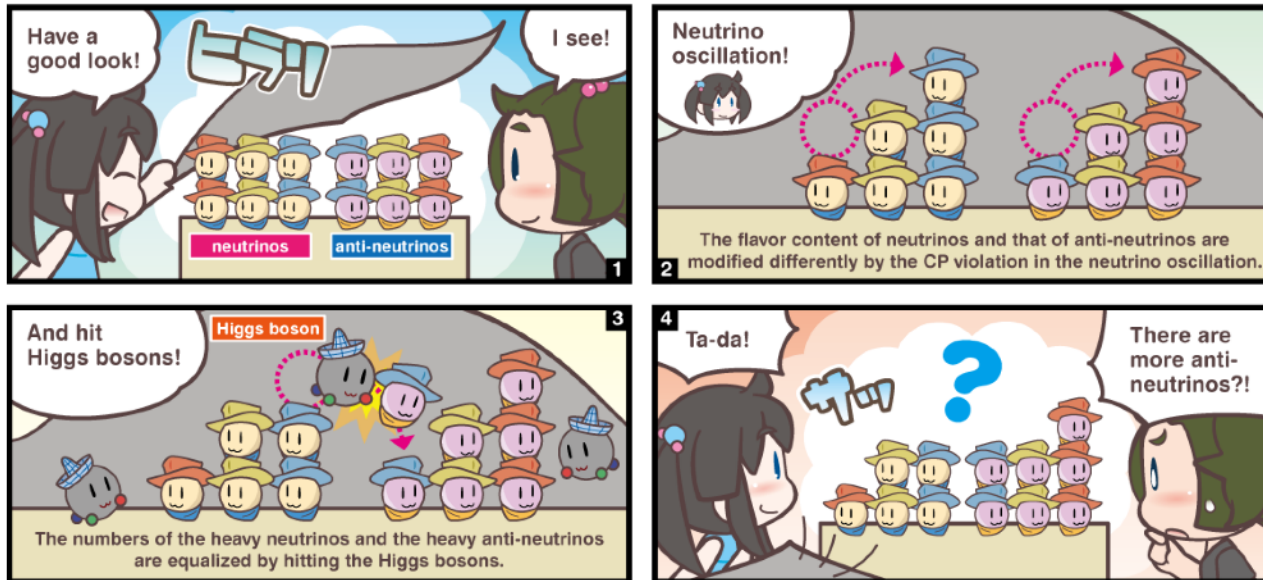


Leptogenesis via active neutrino oscillation

Wen Yin, KAIST in Korea

Neutrino Magic!



©higgstan.com



More anti-neutrinos than neutrinos?
 Starting with the same numbers of neutrinos and anti-neutrinos, some magic under the cloth created an imbalance between them. This CP violating phenomenon, if it has really happened in the early Universe, give the reason for the Universe being made of matter rather than anti-matter.

comic by Yuki Akimoto,
higgstan.com

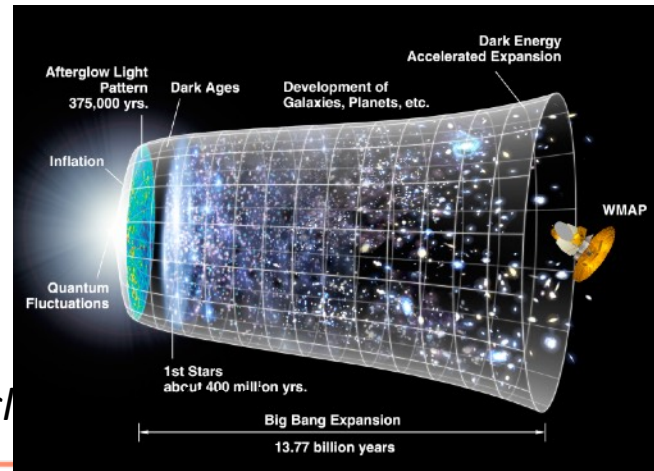
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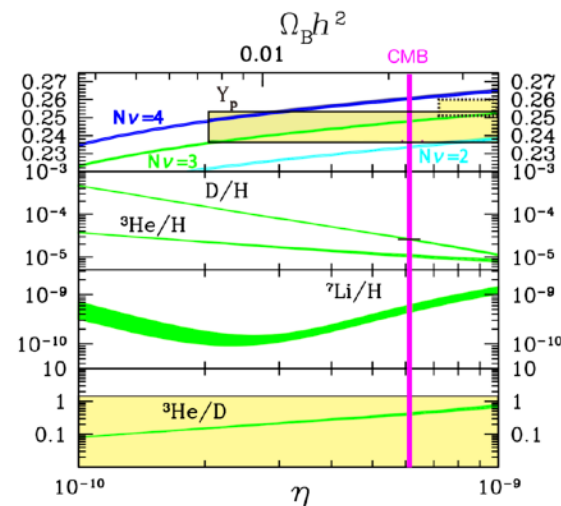
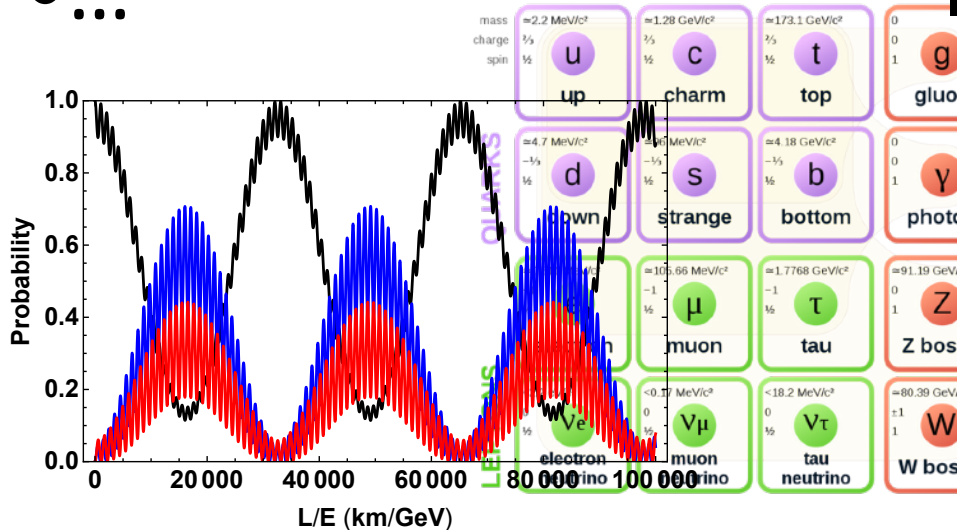
1. Introduction

The mysteries of particle physics and particle cosmology.

- Inflation
- Matter-antimatter asymmetry (Baryon asymmetry)
- Neutrino oscillation



Standard model of particle physics



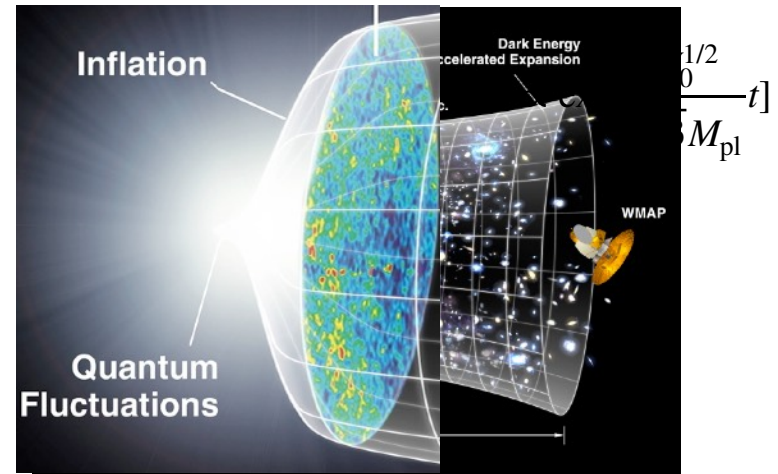
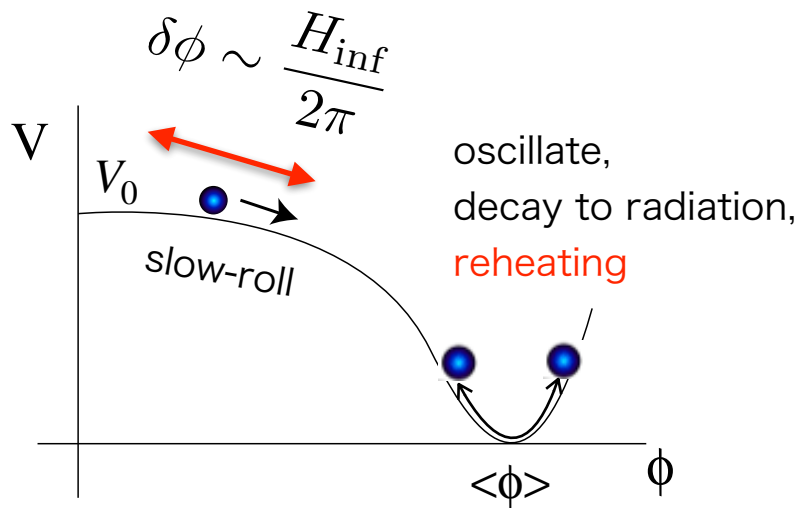
wikipedia, Kawasaki et al, 1709.01211

New physics: inflation

A.Guth, 1980; K.Sato, 1980; A.Starobinsky, 1980; Kazanas, 1980; A.Linde, 1981; Albrecht, Steinhardt, 1981;

The Universe experienced an exponential expansion.

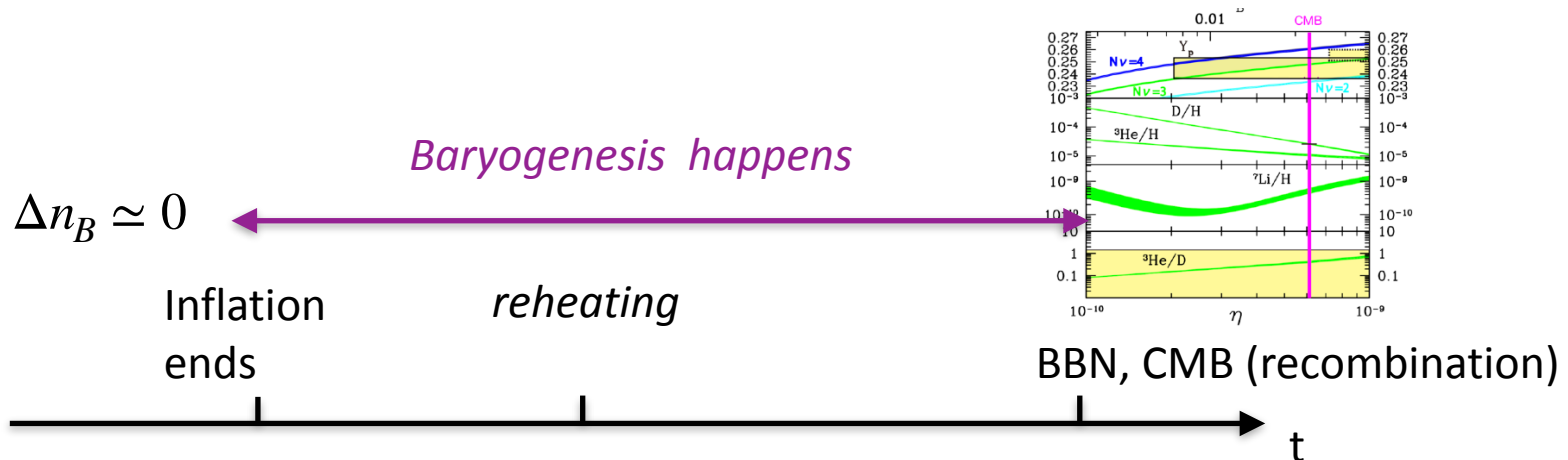
Inflation solves horizon and flatness problems.



Inflaton ϕ :

Quantum fluctuation for anisotropy of the Universe which has been observed in CMB.

New physics: baryogenesis



To generate the baryon asymmetry of our universe (BAU) Sakharov's conditions should be satisfied:

- **Baryon/Lepton number violation* with sphaleron
- **C and CP violation*
- **Out of thermal equilibrium*

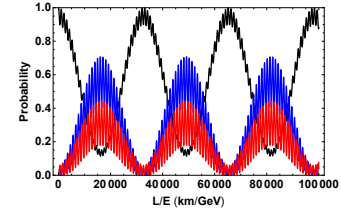
Unfortunately, the SM of the particle theory does not sufficiently satisfy them... **New physics is needed for baryogenesis!**

New physics: neutrino oscillation

A simple explanation:

the SM is non-renormalizable effective theory

i.e. Majorana neutrino



$$\mathcal{L}_{SM} = \mathcal{L}_{SM}^{d \leq 4} - \frac{\kappa_{ij}}{2} \bar{L}_i^c \hat{P}_L L_j H H + h.c. + \dots$$

\Downarrow
 $\frac{m_{\nu ij}}{2} \bar{\nu}_i^c \hat{P}_L \nu_j$

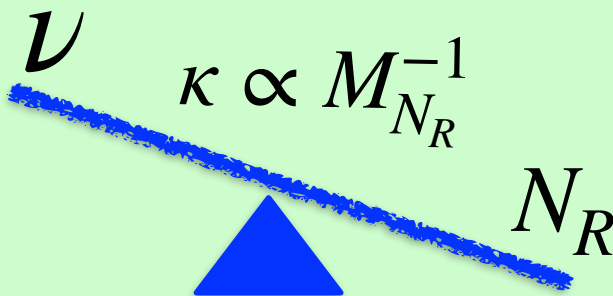
Lepton # violating

Possible origins of higher dimensional terms

Generated by heavy particles

e.g. *seesaw mechanism*

Yanagida 79; Gell-Mann, et al 79; Minkowski, 77;



Just exist as it is valid
up to very high energy
scale.

(cf. Perturbative calculation
is justified up to $10^{17} GeV$.)

Baryogenesis with Majorana neutrino

By assuming seesaw mechanism, Sakharov's conditions are satisfied in N_R sector

- Thermal leptogenesis

M. Fukugita, T. Yanagida 1986

- Resonant leptogenesis

Pilaftsis 1997; Buchmuller Plumacher, 1998

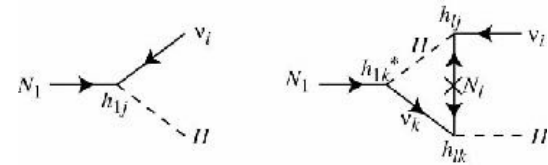
- Baryogenesis via right-handed neutrino oscillation

Akhmedov et al, 1998; Asaka, Shaposhnikov, 2005;

Sakharov's conditions are satisfied at around reheating era, *without* N_R .

- Leptogenesis via active neutrino oscillation

Hamada, Kitano, 2016; Hamada, Kitano, WY, 2018;



CP-violating decay

I will be talking about

BAU can be explained due to neutrino oscillation with

$$\mathcal{L} = \mathcal{L}_{SM}^{d \leq 4} - \frac{\kappa_{ij}}{2} \bar{L}_i^c \hat{P}_L L_j H H + h.c. \quad \text{at around reheating era.}$$

- BAU explained with $T_R \gtrsim 10^8 GeV$ for ϕ decays to leptons.
- If ϕ dominantly decays to Higgs bosons, the scenario can be tested from ground-based experiments.
- Application of the mechanism with lower reheat temperature is discussed.

2. Leptogenesis via active neutrino oscillation

Kitano, Hamada, WY 1807.06582

Setup:

$$\mathcal{L} = \mathcal{L}_{SM}^{d \leq 4} - \frac{\kappa_{ij}}{2} \bar{L}_i^c \hat{P}_L L_j H H + h.c.$$

Sakharov's conditions

* *Baryon/Lepton number violation* ✓

* *C and CP violation* ✓ *neutrino oscillation. CP-violation is favored at 2σ* [T2K,1701.00432](#)

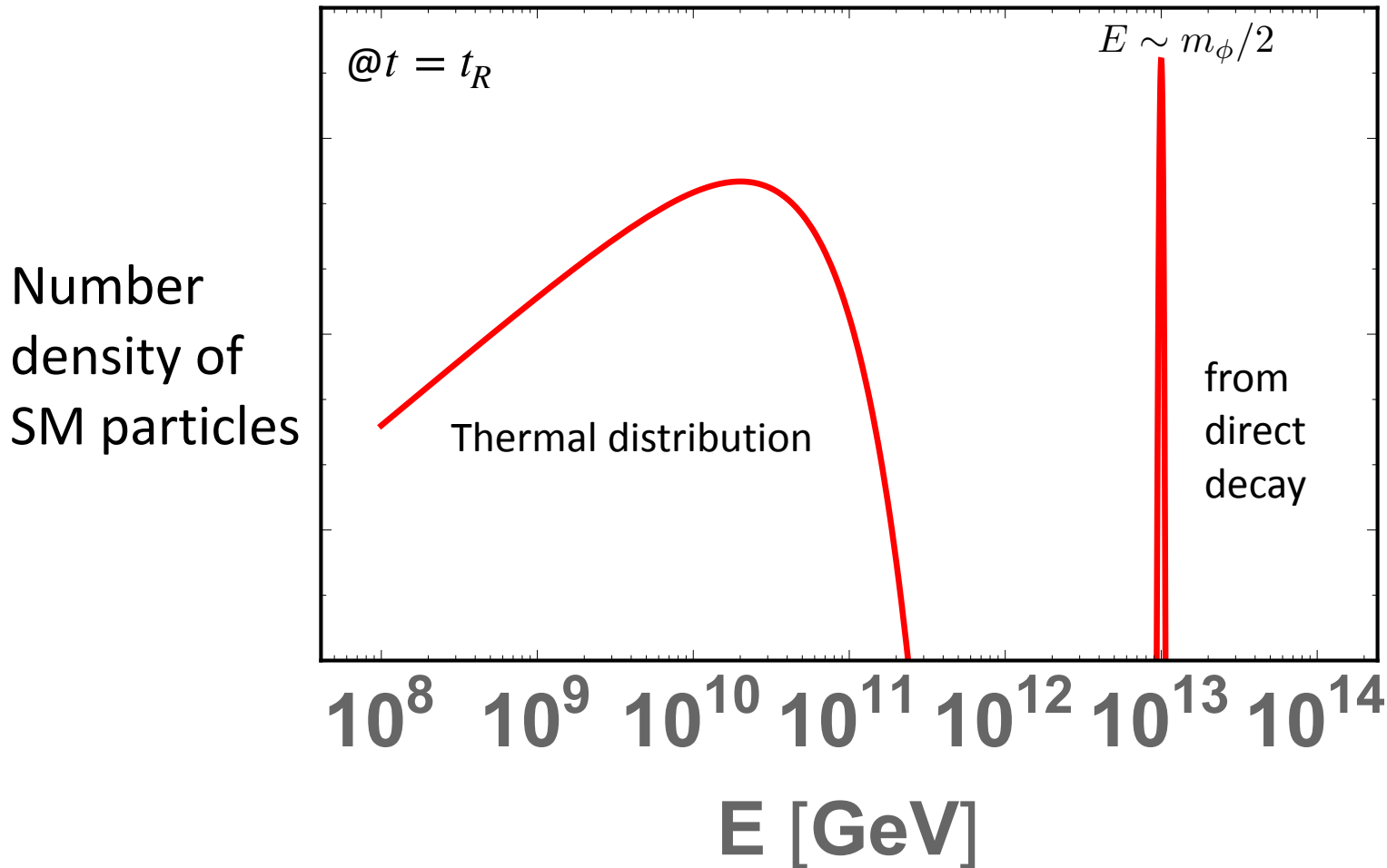
* *Out of thermal equilibrium* ✓ *thermalization around reheating*

See also leptogenesis via active neutrino oscillation with dimension 5 and 8 terms. [Kitano, Hamada 1609.05028](#).

Thermalization during reheating

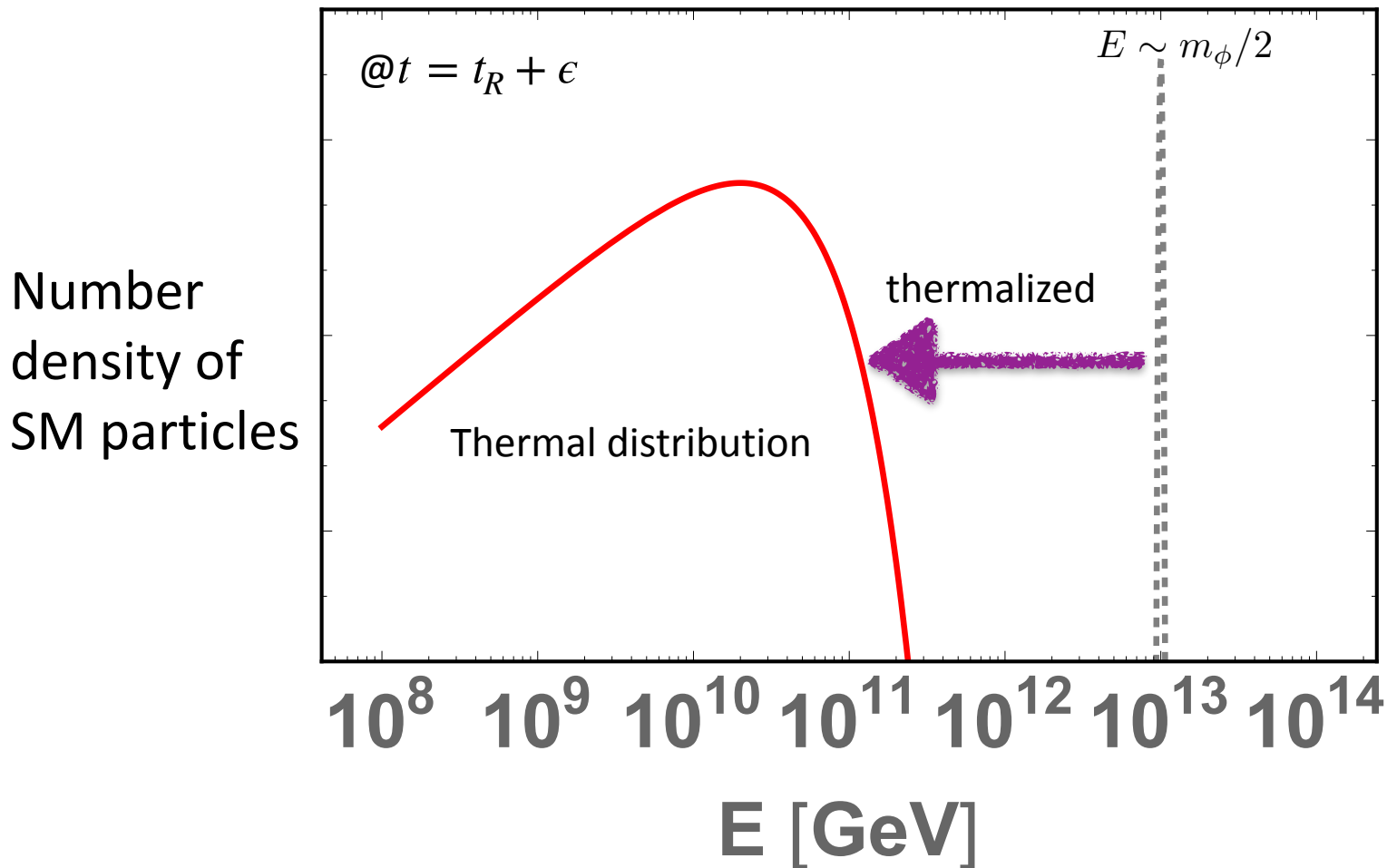
Inflaton decay: $\phi \rightarrow \text{SM particles}$ (2 body)

at the moment of an inflaton decay

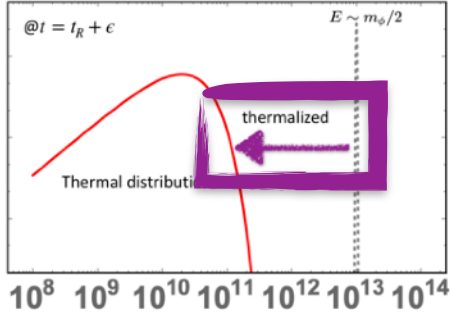


Thermalization during reheating

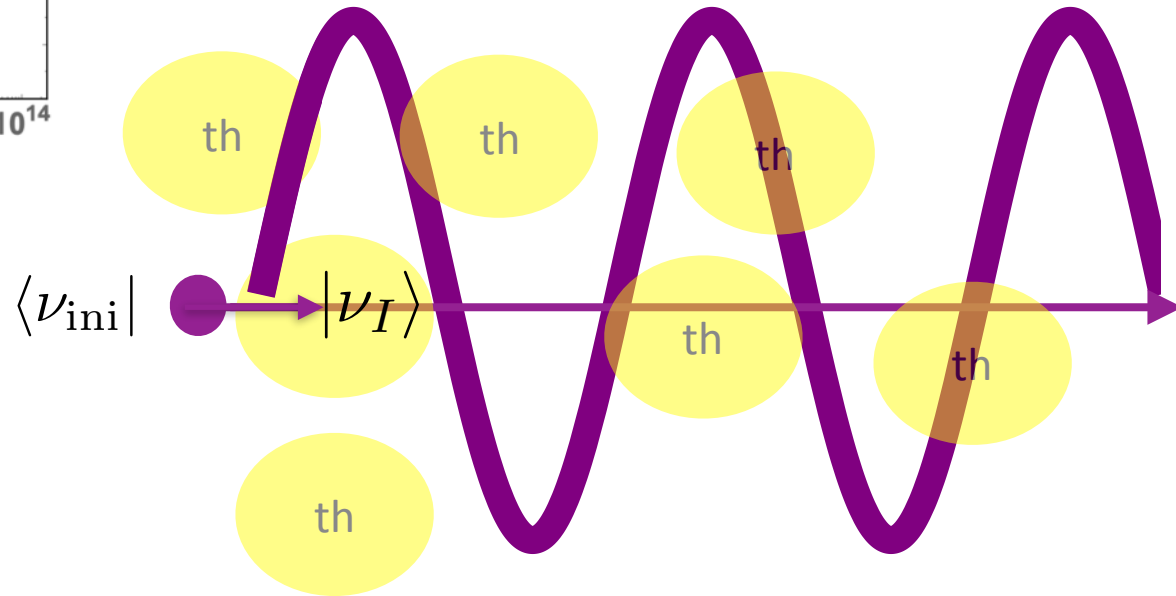
Inflaton decay: $\phi \rightarrow \text{SM particles}$



Neutrino oscillation during thermalization



$$\phi \rightarrow \nu_{\text{ini}} + X, \bar{\nu}_{\text{ini}} + \bar{X}$$



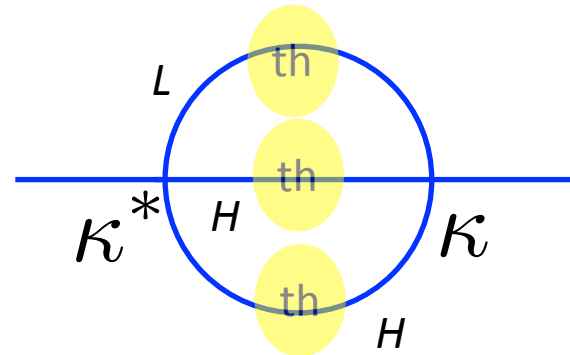
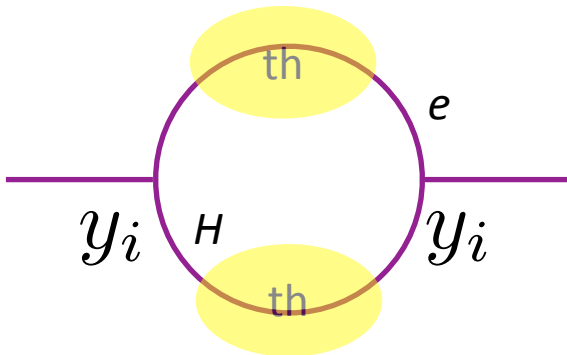
$$P_{\text{ini} \rightarrow I} \simeq \left| \sum_{\alpha} \langle \nu_{\text{ini}} | \nu_{\alpha} \rangle e^{it_{\text{MFP}} (m_{\nu_{\alpha}}^{\text{th}})^2 / k} \langle \nu_{\alpha} | \nu_I \rangle \right|^2$$

c.f. $P_{e \rightarrow \mu} \simeq \left| \sum_{\alpha} \langle \nu_e | \nu_{\alpha} \rangle e^{it_{\text{MFP}} m_{\nu_{\alpha}}^2 / k} \langle \nu_{\alpha} | \nu_{\mu} \rangle \right|^2$ @ vacuum

Thermal mass

$$P_{\text{ini} \rightarrow I} \simeq \left| \sum_{\alpha} \langle \nu_{\text{ini}} | \nu_{\alpha} \rangle e^{it_{\text{MFP}} \underline{(m_{\nu_{\alpha}}^{\text{th}})^2 / k}} \langle \nu_{\alpha} | \nu_I \rangle \right|^2$$

$$(m_{\nu_{\alpha}}^{\text{th}})^2 = \text{eigen} \left[\underline{\frac{y_i^2 T^2}{16}} \delta_{ij} + \underline{0.046 (\kappa^* \kappa)_{ij} T^4} \right] + C \delta_{ij}$$



$|\nu_{\alpha}\rangle$ is the mass eigenstate.

Neutrino oscillation provides CP violation

$$P_{\text{ini} \rightarrow I} \simeq \left| \sum_{\alpha} \langle \nu_{\text{ini}} | \nu_{\alpha} \rangle e^{it_{\text{MFP}} (m_{\nu_{\alpha}}^{\text{th}})^2 / k} \langle \nu_{\alpha} | \nu_I \rangle \right|^2$$

$$t_{\text{MFP}} \sim \frac{1}{\alpha_2^2 T} \sqrt{\frac{k}{T}} \quad (m_{\nu, \alpha}^{\text{th}})^2 = \text{eigen} \left[\frac{y_i^2 T^2}{16} \delta_{ij} + 0.046 (\kappa^* \kappa)_{ij} T^4 \right] + C \delta_{ij}$$

$$P_{\text{ini} \rightarrow I} - P_{\text{ini} \rightarrow \bar{I}} \propto \frac{\Delta(m_{\nu}^{\text{th}})^2}{k} t_{\text{MFP}} \sim 0.01 \sqrt{T/k}$$

c.f. $P_{e \rightarrow \mu} - P_{\bar{e} \rightarrow \bar{\mu}} \propto \sin[t \Delta m_{\nu}^2 / k]$ @vacuum

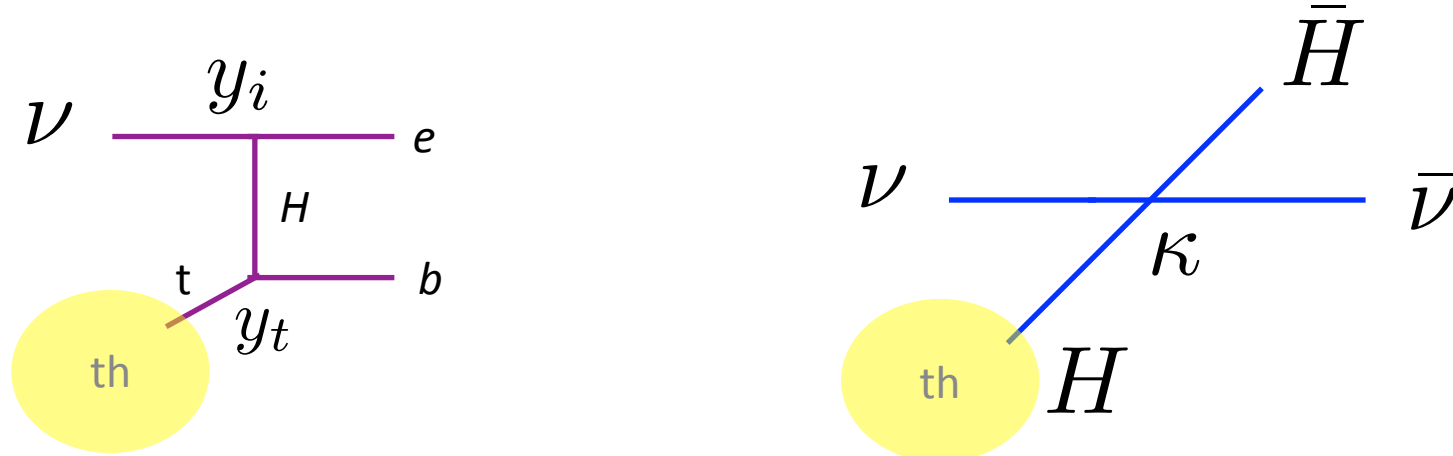
Oscillation phase is not too small at the reheating era.

How to observe “flavor”?

$$P_{\text{ini} \rightarrow I} \simeq \left| \sum_{\alpha} \langle \nu_{\text{ini}} | \nu_{\alpha} \rangle e^{it_{\text{MFP}} (m_{\nu_{\alpha}}^{\text{th}})^2 / k} \langle \nu_{\alpha} | \nu_I \rangle \right|^2$$

Only flavor dependent process can identify the flavor.

“Observation” is made due to the following interaction process.



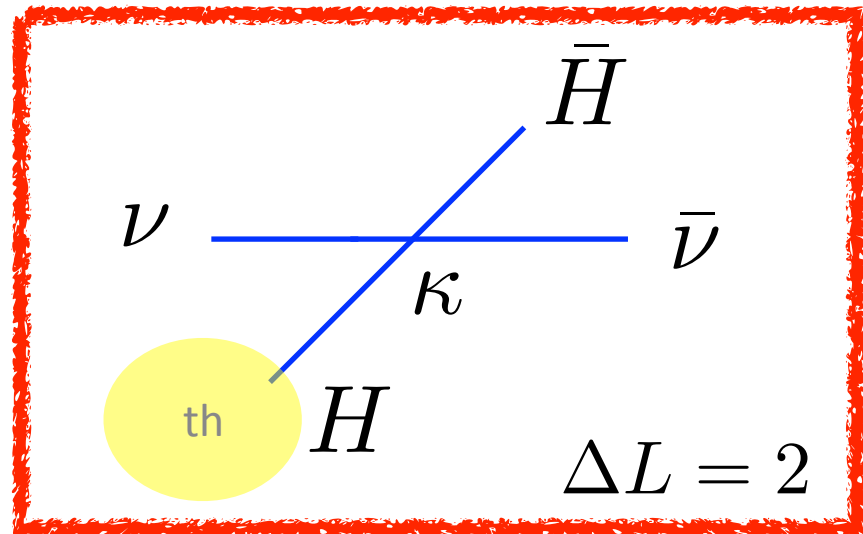
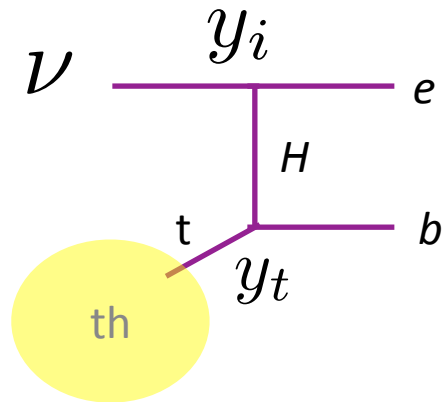
$|\nu_I\rangle$ is the state defined by the interaction.

Lepton number violation happens through “observation”.

$$P_{\text{ini} \rightarrow I} \simeq \left| \sum_{\alpha} \langle \nu_{\text{ini}} | \nu_{\alpha} \rangle e^{it_{\text{MFP}} (m_{\nu_{\alpha}}^{\text{th}})^2 / k} \langle \nu_{\alpha} | \nu_I \rangle \right|^2$$

Only flavor dependent process can identify the flavor.

“Observation” is made due to the following interaction process.



Lepton asymmetry can be made!

The (naive) estimation of lepton asymmetry

$m_\phi \sim T \ll 10^{12} \text{ GeV}$ with O(1) CP phase, general flavor structure

$$\frac{\Delta n_L}{S} \propto B_{\phi \rightarrow \nu_{\text{ini}} + X / \bar{\nu}_{\text{ini}} + \bar{X}} \times \underbrace{t_{MFP} \frac{\Delta m_\nu^2}{T}}_{\text{CP violation}} \times \underbrace{\frac{\sigma_{LLHH}^{\text{th}}}{\sigma_{\text{yukawa}}^{\text{th}}}}_{\text{lepton \# violation}}$$

— Flavor dependent asymmetry of order $\frac{\Delta m_{\text{th}}^2}{T} \frac{1}{\Gamma_{\text{th}}} \sim 0.01$

— How frequently the flavor is observed by the llHH interaction.

$$\frac{\sigma_{llHH}^{\text{th}}}{\sigma_{\text{yukawa}}^{\text{th}}} \sim \frac{\Delta m_\nu^2 T^2}{y_\tau^2 y_t^2 v^4}$$

The (naive) estimation of lepton asymmetry

$m_\phi \sim T \ll 10^{12} \text{ GeV}$ with $O(1)$ CP phase, general flavor structure

$$\frac{\Delta n_L}{s} \propto B_{\phi \rightarrow \nu_{\text{ini}} + X / \bar{\nu}_{\text{ini}} + \bar{X}} \times 10^{-9} \left(\frac{T_R}{10^9 \text{ GeV}} \right)^2$$

c.f. required asymmetry $|\Delta n_L / s| \sim 10^{-10}$

Enough asymmetry can be generated with sufficiently high reheating temperature.

Numerical estimation

density matrix for left-handed leptons $\rho(\mathbf{p}) \equiv \rho_{ij}(\mathbf{p})$ $i, j = e, \mu, \tau$

Kinetic Equation (Extended Boltzmann Eqs)

Sigl, Raffelt, 1993

$$\begin{aligned}
 i \frac{d\rho(\mathbf{p})}{dt} &= [\Omega(\mathbf{p}), \rho(\mathbf{p})] - \frac{i}{2} \{ \Gamma_{\mathbf{p}}^d, \rho(\mathbf{p}) \} + \frac{i}{2} \{ \Gamma_{\mathbf{p}}^p, 1 - \rho(\mathbf{p}) \}, \\
 &\quad \text{Oscillation term} \quad \updownarrow \quad \text{Interaction terms (with CP phase)} \\
 i \frac{d\bar{\rho}(\mathbf{p})}{dt} &= -[\Omega(\mathbf{p}), \bar{\rho}(\mathbf{p})] - \frac{i}{2} \{ \Gamma_{\mathbf{p}}^d, \bar{\rho}(\mathbf{p}) \} + \frac{i}{2} \{ \Gamma_{\mathbf{p}}^p, 1 - \bar{\rho}(\mathbf{p}) \},
 \end{aligned}$$

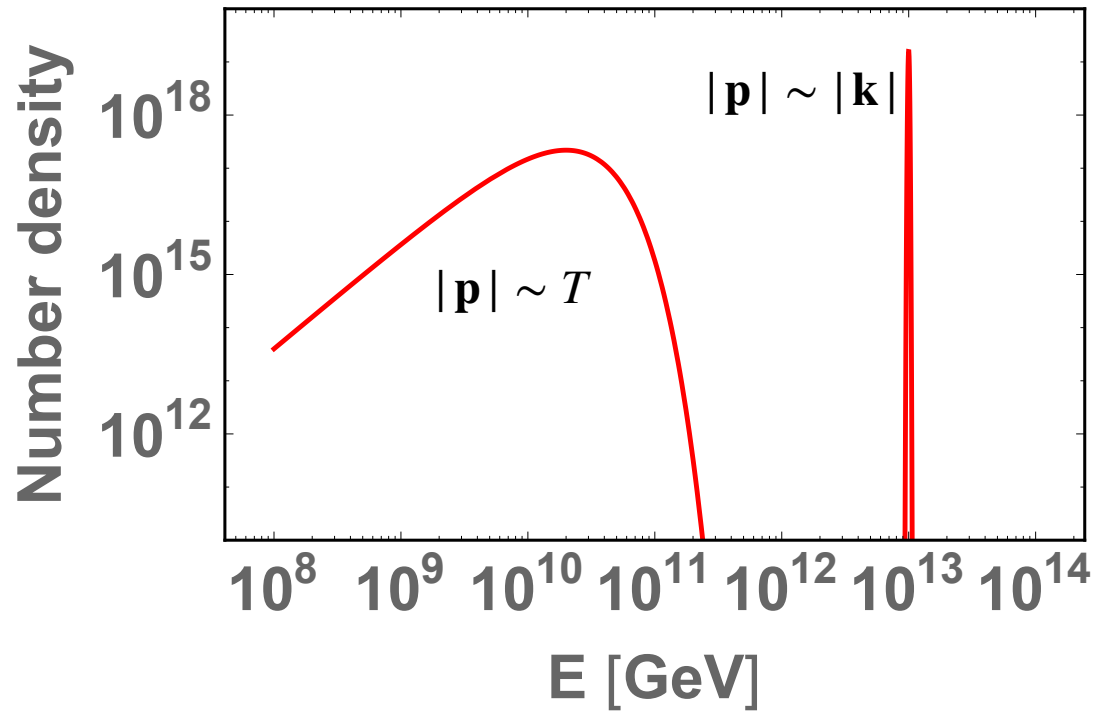
Oscillating phase

Thermalization, observation, L # violation

Hamiltonian: $\Omega_{ij}(\mathbf{p}) \simeq \frac{y_i^2 T^2}{16|\mathbf{p}|} \delta_{ij} + 0.046 (\kappa^* \kappa)_{ij} \frac{T^4}{|\mathbf{p}|}$, for $|\mathbf{p}| \gtrsim T$.

This is absent in ordinary Boltzmann eqs.

Two scale approximation



$$(\rho_{\mathbf{k}})_{ij} = \int_{|\mathbf{p}| \sim |\mathbf{k}|} \frac{d^3 \mathbf{p}}{(2\pi)^3} \frac{\rho_{ij}(\mathbf{p}, t)}{s},$$

$$(\delta \rho_T)_{ij} = \int_{|\mathbf{p}| \sim T} \frac{d^3 \mathbf{p}}{(2\pi)^3} \left(\frac{\rho_{ij}(\mathbf{p})}{s} - \frac{\rho_{ij}^{\text{eq}}(\mathbf{p})}{s} \right),$$

Equations to be solved

$$i\frac{d\rho_{\mathbf{k}}}{dt} = [\Omega_{\mathbf{k}}, \rho_{\mathbf{k}}] - \frac{i}{2}\{\Gamma_{\mathbf{k}}^d, \rho_{\mathbf{k}}\},$$

+ eqs of right-handed charged/anti leptons

$$i\frac{d\delta\rho_T}{dt} = [\Omega_T, \delta\rho_T] - \frac{i}{2}\{\Gamma_T^d, \delta\rho_T\} + i\delta\Gamma_T^p,$$

$$\Omega_{\mathbf{k}} \simeq \frac{y_i^2 T^2}{16m_\phi} \delta_{ij} + 0.046(\kappa^* \kappa)_{ij} \frac{T^4}{m_\phi} \quad \Omega_T \simeq \frac{y_i^2 T}{16} \delta_{ij} + 0.046(\kappa^* \kappa)_{ij} T^3$$

$$(\Gamma_{\mathbf{k}}^d)_{ij} \simeq C\alpha_2^2 T \sqrt{\frac{T}{|\mathbf{k}|}} \delta_{ij} + \frac{9y_t^2}{64\pi^3 |\mathbf{k}|} T^2 (\delta_{i\tau} \delta_{\tau j} y_\tau^2 + \delta_{i\mu} \delta_{\mu j} y_\mu^2) + \frac{21\zeta(3)}{32\pi^3} (\kappa^* \cdot \kappa)_{ij} T^3,$$

$$(\Gamma_T^d)_{ij} \simeq C'\alpha_2^2 T \delta_{ij} + \frac{9y_t^2}{64\pi^3} T (\delta_{i\tau} \delta_{\tau j} y_\tau^2 + \delta_{i\mu} \delta_{\mu j} y_\mu^2) + \frac{21\zeta(3)}{32\pi^3} (\kappa^* \cdot \kappa)_{ij} T^3,$$

$$(\delta\Gamma_T^p)_{ij} \simeq C\alpha_2^2 T \sqrt{\frac{T}{|\mathbf{k}|}} (\rho_{\mathbf{k}})_{ij} - C'\alpha_2^2 T (\delta\bar{\rho}_T)_{ij} \\ + \frac{3\zeta(3)}{8\pi^3} (\kappa^* \cdot (\bar{\rho}_{\mathbf{k}} - 3/4\rho_{\mathbf{k}})^t \cdot \kappa)_{ij} T^3 + \frac{3\zeta(3)}{8\pi^3} (\kappa^* \cdot (\delta\bar{\rho}_T - 3/4\delta\rho_T)^t \cdot \kappa)_{ij} T^3.$$

Some formula can be also found in [Akhmedov, et al. 9803255](#); [Abada, et al. 0601083](#).; [Asaka, et al. 1112.5565](#).
See Refs. [[Landau, Pomeranchuk 1953](#); [Migdal 1956](#)] for LPM effect.

$$\phi \rightarrow \nu_{\text{ini}} + X, \bar{\nu}_{\text{ini}} + \bar{X}$$

Initial condition

$$\rho_{\mathbf{k}}|_{t=t_R} = \bar{\rho}_{\mathbf{k}}|_{t=t_R} = \mathcal{N} V_i V_j^*, \quad \delta\rho_T|_{t=t_R} = \delta\bar{\rho}_T|_{t=t_R} = 0.$$

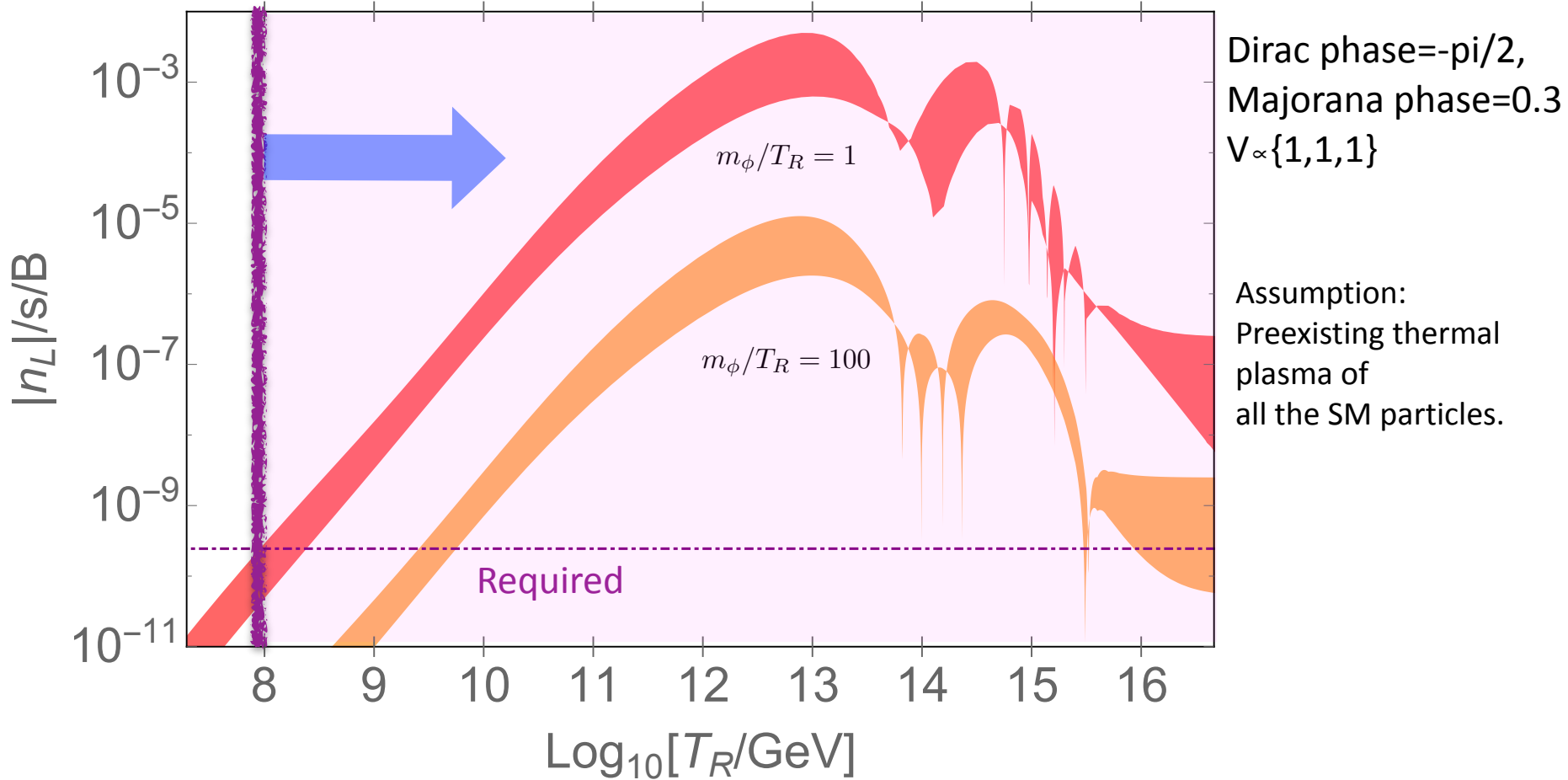
$$\mathcal{N} = \frac{3}{4} \frac{T_R}{m_\phi} B,$$

Free parameters

$$T_R, m_\phi, B, V_i$$

+Parameters in neutrino sector.

Numerical result (Normal Hierarchy)



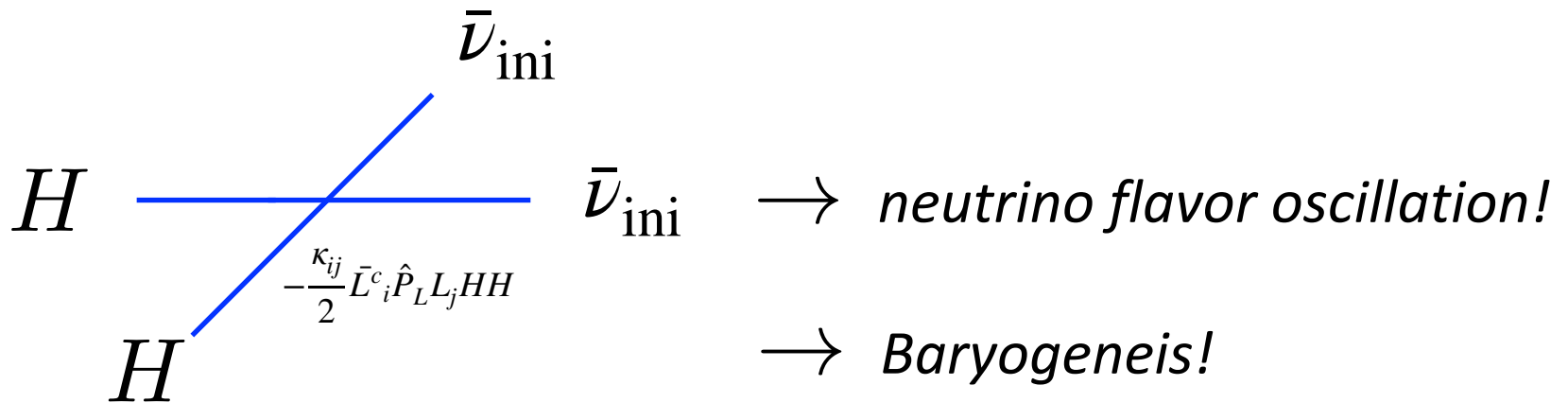
Baryogenesis can be successful for $T_R \gtrsim 10^8 \text{ GeV}$ due to active neutrino oscillation during thermalization.

3. Baryogenesis from PMNS matrix

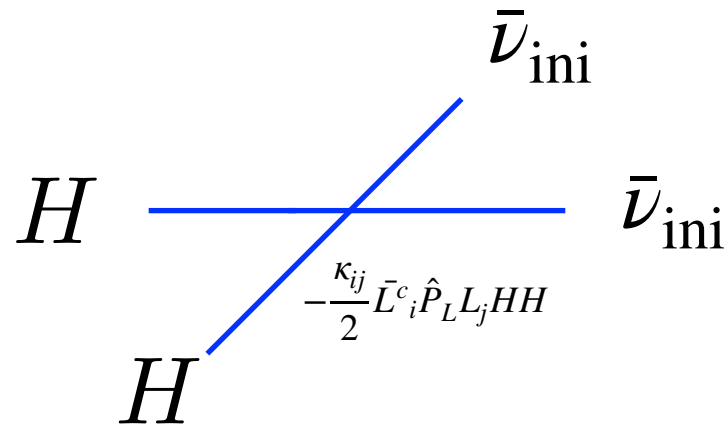
Let us consider the renormalizable inflaton coupling to the SM

$$\mathcal{L} \supset -A\phi |H|^2 - \lambda_\phi \phi^2 |H|^2 \quad A, \lambda_\phi: \text{real parameters}$$

$$\phi \rightarrow HH^*$$



***CP phase can appear only through κ_{ij} , i.e. the PMNS matrix.
The BAU is related with the PMNS matrix***



Initial conditions

$$(\rho_{\mathbf{k}})_{ij} = (\bar{\rho}_{\mathbf{k}})_{ij} = \mathcal{N} t_{MFP}^H \Gamma_{ij}^{LLHH}$$

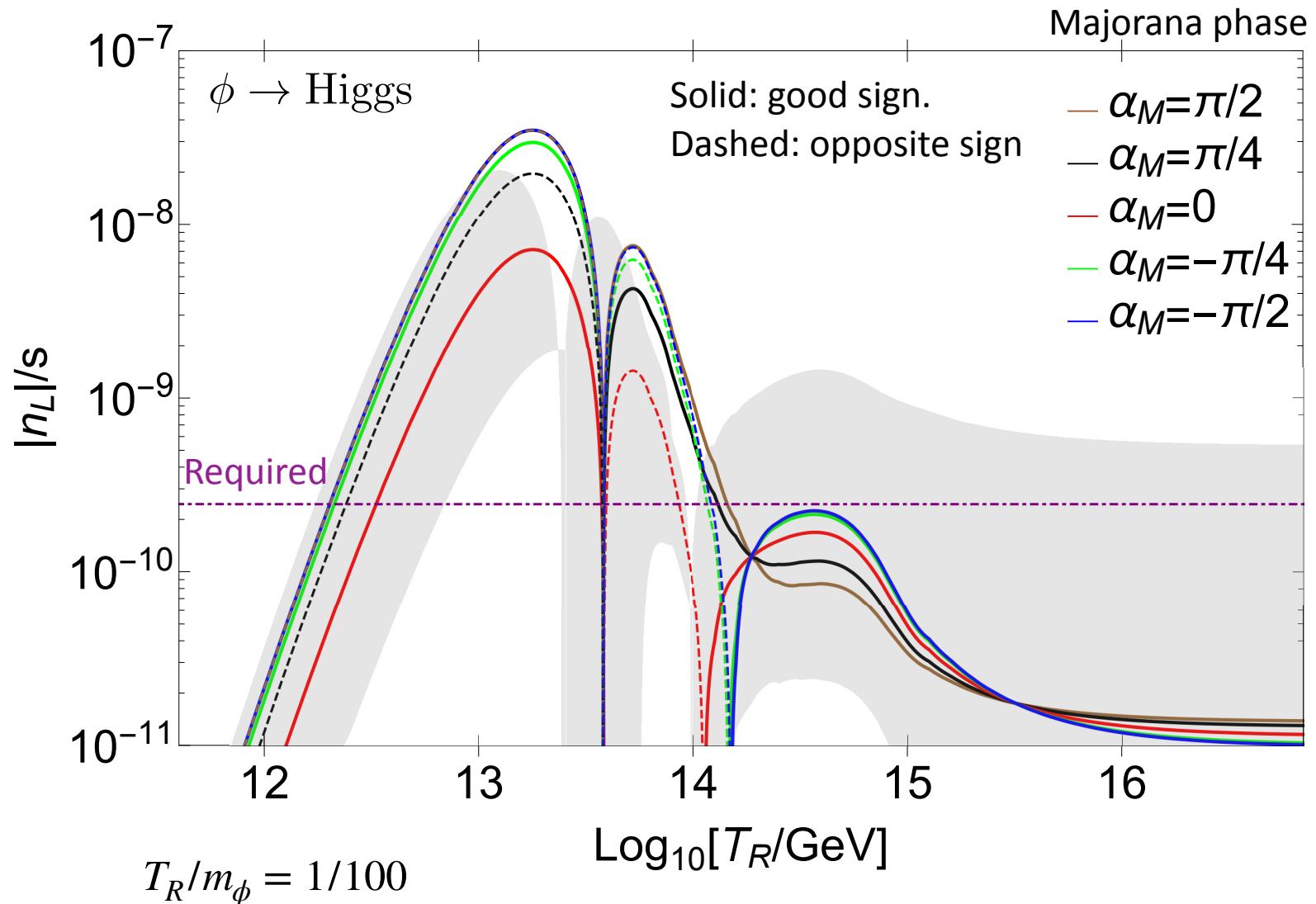
$$\rho_T|_{t=t_R} = \bar{\rho}_T|_{t=t_R} = 0 \quad (\text{Leptons are not thermalized initially})$$

Free parameters

$$T_R, m_\phi$$

and those for neutrino sector.

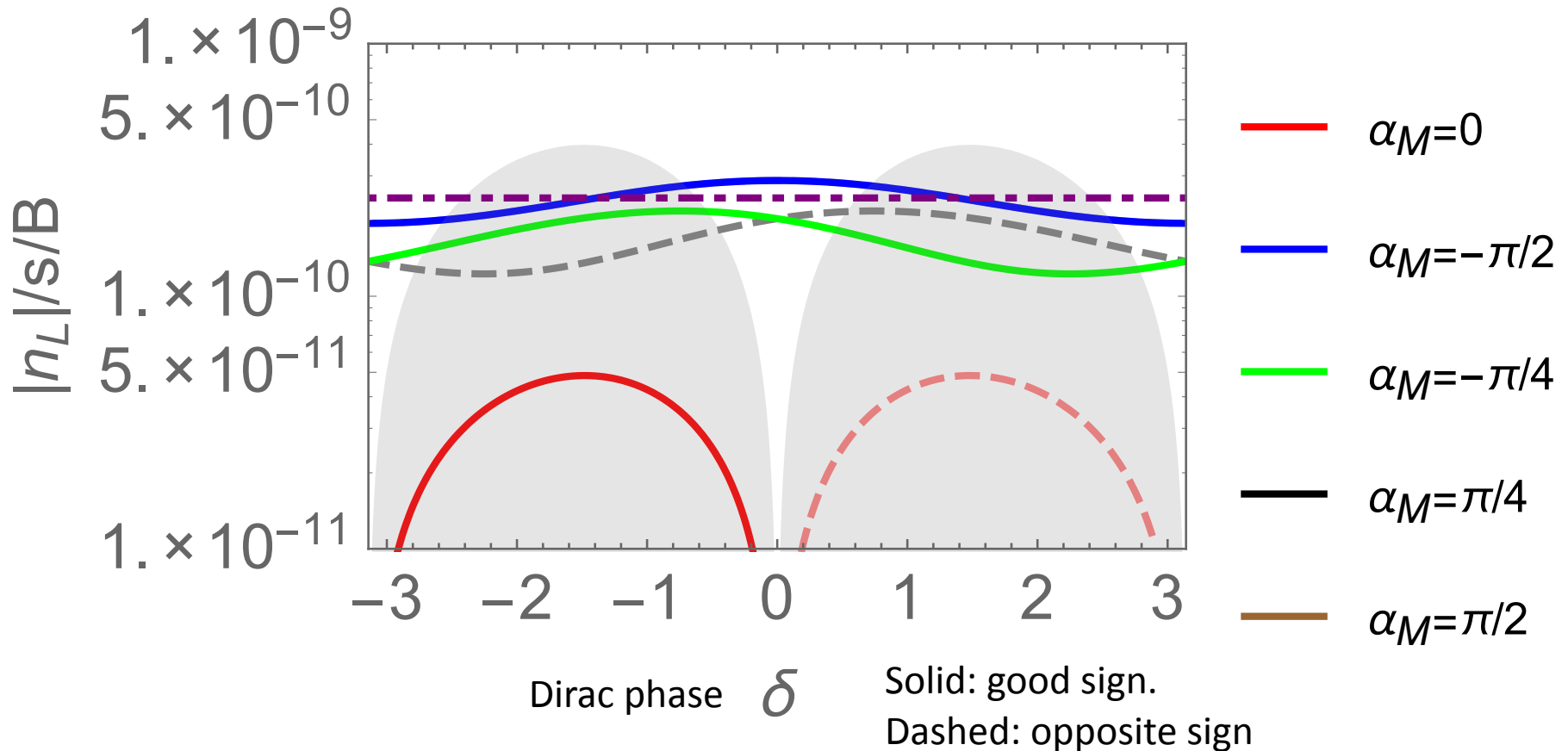
Numerical result (Normal Hierarchy)



Two massive neutrinos. Dirac Phase = $-\pi/2$

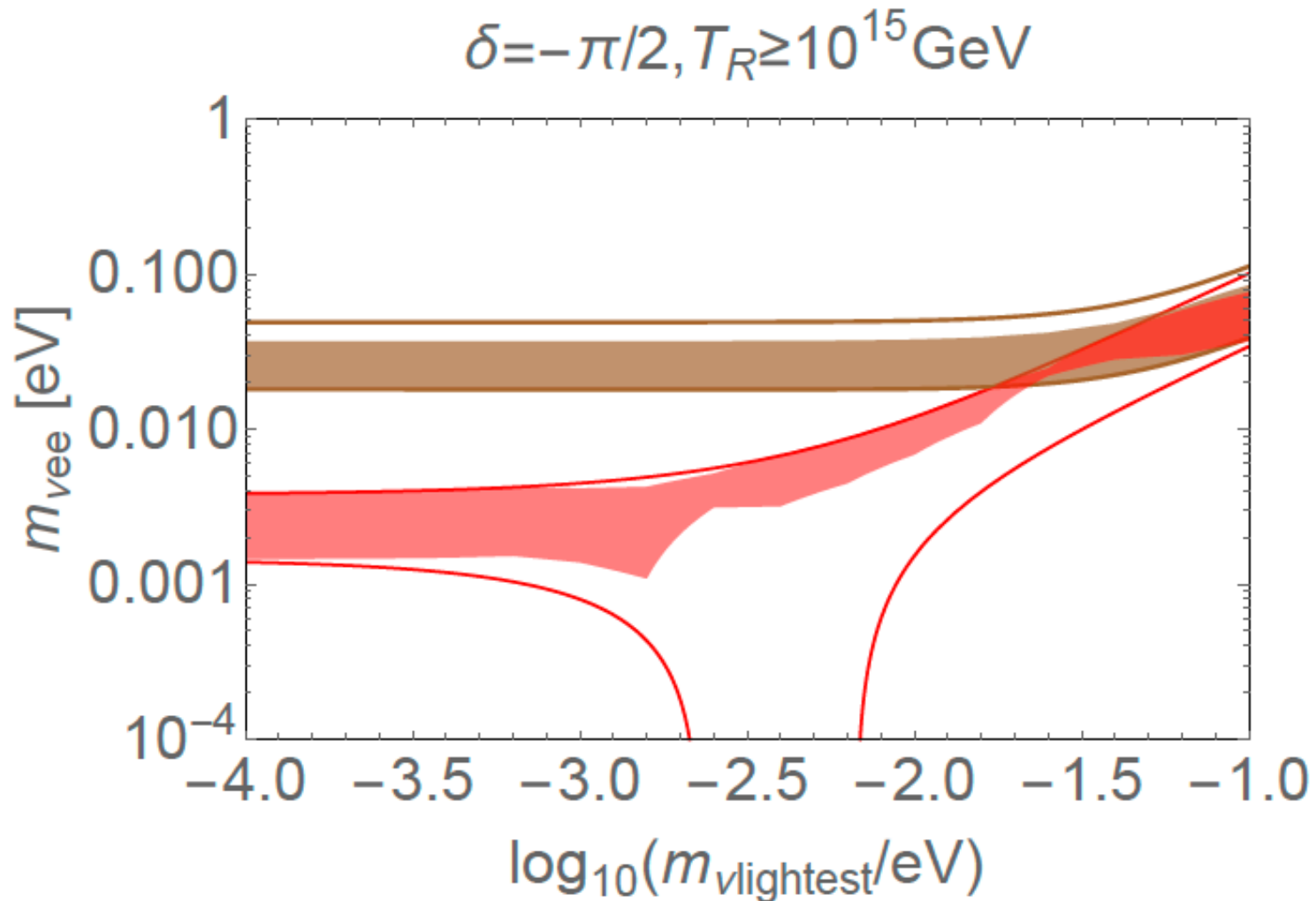
Dirac phase dependence (Normal hierarchy)

Normal, $T_R = m_\phi / 100 = 2 \times 10^{12} \text{ GeV}$, $m_{\nu \text{ lightest}} = 0 \text{ eV}$



Neutrinoless double beta decay

The CP phase and neutrino mass are related and can be tested from neutrino exps.



4. Leptogenesis with low reheat temp

1908.11864 with Shintaro Eijima, Ryuichiro Kitano

What if RHNs are very light? $T_R > M$

$$\mathcal{L} = \mathcal{L}_{SM}^{d \leq 4} + \mathcal{L}_N$$

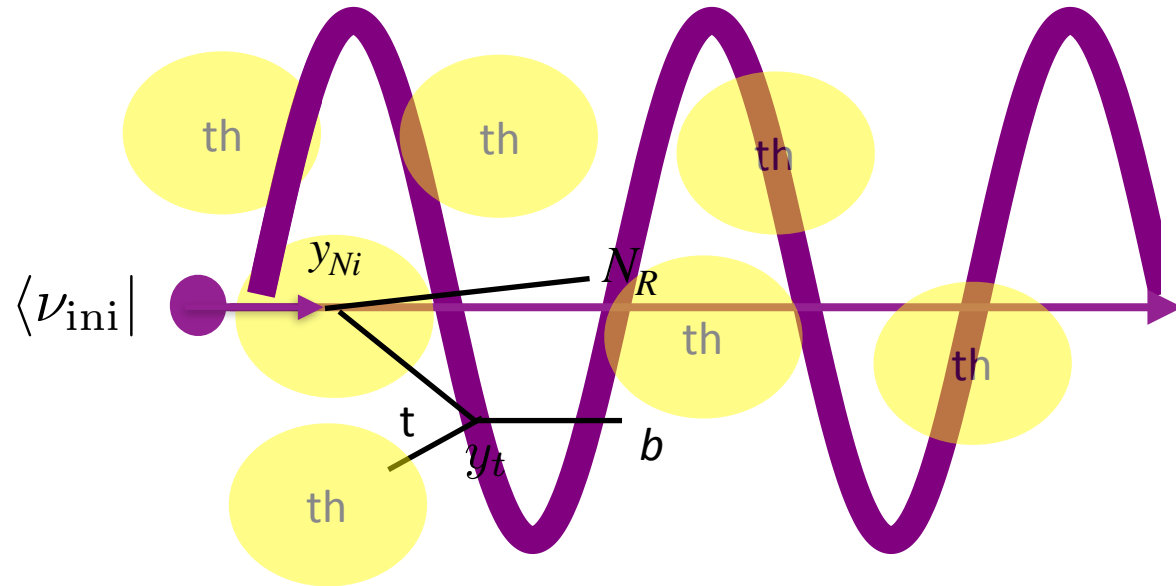
$$\mathcal{L}_N = -y_{Ni} \tilde{H}^* \bar{N}_R \hat{P}_L L_i + \frac{M}{2} \bar{N}_R \hat{P}_L N_R$$

Lepton # violation is suppressed at the reheating era.

However, I will show enough baryon asymmetry can be generated due to an asymmetry separation process.

Distributing neutrinos during thermalization

$$\phi \rightarrow \nu_{\text{ini}} + X, \bar{\nu}_{\text{ini}} + \bar{X}$$



CP-violation!

$$\frac{\Delta n_{N_R}}{S} = - \frac{\Delta n_L}{S} \neq 0$$

The (naive) estimation of lepton asymmetry

$m_\phi \sim T$ with O(1) CP phase, general flavor structure

$$\frac{\Delta n_L}{S} = - \frac{\Delta n_{N_R}}{S} \propto B_{\phi \rightarrow \nu_{\text{ini}} + X / \bar{\nu}_{\text{ini}} + \bar{X}} \times \underbrace{t_{MFP} \frac{\Delta m_\nu^2}{T}}_{\text{CP violation}} \times \underbrace{\frac{\sigma_{y_N}^{\text{th}}}{\sigma_{\text{yukawa}}^{\text{th}}}}_{\text{lepton \# separation}}$$

—— Flavor dependent asymmetry of order $\frac{\Delta m_{\text{th}}^2}{T} \frac{1}{\Gamma_{\text{th}}} \sim 0.01$

—— How frequently the flavor is observed by the \mathcal{L}_N interaction.

$$\frac{\sigma_{y_N}^{\text{th}}}{\sigma_{\text{yukawa}}^{\text{th}}} \sim \frac{y_N^2}{y_\tau^2}$$

The (naive) estimation of lepton asymmetry

$m_\phi \sim T$ · with O(1) CP phase, general flavor structure

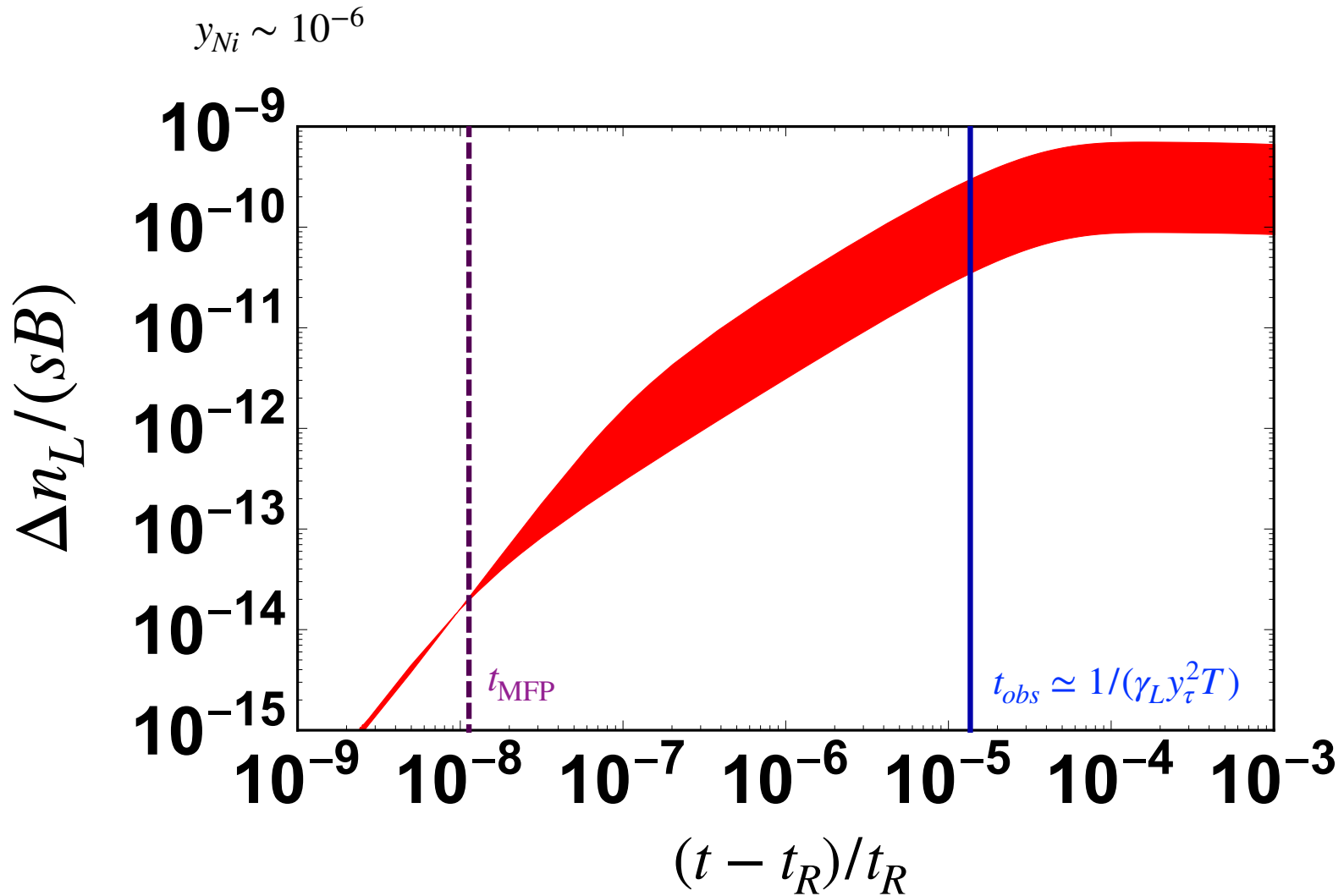
$$\frac{\Delta n_L}{s} \propto Br_{\phi \rightarrow \nu_{\text{ini}} + X / \bar{\nu}_{\text{ini}} + \bar{X}} \times 10^{-10} \left(\frac{|y_N|}{10^{-6}} \right)^2$$

(temperature independent)

c.f. required asymmetry $|\Delta n_L / s| \sim 10^{-10}$

Enough asymmetry can be obtained for not too large y_N .

Numerical result of asymmetry production



Lower bound of reheat temperature

N_R should not be thermalized:

$$T_R \gtrsim M \gtrsim T_{\text{th}}^N \simeq 7 \text{ TeV} \left(\frac{|y_N|}{10^{-6}} \right)^2.$$

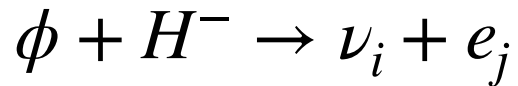
Leptogenesis can be successful with

$$T_R \gtrsim O(10) \text{ TeV} \quad (\text{without tuning among RHN masses.})$$

The scenario also predicts the neutrinos are in normal or inverted hierarchies (but not degenerated). Some hierarchies of right-handed neutrino masses are also predicted.

Enhancement by non-trivial reheating dynamics

Reheating can complete via the scattering process:



[Daido, Takahashi, WY, 1710.11107,1903.00462,](#)

i.e. due to dissipation effect. [Yokoyama 0510091 etc.](#)

No thermal blocking process:

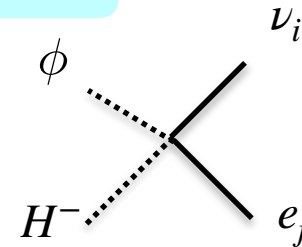
$$\frac{n_\phi}{s} \simeq \frac{3T_R}{4m_\phi} \gg 1$$

$T_R/m_\phi \sim 10^{2-3}$ in [Refs. 1710.11107,1903.00462](#)

Thus, the asymmetry is enhanced.

Inflaton
condensate

Thermal
Plasma



Thermal
Plasma

Thermal
Plasma

LLHH scenario:

$$T_R \gtrsim 10^6 \text{ GeV} \times \left(\frac{10^3}{T_R/m_\phi} \right)^{1/2}$$

seesaw scenario:

$$T_R \gtrsim 10^2 \text{ GeV} \left(\frac{10^2}{T_R/m_\phi} \right)$$

Summary

BAU can be explained due to neutrino oscillation with

$$\mathcal{L} = \mathcal{L}_{SM}^{d \leq 4} - \frac{\kappa_{ij}}{2} \bar{L}_i^c \hat{P}_L L_j H H + h.c \quad \text{at around reheating era.}$$

- BAU explained with $T_R \gtrsim 10^8 GeV$ for $\phi \rightarrow \nu + X, \bar{\nu} + \bar{X}$
- If ϕ dominantly decays to Higgs bosons, the scenario can be tested from ground based experiments.

If there is a light right-handed neutrino,

$$T_R \gtrsim O(10) TeV \text{ for } \phi \rightarrow \nu + X, \bar{\nu} + \bar{X}$$

- $T_R \sim 100 GeV$ is possible to explain the BAU if reheating completes via dissipation.