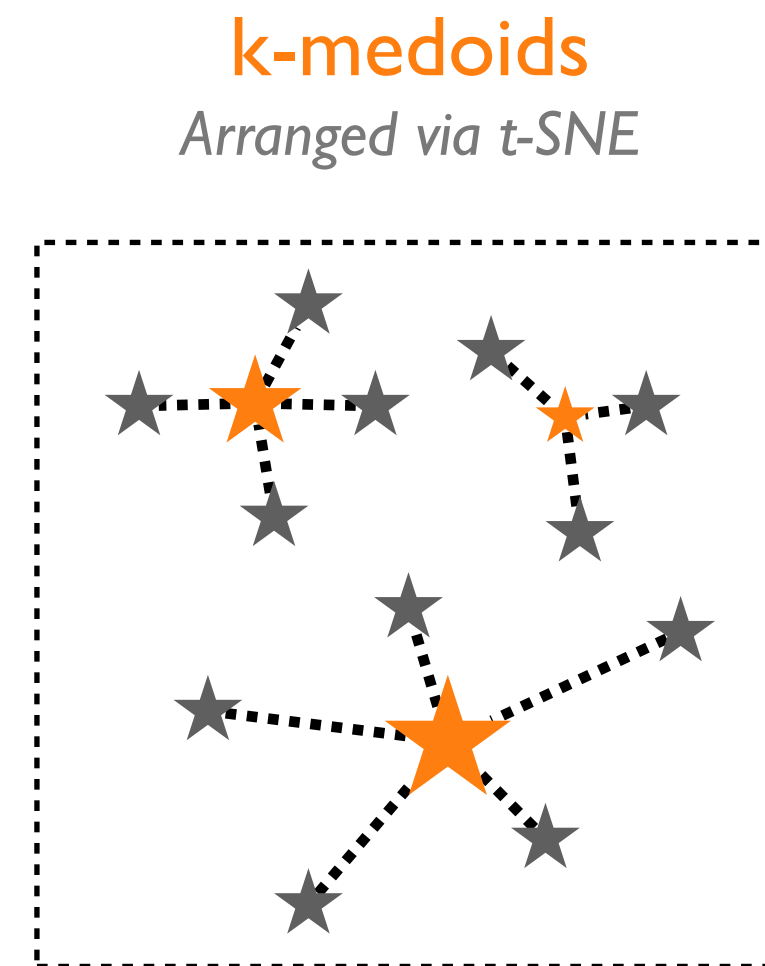
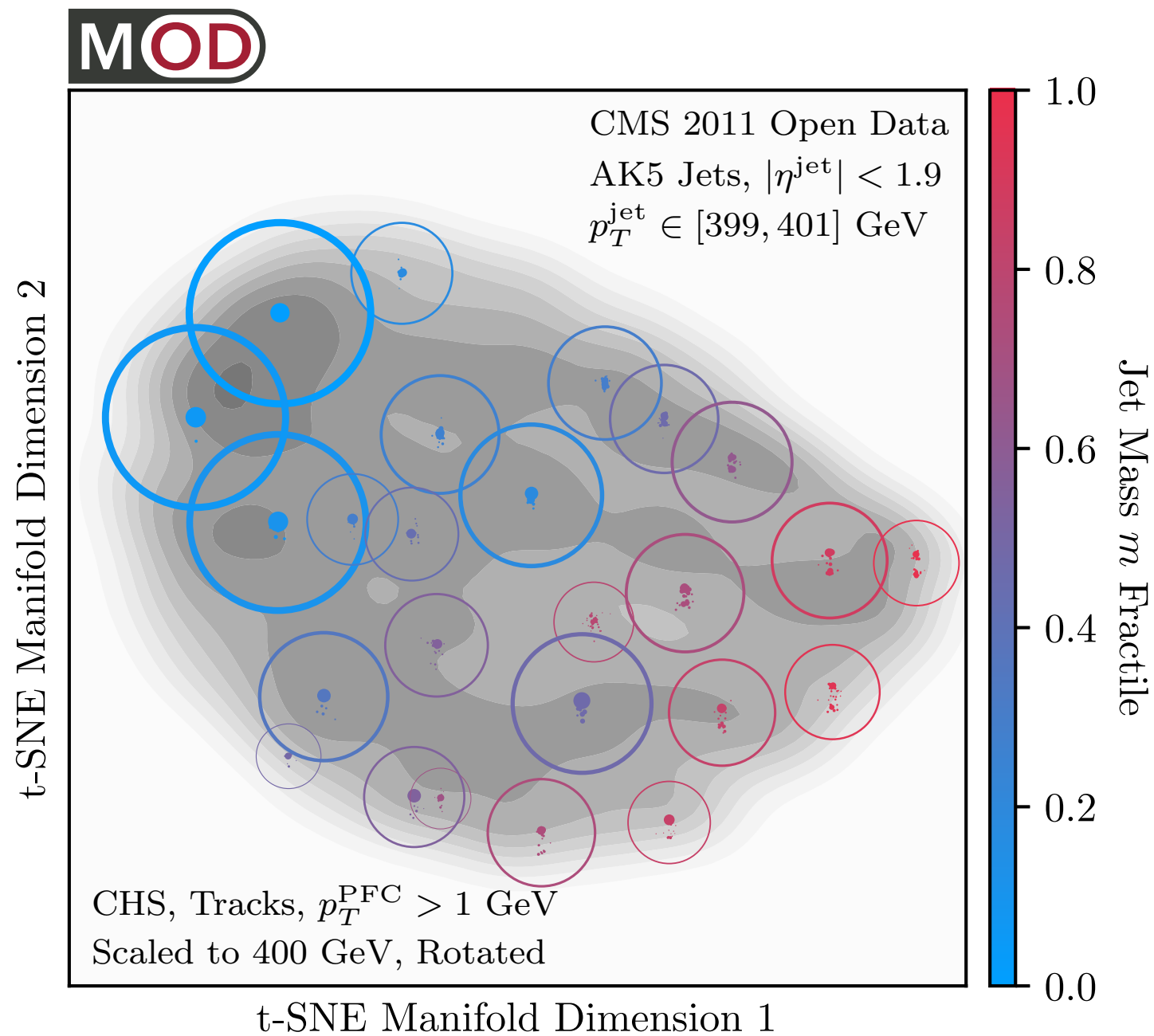
[Komiske, Moulton, JDT, et al., in progress; see talks by Moulton, [BOOST 2019](#), [BOOST 2020](#)]



Most Representative Jets

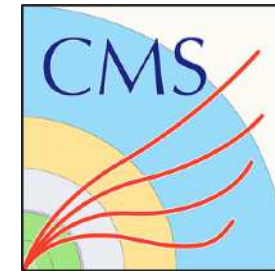


[<http://opendata.cern.ch/>]

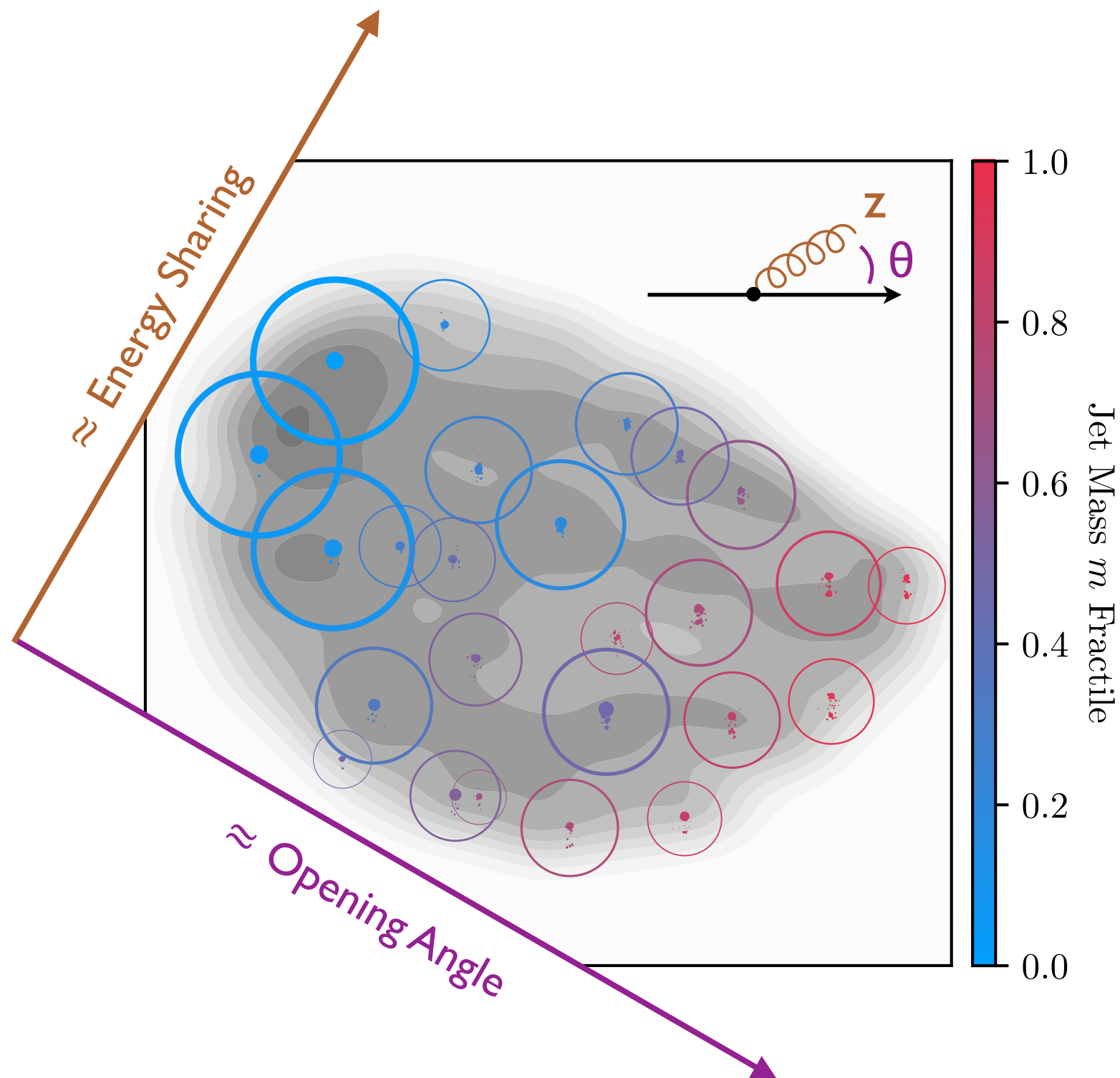


[Komiske, Mastandrea, Metodiev, Naik, JDT, [PRD 2020](#); using van der Maaten, Hinton, [JMLR 2008](#)]

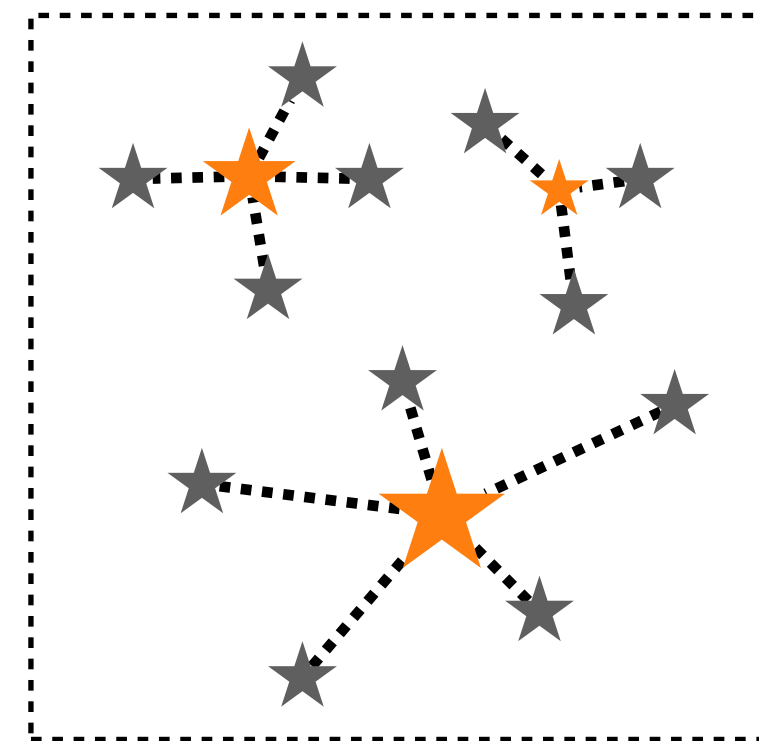
Most Representative Jets



[<http://opendata.cern.ch/>]

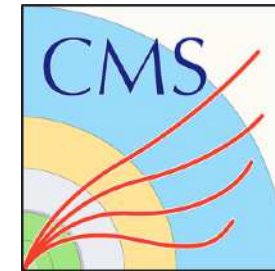


k-medoids
Arranged via *t*-SNE

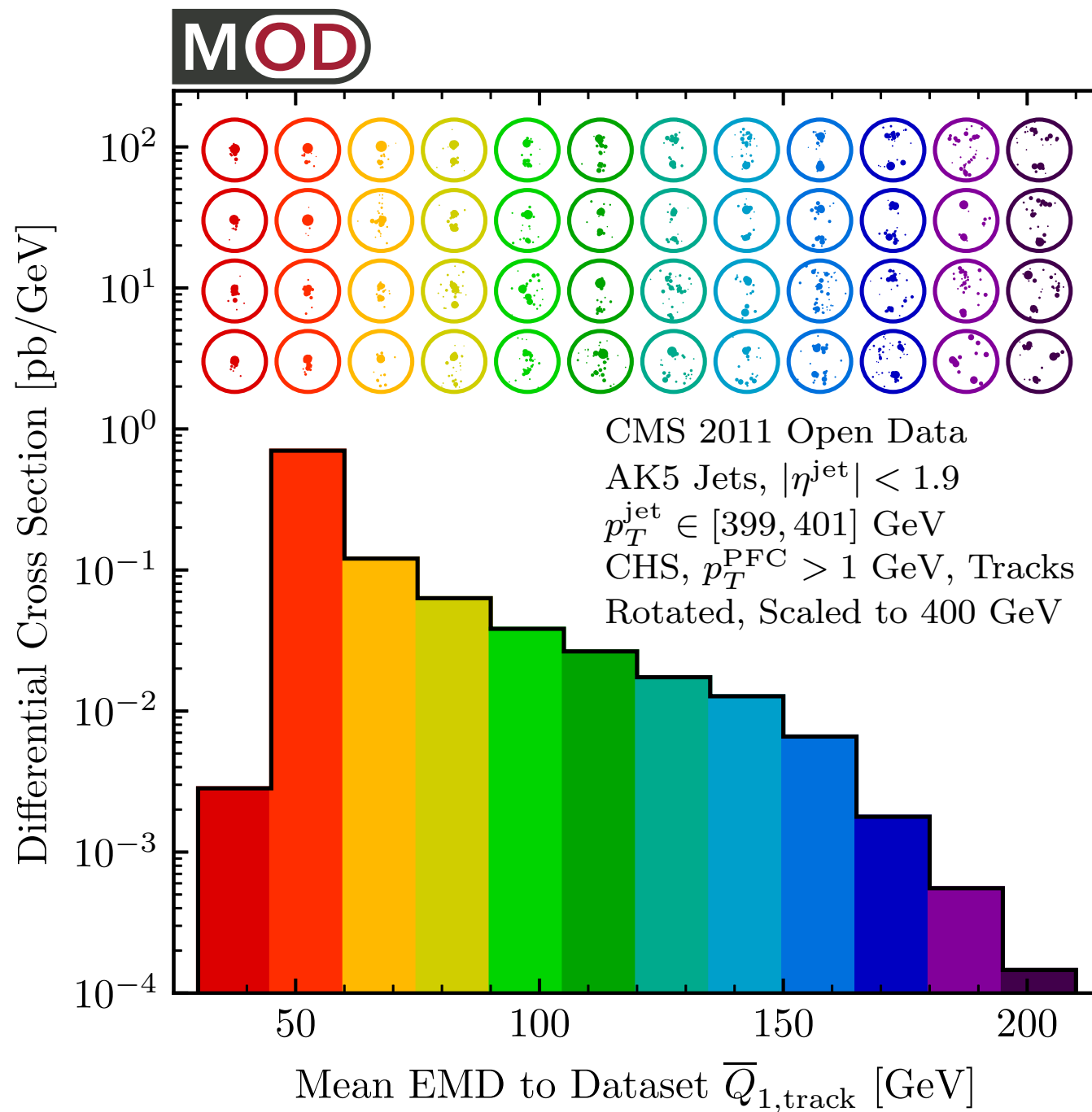


[Komiske, Mastandrea, Metodiev, Naik, JDT, PRD 2020; using van der Maaten, Hinton, JMLR 2008]

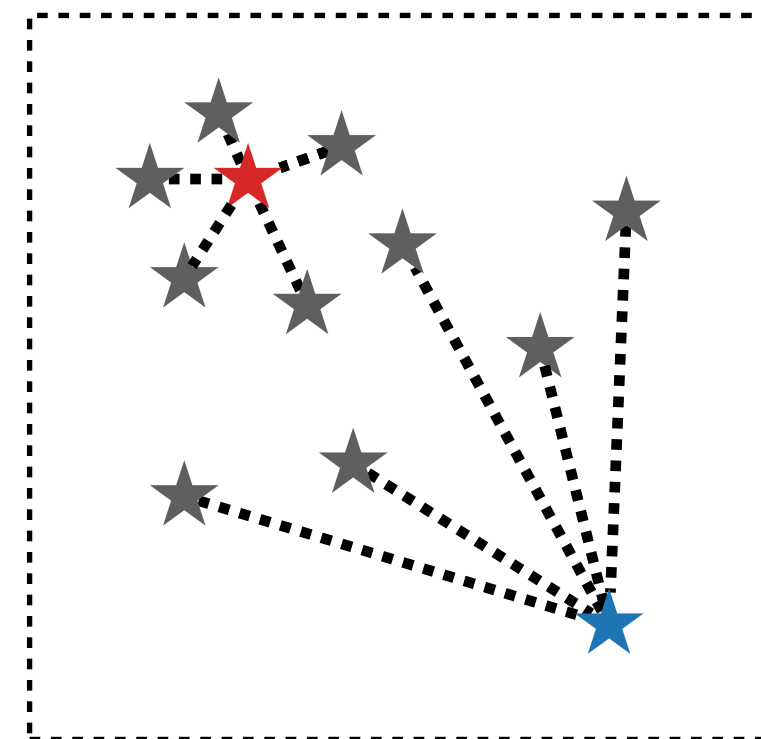
Least Representative Jets



[<http://opendata.cern.ch/>]



New Physics?
 Or tails of QCD?



[Komiske, Mastandrea, Metodiev, Naik, JDT, PRD 2020]

Additional Travel Documentation

