

# In insensitive Unification of Gauge Couplings, Muon $g-2$ and Higgs decays

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Radovan Dermisek

*Indiana University, Bloomington*

R.D., arXiv:1204.6533 [hep-ph], arXiv:1212.3035 [hep-ph]

R.D. and A. Raval, arXiv:1305.3522 [hep-ph], to appear

**Gunion Fest, UC Davis, March 28, 2014**

### Escaping the large fine tuning and little hierarchy problems in the next to minimal supersymmetric model and $h \rightarrow aa$ decays

Radovan Dermisek, John F. Gunion (UC, Davis). Feb 2005. 4 pp.

Published in *Phys.Rev.Lett.* **95** (2005) 041801

DOI: [10.1103/PhysRevLett.95.041801](https://doi.org/10.1103/PhysRevLett.95.041801)

e-Print: [hep-ph/0502105](https://arxiv.org/abs/hep-ph/0502105) | [PDF](#)

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### Consistency of LEP event excesses with an $h \rightarrow aa$ decay scenario and low-fine-tuning NMSSM models

Radovan Dermisek (Princeton, Inst. Advanced Study), John F. Gunion (UC, Davis). Oct 2005. 5 pp.

Published in *Phys.Rev.* **D73** (2006) 111701

DOI: [10.1103/PhysRevD.73.111701](https://doi.org/10.1103/PhysRevD.73.111701)

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### Nonstandard Higgs Boson Decays

Spencer Chang (New York U., CCFP), Radovan Dermisek (Princeton, Inst. Advanced Study)

Published in *Ann.Rev.Nucl.Part.Sci.* **58** (2008)

DOI: [10.1146/annurev.nucl.58.110707.171200](https://doi.org/10.1146/annurev.nucl.58.110707.171200)

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### Probing NMSSM Scenarios with Mini-ILD

Radovan Dermisek (Princeton, Inst. Advanced Study)

Published in *Phys.Rev.* **D76** (2007) 051105

UCD-2006-17

DOI: [10.1103/PhysRevD.76.051105](https://doi.org/10.1103/PhysRevD.76.051105)

e-Print: [hep-ph/0612031](https://arxiv.org/abs/hep-ph/0612031) | [PDF](#)

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### The NMSSM Close to the R-symmetry

Radovan Dermisek (Princeton, Inst. Advanced Study)

Published in *Phys.Rev.* **D75** (2007) 075019

UCD-2006-16

DOI: [10.1103/PhysRevD.75.075019](https://doi.org/10.1103/PhysRevD.75.075019)

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### The NMSSM Solution to the Fine-Tuning Problem

Radovan Dermisek (Princeton, Inst. Advanced Study)

Published in *Phys.Rev.* **D76** (2007) 095006

DOI: [10.1103/PhysRevD.76.095006](https://doi.org/10.1103/PhysRevD.76.095006)

e-Print: [arXiv:0705.4387](https://arxiv.org/abs/0705.4387) [hep-ph] | [PDF](#)

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$h_{\text{HEP}}$  index [\[?\]](#)

11

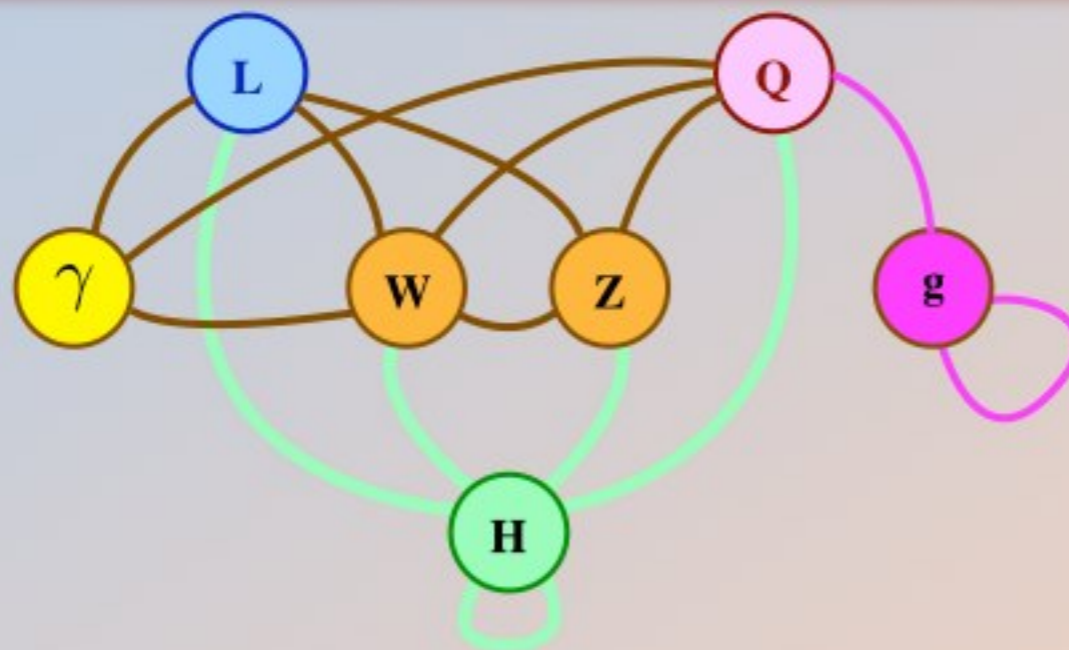
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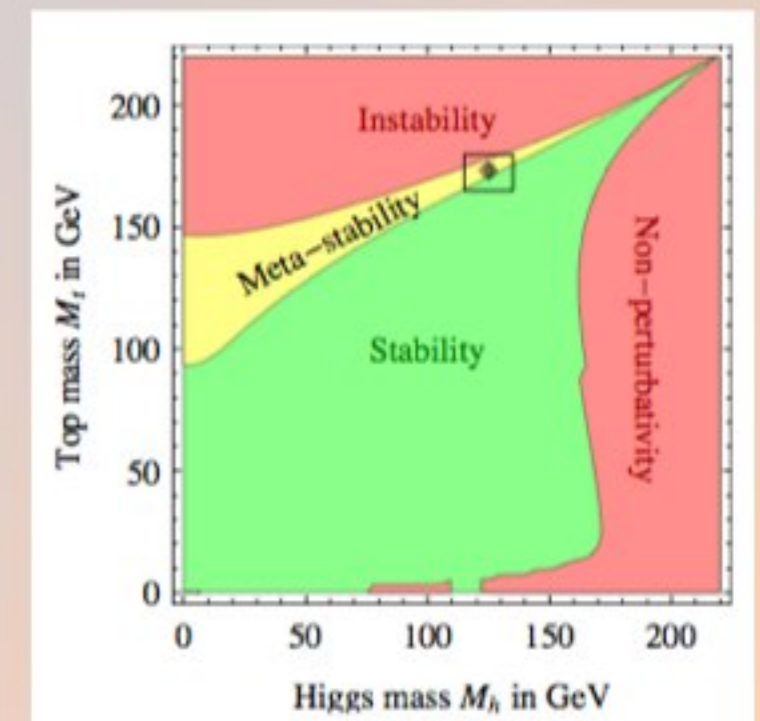
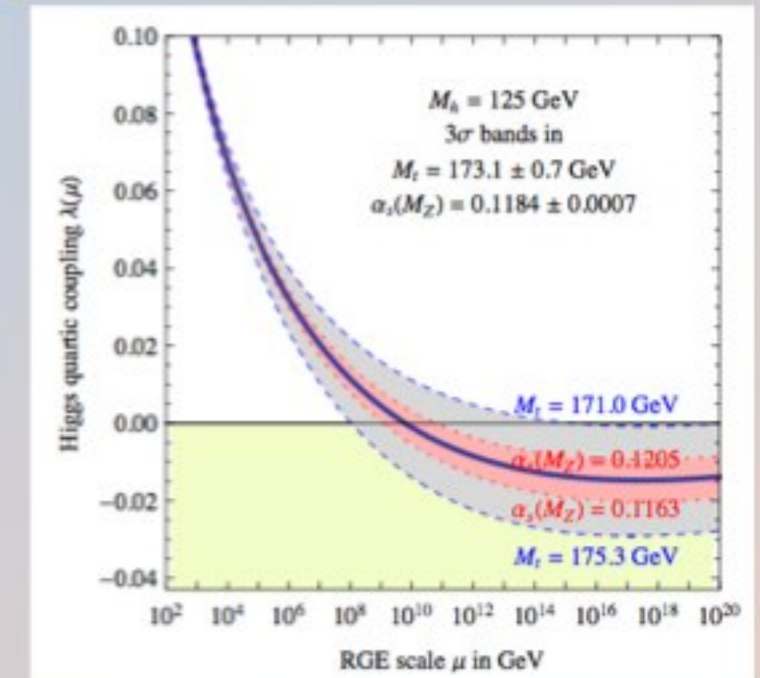
# Motivation - Just the Standard Model?

$$SM \equiv SU(3)_c \times SU(2)_L \times U(1)_Y$$

Names	Content			SM
<b>Quarks and Leptons</b>	$i = 1$	2	3	
$Q_i$	$\begin{pmatrix} u \\ d \end{pmatrix}_\alpha$	$\begin{pmatrix} c \\ s \end{pmatrix}_\alpha$	$\begin{pmatrix} t \\ b \end{pmatrix}_\alpha$	$(3, 2, 1/3)$
$\bar{u}_i$	$\bar{u}_\alpha$	$\bar{c}_\alpha$	$\bar{t}_\alpha$	$(\bar{3}, 1, -4/3)$
$\bar{d}_i$	$\bar{d}_\alpha$	$\bar{s}_\alpha$	$\bar{b}_\alpha$	$(\bar{3}, 1, 2/3)$
$L_i$	$\begin{pmatrix} \nu_e \\ e \end{pmatrix}$	$\begin{pmatrix} \nu_\mu \\ \mu \end{pmatrix}$	$\begin{pmatrix} \nu_\tau \\ \tau \end{pmatrix}$	$(1, 2, -1)$
$\bar{e}_i$	$\bar{e}$	$\bar{\mu}$	$\bar{\tau}$	$(1, 1, 2)$
<b>Higgs <math>H</math></b>	$\begin{pmatrix} H^+ \\ H^0 \end{pmatrix}$			$(1, 2, 1)$
<b>Gauge bosons</b>				
gluon				$(8, 1, 0)$
W bosons	$W^\pm, W^0$			$(1, 3, 0)$
B boson	$B^0$			$(1, 1, 0)$



Degrassi et al, arXiv:1205.6497



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16 of  $SO(10)$

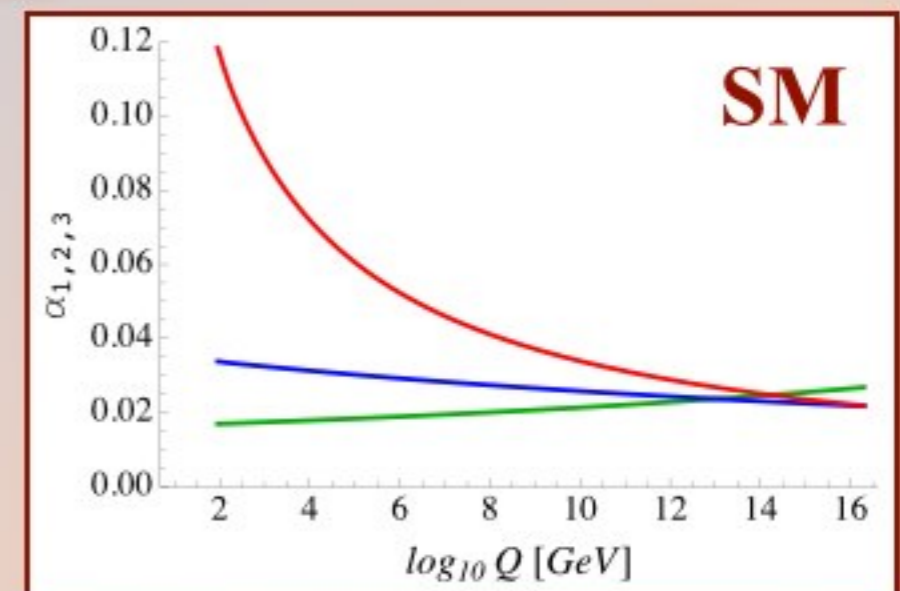
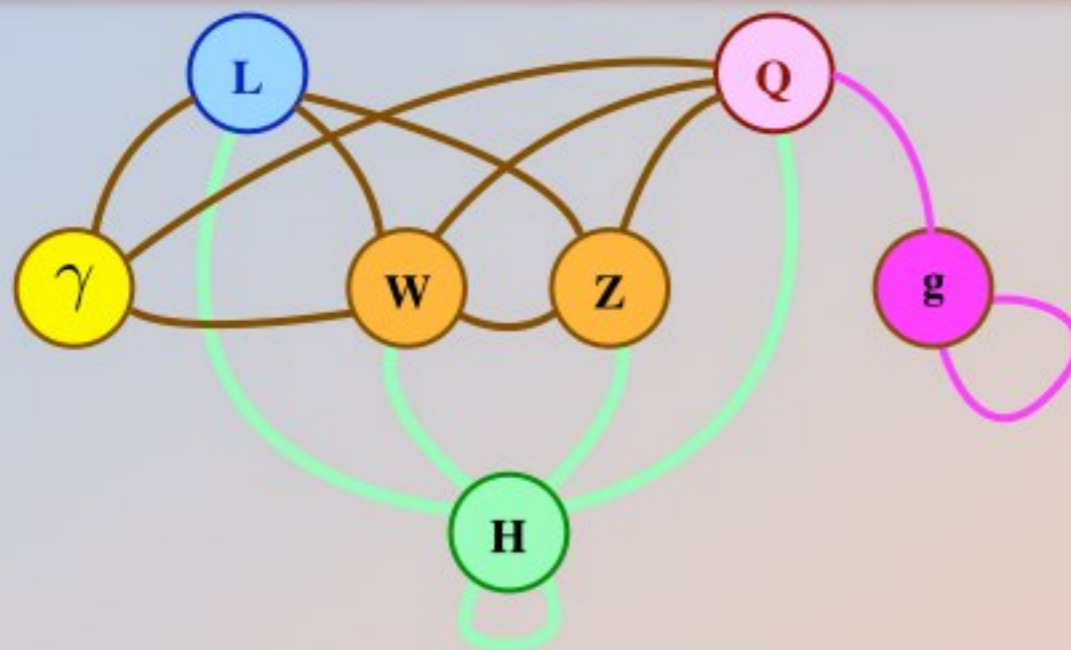
$$\alpha_3(M_Z)_{exp} = 0.1184$$

$$\alpha_2(M_Z)_{exp} = 0.03380$$

$$\alpha_1(M_Z)_{exp} = 0.01695$$

$$\alpha_{EM}(M_Z) = 1/127.916$$

$$\sin^2 \theta_W = 0.2313$$



# Outline

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## Extensions of the SM by complete vector-like families:

### ◆ gauge coupling unification

couplings at the EW scale are highly insensitive to fundamental parameters, their ratios are understood from the particle content, GUT scale can be identified with string/Planck scale

### ◆ top Yukawa can be understood from closeness to the IR f.p.

### ◆ the electroweak minimum is stable

Higgs quartic coupling remains positive all the way to GUT scale, the EW scale value less sensitive to boundary conditions

## Possible phenomenological consequences:

○ muon  $g-2$

○  $h \rightarrow \mu\mu$

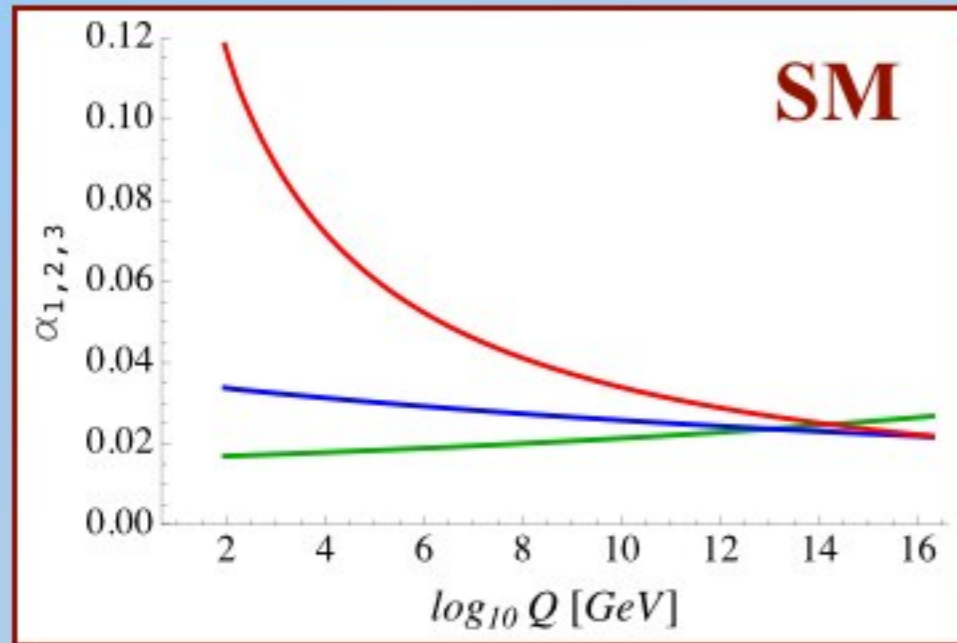
○  $h \rightarrow \gamma\gamma$

○  $h \rightarrow ZZ^*$

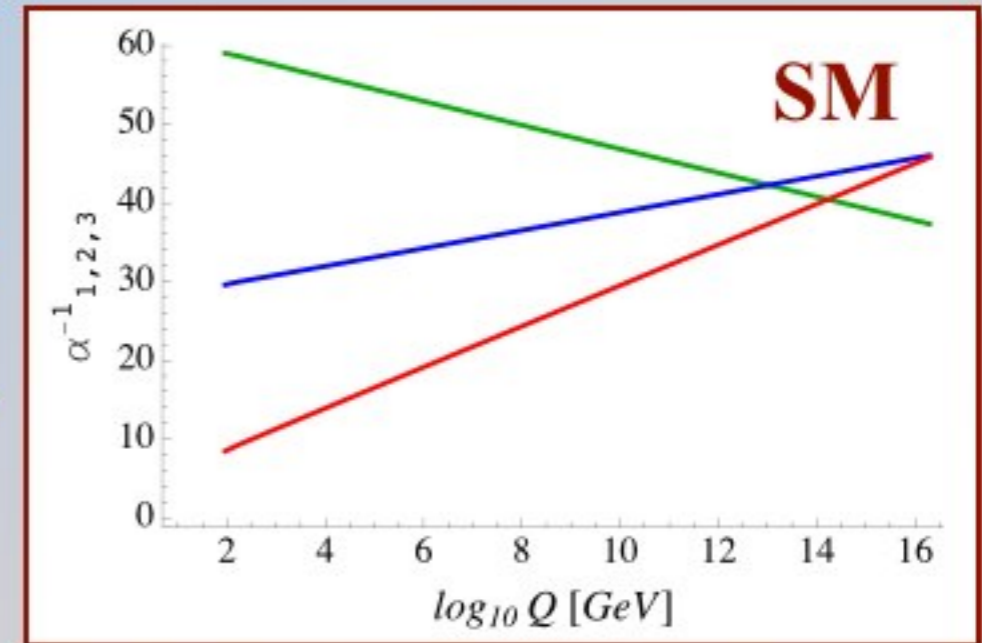
# In insensitive Unification of Gauge Couplings

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# Gauge couplings in the standard model



$$\begin{aligned} \alpha_3(M_Z)_{exp} &= 0.1184 \\ \alpha_2(M_Z)_{exp} &= 0.03380 \\ \alpha_1(M_Z)_{exp} &= 0.01695 \\ \hline \alpha_{EM}(M_Z) &= 1/127.916 \\ \sin^2 \theta_W &= 0.2313 \end{aligned}$$



**RGEs:**

$$\frac{d\alpha_i}{dt} = \beta(\alpha_i) = \frac{\alpha_i^2}{2\pi} b_i$$

$$t = \ln Q/Q_0$$

$$b_i = (41/10, -19/6, -7)$$

$$b_i = \left( \frac{1}{10} + \frac{4}{3}n_g, -\frac{43}{6} + \frac{4}{3}n_g, -11 + \frac{4}{3}n_g \right)$$

**sensitivity**

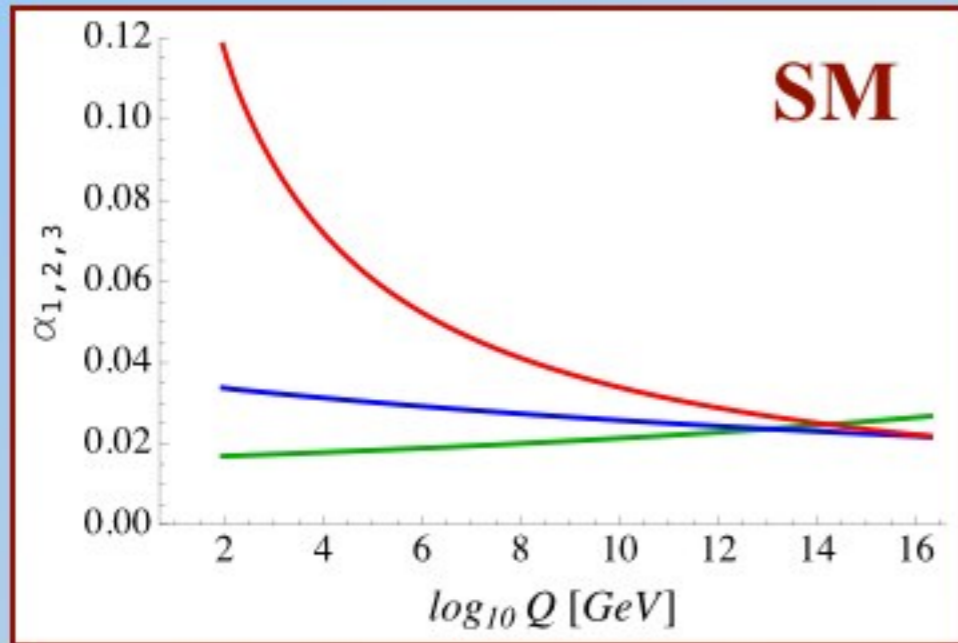
$$\frac{\delta\alpha_3(M_Z)}{\alpha_3(M_Z)} = \underbrace{\frac{\alpha_3(M_Z)}{\alpha_G}}_{\sim 4} \frac{\delta\alpha_G}{\alpha_G}$$

**solution:**

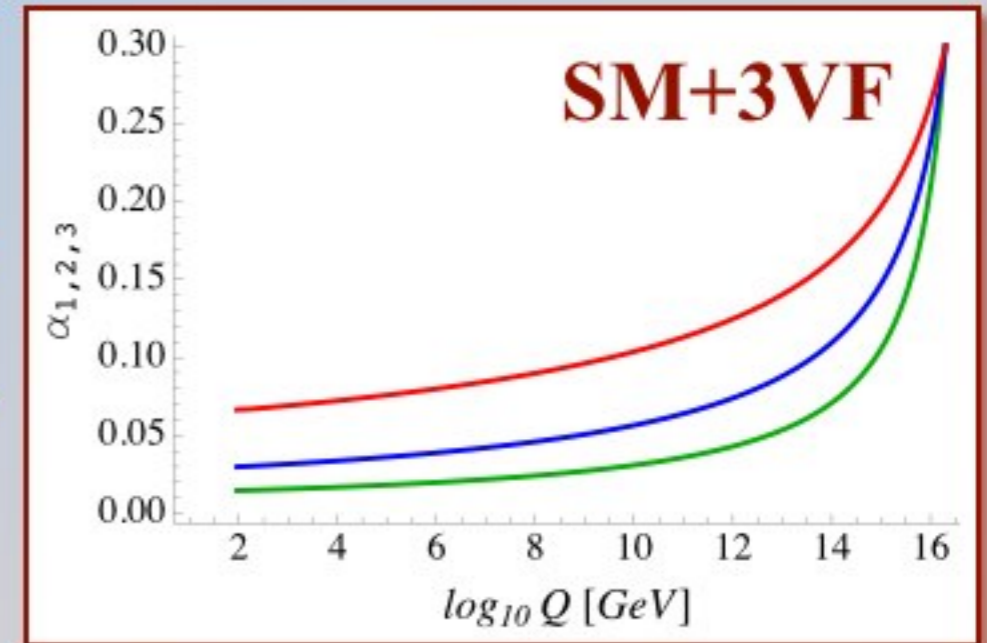
$$\alpha_i^{-1}(M_Z) = \frac{b_i}{2\pi} \ln \frac{M_G}{M_Z} + \alpha_i^{-1}(M_G)$$

# SM

# SM+3VF



$$\begin{aligned} \alpha_3(M_Z)_{exp} &= 0.1184 \\ \alpha_2(M_Z)_{exp} &= 0.03380 \\ \alpha_1(M_Z)_{exp} &= 0.01695 \\ \hline \alpha_{EM}(M_Z) &= 1/127.916 \\ \sin^2 \theta_W &= 0.2313 \end{aligned}$$



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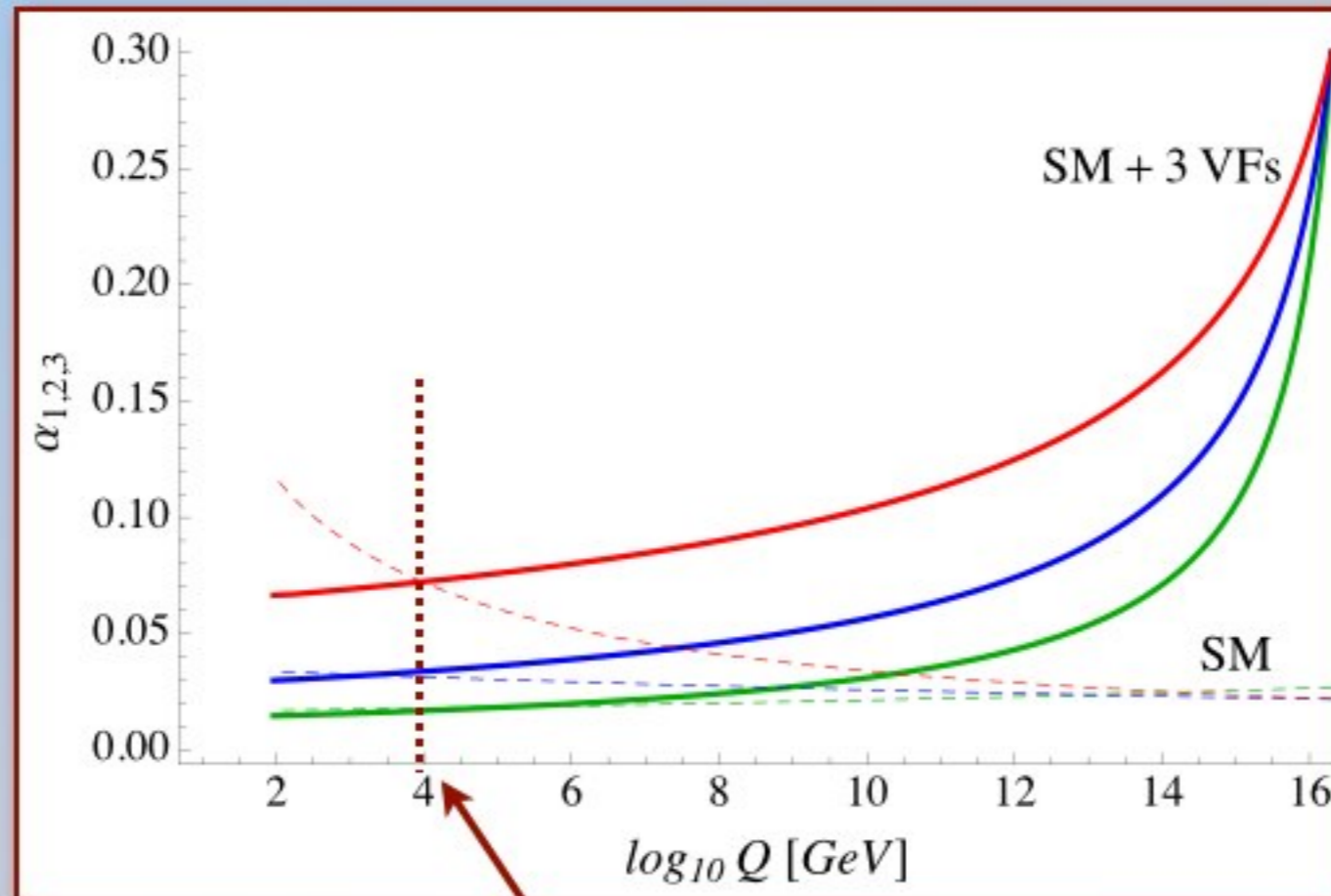
$$b_i = (121/10, 29/6, +1)$$

**solution:**

$$\alpha_i^{-1}(M_Z) = \frac{b_i}{2\pi} \ln \frac{M_G}{M_Z} + \alpha_i^{-1}(M_G)$$

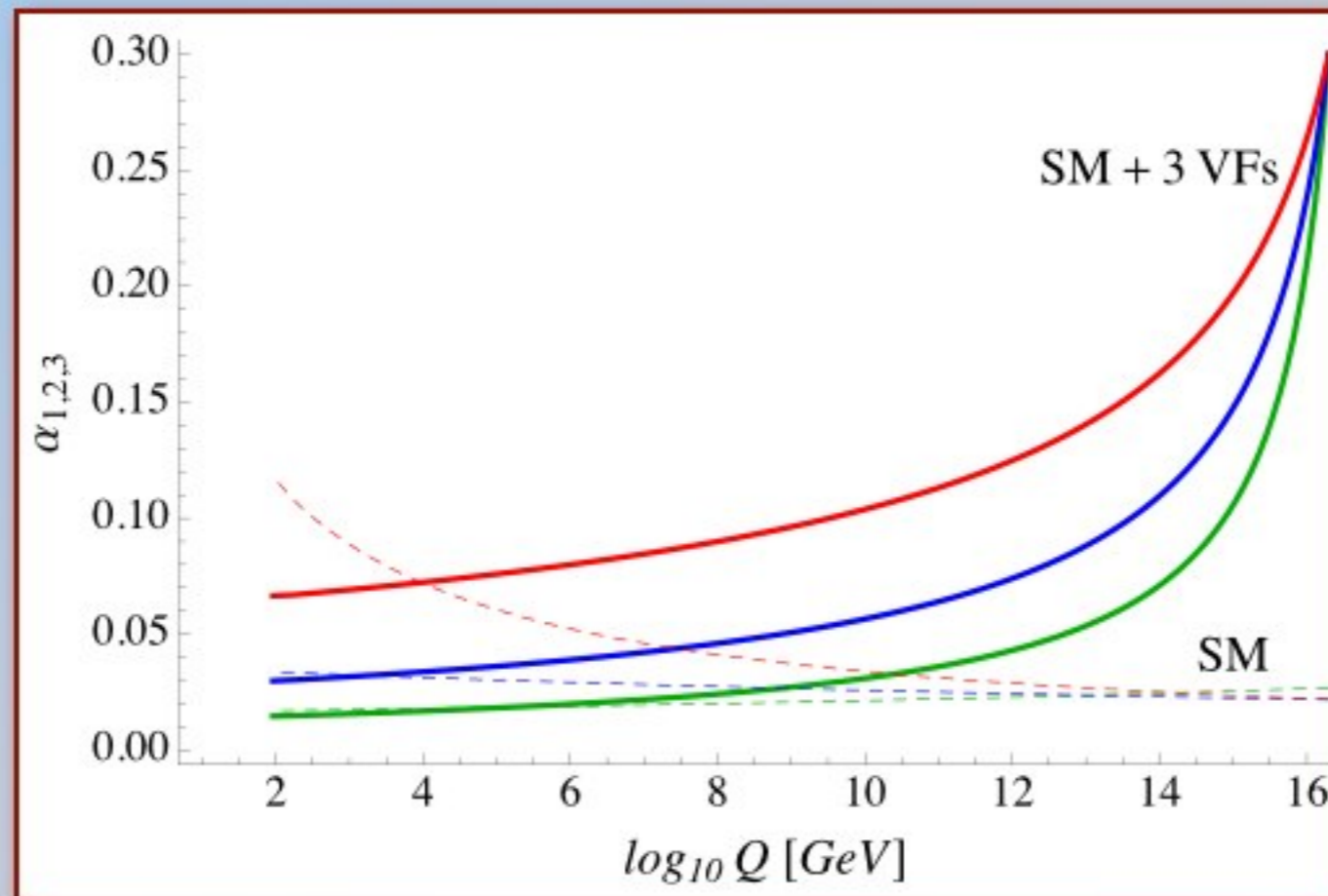


# Gauge couplings in the SM + 3 VFs



**Is this a threshold effect?**

# Gauge couplings in the SM + 3 VFs



$$\frac{\alpha_i(M_Z)}{\alpha_j(M_Z)} \simeq \frac{b_j}{b_i}$$

$$\alpha_i^{-1}(M_Z) = \frac{b_i}{2\pi} \ln \frac{M_G}{M_Z} + \alpha_i^{-1}(M_G)$$

gauge couplings understood from:

● IR fixed point predictions (two parameter free predictions)

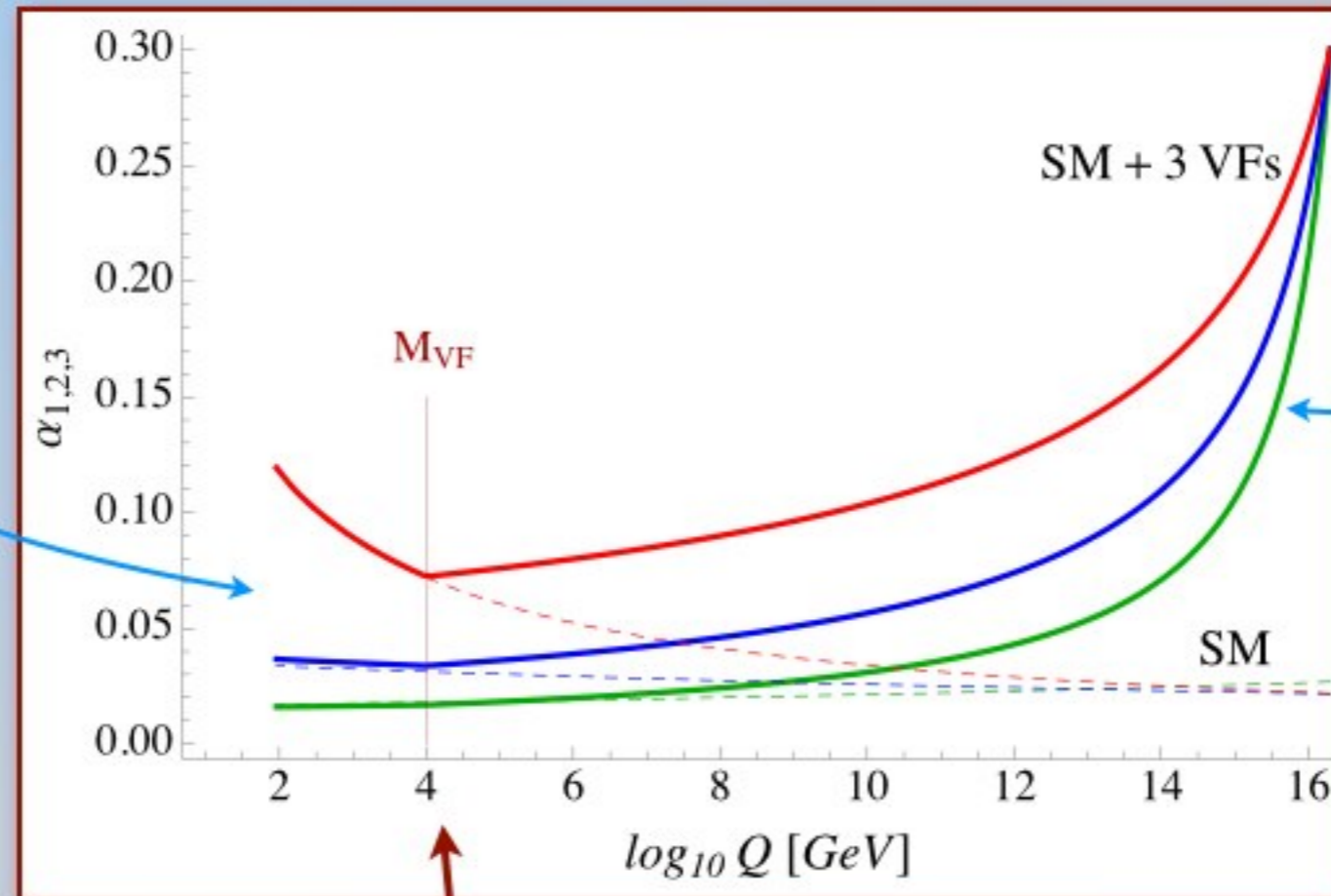
$$\sin^2 \theta_W \equiv \frac{\alpha'}{\alpha_2 + \alpha'} = \frac{b_2}{b_2 + b'} = 0.193$$

Maiani, Parisi, and Petronzio (1978)

$$\alpha_3 |_{\alpha_{EM}^{exp}} \simeq 0.072$$

(includes 2-loop)

# Gauge couplings in the SM + 3 VFs



$$b_i = (41/10, -19/6, -7)$$

$$b_i = (121/10, 29/6, +1)$$

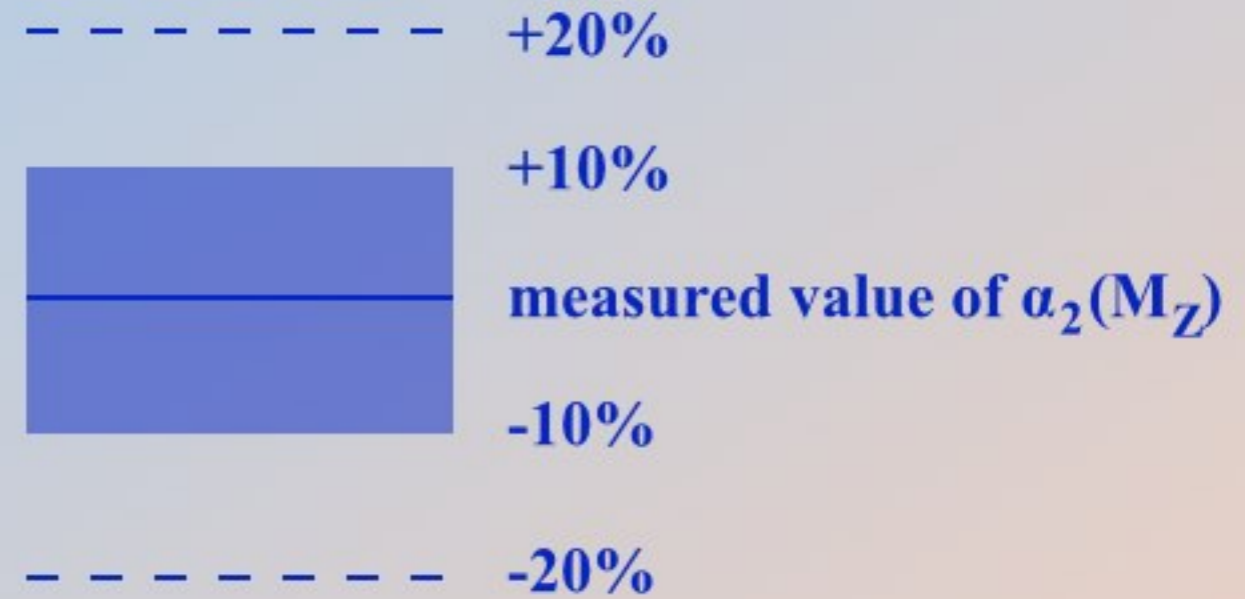
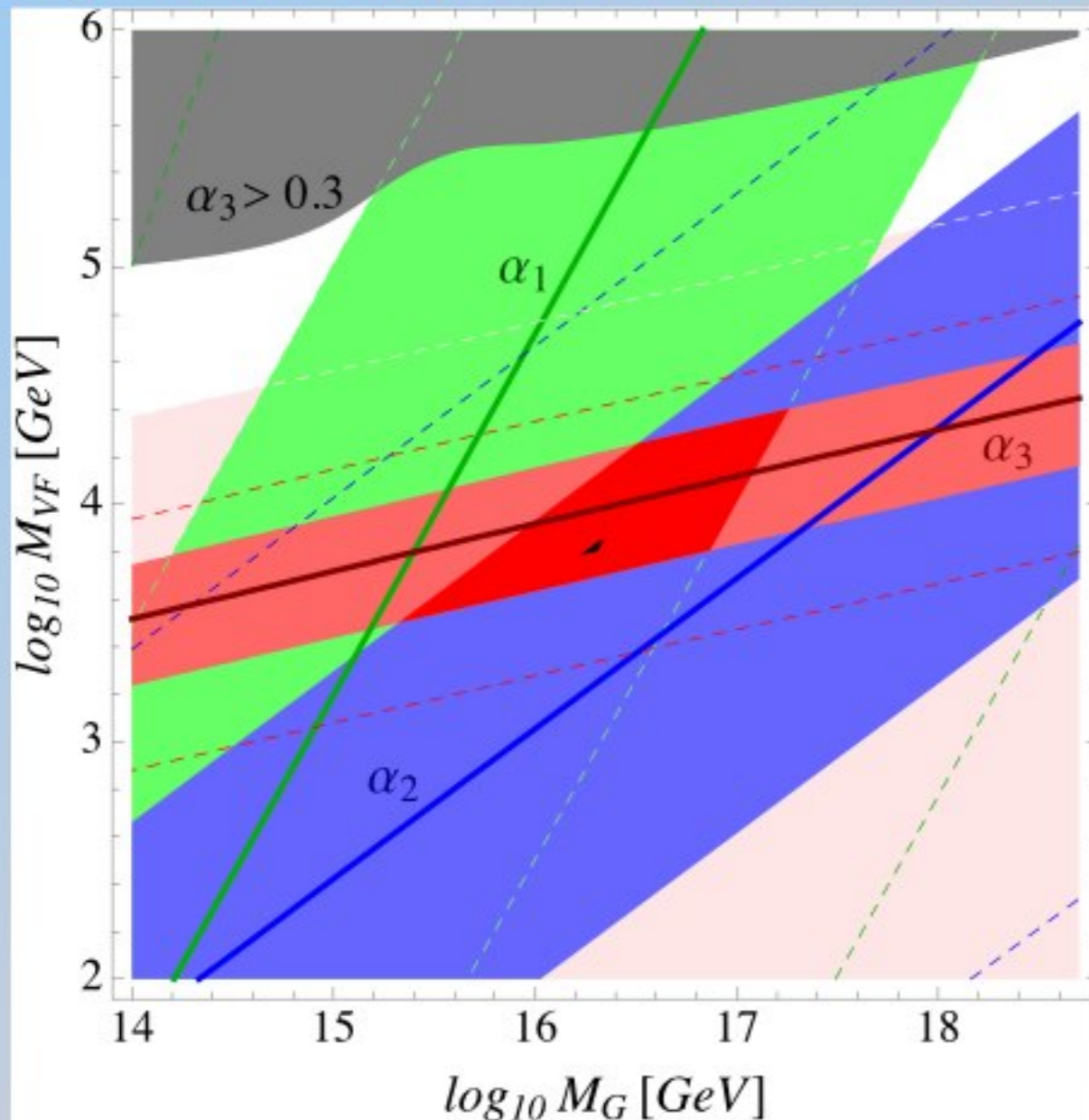
**gauge couplings understood from:**

$$\alpha_i^{-1}(M_Z) = \frac{b_i}{2\pi} \ln \frac{M_G}{M_Z} + \alpha_i^{-1}(M_G)$$

- IR fixed point predictions (two parameter free predictions)
- threshold effects from masses of VFs

# Ranges of $M_G$ , and $M_{VF}$

$\alpha_G = 0.3$  (for larger values results almost identical)



● the best fit  
(all three couplings within 6%)

**Gauge couplings at  $M_Z$  within 10%  
in a large range of parameters!**

**And within 50% in basically the  
whole range!**

# Realistic example

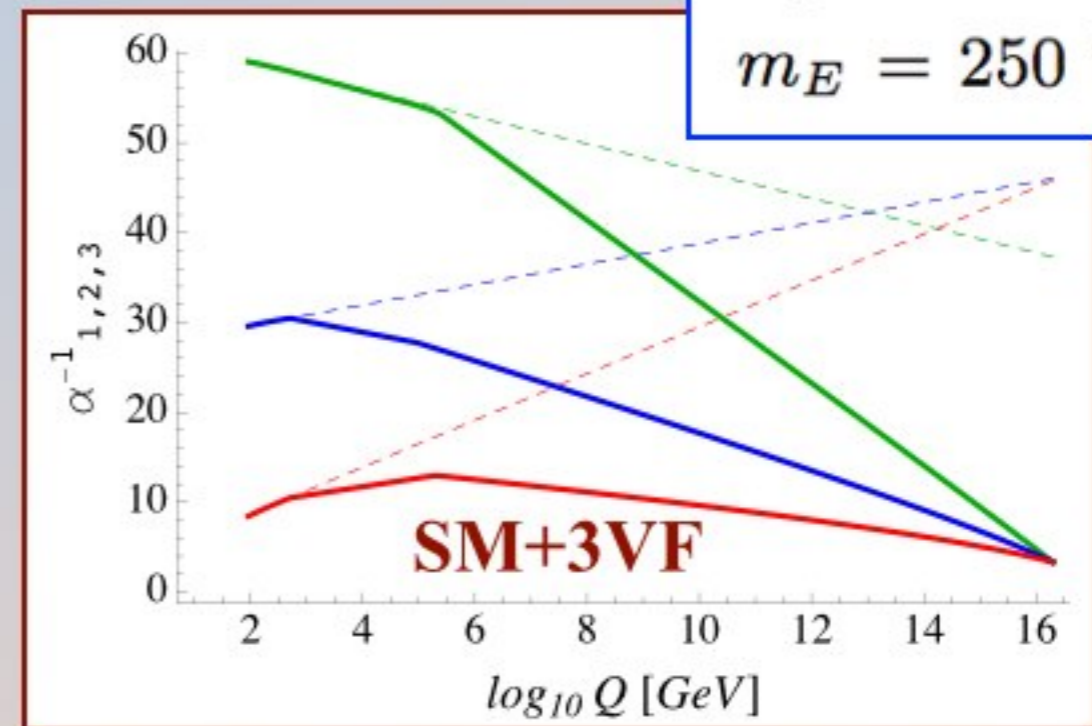
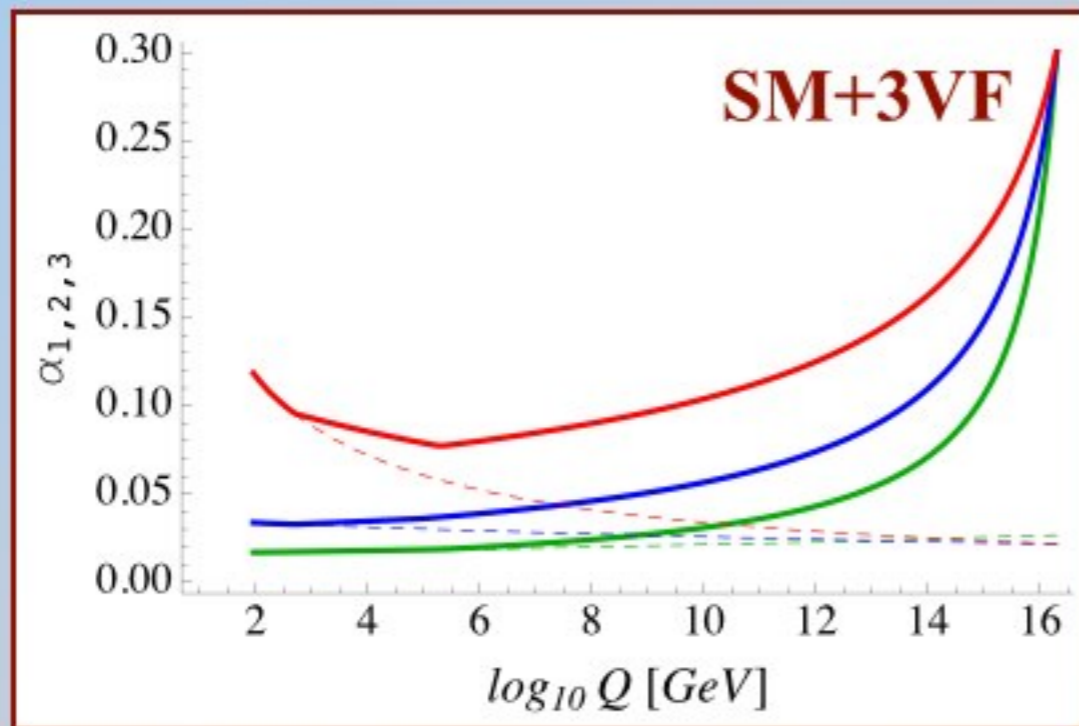
$$\begin{aligned} \alpha_3(M_Z)_{exp} &= 0.1184 \\ \alpha_2(M_Z)_{exp} &= 0.03380 \\ \alpha_1(M_Z)_{exp} &= 0.01695 \\ \alpha_{EM}(M_Z) &= 1/127.916 \\ \sin^2 \theta_W &= 0.2313 \end{aligned}$$

Gauge couplings reproduced (within fractions of exp. uncertainties) for :

4 sig. figures

2 sig. figures

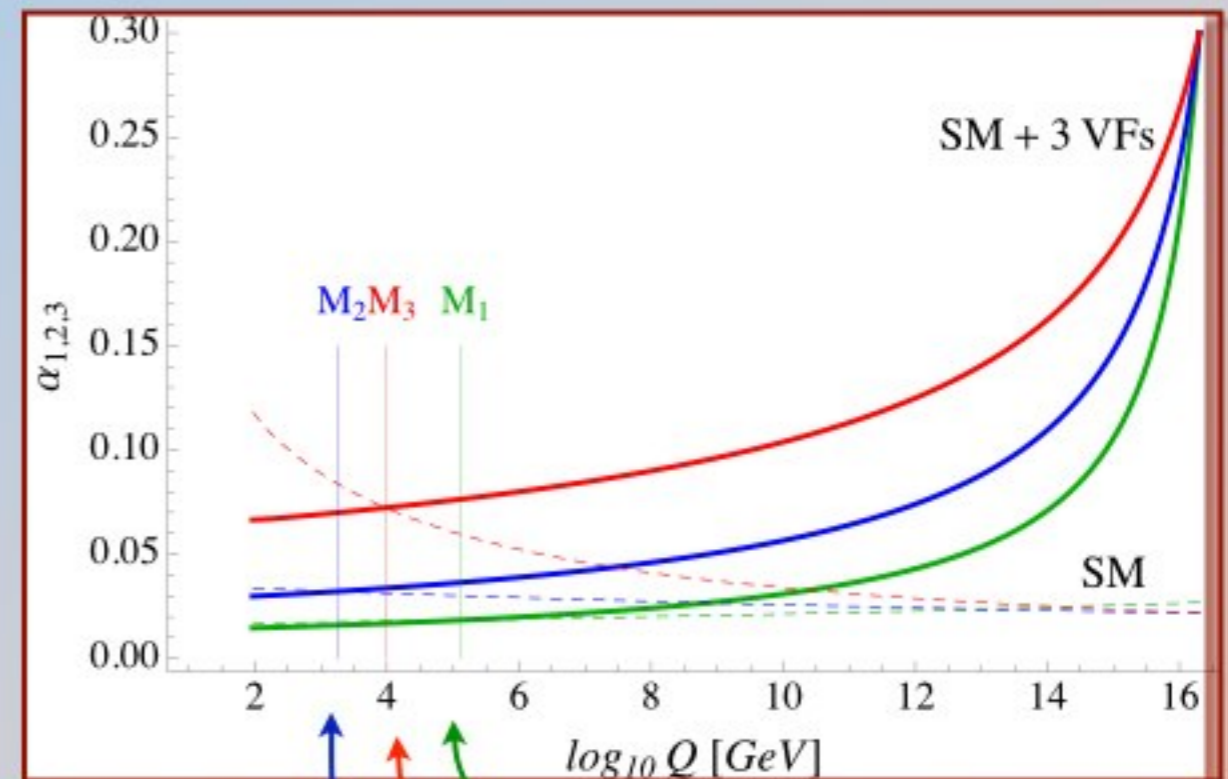
$$\begin{aligned} m_Q &= 500 \text{ GeV} \\ m_L &= 95 \text{ TeV} \\ m_U &= 220 \text{ TeV} \\ m_D &= 180 \text{ TeV} \\ m_E &= 250 \text{ TeV} \end{aligned}$$



Many possible solutions!

# Classifying solutions - mass rules

To get gauge coupling unification, weighted sum of logs of masses of particles charged under given symmetry must be as if all particles had the mass equal to the crossing scale of RG evolutions of the gauge coupling in the SM and SM+3VFs:



$$\frac{1}{2\pi} \sum_{i=1}^3 \left( b_3^Q \ln \frac{M_{Qi}}{M_Z} + b_3^U \ln \frac{M_{Ui}}{M_Z} + b_3^D \ln \frac{M_{Di}}{M_Z} \right) = \frac{4}{\pi} \ln \frac{M_3}{M_Z}$$

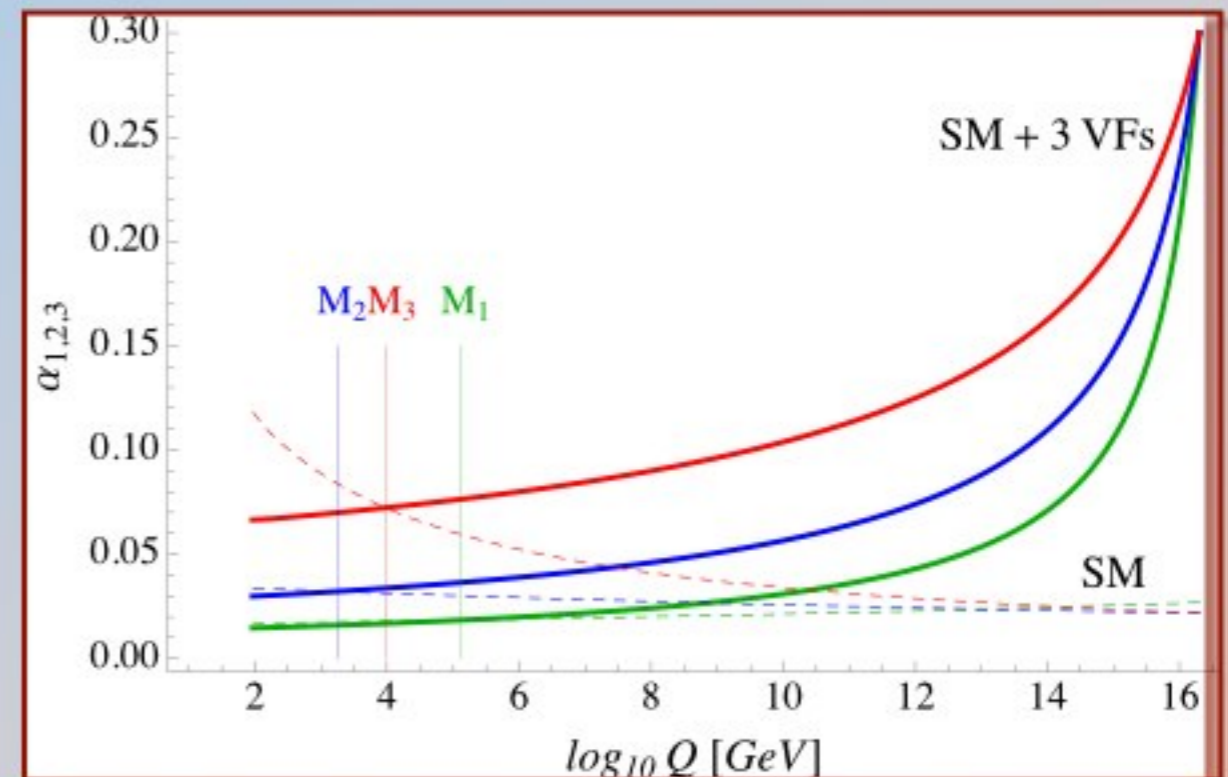
$$\frac{1}{2\pi} \sum_{i=1}^3 \left( b_2^Q \ln \frac{M_{Qi}}{M_Z} + b_2^L \ln \frac{M_{Li}}{M_Z} \right) = \frac{4}{\pi} \ln \frac{M_2}{M_Z}$$

$$\frac{1}{2\pi} \sum_{i=1}^3 \left( b_1^Q \ln \frac{M_{Qi}}{M_Z} + b_1^U \ln \frac{M_{Ui}}{M_Z} + b_1^D \ln \frac{M_{Di}}{M_Z} + b_1^L \ln \frac{M_{Li}}{M_Z} + b_1^E \ln \frac{M_{Ei}}{M_Z} \right) = \frac{4}{\pi} \ln \frac{M_1}{M_Z}$$

$$T_i = \frac{1}{2\pi} \sum_f b_i^f \ln \frac{M_f}{M_Z}$$

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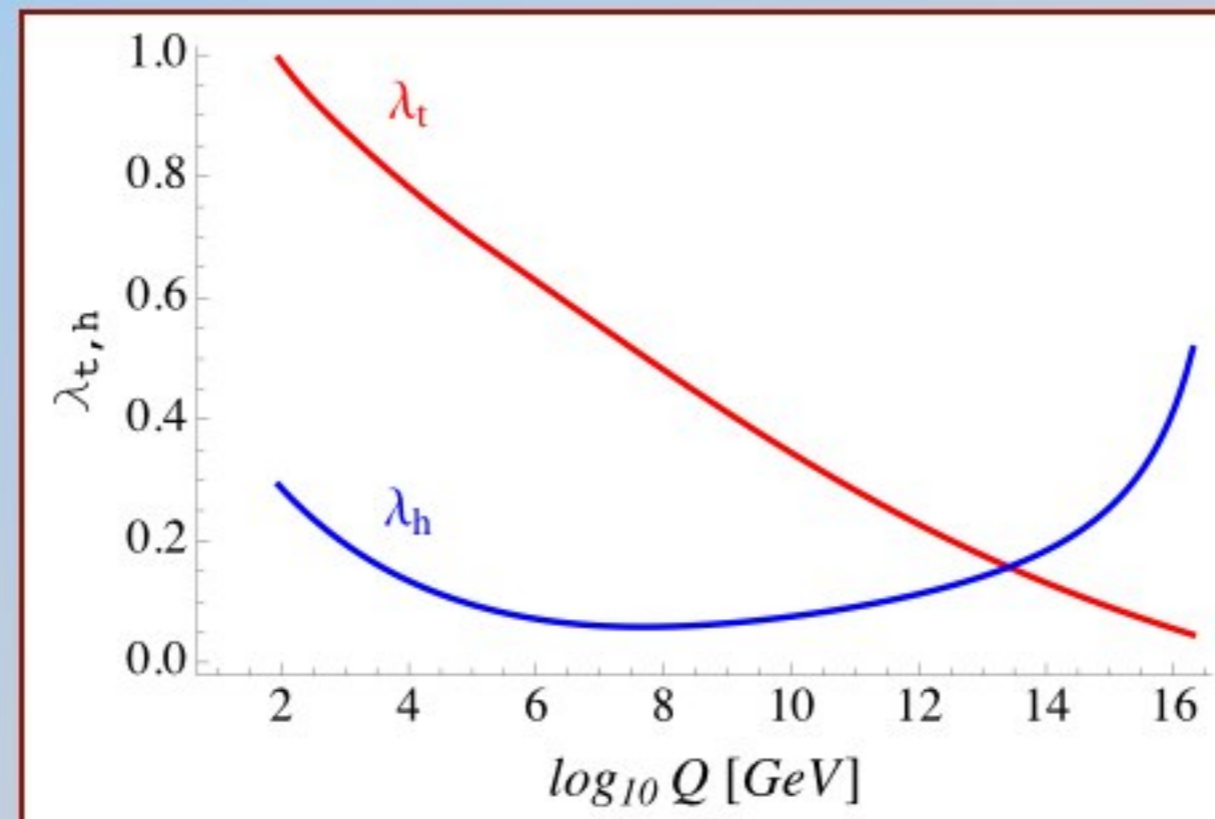
$$M_3^4 = M_Q^2 M_U M_D,$$

$$M_2^4 = M_Q^3 M_L,$$

$$M_1^{20} = M_Q M_U^8 M_D^2 M_L^3 M_E^6.$$

$$M_F \equiv (M_{F_1} M_{F_2} \dots M_{F_N})^{1/N}$$

# Top Yukawa and Higgs quartic couplings



$m_H = 125 \text{ GeV}$

- top Yukawa can be understood from closeness to the IR f.p.  
(different textures for fermion masses compared to usual GUTs)
- the electroweak minimum is stable  
Higgs quartic coupling remains positive all the way to GUT scale,  
the EW scale value less sensitive to boundary conditions



# Muon $g-2$ and Higgs decays

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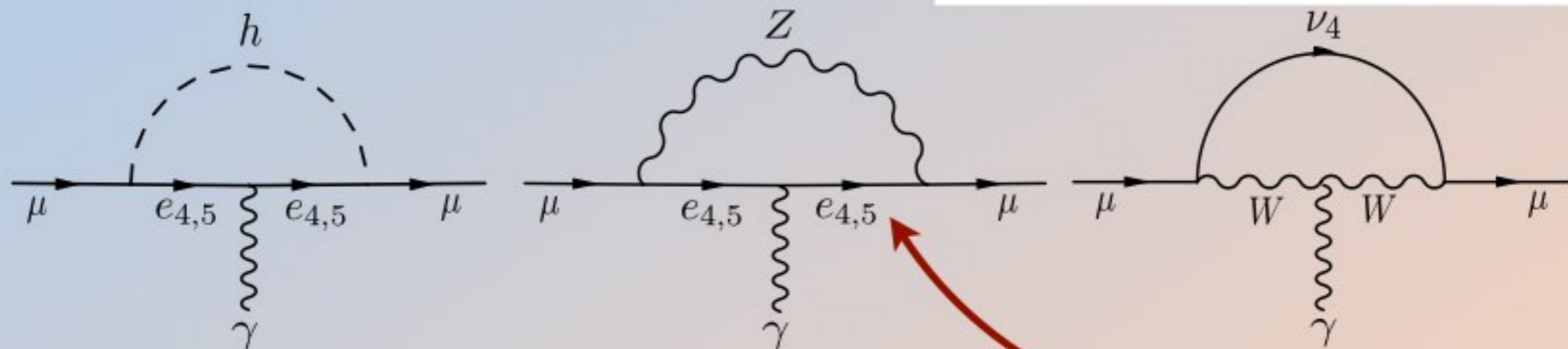
# Muon $g-2$

K. Kannike, M. Raidal, D.M. Straub and A. Strumia, 1111.2551 [hep-ph]

R.D. and A. Raval, 1305.3522 [hep-ph]

$$\mathcal{L} \supset -\bar{l}_{Li} y_{ij} e_{Rj} H - \bar{l}_{Li} \lambda_i^E E_R H - \bar{L}_L \lambda_j^L e_{Rj} H - \lambda \bar{L}_L E_R H - \bar{\lambda} H^\dagger \bar{E}_L L_R - M_L \bar{L}_L L_R - M_E \bar{E}_L E_R + h.c.,$$

$$(\bar{e}_{Li}, \bar{L}_L^-, \bar{E}_L) \begin{pmatrix} y_{ij} v & 0 & \lambda_i^E v \\ \lambda_j^L v & M_L & \lambda v \\ 0 & \bar{\lambda} v & M_E \end{pmatrix} \begin{pmatrix} e_{Rj} \\ L_R^- \\ E_R \end{pmatrix}$$



$$\delta a_\mu^Z = -\frac{g^2 m_\mu}{8\pi^2 M_W^2} \{ (g_L^2 + g_R^2) m_\mu F_Z(x) + g_L g_R m_f G_Z(x) \}$$

$$x = (m_f / M_Z)^2$$

Interesting insight can be obtained by integrating out vectorlike leptons:

$$\mathcal{L} \supset -\bar{l}_{Li} y_{ij} e_{Rj} H - \bar{l}_{Li} \lambda_i^E E_R H - \bar{L}_L \lambda_j^L e_{Rj} H - \lambda \bar{L}_L E_R H - \bar{\lambda} H^\dagger \bar{E}_L L_R - M_L \bar{L}_L L_R - M_E \bar{E}_L E_R + h.c.,$$

$$\lambda_E v, \lambda_L v, \bar{\lambda} v, \lambda v \ll M_E, M_L$$

Effective lagrangian is given by:

$$\mathcal{L}_{eff} \supset -\bar{\mu}_L \left( y_\mu + \frac{\lambda^L \bar{\lambda} \lambda^E}{M_L M_E} H H^\dagger \right) \mu_R H + h.c. \longrightarrow - (m_\mu^H + m_\mu^{LE}) \bar{\mu}_L \mu_R + h.c.$$

Contribution to the muon g-2 can be written as:

$$\Delta a_\mu \simeq c \frac{m_\mu m_\mu^{LE}}{(4\pi v)^2} \simeq 0.85 c \frac{m_\mu^{LE}}{m_\mu} \Delta a_\mu^{exp}$$

contribution to the muon mass and muon g-2 is correlated!

$$c = -1$$

$$M_E \simeq M_L \gg M_Z$$

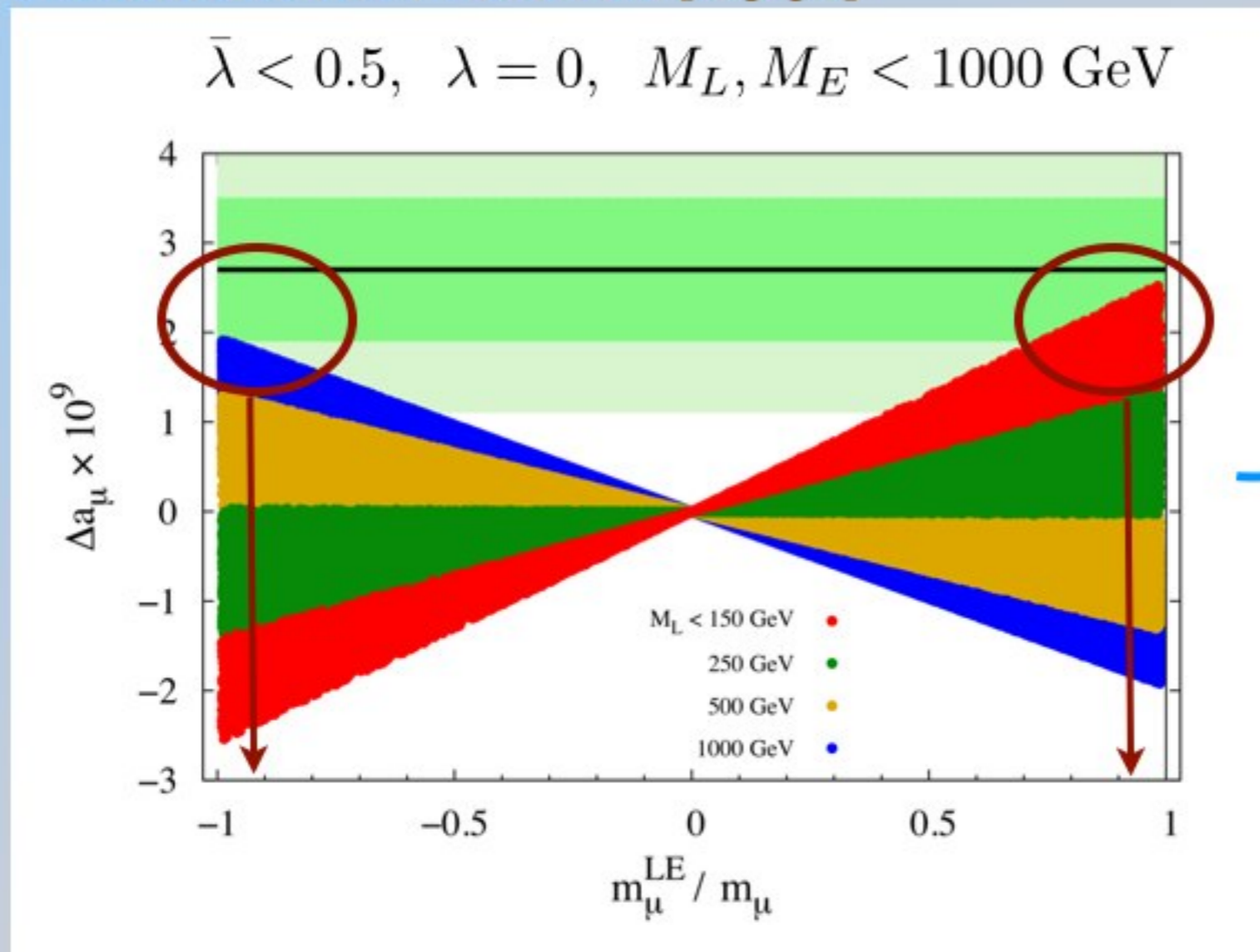
## integrating out vectorlike leptons:

$$\mathcal{L}_{eff} \supset -\bar{\mu}_L \left( y_\mu + \frac{\lambda^L \bar{\lambda} \lambda^E}{M_L M_E} H H^\dagger \right) \mu_R H + h.c. \longrightarrow - (m_\mu^H + m_\mu^{LE}) \bar{\mu}_L \mu_R + h.c.$$

$$\Delta a_\mu \simeq c \frac{m_\mu m_\mu^{LE}}{(4\pi v)^2} \simeq 0.85 c \frac{m_\mu^{LE}}{m_\mu} \Delta a_\mu^{exp}$$

## Random scan:

R.D. and A. Raval, 1305.3522 [hep-ph]



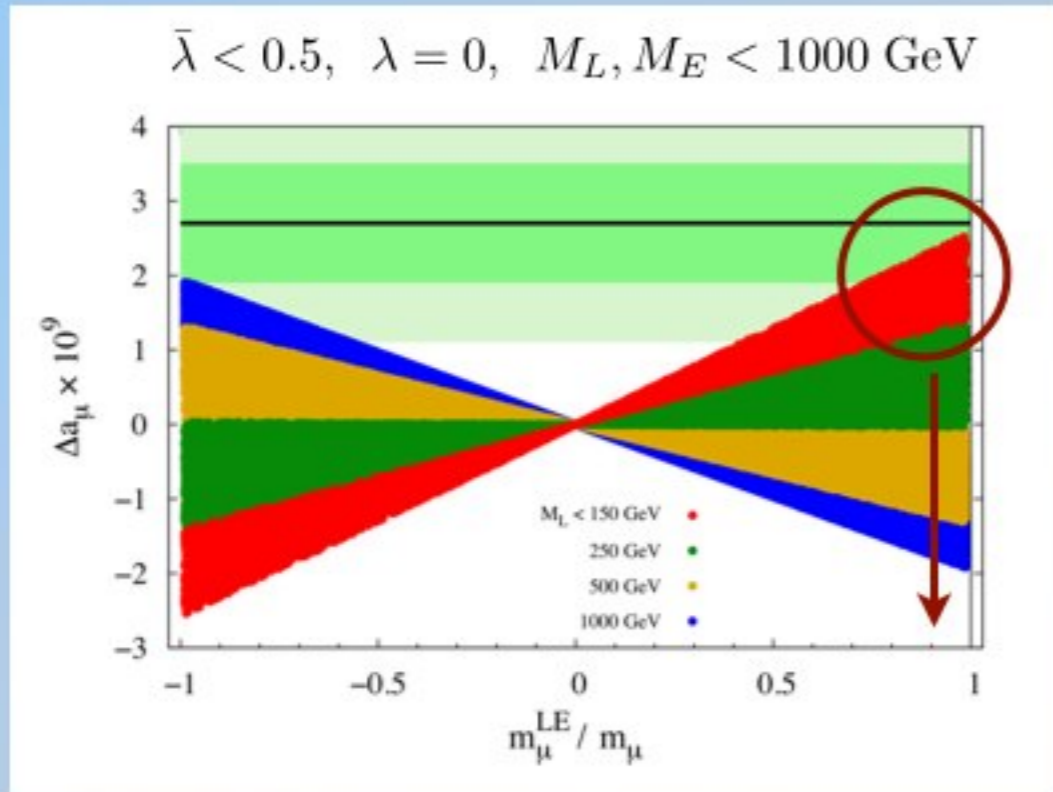
$$c = f(M_L)$$

Constraints from precision EW data:

$$\frac{\lambda_{E^c} v}{M_E} < 0.03, \quad \frac{\lambda_{L^c} v}{M_L} < 0.04$$

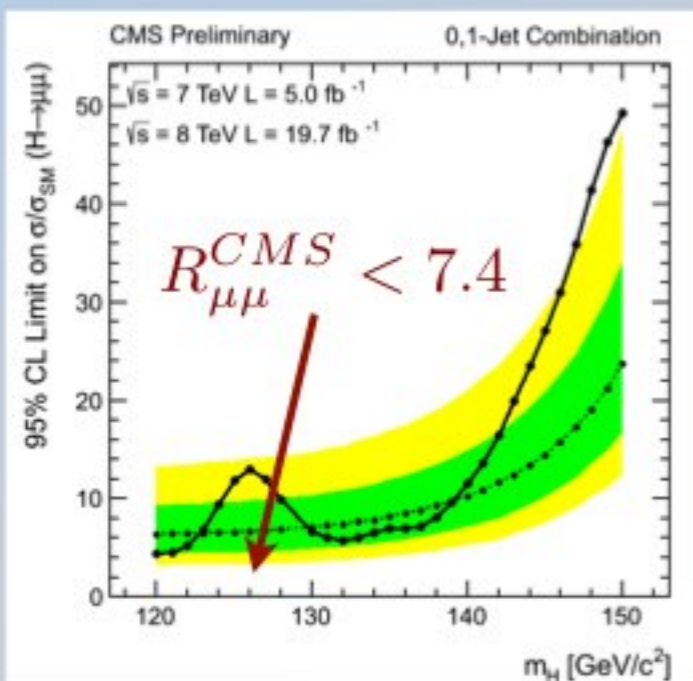
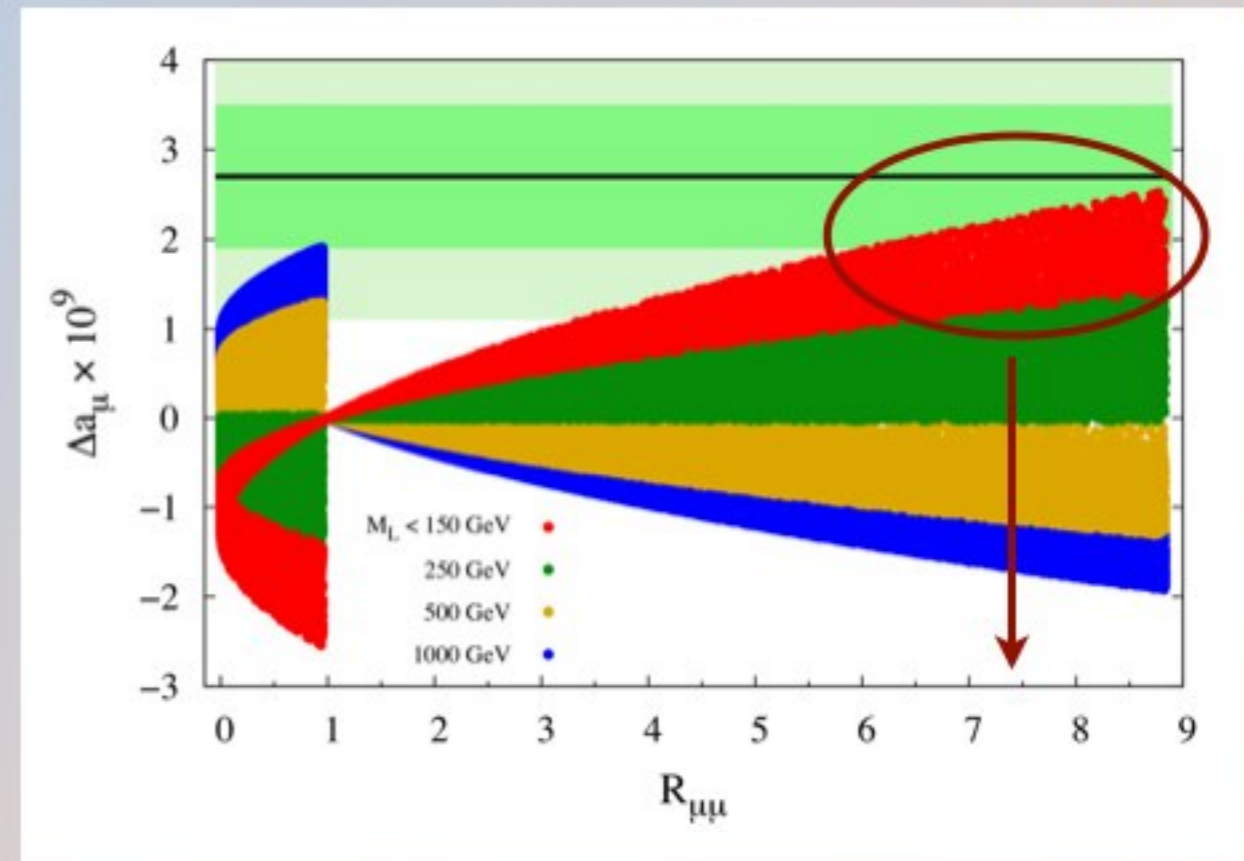
$$(\bar{e}_{Li}, \bar{L}_L^-, \bar{E}_L) \begin{pmatrix} y_{ij} v & 0 & \lambda_i^E v \\ \lambda_j^L v & M_L & \lambda v \\ 0 & \bar{\lambda} v & M_E \end{pmatrix} \begin{pmatrix} e_{Rj} \\ L_R^- \\ E_R \end{pmatrix}$$

# $h \rightarrow \mu\mu$



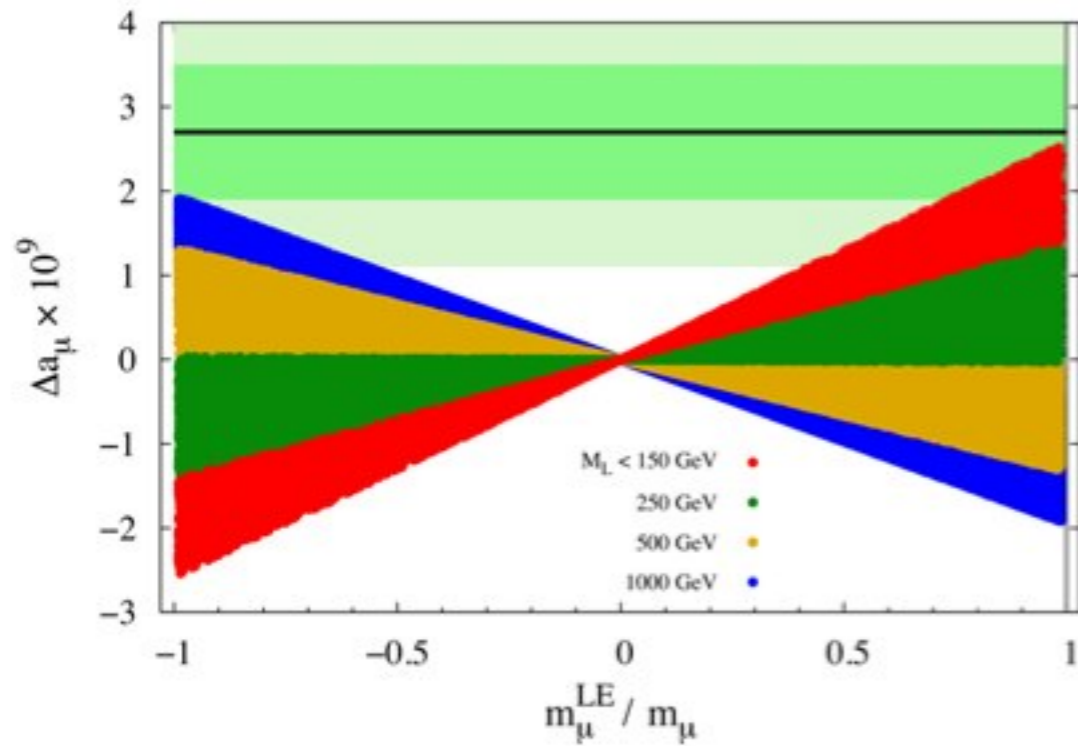
$$\mathcal{L}_{eff} \supset -\bar{\mu}_L \left( y_\mu + \frac{\lambda^L \bar{\lambda} \lambda^E}{M_L M_E} H H^\dagger \right) \mu_R H + h.c. \rightarrow - (m_\mu^H + m_\mu^{LE}) \bar{\mu}_L \mu_R + h.c.$$

R.D. and A. Raval, 1305.3522 [hep-ph]



$$R_{\mu\mu} = \frac{\Gamma(h \rightarrow \mu^+ \mu^-)}{\Gamma(h \rightarrow \mu^+ \mu^-)_{SM}}$$

$\bar{\lambda} < 0.5, \lambda = 0, M_L, M_E < 1000 \text{ GeV}$

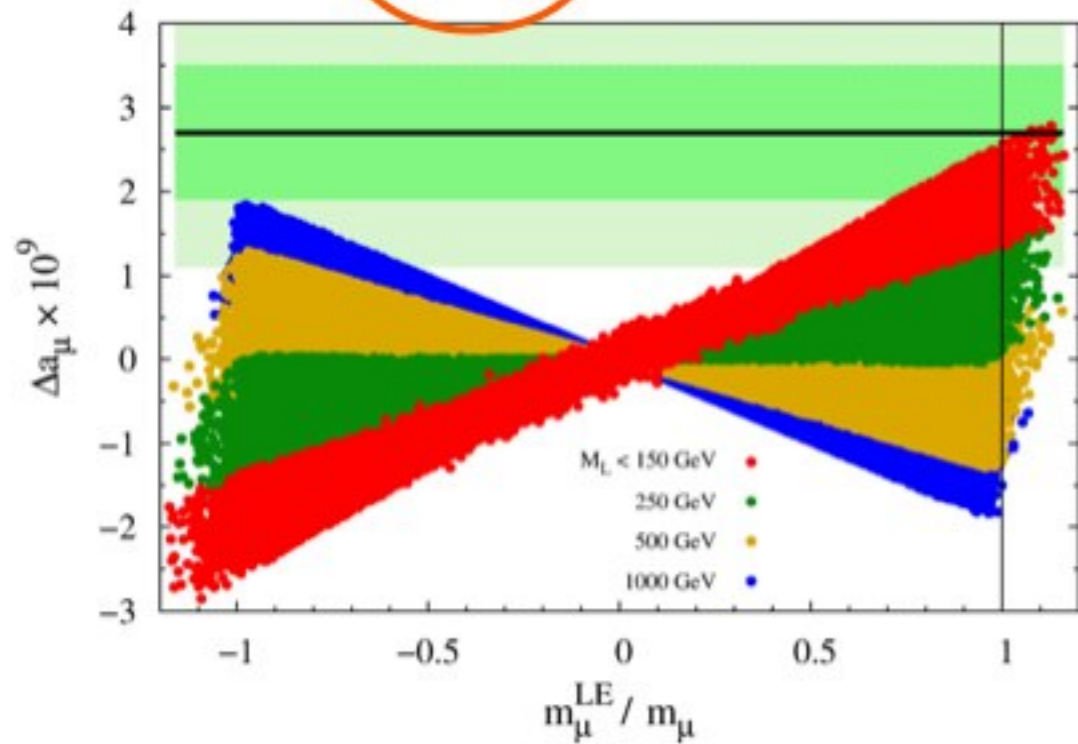


$$\mathcal{L} \supset -\bar{l}_{Li} y_{ij} e_{Rj} H - \bar{l}_{Li} \lambda_i^E E_R H - \bar{L}_L \lambda_j^L e_{Rj} H - \lambda \bar{L}_L E_R H - \bar{\lambda} H^\dagger \bar{E}_L L_R - M_L \bar{L}_L L_R - M_E \bar{E}_L E_R + h.c.,$$

$$(\bar{e}_{Li}, \bar{L}_L^-, \bar{E}_L) \begin{pmatrix} y_{ij} v & 0 & \lambda_i^E v \\ \lambda_j^L v & M_L & \lambda v \\ 0 & \bar{\lambda} v & M_E \end{pmatrix} \begin{pmatrix} e_{Rj} \\ L_R^- \\ E_R \end{pmatrix}$$

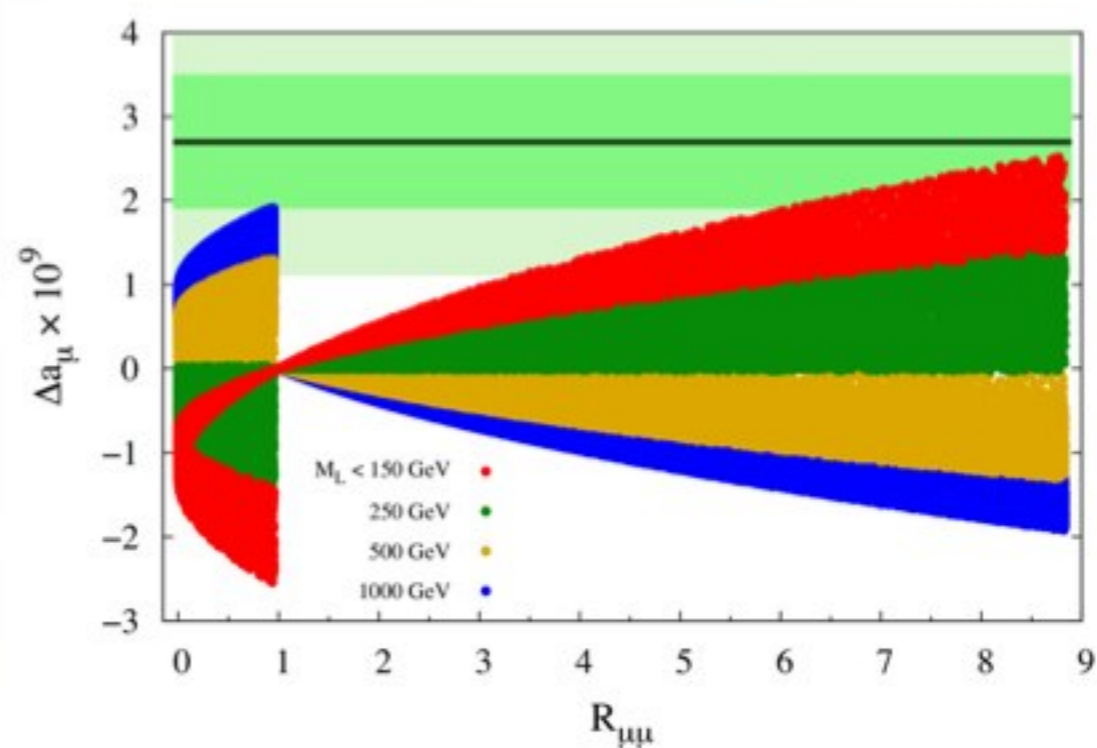
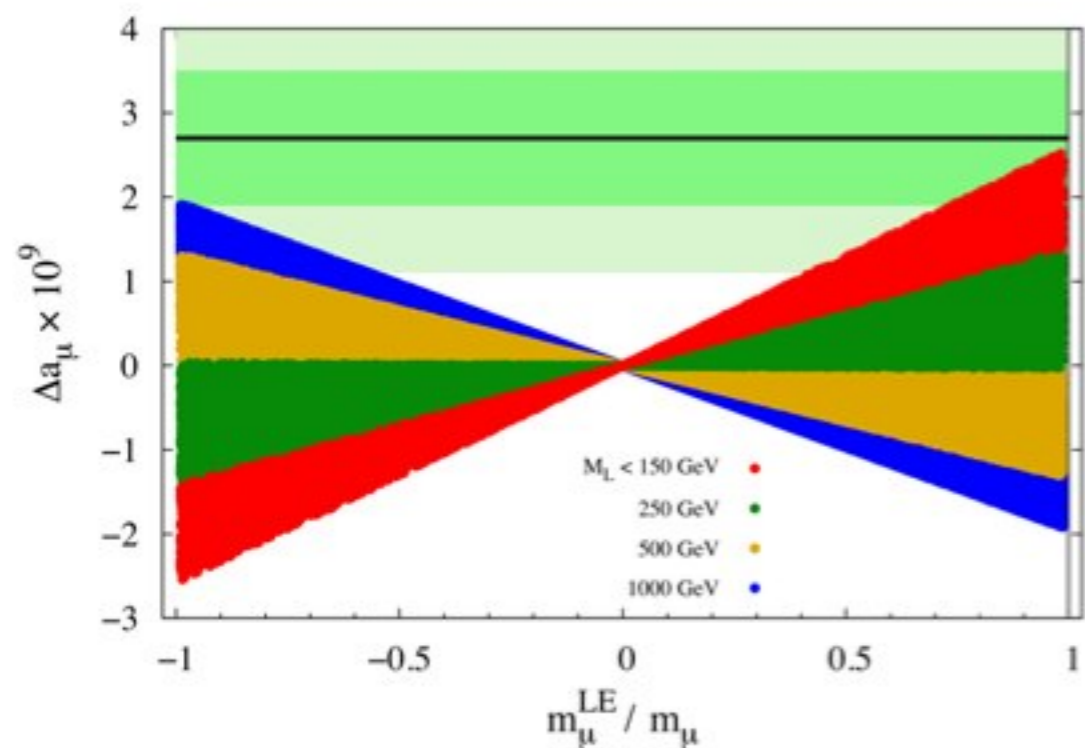
$$\mathcal{L}_{eff} \supset -\bar{\mu}_L \left( y_\mu + \frac{\lambda^L \bar{\lambda} \lambda^E}{M_L M_E} H H^\dagger \right) \mu_R H + h.c. \rightarrow -(m_\mu^H + m_\mu^{LE}) \bar{\mu}_L \mu_R + h.c.$$

$\bar{\lambda} < 0.5, \lambda < 0.5, M_L, M_E < 1000 \text{ GeV}$

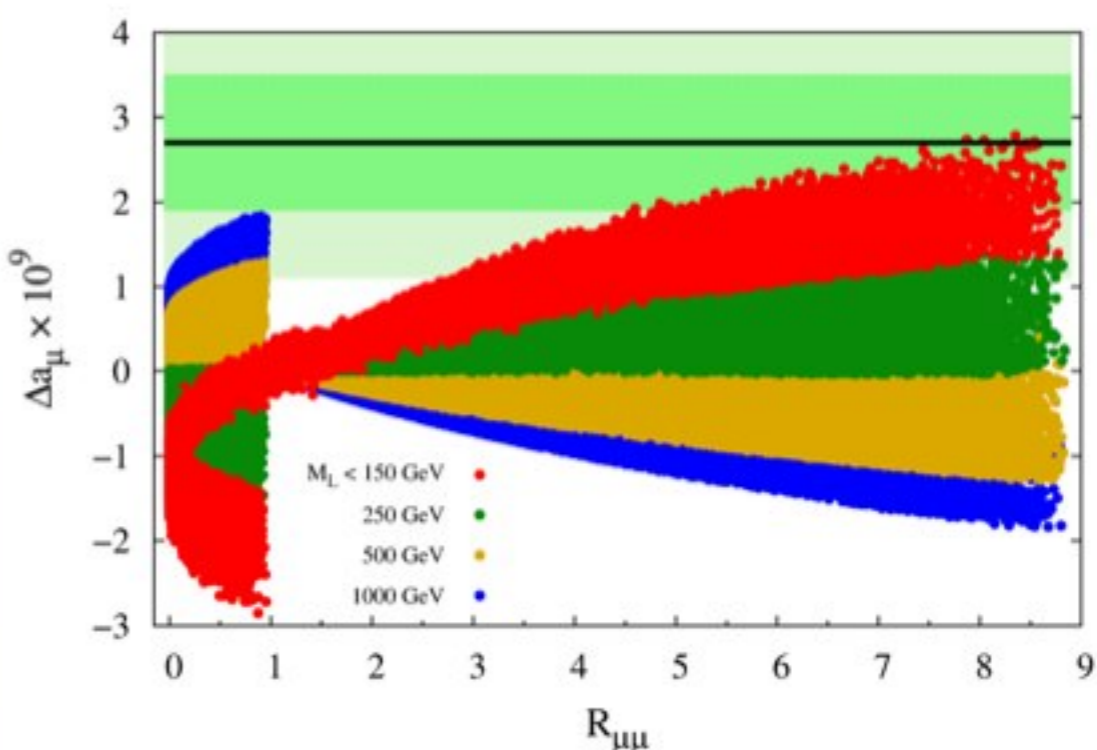
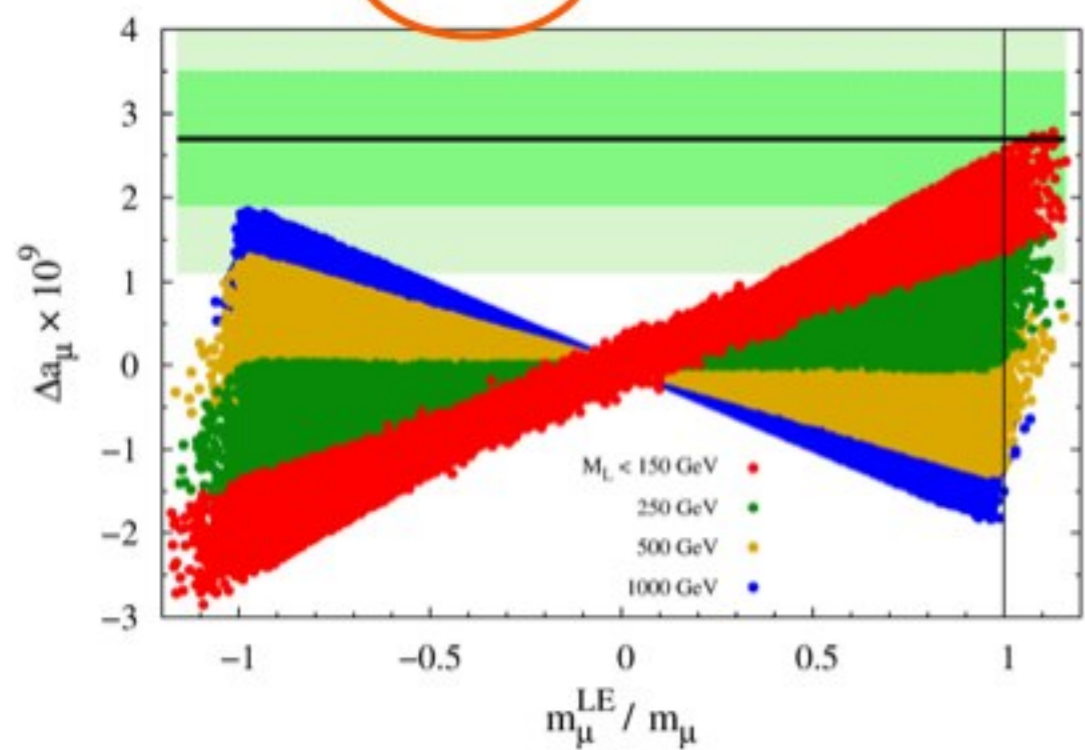


$$\Delta a_\mu \simeq c \frac{m_\mu m_\mu^{LE}}{(4\pi v)^2} \simeq 0.85 c \frac{m_\mu^{LE}}{m_\mu} \Delta a_\mu^{exp}$$

$\bar{\lambda} < 0.5, \lambda = 0, M_L, M_E < 1000 \text{ GeV}$

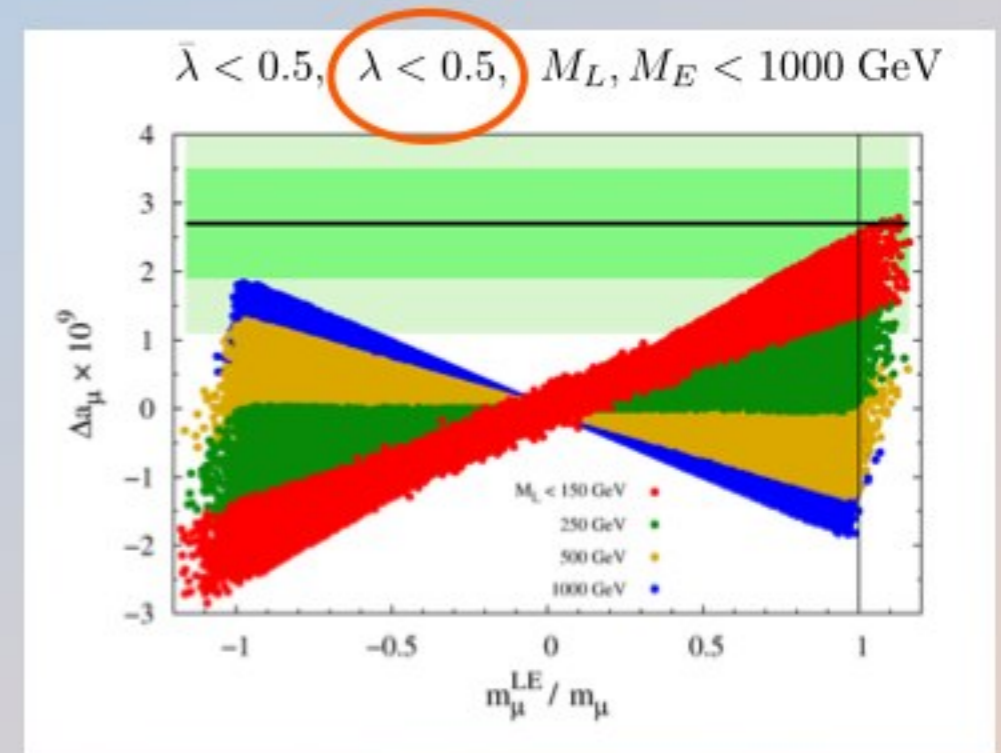
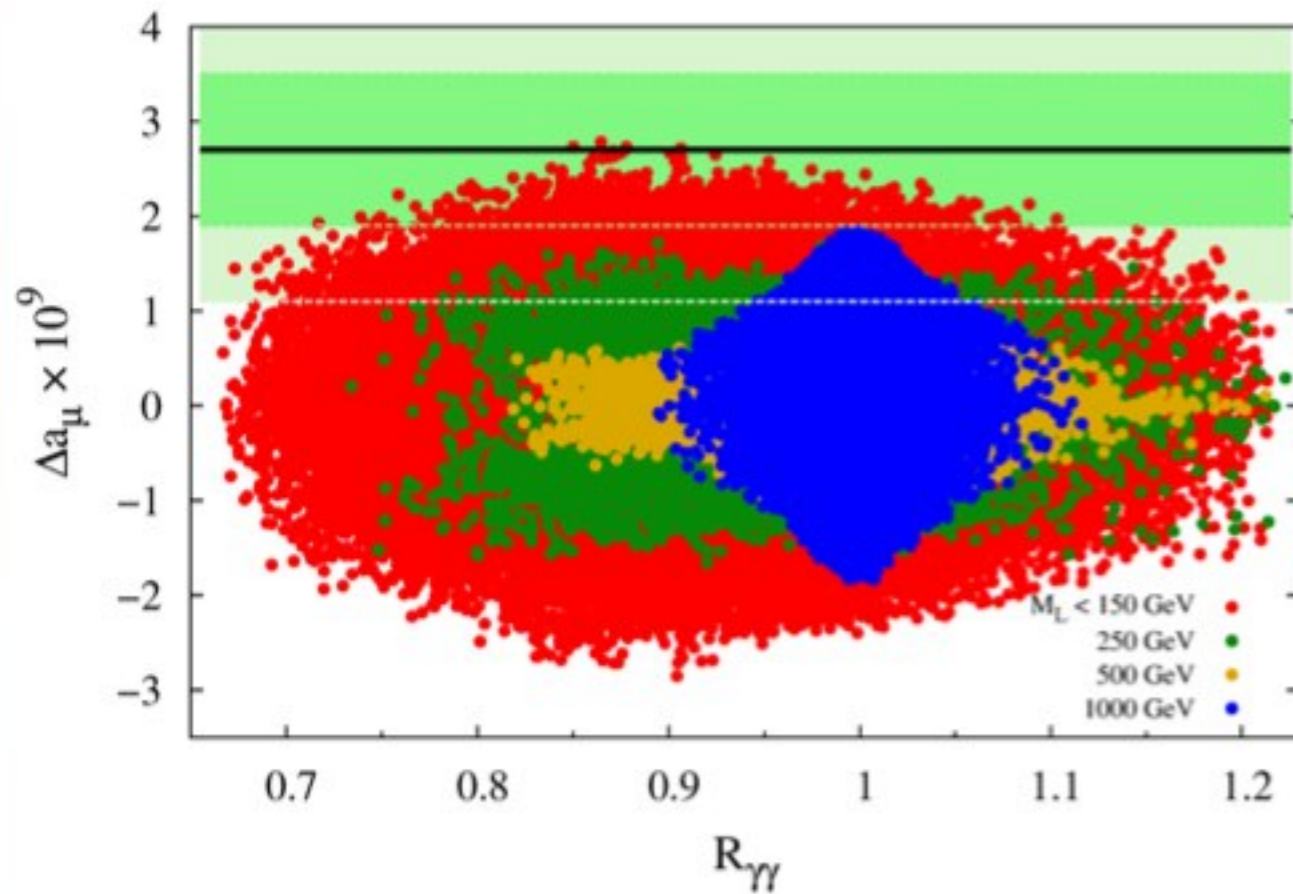


$\bar{\lambda} < 0.5, \lambda < 0.5, M_L, M_E < 1000 \text{ GeV}$



# $h \rightarrow \gamma \gamma$

$$R_{\gamma\gamma} = \frac{\Gamma(h \rightarrow \gamma\gamma)}{\Gamma(h \rightarrow \gamma\gamma)_{SM}}$$

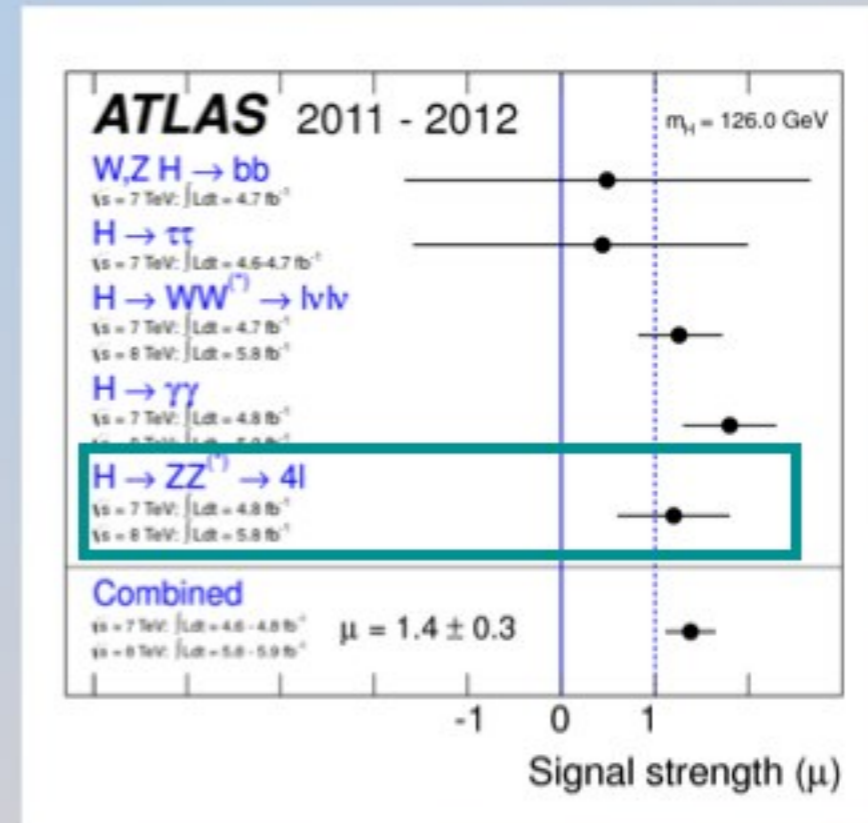
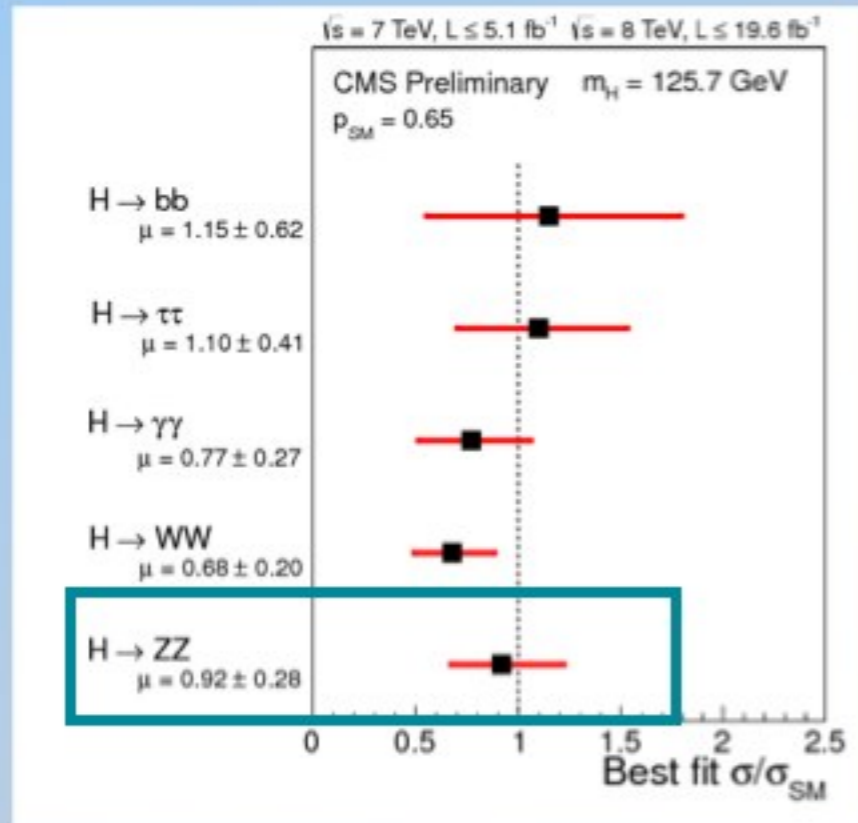


$$(\bar{e}_{Li}, \bar{L}_L^-, \bar{E}_L) \begin{pmatrix} y_{ij}v & 0 & \lambda_i^E v \\ \lambda_j^L v & M_L & \lambda v \\ 0 & \bar{\lambda} v & M_E \end{pmatrix} \begin{pmatrix} e_{Rj} \\ L_R^- \\ E_R \end{pmatrix}$$

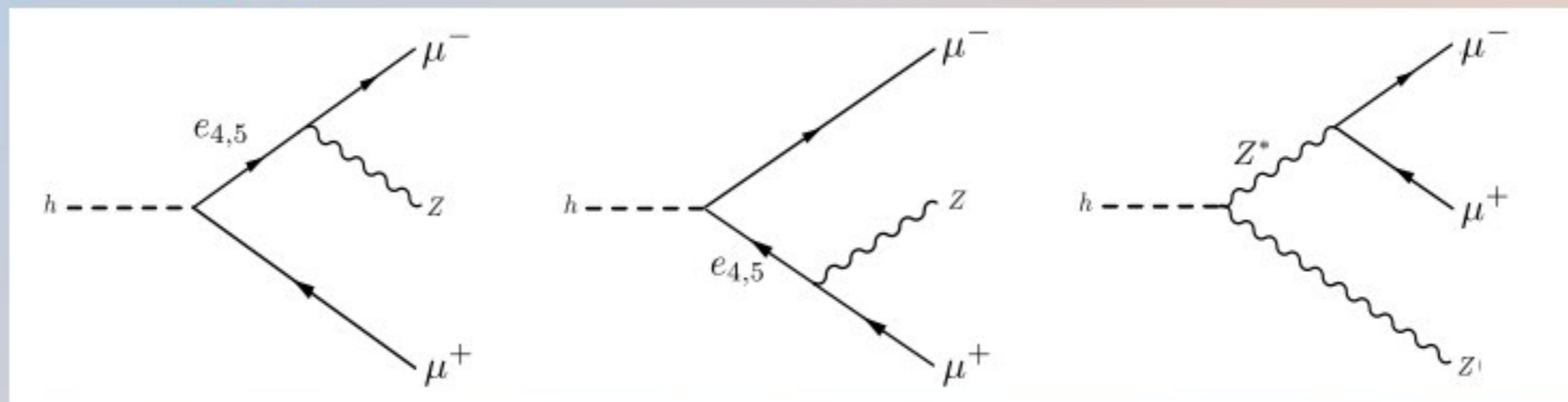
$$\text{amplitude} \propto -\frac{\bar{\lambda}\lambda v^2}{M_L M_E - \bar{\lambda}\lambda v^2}$$



# $h \rightarrow ZZ^*$



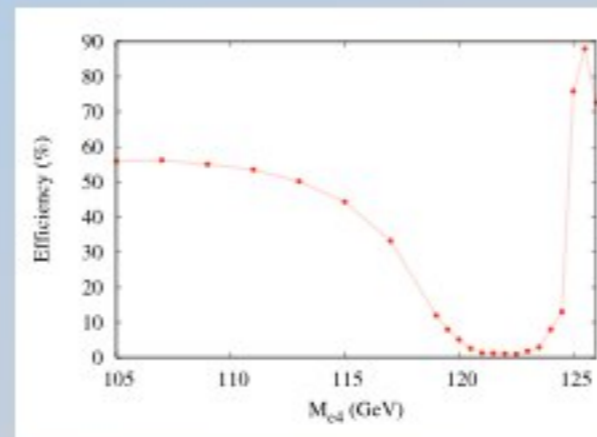
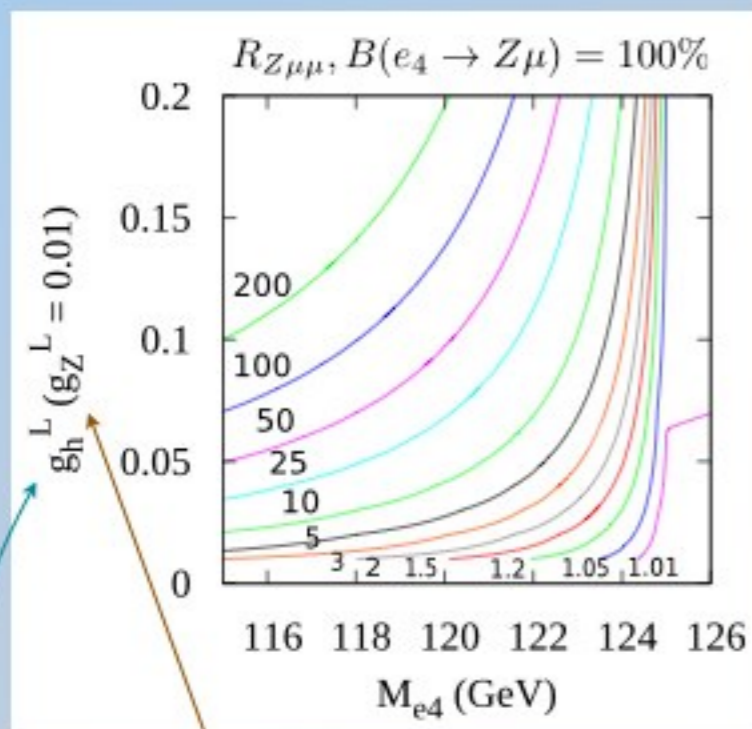
$h \rightarrow E\mu \rightarrow Z\mu\mu$  produces the same final state as  $h \rightarrow ZZ^* \rightarrow Z\mu\mu$ :



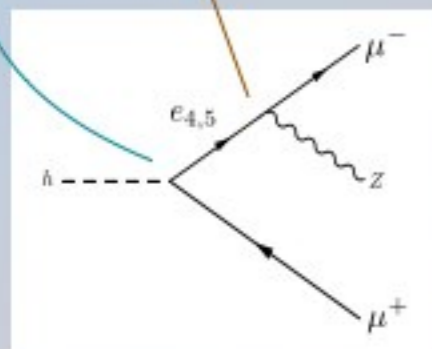
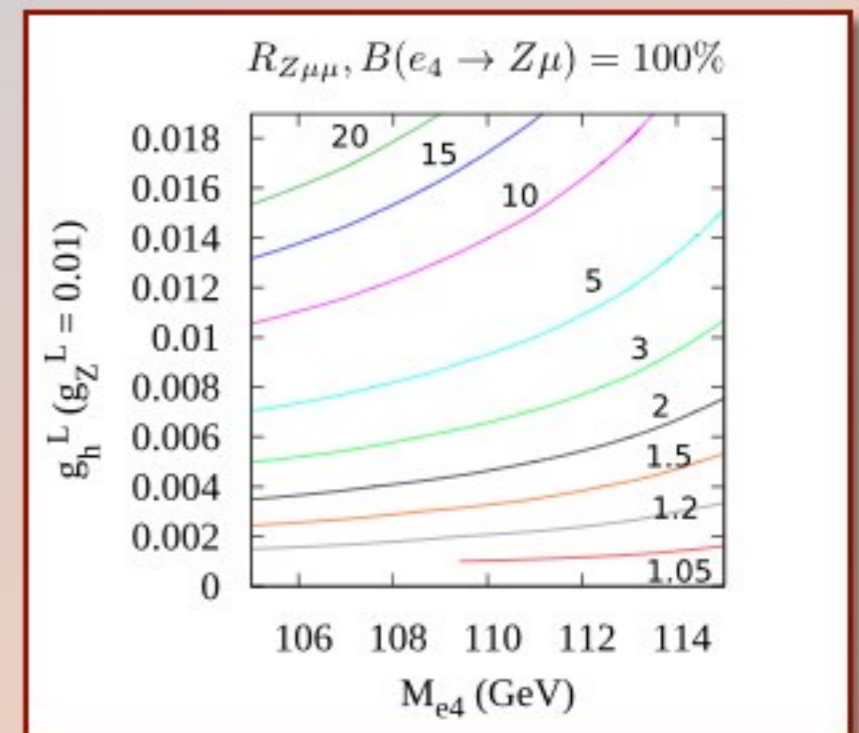
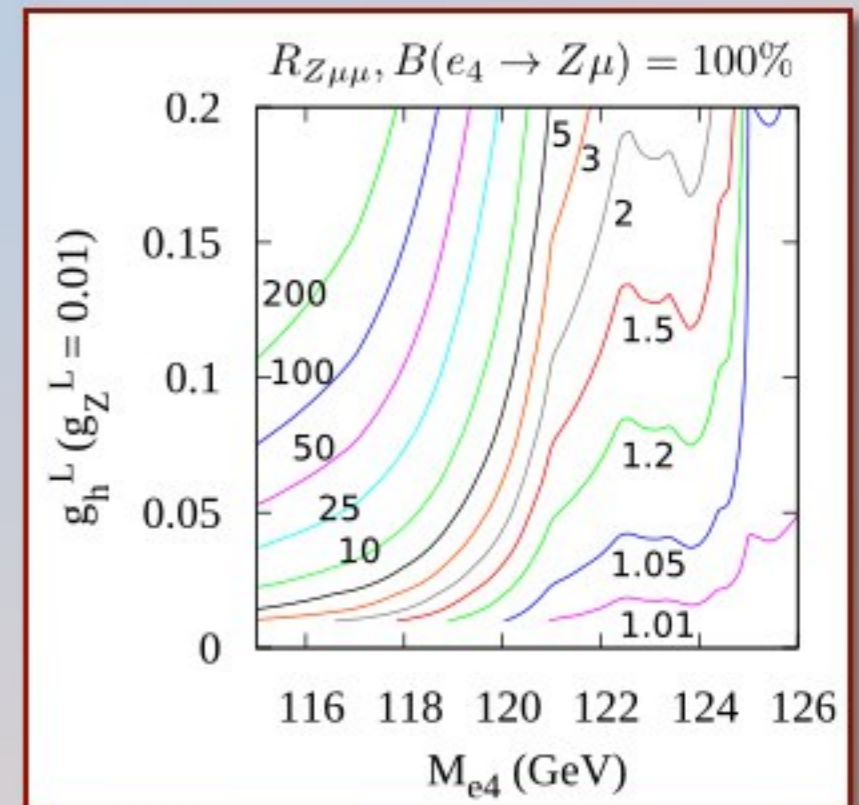
# $h \rightarrow ZZ^*$

## contribution from heavy leptons:

$$R_{Z\mu\mu} = \frac{\Gamma(h \rightarrow Z\mu\mu)}{\Gamma(h \rightarrow Z\mu\mu)_{SM}}$$

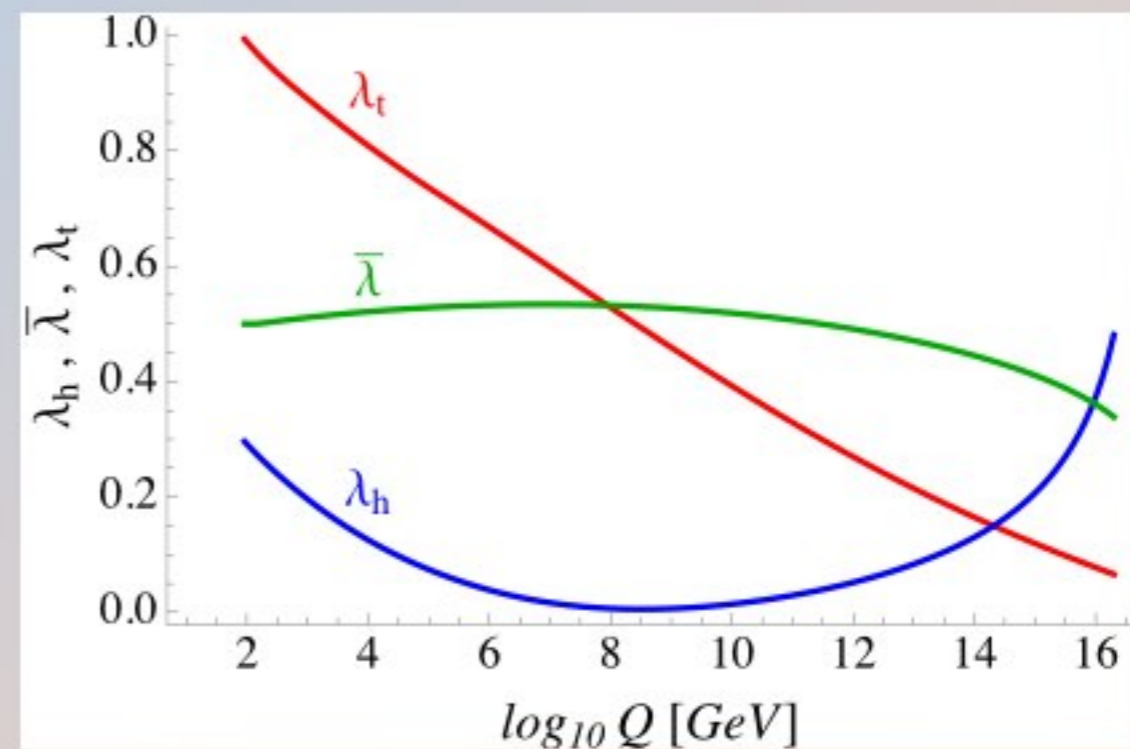
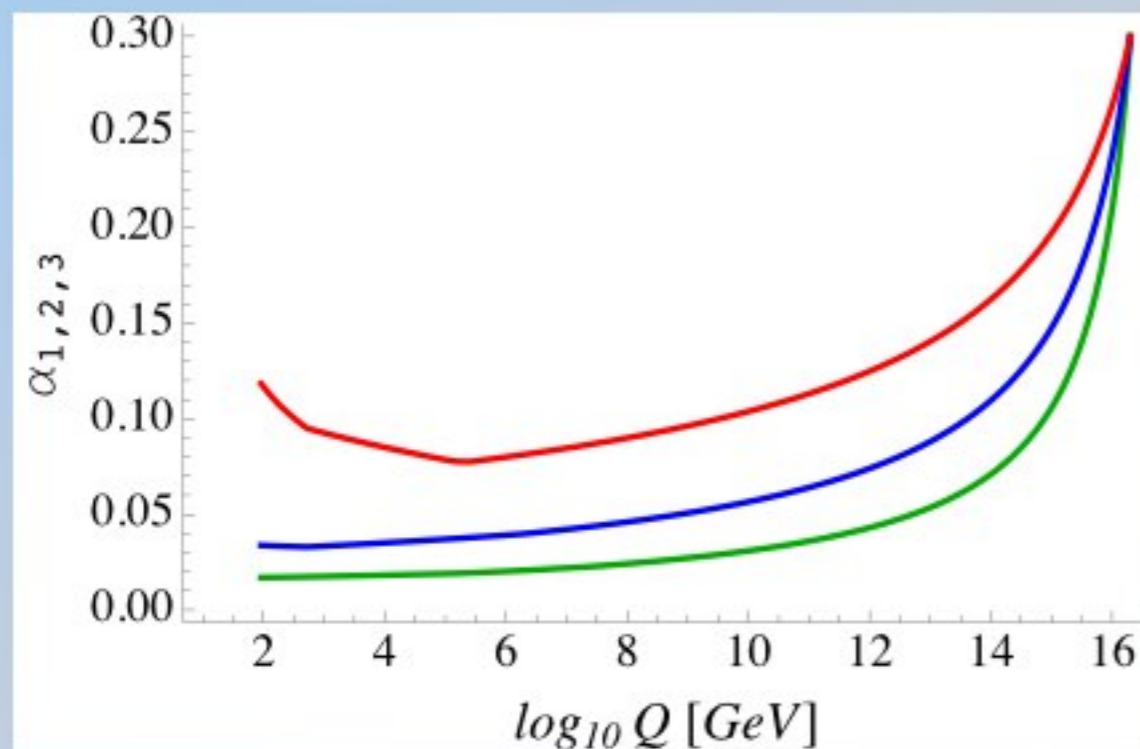


efficiency to pass  $ZZ^*$  cuts



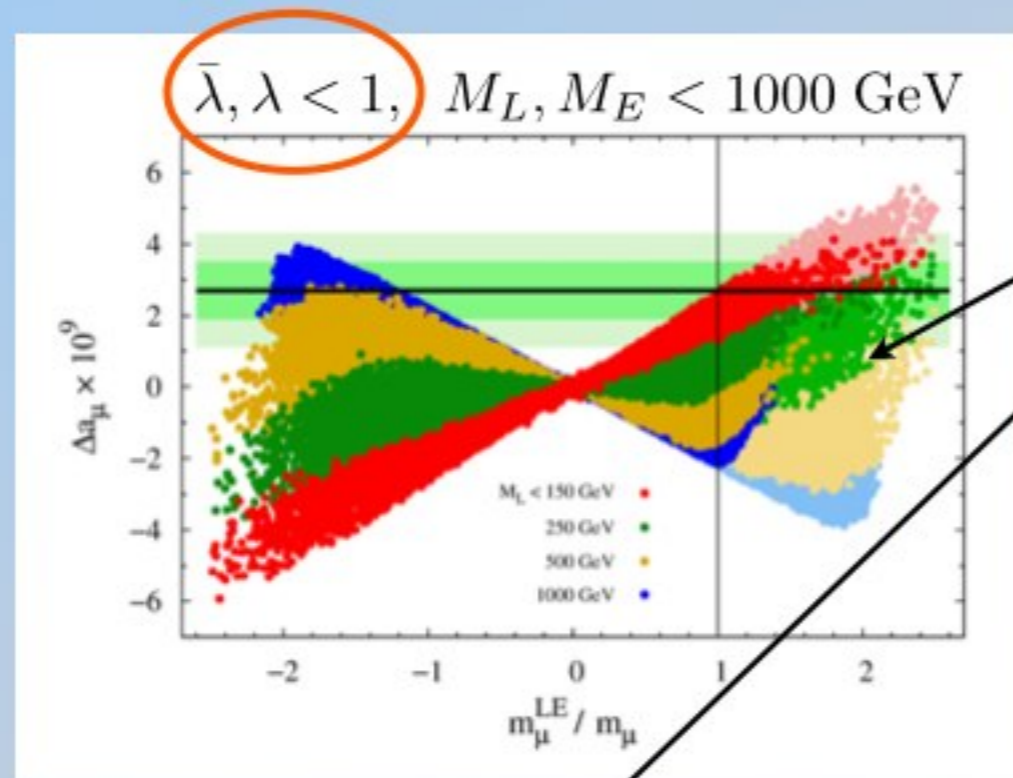
# UV completion with 3 VFs

All the features of insensitive unification, including the stability of the EW minimum of the Higgs potential are preserved even with extra Yukawa couplings needed for the explanation of the muon  $g-2$  anomaly:

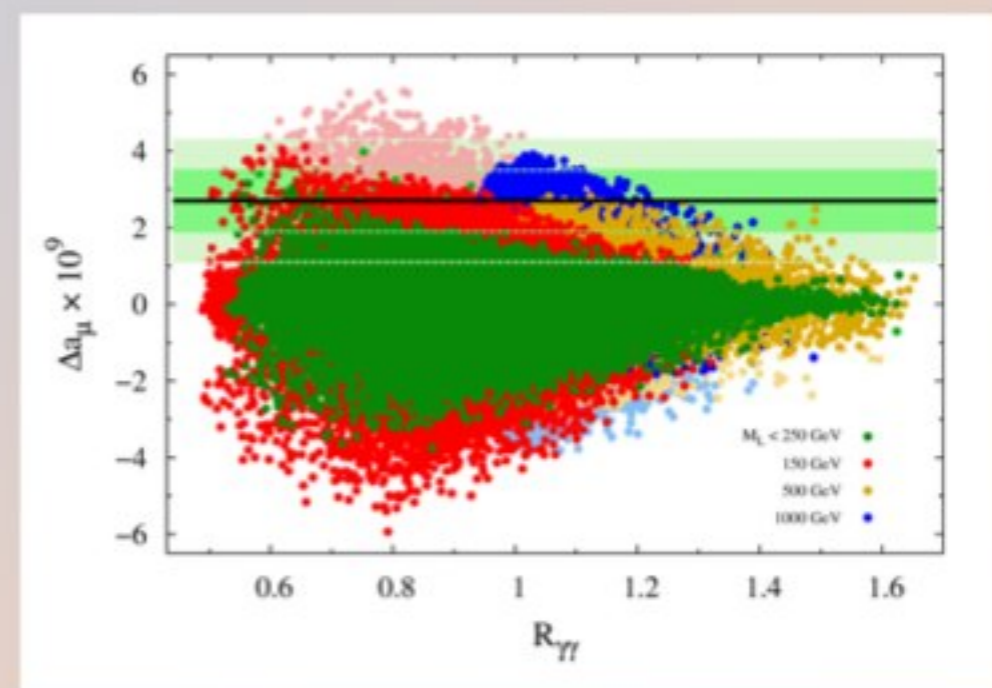
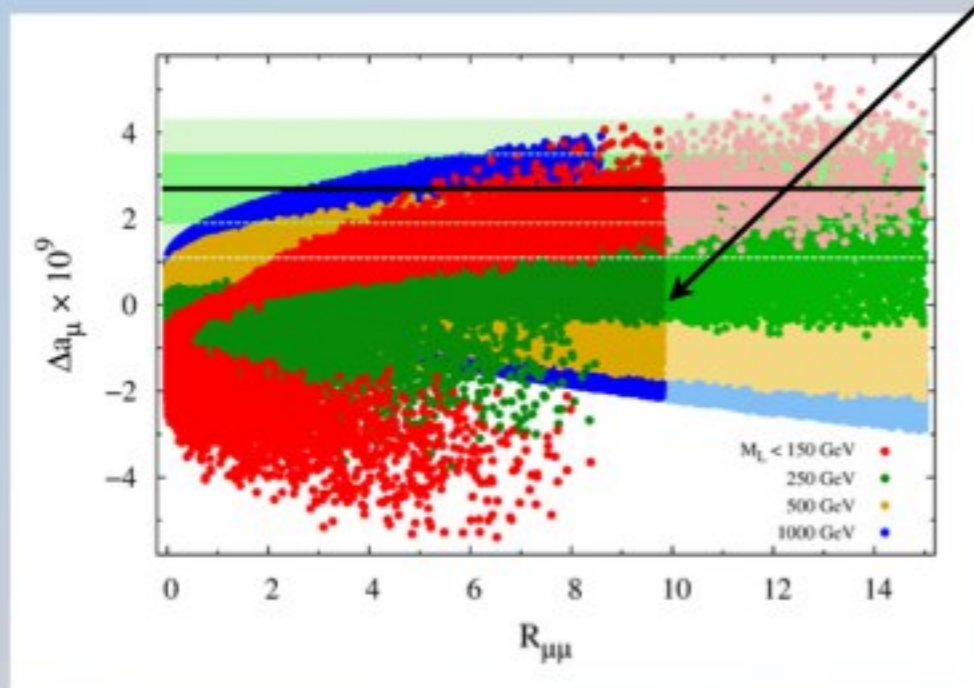
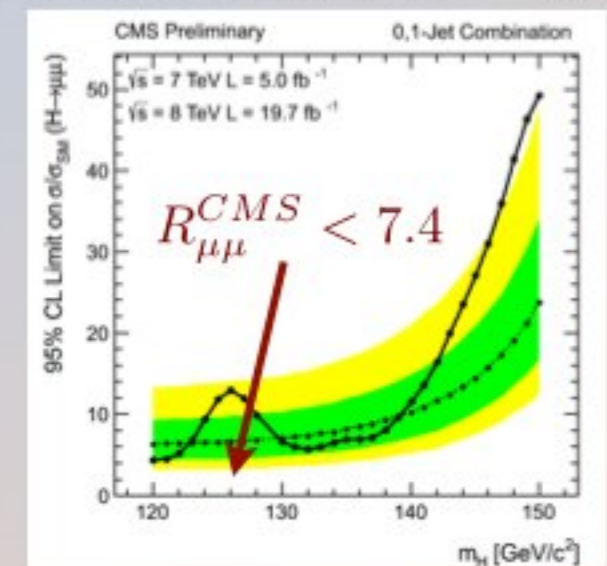


$$M_{L_1} = M_{E_1} = 150 \text{ GeV}$$

# Allowing larger Yukawa couplings



lightly shaded points ruled out by Atlas search for  $h \rightarrow \mu\mu$



# Conclusions

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- ◆ **3 (or more) pairs of vectorlike families allow for **insensitive unification of gauge couplings****  
**predictive**
- ◆ **resurrects simple non-supersymmetric GUTs (proton decay)**  
**the GUT scale is adjustable and could be identified with the string or Planck scale**
- ◆ **the electroweak minimum is stable all the way to the GUT scale**
- ◆ **some of the extra fermions might be within the reach of the LHC**  
**and modify phenomenology of the SM:  
small flavor violation from mixing through  
Yukawa couplings, contributions in loops, ...**