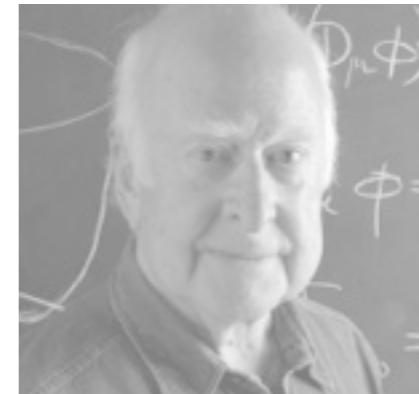


Goldstone meets Higgs @ the LHC



Javi Serra



UC Davis Joint Theory Seminar, March 18, 2013

*What does the recently discovered
125 GeV Higgs
imply for models of **strong dynamics**?*

... besides



TECHNICOLOR

$$\mathcal{L}_{eff}(\mu < \Lambda)$$

d<4

$$\epsilon \Lambda^2 |H|^2$$

d=4

$$\bar{\psi} \not{D} \mu \psi$$

$$F_{\mu\nu}^2 / g^2$$

$$Y_{ij} \bar{\psi}_i H \psi_j$$

$$\lambda |H|^4$$

d>4

$$\frac{C_{ij}}{\Lambda} \ell_i H H \ell_j$$

$$\frac{C_{ijkl}}{\Lambda^2} \bar{\psi}_i \psi_j \bar{\psi}_k \psi_l$$

$$\frac{1}{\Lambda^2} H^\dagger W_{\mu\nu} H B^{\mu\nu}$$

•
•
•

$$\mathcal{L}_{eff}(\mu < \Lambda)$$

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$$\frac{1}{\Lambda^2} H^\dagger W_{\mu\nu} H B^{\mu\nu}$$

•
•
•

Nature seems to suggest the point-like limit of the SM:

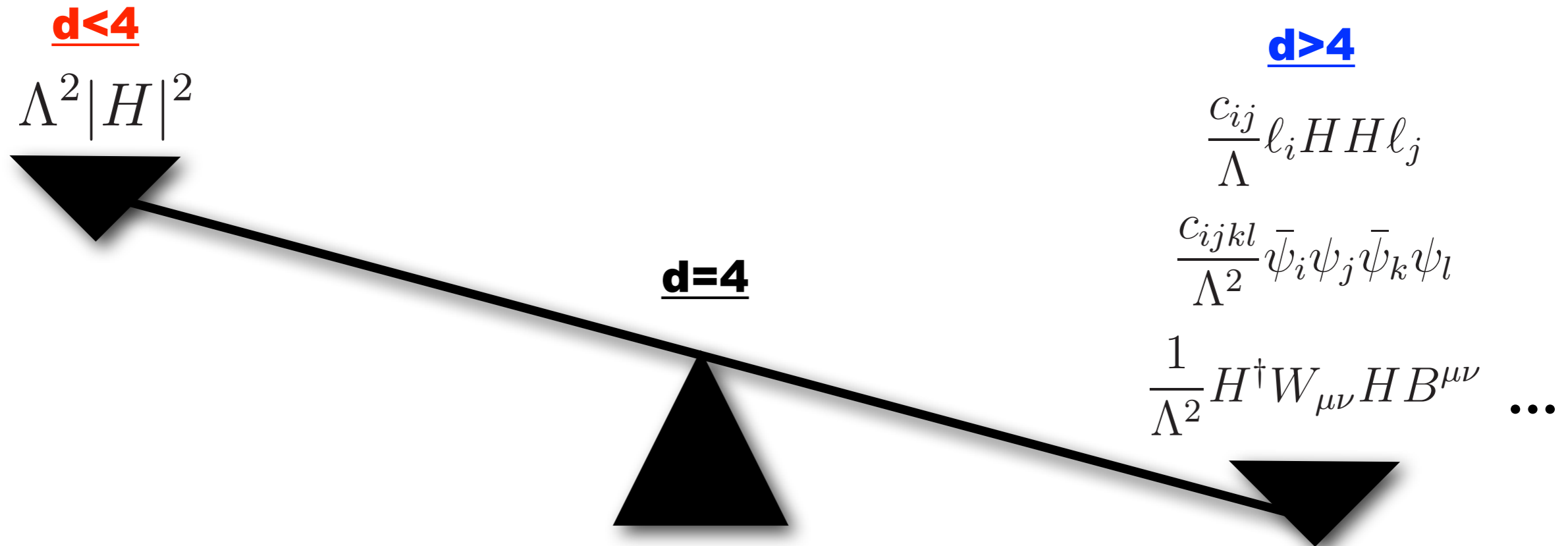
$$\Lambda \longrightarrow M_{Pl}$$

$$\epsilon \longrightarrow 10^{-34}$$

it would be unprecedented!

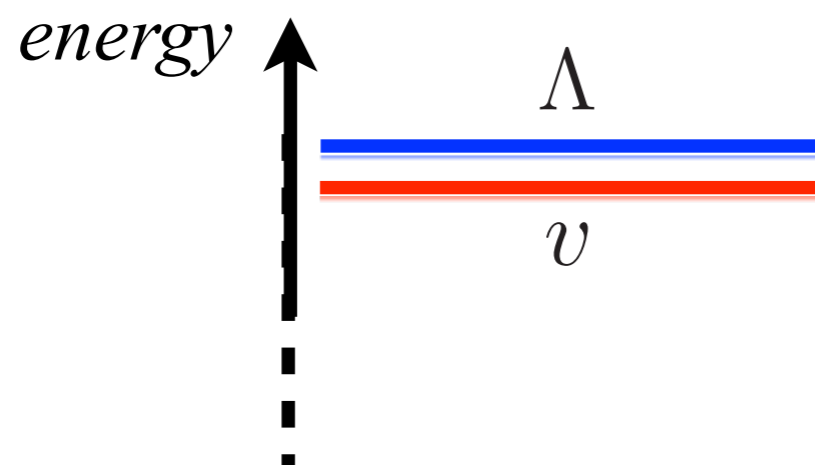
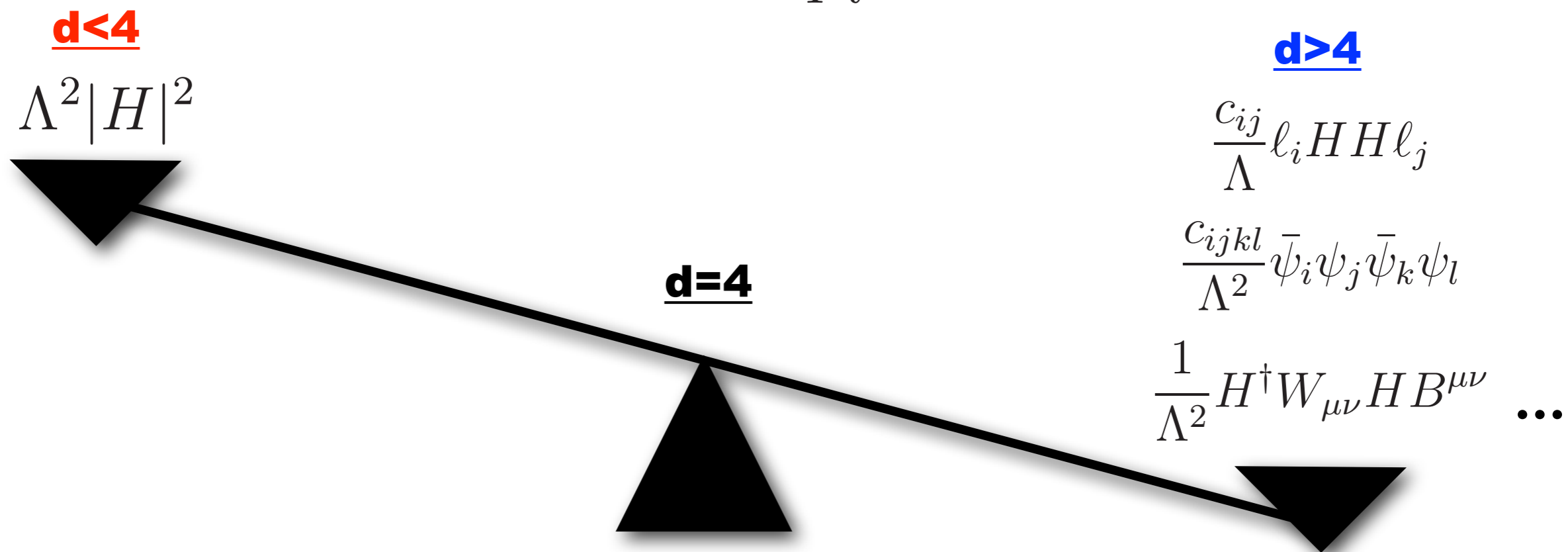
With an elementary scalar & Quantum EFT:

$$\Lambda \longrightarrow M_{Pl}$$



With an elementary scalar & Quantum EFT:

$$\Lambda \longrightarrow M_{Pl}$$



No hierarchy is generated

$$\Lambda \rightarrow M_{Pl}$$



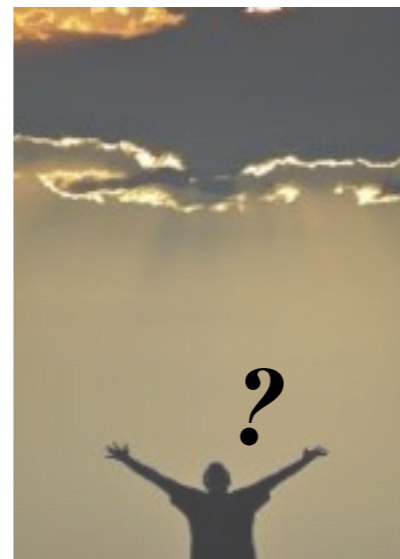
I am tuning!



$$\Lambda^2 |H|^2$$

d=4

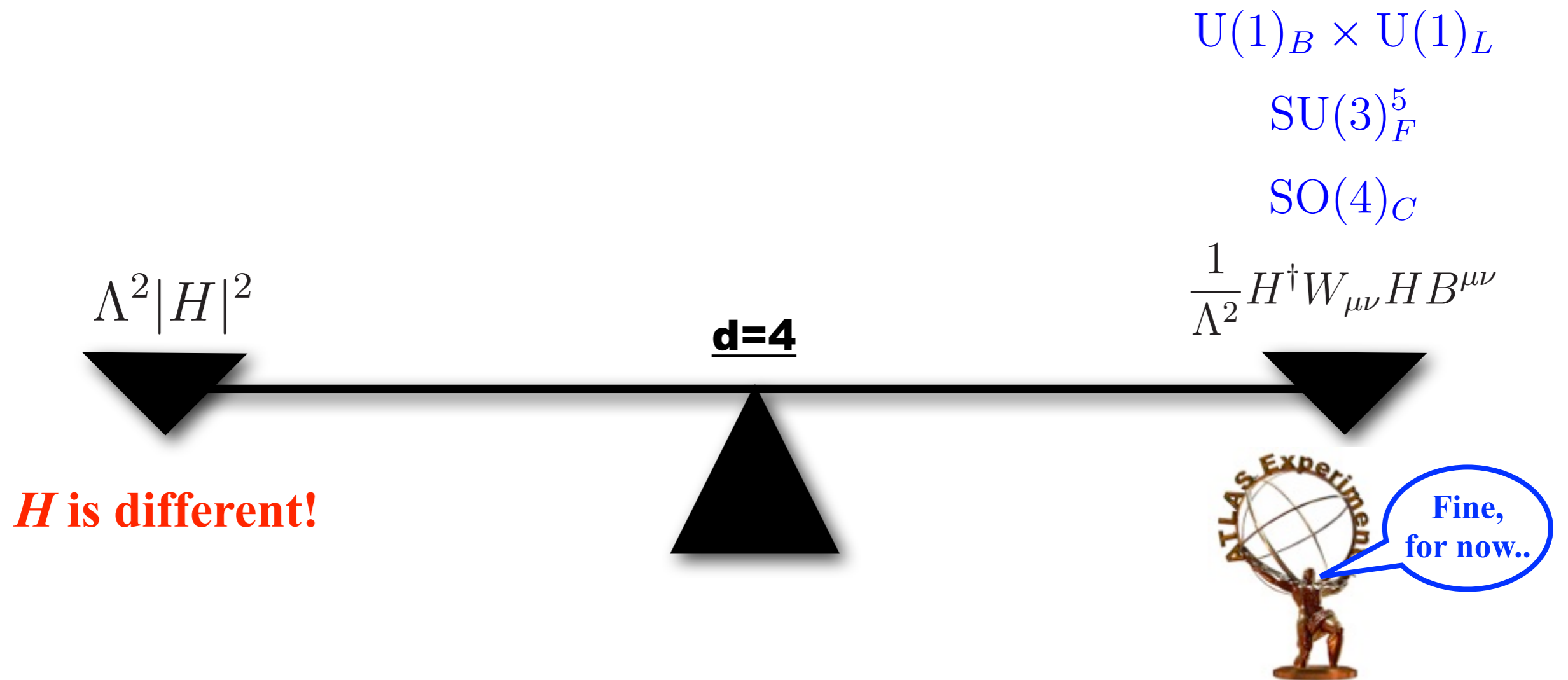
$$\frac{C_{ij}}{\Lambda} \ell_i H H \ell_j \dots$$



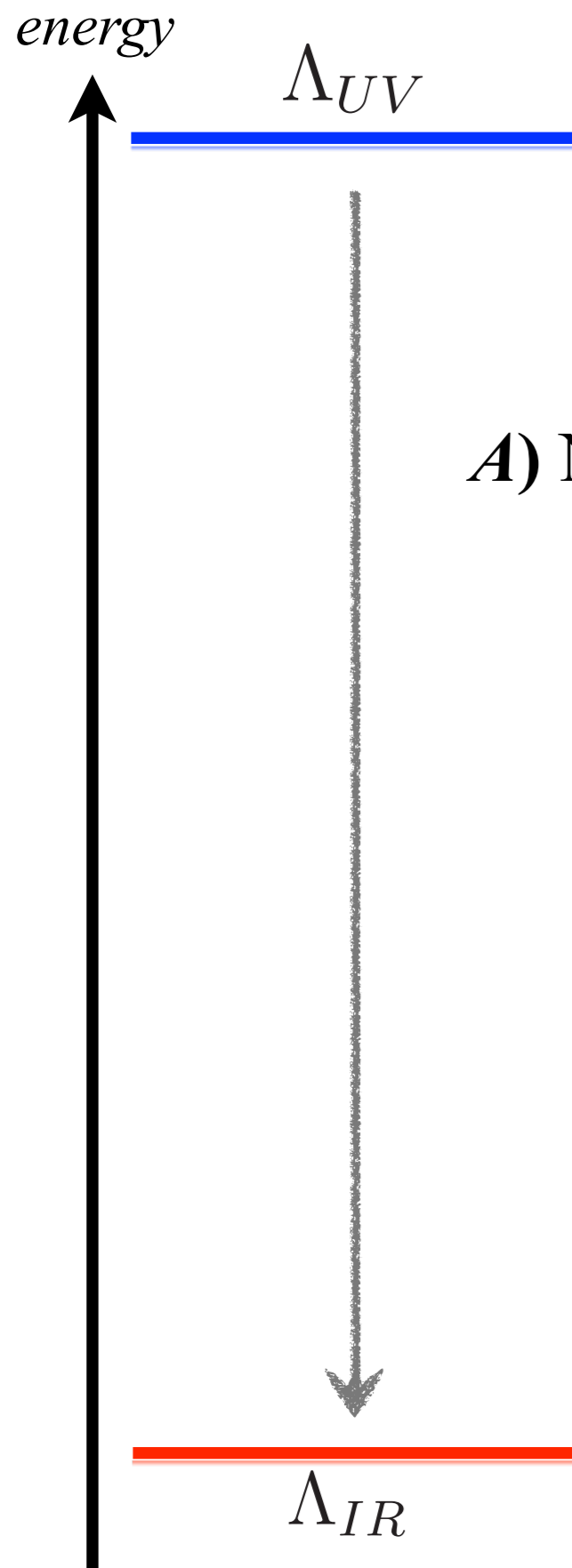
- anthropic reasoning
- beyond EFT
- ???

$$\Lambda \sim \text{TeV}$$

- a) Most dangerous operators can be protected by symmetries.
- b) Dynamical mechanisms allow to split Higgs sector.



It is for **Experiment** to decide if there is **New Physics** at the TeV



$$\Lambda_{UV} \gg \Lambda_{IR}$$

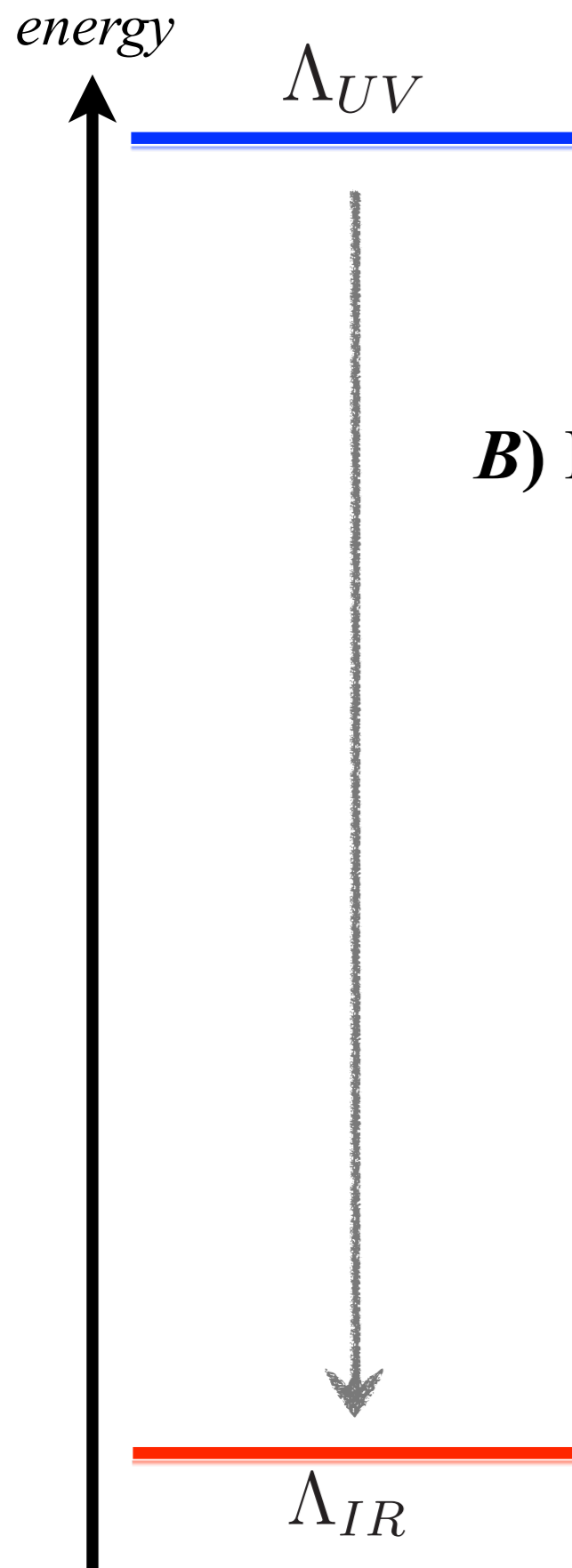
Natural Hierarchy from Scale Invariance:

A) No strongly relevant operators: $\mathcal{L} \supset \lambda \mathcal{O}$, $[\mathcal{O}] = 4 - \epsilon$

$$\lambda(\mu) = \lambda_0 \left(\frac{\Lambda_{UV}}{\mu} \right)^\epsilon$$

$$\lambda(\Lambda_{IR}) \sim 1, \quad \Lambda_{IR} \sim \Lambda_{UV} \lambda_0^{1/\epsilon}$$

Dimensional Transmutation



$$\Lambda_{UV} \gg \Lambda_{IR}$$

Natural Hierarchy from Scale Invariance:

B) If relevant operators, protected by symmetry:

- **Compositeness:** $H \sim \langle \psi \bar{\psi} \rangle$ *the Higgs is composite*

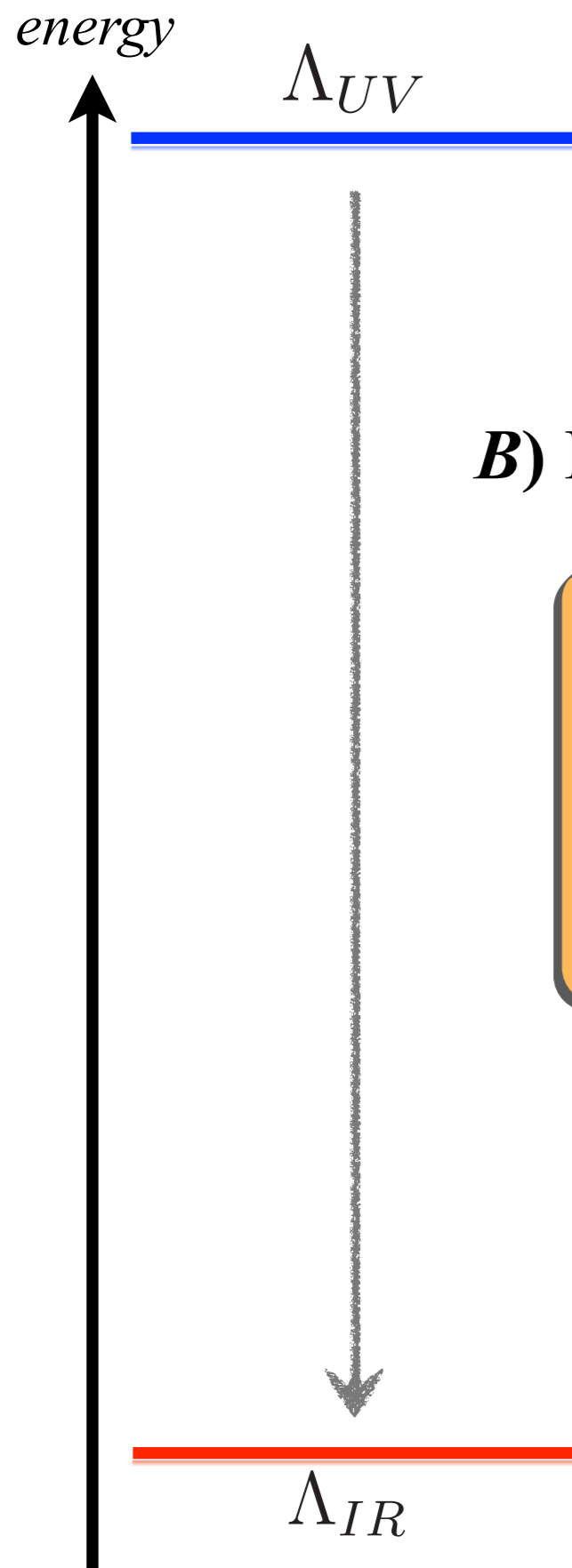
fermion masses protected by Chiral sym.

new states at $4\pi v \sim 2 \text{ TeV}$

- **Supersymmetry:** $H \sim \psi$ *the Higgs is chiral*

scalar masses protected by Chiral sym.

new states at $gv \sim 100 \text{ GeV}$



$$\Lambda_{UV} \gg \Lambda_{IR}$$

Natural Hierarchy from Scale Invariance:

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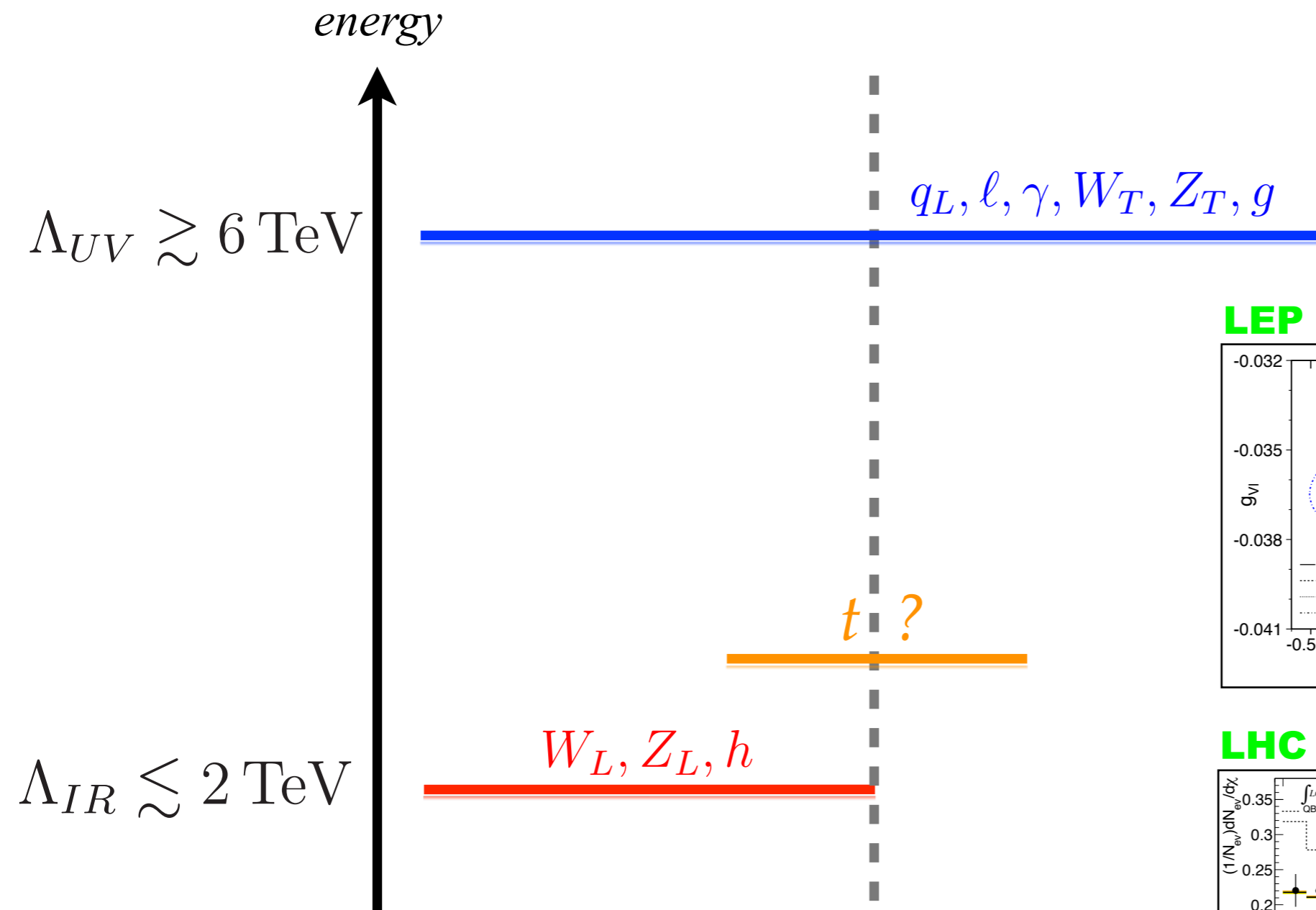
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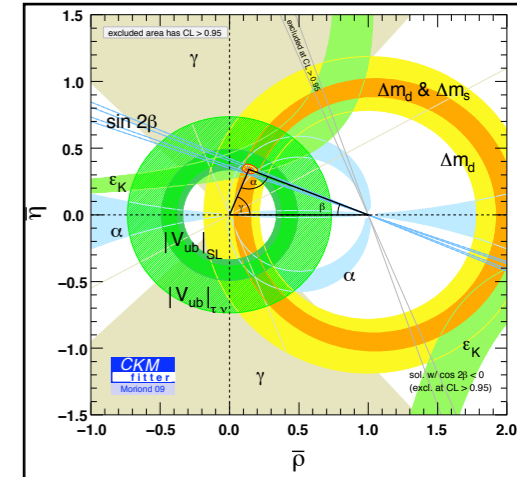
new states at $gv \sim 100 \text{ GeV}$

The Strongly Coupled (Composite) Sector

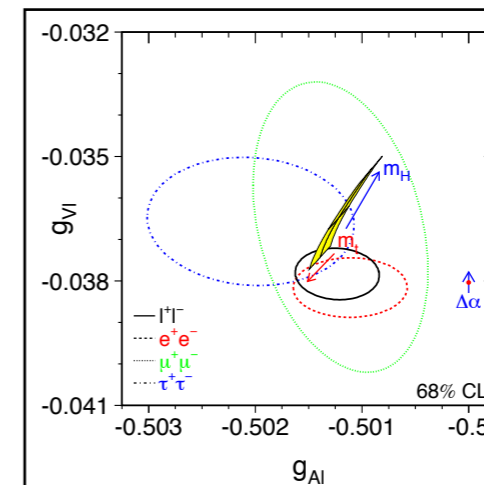
The emergent picture of the *Composite world*:



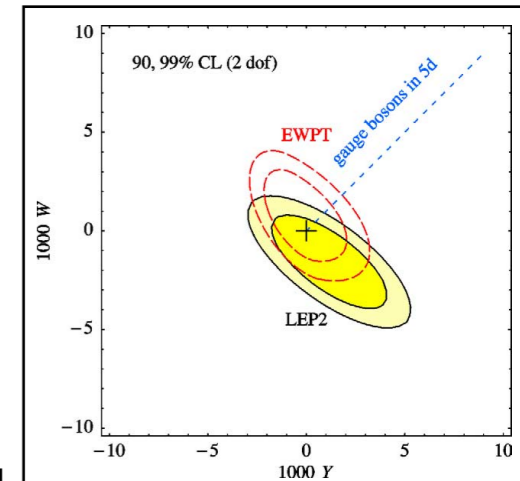
CKM fitter



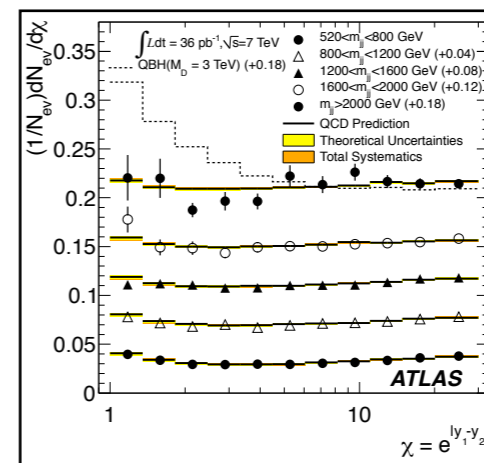
LEP



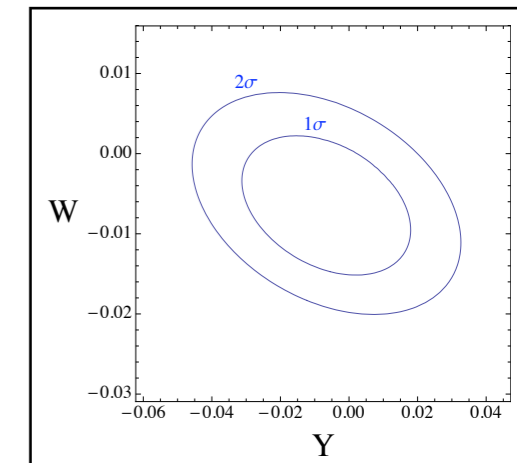
Barbieri et al. '04



LHC

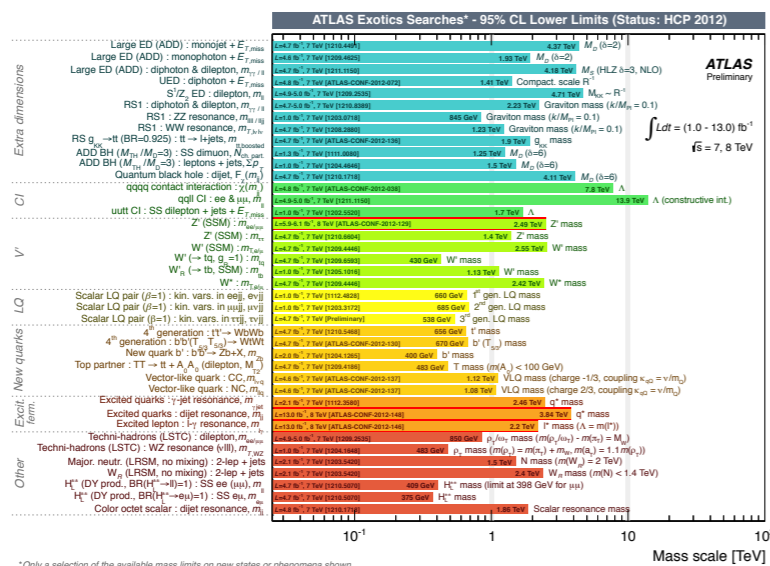


Pomarol et al. '12

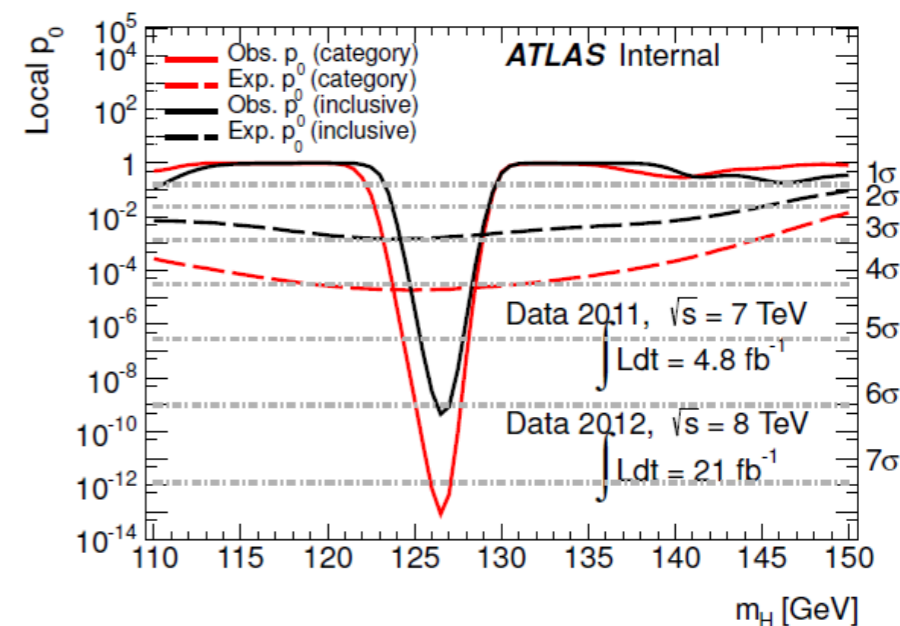


Absence of physics beyond the SM:

Discovery of a 125 GeV Higgs:

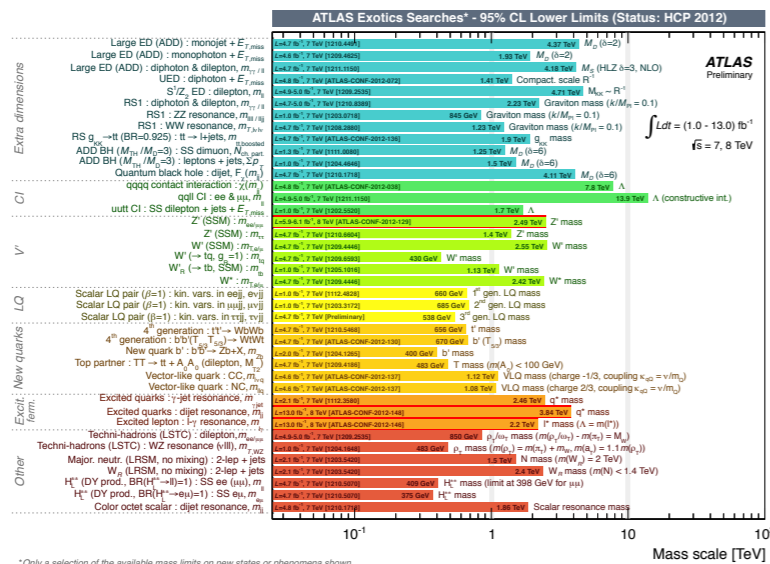


&

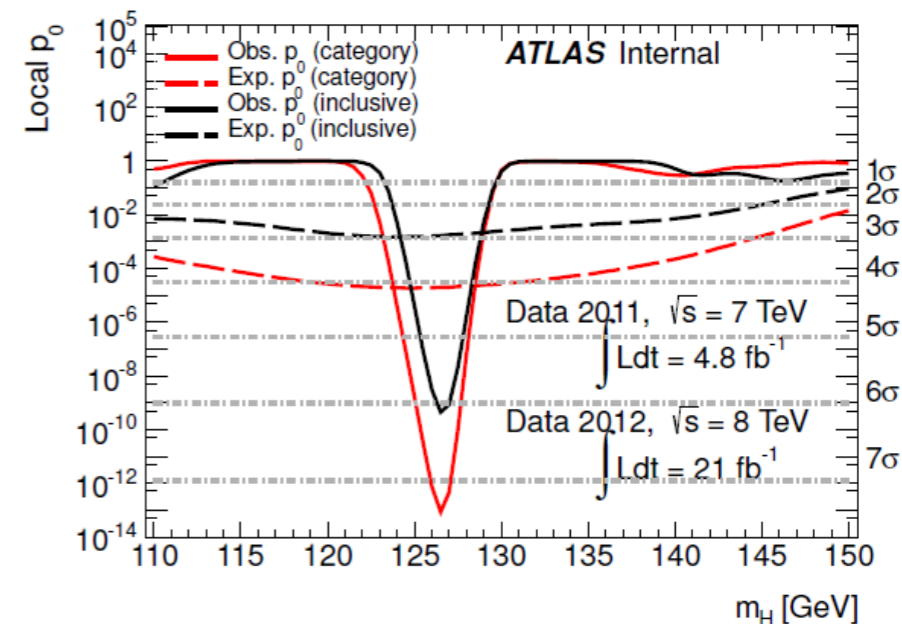


Absence of physics beyond the SM:

Discovery of a 125 GeV Higgs:



&



$$m_h \ll \Lambda_{IR}$$

The Higgs doublet must be a (pseudo-)Goldstone boson of the new strong dynamics

Georgi, Kaplan '84

Arkani-Hamed, Cohen, Katz, Nelson '02

Banks '84

Agashe, Contino, Pomarol '04

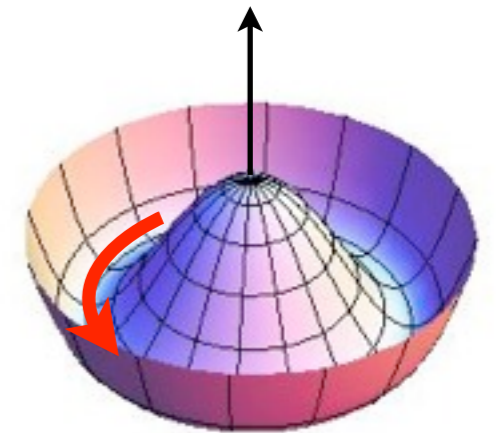
Spontaneous Global Symmetry Breaking

E.g.: $V(\phi) \simeq -m_\rho^2 \phi^2 + g_\rho^2 \phi^4$, $\phi = 5 \in \text{SO}(5)$

$$\langle \phi \rangle = \begin{pmatrix} 0 \\ 0 \\ 0 \\ 0 \\ f \end{pmatrix}, \quad f \sim \frac{m_\rho}{g_\rho} \longrightarrow \text{SO}(5)/\text{SO}(4)$$

4 **GB**'s: $H = \begin{pmatrix} h_1 + ih_2 \\ h + ih_3 \end{pmatrix}$

$$H \rightarrow H + \alpha \longrightarrow V_{tree}(H) = 0$$



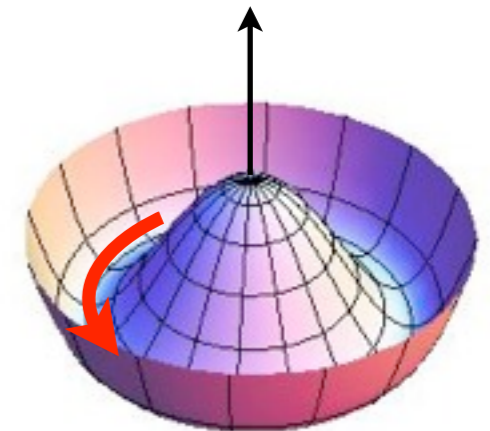
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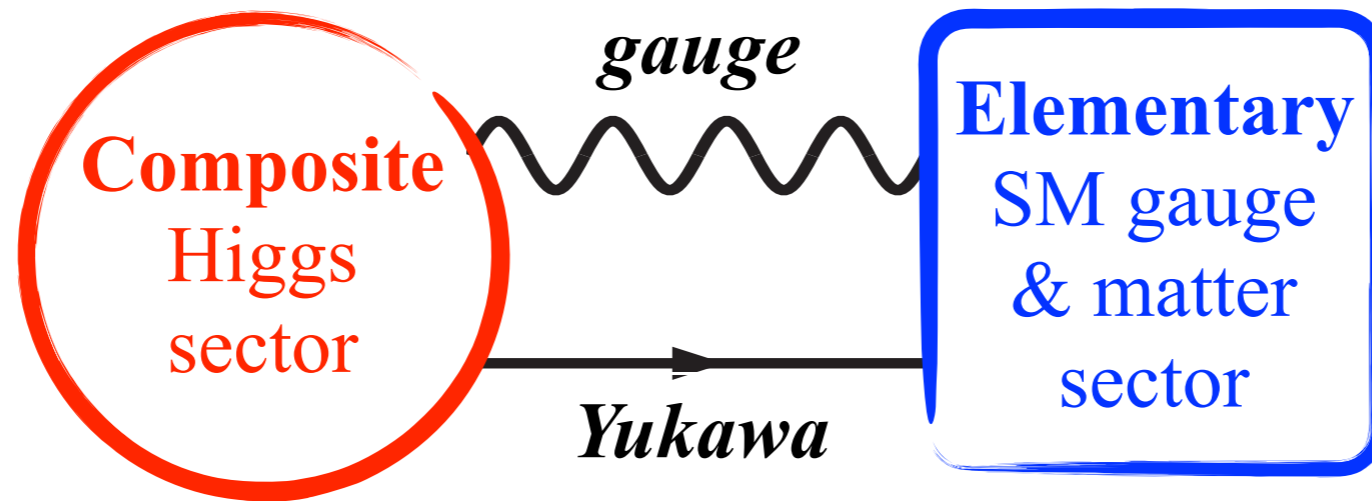
Phenomenological requirements on \mathcal{G}/\mathcal{H} :

i) $\mathcal{G} \supset \text{SU}(2)_L \times \text{U}(1)_Y$ *weakly gauged*

ii) $\mathcal{H} \supset \text{SO}(4) \cong \text{SU}(2)_L \times \text{SU}(2)_R$ *custodial symmetry*

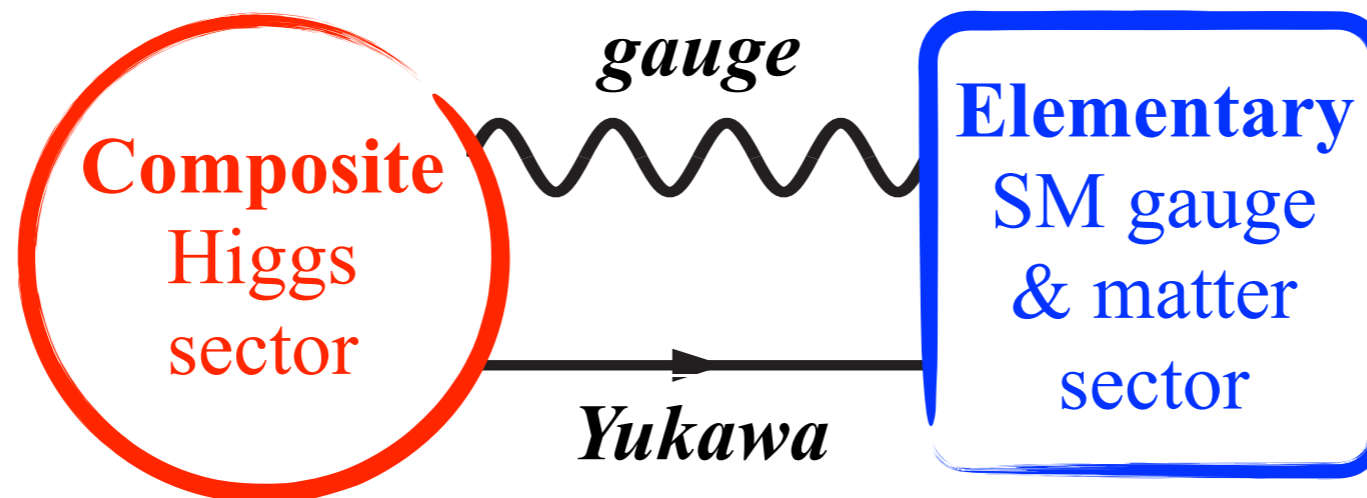
iii) $\mathcal{G}/\mathcal{H} \supset 4 = (\mathbf{2}, \mathbf{2})$ *Higgs doublet*

Explicit Breaking of Global Symmetry & Higgs Potential

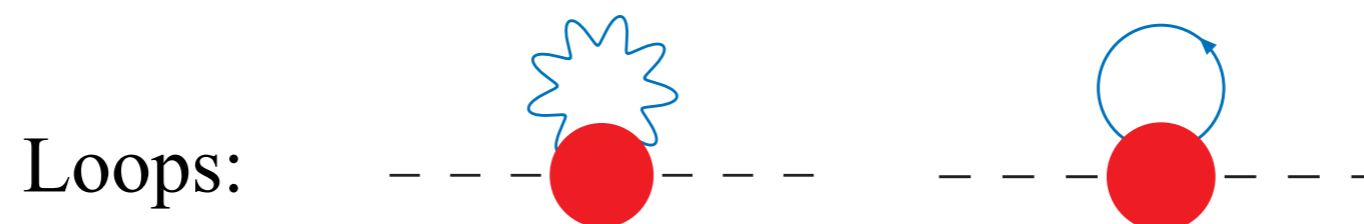


$$\mathcal{L}_{mixing} = g A_\mu \mathcal{J}^\mu + y \bar{\psi} \mathcal{O}_\psi$$

Explicit Breaking of Global Symmetry & Higgs Potential



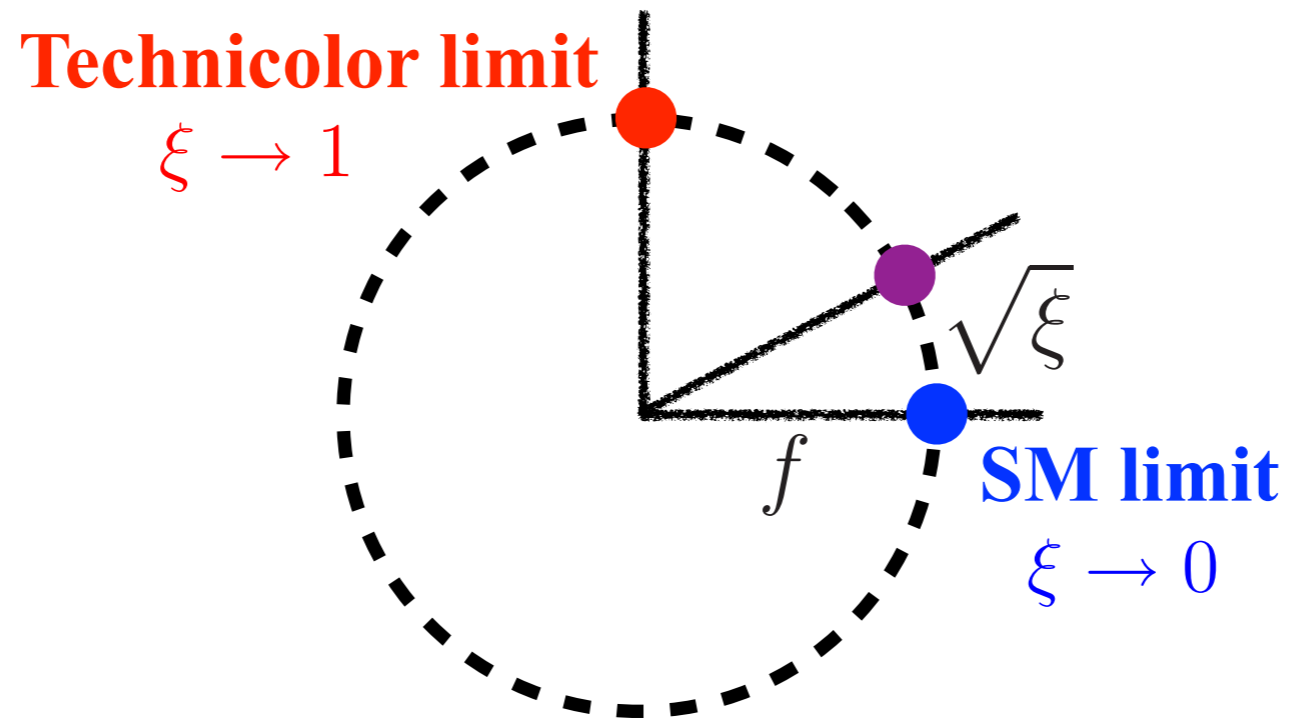
$$\mathcal{L}_{mixing} = g A_\mu \mathcal{J}^\mu + y \bar{\psi} \mathcal{O}_\psi$$



$$V(H) \simeq 0 + \xi \frac{g_{SM}^2}{16\pi^2} m_\rho^2 |H|^2 + \frac{g_{SM}^2}{16\pi^2} g_\rho^2 |H|^4 + O(H^6)$$

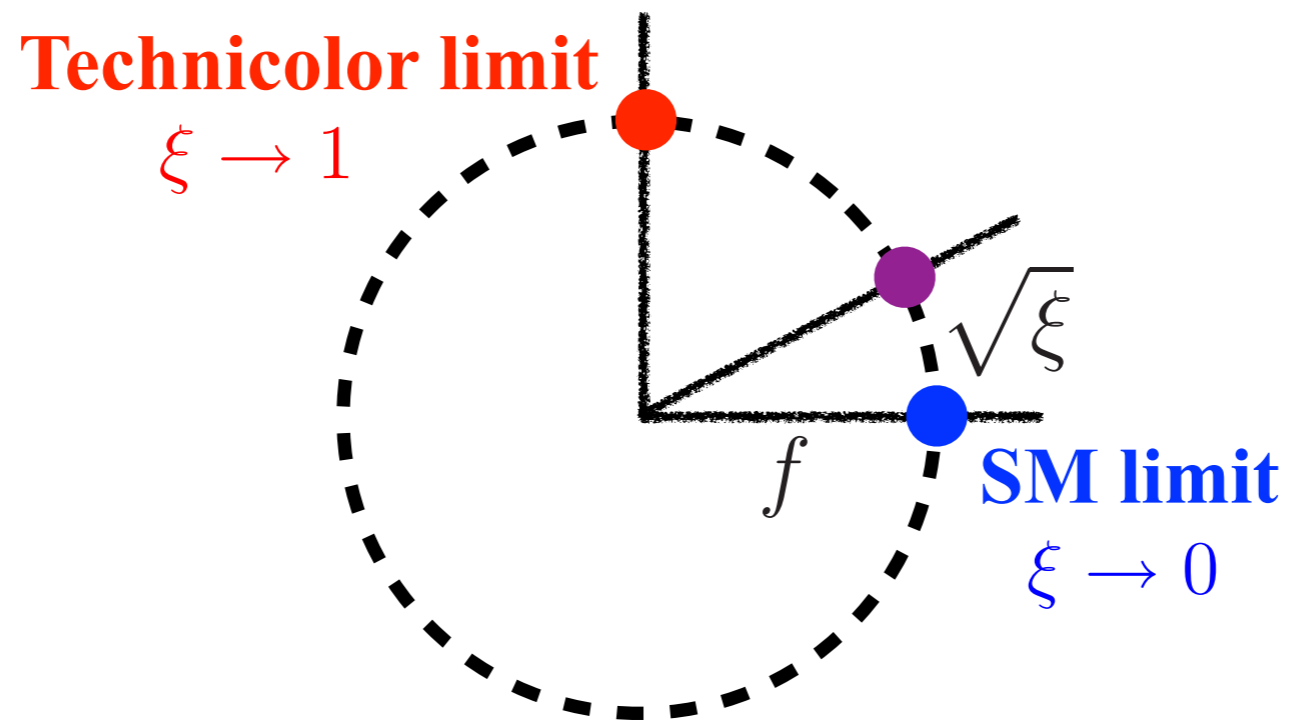
Vacuum Alignment

$$\langle h \rangle \sim \sqrt{\xi} \frac{m_\rho}{g_\rho} = \sqrt{\xi} f \lesssim v = 246 \text{ GeV} \quad \xi = \frac{v^2}{f^2} = O(1)$$



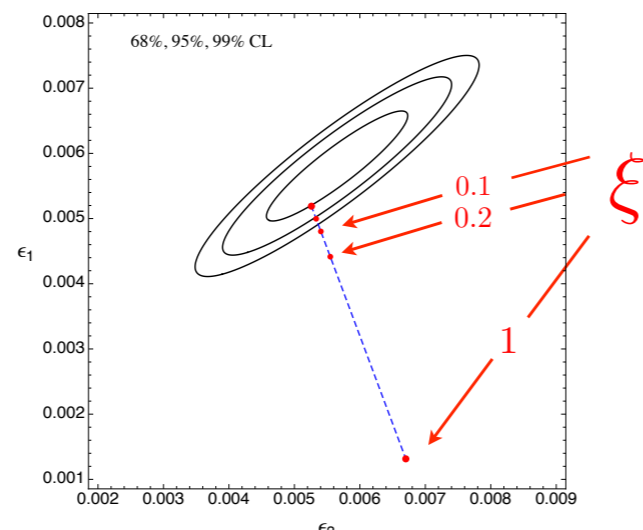
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Electroweak (Higgs) precision observables:

$$\propto \xi \log(\Lambda^2/m_W^2)$$

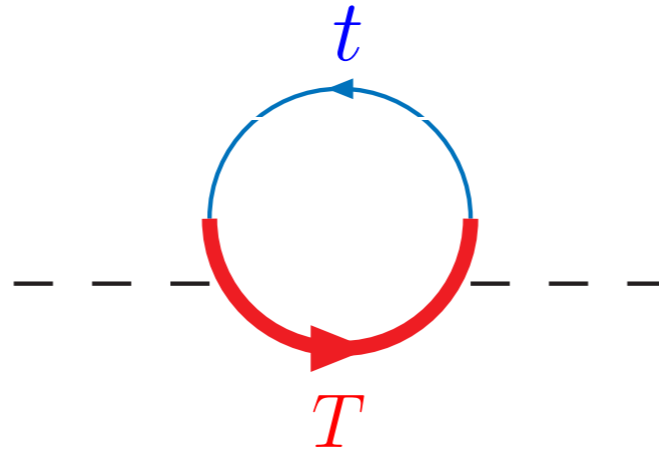


$\xi \lesssim 0.1$

naive tuning

clever structure

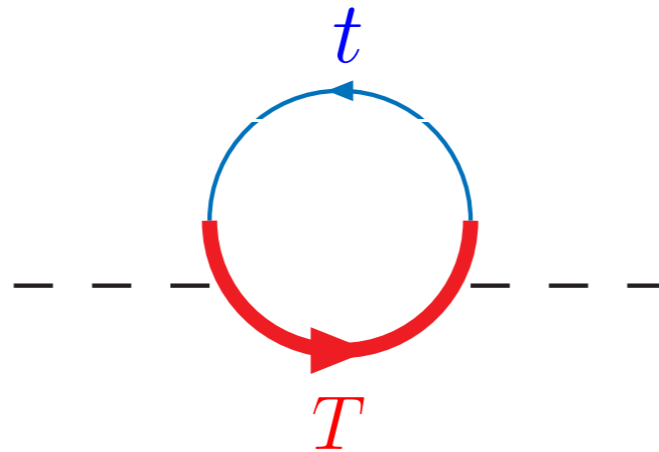
As in SUSY, the top is expected to give the largest contribution:



$$m_h^2 \sim \frac{N_C m_t^2 m_T^2}{\pi^2 f^2} \sim (125 \text{ GeV})^2 \left(\frac{m_T}{700 \text{ GeV}} \right)^2 \left(\frac{500 \text{ GeV}}{f} \right)^2 \sim (125 \text{ GeV})^2 \left(\frac{g_T}{1.5} \right)^2$$

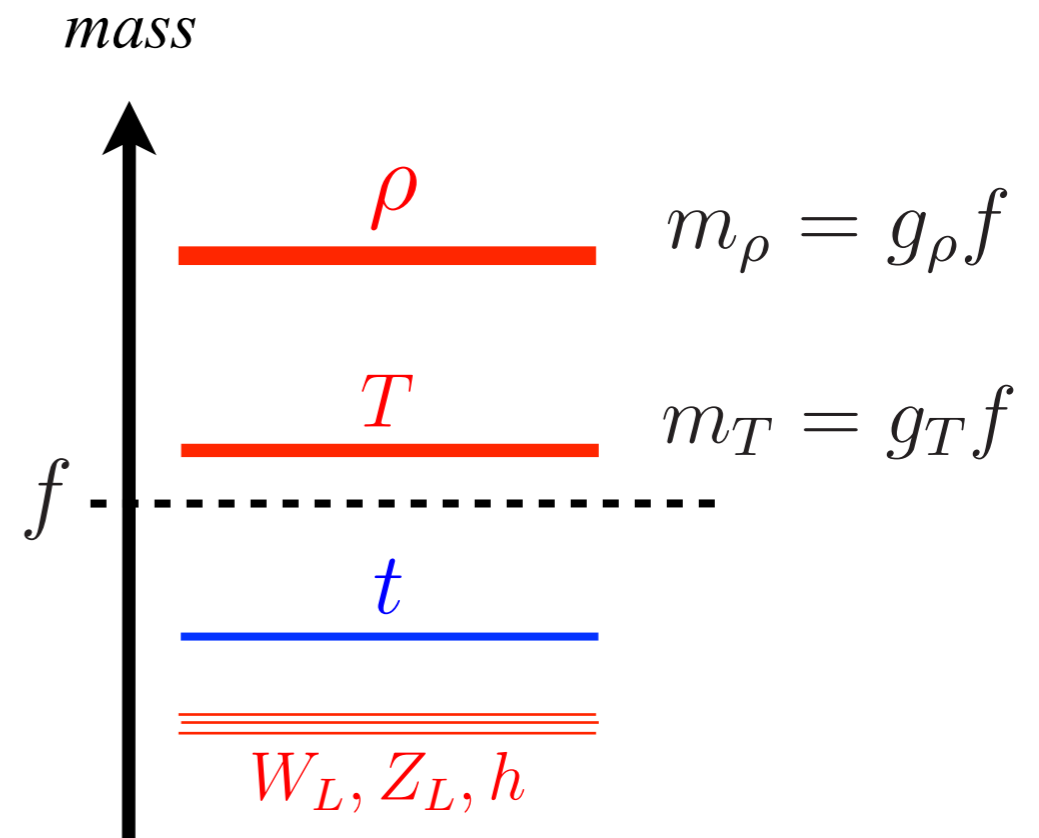
Higgs mass & Light Top-partners

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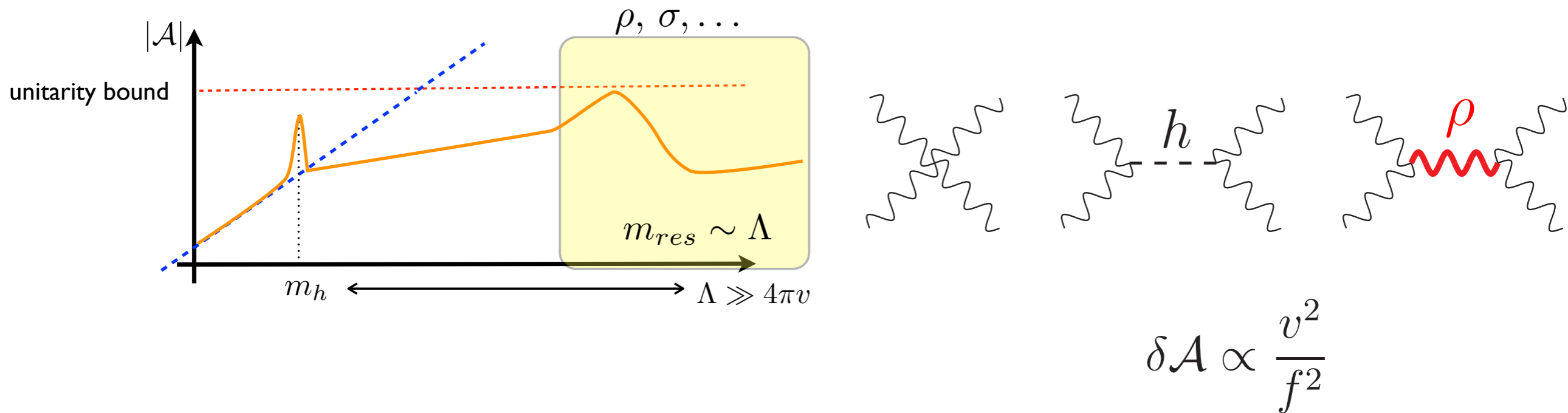


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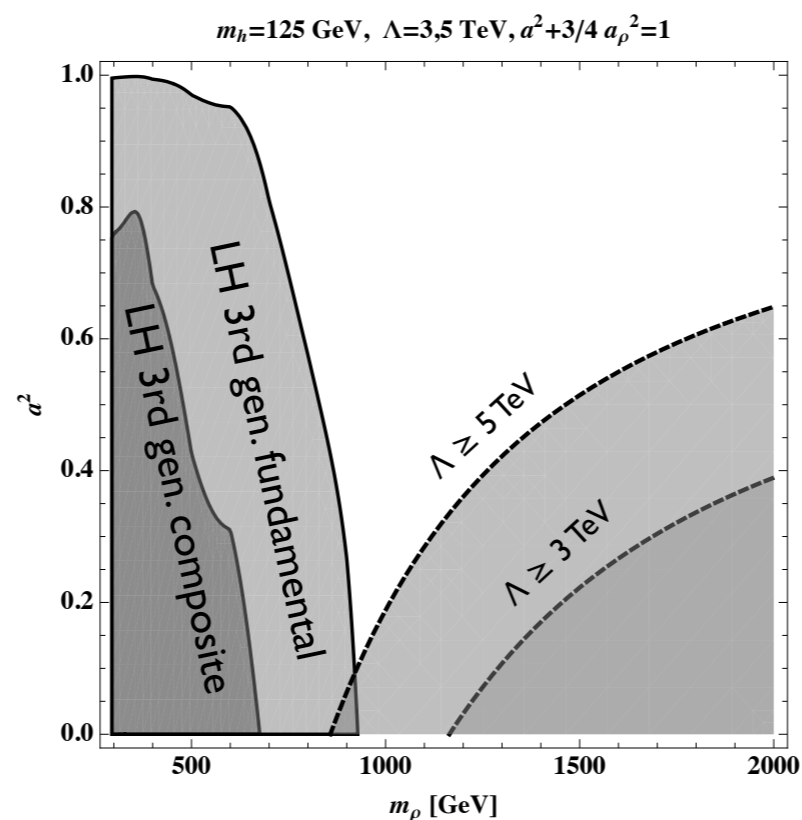
Top-partners must be parametrically lighter
(approximate Chiral sym.)




Expected *subleading* contribution to the potential, but enter ***WW* scattering**:



Bellazzini et al. '12

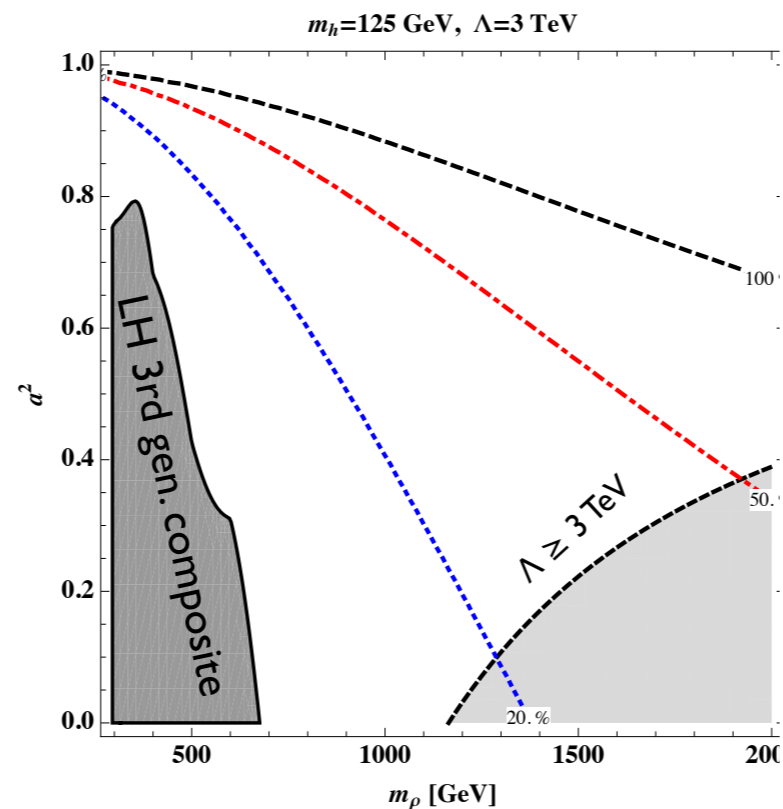


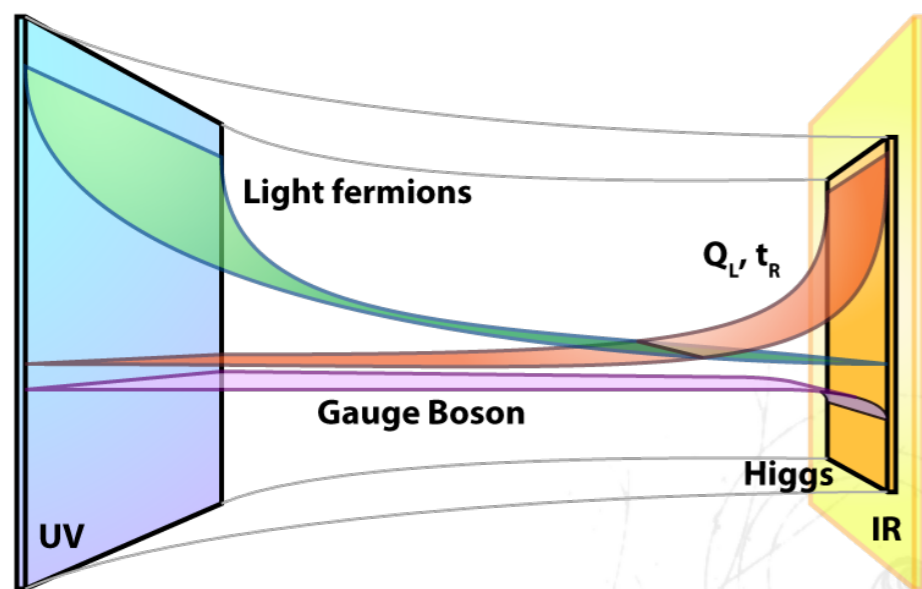
However also contribute to \mathcal{S} -parameter:


$$\hat{\mathcal{S}} \sim \frac{m_W^2}{m_\rho^2}$$

$$\hat{\mathcal{S}} \lesssim 10^{-3} \rightarrow m_\rho \gtrsim 2.5 \text{ TeV}$$

Bellazzini et al. '12



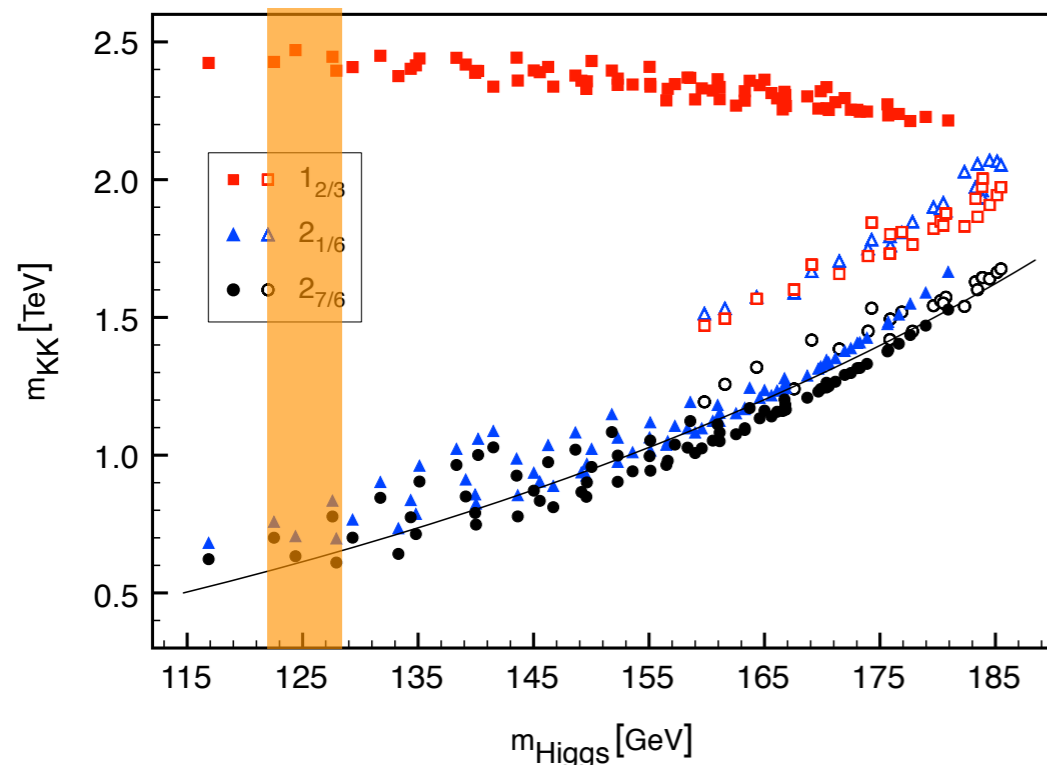


$$\mathcal{L}_{mixing} = y \bar{\psi} \mathcal{O}_\psi$$

$$d[\mathcal{O}_\psi] \simeq 2 + M_\psi \longrightarrow y(\mu < f) \simeq y(\mu_0) \left(\frac{f}{\mu_0} \right)^{M_\psi - \frac{1}{2}}$$

5D mass: $M_\psi > 1/2$ irrelevant
 $|M_\psi| < 1/2$ relevant

Contino, DaRold, Pomarol '07

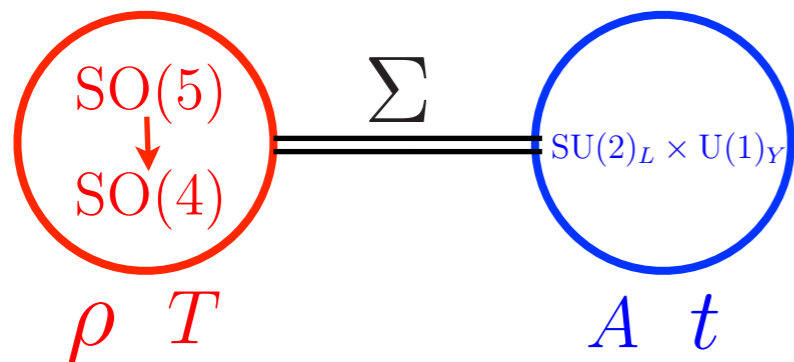


$M_\psi \rightarrow -1/2$
 strongly coupled limit \longrightarrow $d[\mathcal{O}_\psi] = 3/2$
 free field

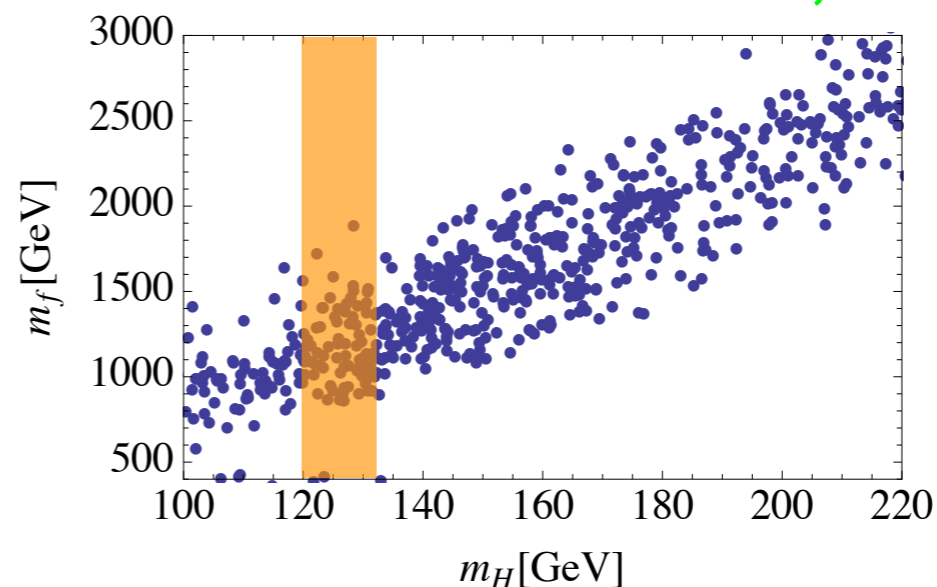
Light top-partners byproduct of composite top (IR localized)

Top-partners from Desconstruction or “Weinberg Sum Rules”

Deconstruction:

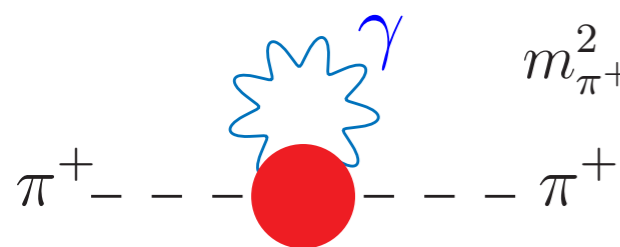


Redi, Tesi '12



“Weinberg Sum Rules”:

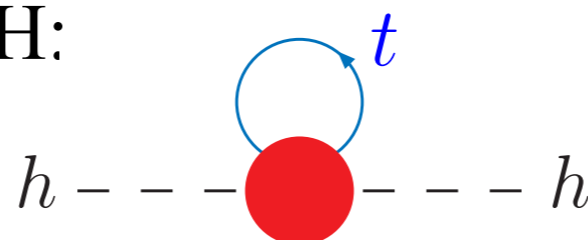
as in QCD:



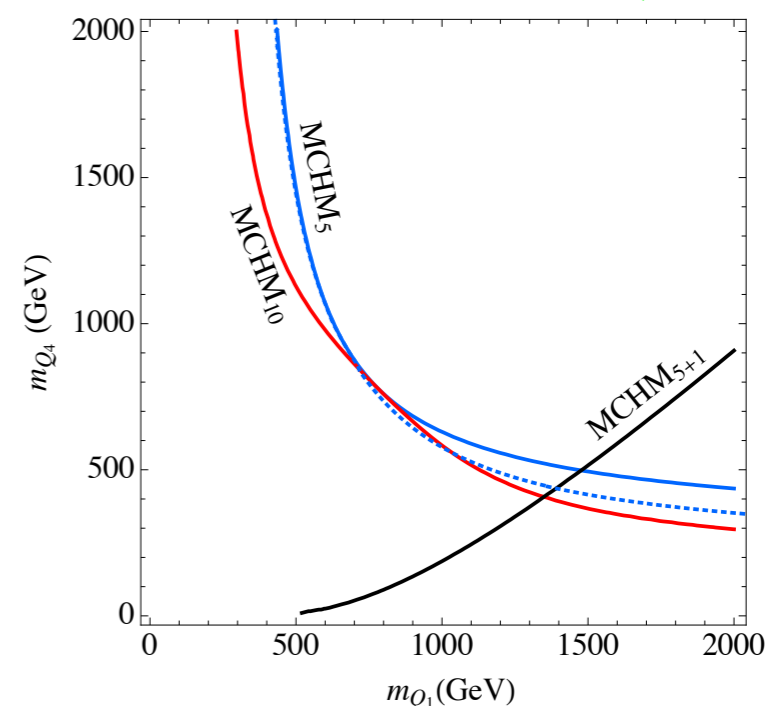
$$m_{\pi^+}^2 - m_{\pi^0}^2 \simeq \frac{3\alpha}{2\pi} m_\rho^2 \log 2 \simeq (37 \text{ MeV})^2$$

Exp.: (35 MeV)²

in CH:



Pomarol, Riva '12



Higgs mass & Tuning: Survey of Models

$$V(h) = \frac{3y_t^2 m_T^2}{16\pi^2} (ah^2 + bh^4/f^2 + \dots)$$

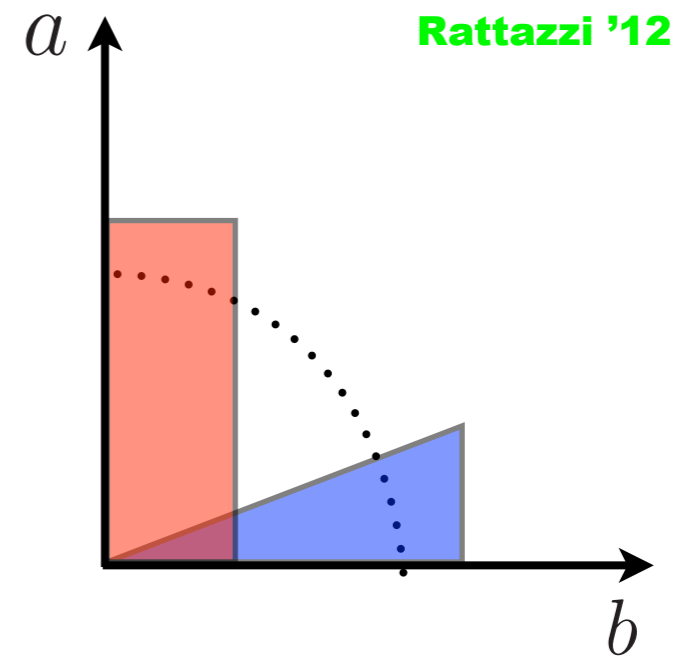
Instead of $a, b \sim O(1)$:

v/f tuning

$$a \lesssim \left(\frac{500 \text{ GeV}}{m_T} \right)^2$$

m_h tuning

$$b \lesssim \left(\frac{2}{g_T} \right)^2$$



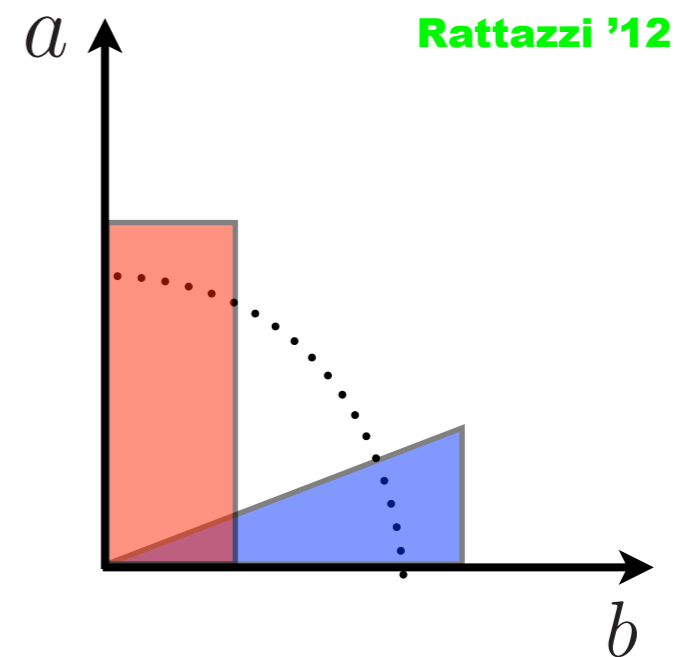
Higgs mass & Tuning: Survey of Models

$$V(h) = \frac{3y_t^2 m_T^2}{16\pi^2} (ah^2 + bh^4/f^2 + \dots)$$

Instead of $a, b \sim O(1)$:

$$a \lesssim \left(\frac{500 \text{ GeV}}{m_T} \right)^2 \quad \text{v/f tuning}$$

$$b \lesssim \left(\frac{2}{g_T} \right)^2 \quad m_h \text{ tuning}$$

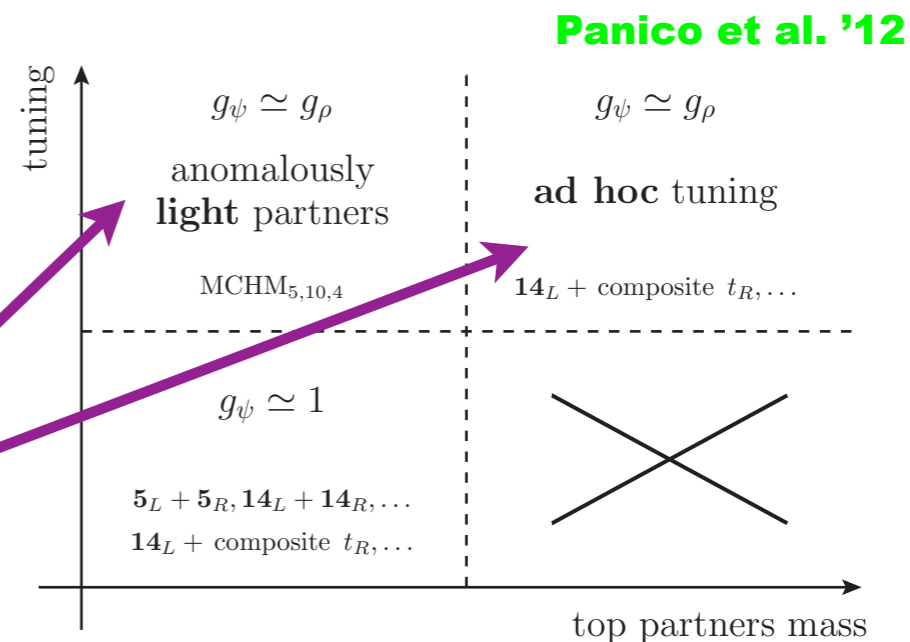


but there are unknown factors and *model dependence*:

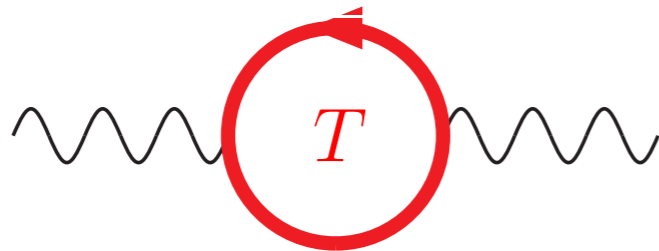
$$\mathcal{L}_{mixing} = y \bar{\psi} \mathcal{O}_\psi$$

$$\mathbf{r}(\mathcal{O}_\psi) = \mathbf{5}_L + \mathbf{5}_R \quad a \sim O(y_t^2/g_T^2), \quad b \sim O(y_t^4/g_T^4)$$

$$\mathbf{r}(\mathcal{O}_\psi) = \mathbf{14}_L + \mathbf{1}_R \quad a, b \sim O(y_t^2/g_T^2)$$

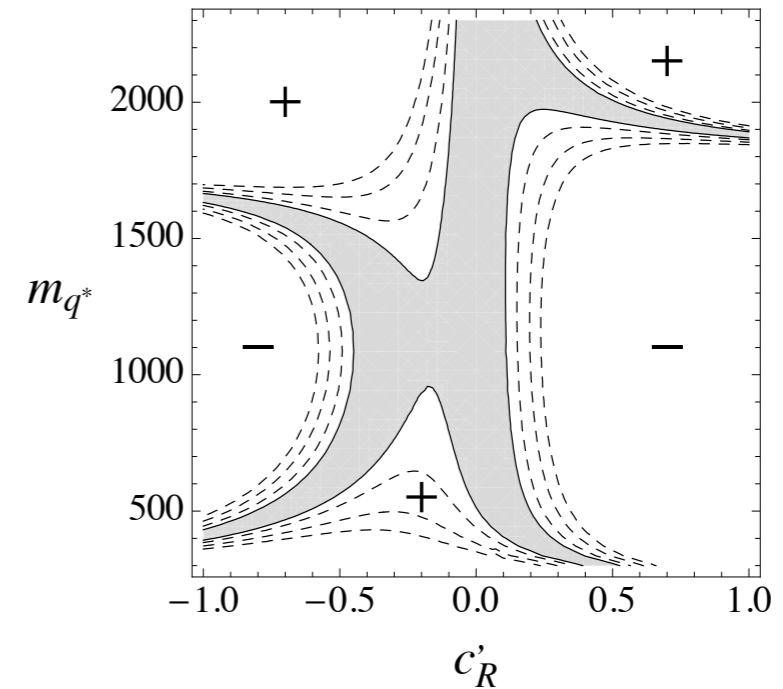


Electroweak Precision Tests:



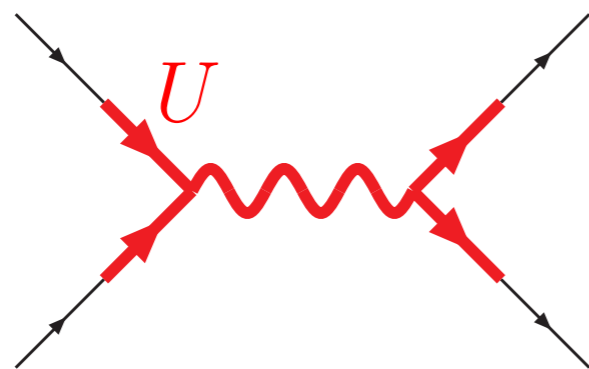
$$\Delta\hat{T} \gtrsim 10^{-3} \longrightarrow m_T \lesssim 2 \text{ TeV}$$

Pomarol, JS '08



Flavor:

$$\epsilon_K, B_{d,s} - \bar{B}_{d,s}, \dots$$



$$m_T \sim m_C \sim m_U$$

Barbieri et al. '12

	doublet	triplet	bidoublet
\mathbb{A}	4.9	1.7	1.2*
$U(3)_{LC}^3$	4.6	5.3	4.3
$U(3)_{RC}^3$	-	-	3.3
$U(2)_{LC}^3$	4.9	0.6	0.6
$U(2)_{RC}^3$	-	-	1.1*

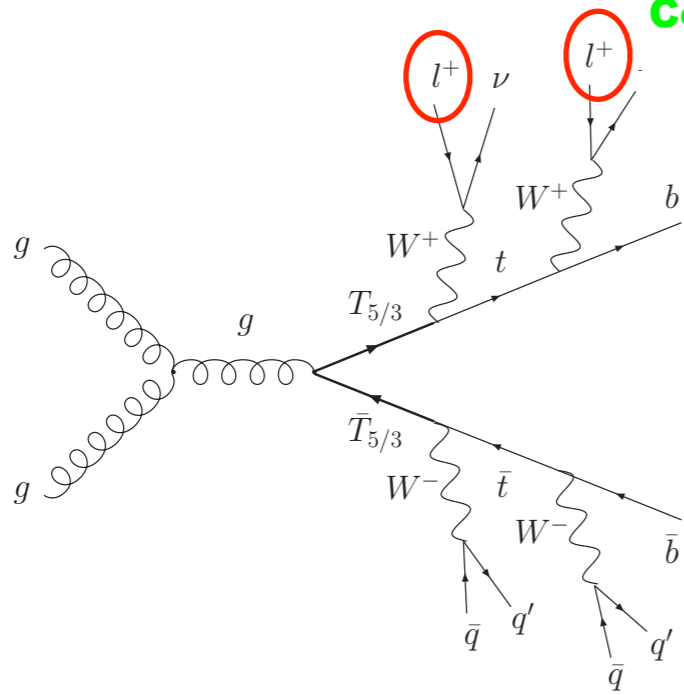
$SU(2)_L \times SU(2)_R$

	Q	T
Case (a)	$(\mathbf{2}, \mathbf{2})_{2/3}$	$(\mathbf{1}, \mathbf{1})_{2/3}$
Case (b)	$(\mathbf{2}, \mathbf{2})_{2/3}$	$(\mathbf{1}, \mathbf{3})_{2/3} + (\mathbf{3}, \mathbf{1})_{2/3}$

$q = +\frac{5}{3}, +\frac{2}{3}$ ← → $q = +\frac{5}{3}, +\frac{2}{3}, -\frac{1}{3}$

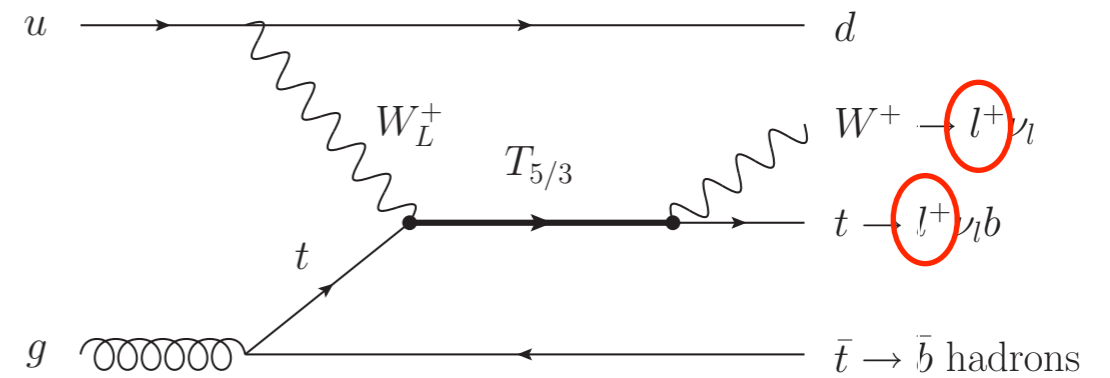
Double production

Contino, Servant '08



Single production

Mrazek, Wulzer '10



same sign dileptons!

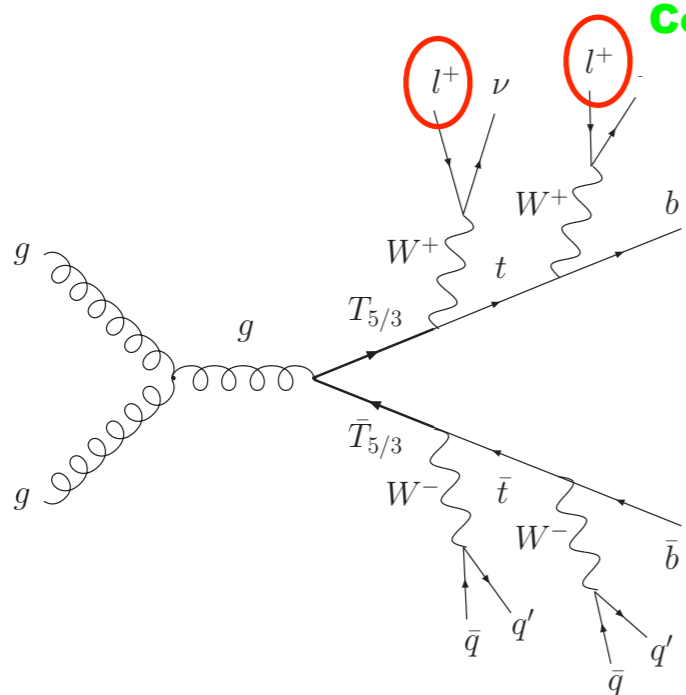
$SU(2)_L \times SU(2)_R$

	Q	T
Case (a)	$(2, 2)_{2/3}$	$(1, 1)_{2/3}$
Case (b)	$(2, 2)_{2/3}$	$(1, 3)_{2/3} + (3, 1)_{2/3}$

$q = +\frac{5}{3}, +\frac{2}{3}$ ← (left arrow) (right arrow) $q = +\frac{5}{3}, +\frac{2}{3}, -\frac{1}{3}$

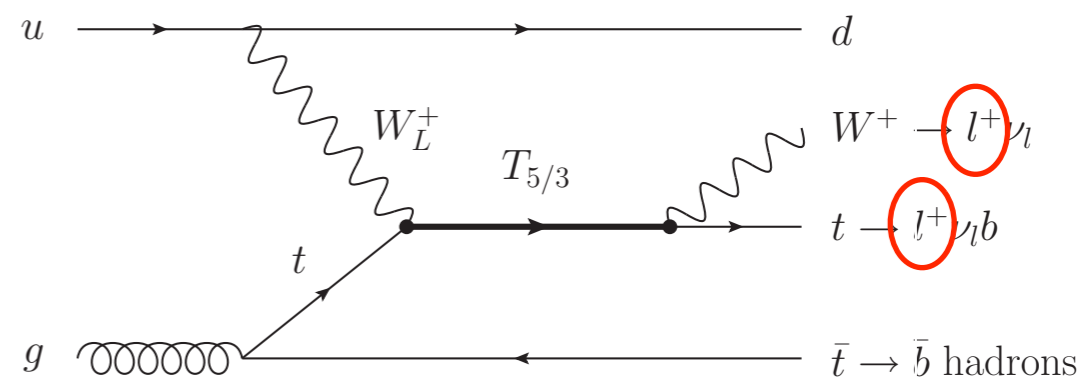
Double production

Contino, Servant '08

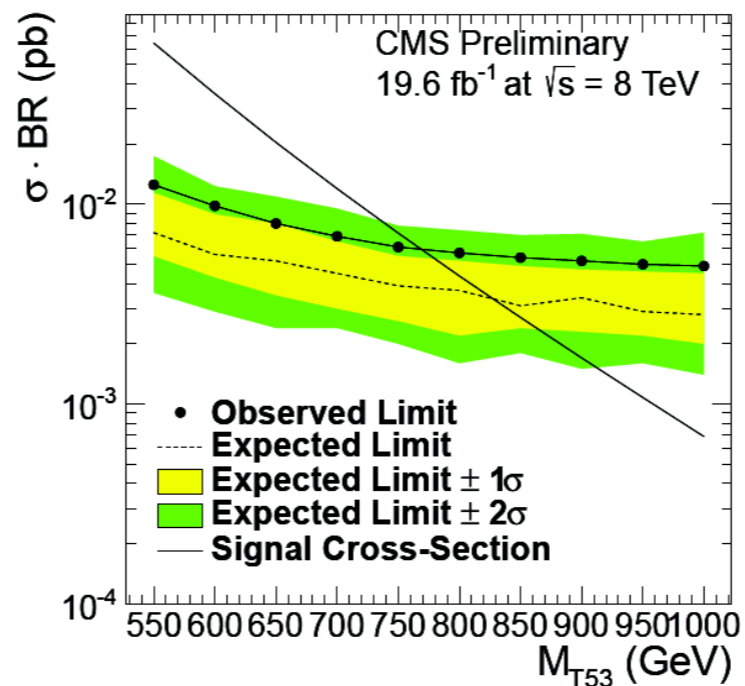


Single production

Mrazek, Wulzer '10



same sign dileptons!



G	H	N_G	NGBs rep. $[H] = \text{rep.}[SU(2) \times SU(2)]$
SO(5)	SO(4)	4	$4 = (\mathbf{2}, \mathbf{2})$
SO(6)	SO(5)	5	$5 = (\mathbf{1}, \mathbf{1}) + (\mathbf{2}, \mathbf{2})$
SO(6)	SO(4) \times SO(2)	8	$4_{+2} + \bar{4}_{-2} = 2 \times (\mathbf{2}, \mathbf{2})$
SO(7)	SO(6)	6	$6 = 2 \times (\mathbf{1}, \mathbf{1}) + (\mathbf{2}, \mathbf{2})$
SO(7)	G_2	7	$7 = (\mathbf{1}, \mathbf{3}) + (\mathbf{2}, \mathbf{2})$
SO(7)	SO(5) \times SO(2)	10	$10_0 = (\mathbf{3}, \mathbf{1}) + (\mathbf{1}, \mathbf{3}) + (\mathbf{2}, \mathbf{2})$
SO(7)	$[SO(3)]^3$	12	$(\mathbf{2}, \mathbf{2}, \mathbf{3}) = 3 \times (\mathbf{2}, \mathbf{2})$
Sp(6)	Sp(4) \times SU(2)	8	$(\mathbf{4}, \mathbf{2}) = 2 \times (\mathbf{2}, \mathbf{2}), (\mathbf{2}, \mathbf{2}) + 2 \times (\mathbf{2}, \mathbf{1})$
SU(5)	SU(4) \times U(1)	8	$4_{-5} + \bar{4}_{+5} = 2 \times (\mathbf{2}, \mathbf{2})$
SU(5)	SO(5)	14	$14 = (\mathbf{3}, \mathbf{3}) + (\mathbf{2}, \mathbf{2}) + (\mathbf{1}, \mathbf{1})$

Minimal Composite Higgs Model

Agashe, Contino, Pomarol '04

G	H	N_G	NGBs rep. $[H] = \text{rep.}[SU(2) \times SU(2)]$
SO(5)	SO(4)	4	$4 = (\mathbf{2}, \mathbf{2})$
SO(6)	SO(5)	5	$5 = (\mathbf{1}, \mathbf{1}) + (\mathbf{2}, \mathbf{2})$
SO(6)	SO(4) \times SO(2)	8	$4_{+2} + \bar{4}_{-2} = 2 \times (\mathbf{2}, \mathbf{2})$
SO(7)	SO(6)	6	$6 = 2 \times (\mathbf{1}, \mathbf{1}) + (\mathbf{2}, \mathbf{2})$
SO(7)	G_2	7	$7 = (\mathbf{1}, \mathbf{3}) + (\mathbf{2}, \mathbf{2})$
SO(7)	SO(5) \times SO(2)	10	$10_0 = (\mathbf{3}, \mathbf{1}) + (\mathbf{1}, \mathbf{3}) + (\mathbf{2}, \mathbf{2})$
SO(7)	$[SO(3)]^3$	12	$(\mathbf{2}, \mathbf{2}, \mathbf{3}) = 3 \times (\mathbf{2}, \mathbf{2})$
Sp(6)	Sp(4) \times SU(2)	8	$(\mathbf{4}, \mathbf{2}) = 2 \times (\mathbf{2}, \mathbf{2}), (\mathbf{2}, \mathbf{2}) + 2 \times (\mathbf{2}, \mathbf{1})$
SU(5)	SU(4) \times U(1)	8	$4_{-5} + \bar{4}_{+5} = 2 \times (\mathbf{2}, \mathbf{2})$
SU(5)	SO(5)	14	$14 = (\mathbf{3}, \mathbf{3}) + (\mathbf{2}, \mathbf{2}) + (\mathbf{1}, \mathbf{1})$

Beyond the Minimal Composite Higgs Model

Gripaios et al. '09

Galloway et al. '10

Interesting fact: Minimal coset from constituent fermions

$$\langle \Psi_a \Psi_b \rangle \cong SU(4)/Sp(4) \longrightarrow 5 = 4 + 1 = (\mathbf{2}, \mathbf{2}) + (\mathbf{1}, \mathbf{1})$$

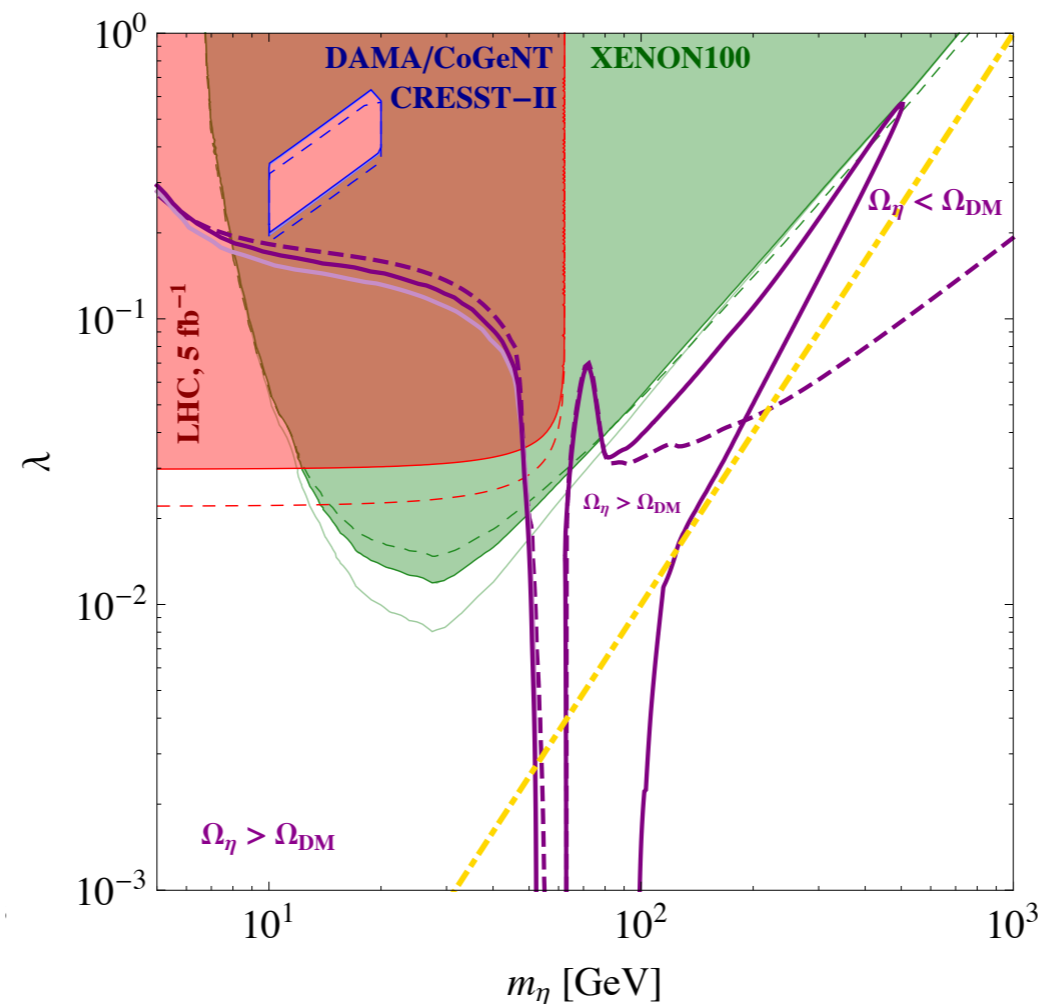
extra singlet!

$$\text{SO}(6)/\text{SO}(5) \longrightarrow H + \eta$$

- a) Mass of singlet very model dependent: $\text{SO}(2)$ explicit breaking?
- b) Discrete symmetry $\eta \longrightarrow -\eta$ might be an exact symmetry.

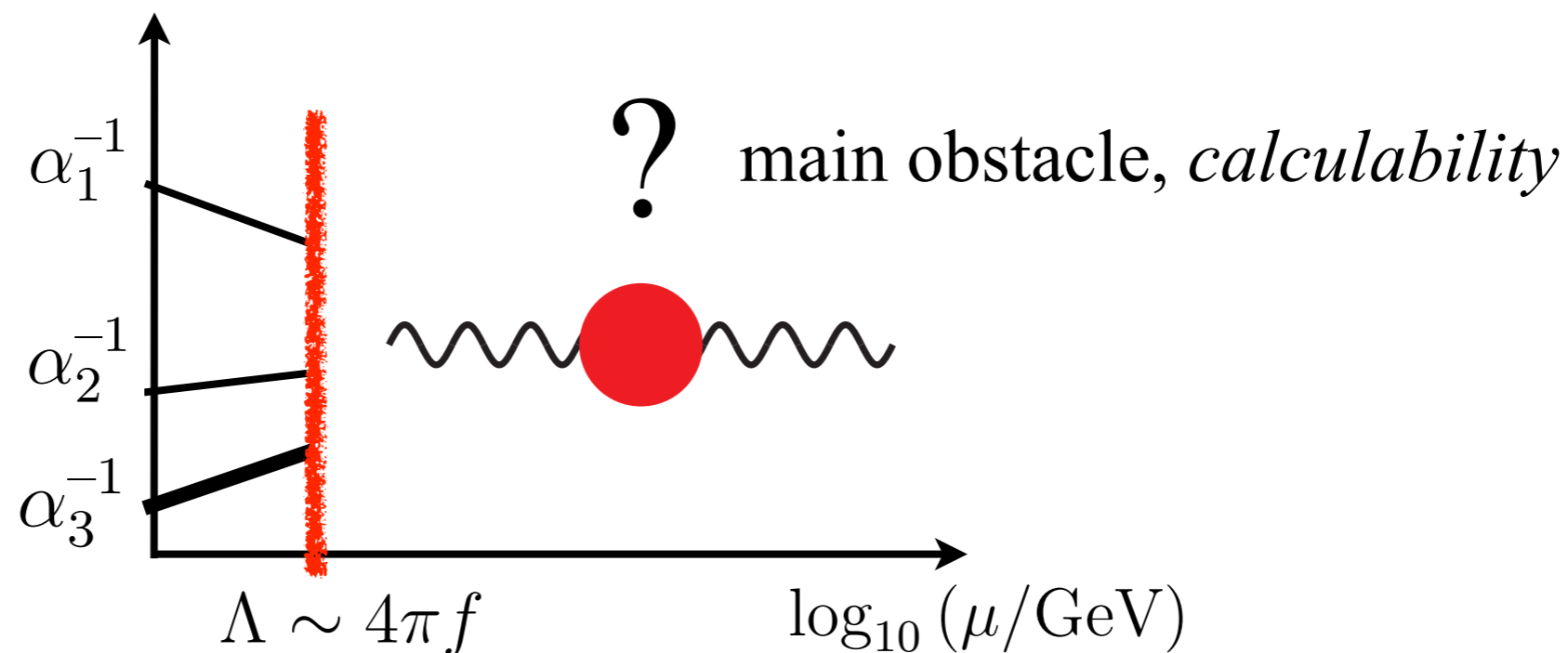
Singlet could be DM!

Frigerio et al. '12



G	H	N_G	NGBs rep. $[H] = \text{rep.}[SU(2) \times SU(2)]$
SO(5)	SO(4)	4	$4 = (\mathbf{2}, \mathbf{2})$
SO(6)	SO(5)	5	$5 = (\mathbf{1}, \mathbf{1}) + (\mathbf{2}, \mathbf{2})$
SO(6)	SO(4) \times SO(2)	8	$4_{+2} + \bar{4}_{-2} = 2 \times (\mathbf{2}, \mathbf{2})$
SO(7)	SO(6)	6	$6 = 2 \times (\mathbf{1}, \mathbf{1}) + (\mathbf{2}, \mathbf{2})$
SO(7)	G_2	7	$7 = (\mathbf{1}, \mathbf{3}) + (\mathbf{2}, \mathbf{2})$
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SU(5)	SU(4) \times U(1)	8	$4_{-5} + \bar{4}_{+5} = 2 \times (\mathbf{2}, \mathbf{2})$
SU(5)	SO(5)	14	$14 = (\mathbf{3}, \mathbf{3}) + (\mathbf{2}, \mathbf{2}) + (\mathbf{1}, \mathbf{1})$

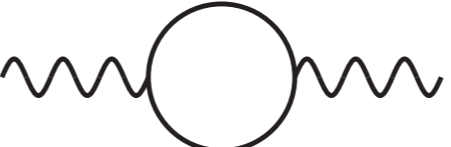
many more...



Simplest Solution:

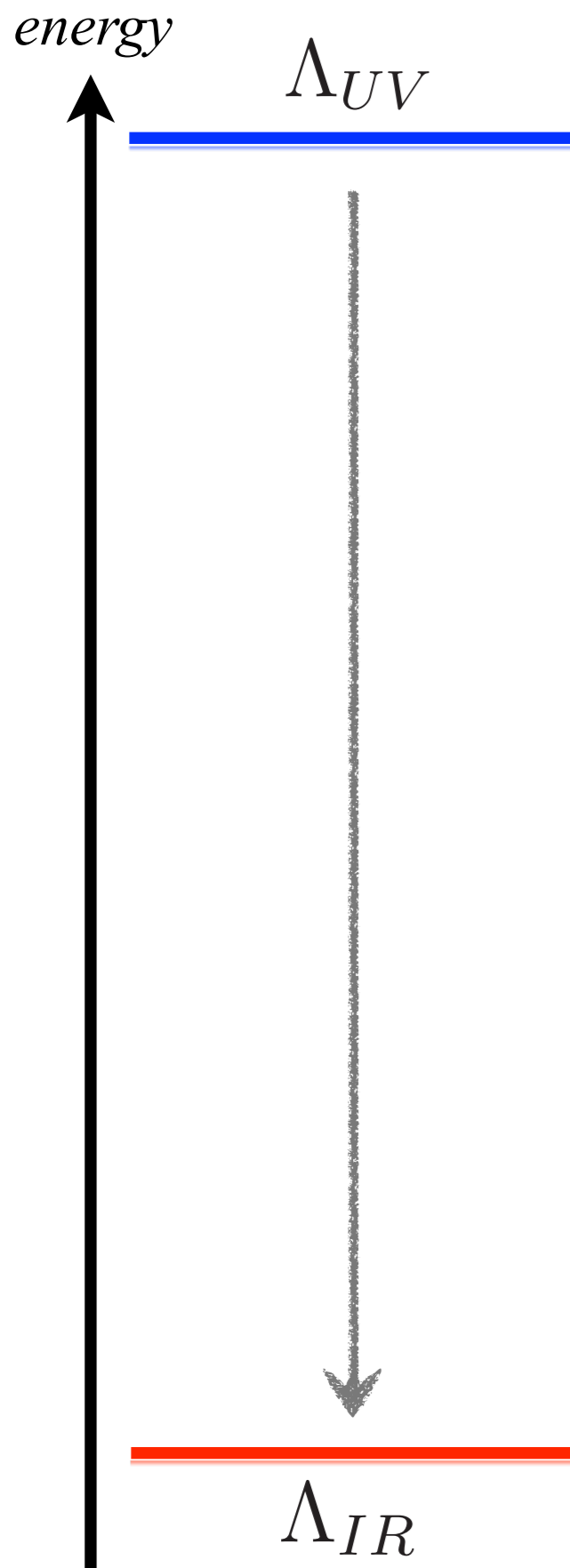
Agashe, Contino, Sundrum '05
 Frigerio, JS, Varagnolo '12

a) $\text{SO}(11)/\text{SO}(10) \rightarrow$  $\frac{d\alpha_i^{-1}}{d\ln\mu} = -\frac{b^{\text{strong}}}{2\pi}$

b) Composite R-handed top \rightarrow  $\{\text{SM}\} - h - t_R + T's$

$$R \equiv (b_1 - b_2)/(b_2 - b_3) \simeq \mathbf{1.45}$$

Exp.: 1.395



Scale Invariant Sector (CFT)

$$\Lambda_{UV} \gg \Lambda_{IR}$$

$$x \rightarrow e^\alpha x, \quad \Phi(x) \rightarrow e^{d_\Phi \alpha} \Phi(e^\alpha x)$$

$$\mathcal{S}_{CFT} = \sum_{\mathcal{O}} \int d^4 x \mathcal{O}, \quad d_{\mathcal{O}} = 4$$

Spontaneous Breaking of Scale Invariance

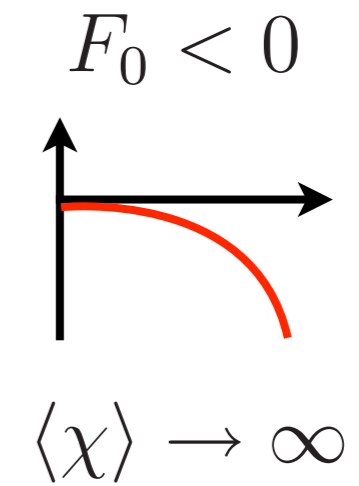
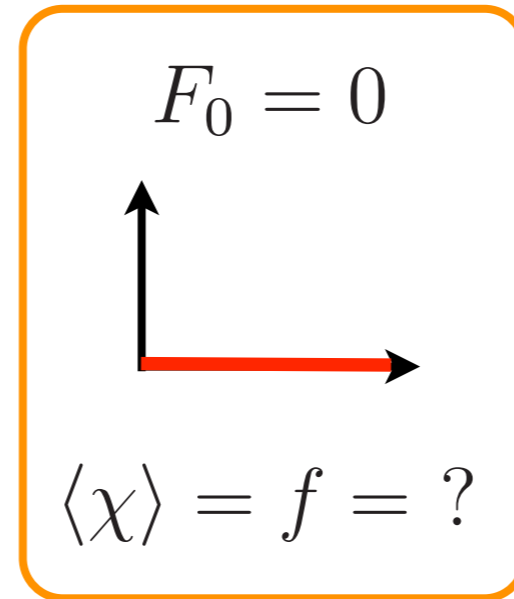
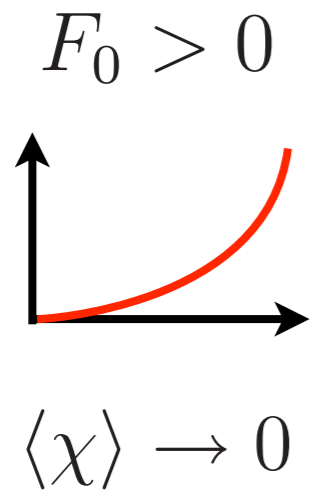
$$\langle \Phi \rangle = f^{d_\Phi}, \quad \Lambda_{IR} \sim 4\pi f$$

1 GB (enough), $SO(4, 2)/SO(3, 1)$

$$\chi \equiv f e^{\sigma/f} \rightarrow e^\alpha \chi$$

Explicit Breaking of Scaling Symmetry & Dilaton Potential

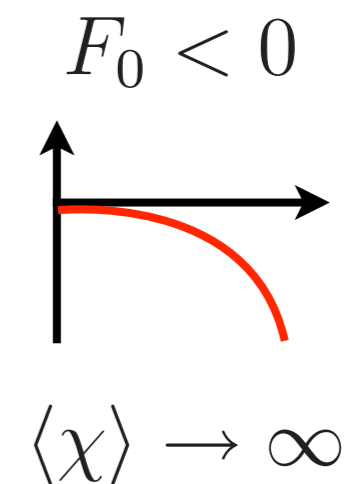
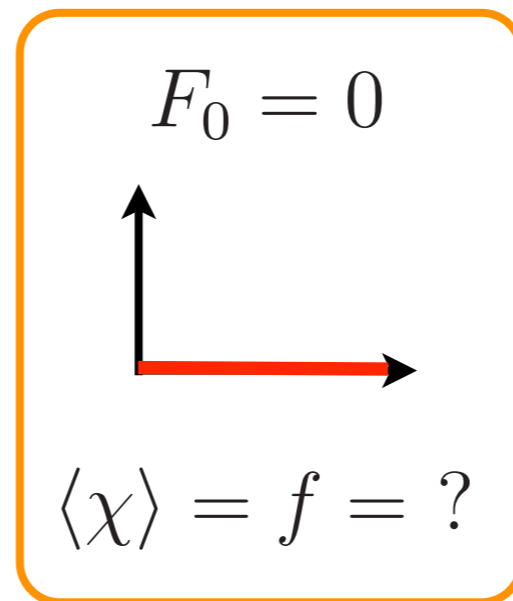
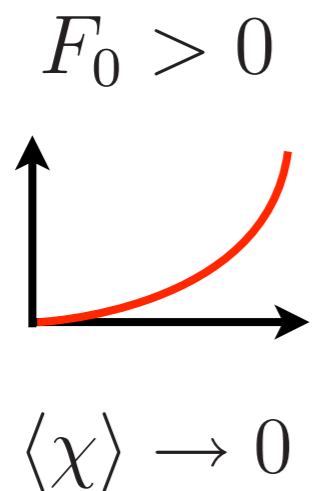
$$V(\chi) = F_0 \chi^4$$



Need “vacuum alignment”

Explicit Breaking of Scaling Symmetry & Dilaton Potential

$$V(\chi) = F_0 \chi^4$$



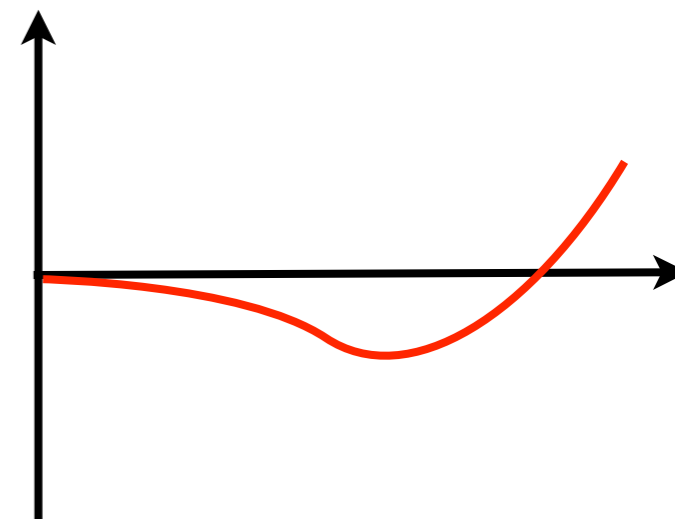
Need “vacuum alignment”

Add explicit breaking

$$\mathcal{L} \supset \lambda \mathcal{O}, \quad [\mathcal{O}] = 4 - \epsilon$$

$$\frac{d\lambda}{d \log \mu} = \beta(\lambda) \neq 0$$

$$\rightarrow V(\chi) = \chi^4 F(\lambda(\chi))$$



F_0 still matters for the **dilaton mass**

F at the minimum:
$$F(\lambda) = F_0 + \sum_n a_n \lambda(f)^n$$

Minimization condition:
$$V' = f^3 [4F(\lambda(f)) + \beta F'(\lambda(f))] = 0$$

Dilaton mass:
$$m_d^2 \simeq 4f^2 \beta F'(\lambda(f))$$

Dilaton mass & Tuning

F_0 still matters for the **dilaton mass**

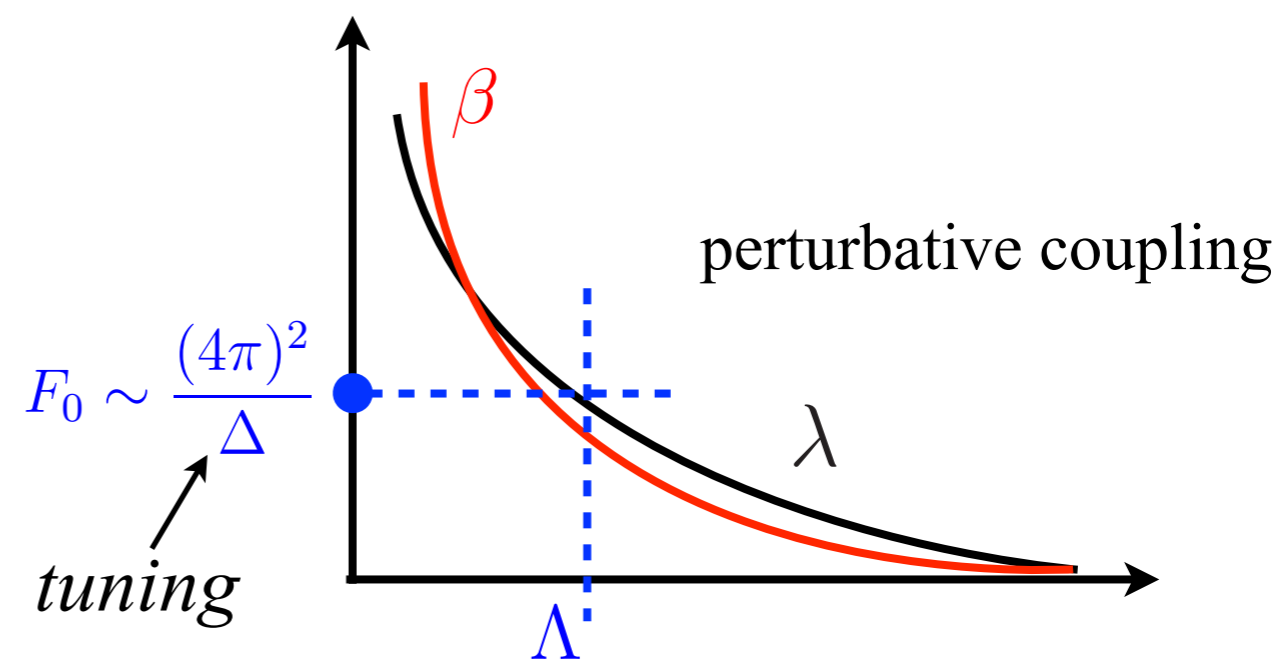
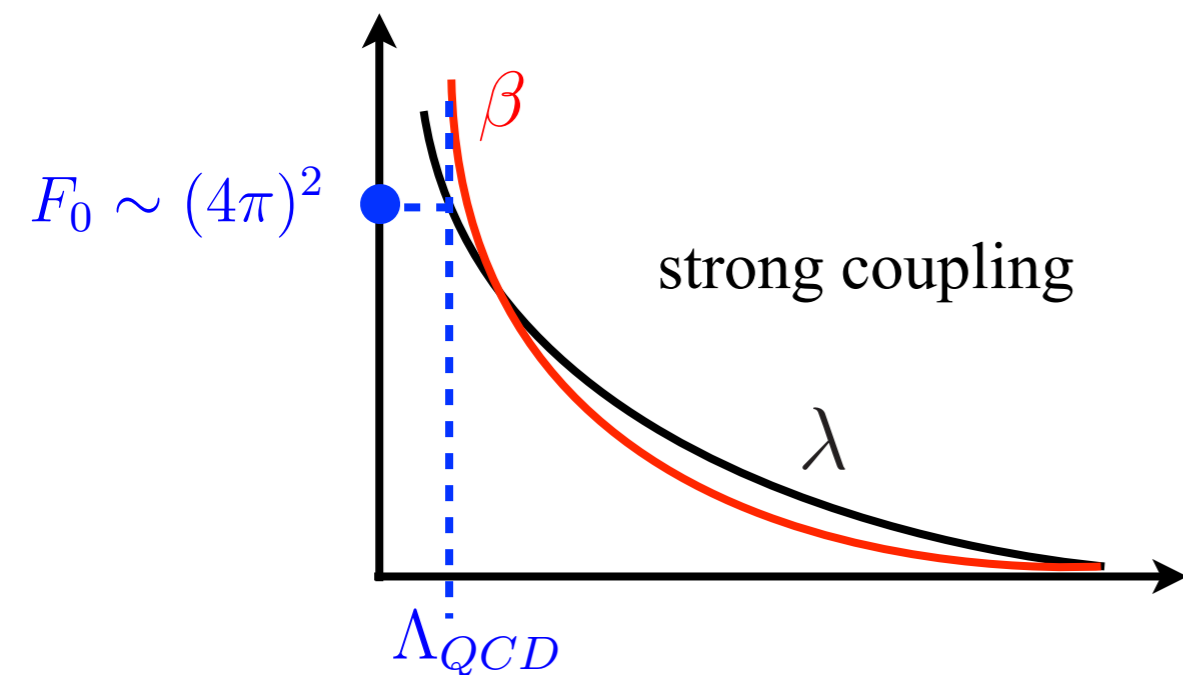
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$$F(\lambda) = F_0 + \sum_n a_n \lambda(f)^n$$

Minimization condition:
$$V' = f^3 [4F(\lambda(f)) + \beta F'(\lambda(f))] = 0$$

Dilaton mass:
$$m_d^2 \simeq 4f^2 \beta F'(\lambda(f))$$

QCD

“tuned” QCD



$$\Delta \gtrsim 2\Lambda/m_{dil} \simeq 50 \left(\frac{f}{246\text{GeV}} \right)$$

loophole

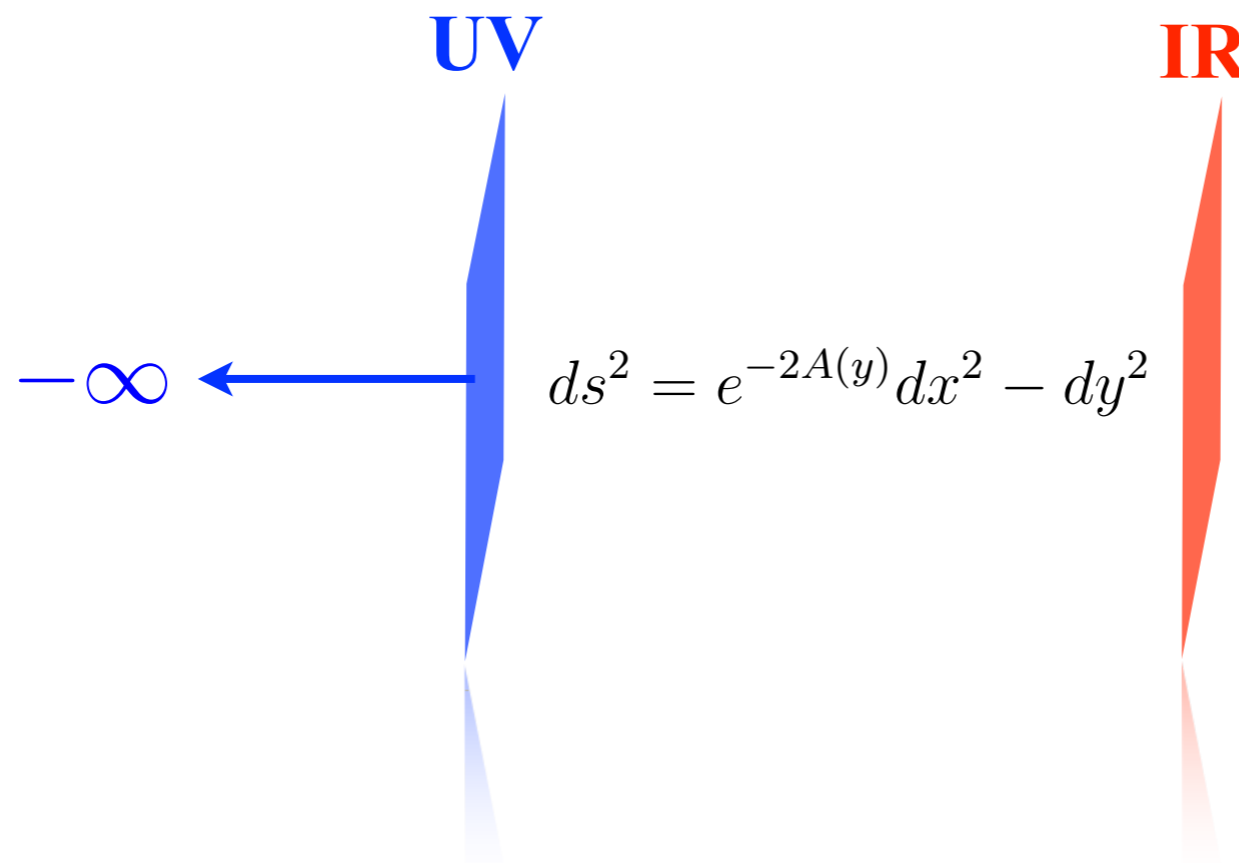
$$\beta = \epsilon(\lambda + b\lambda^2 + \dots) \ll 1$$

$$\lambda^* : F(\lambda^*) \sim O(\beta), V'(\lambda^*) = 0, m_d^2 \sim O(\beta)$$

Realizable in a warped extra-d:

not like Goldberger-Wise

Goldberger, Wise '99



Sundrum '04

Contino, Pomarol, Rattazzi, '10

Still one needs to accomplish: $v/f \simeq 1$

loophole

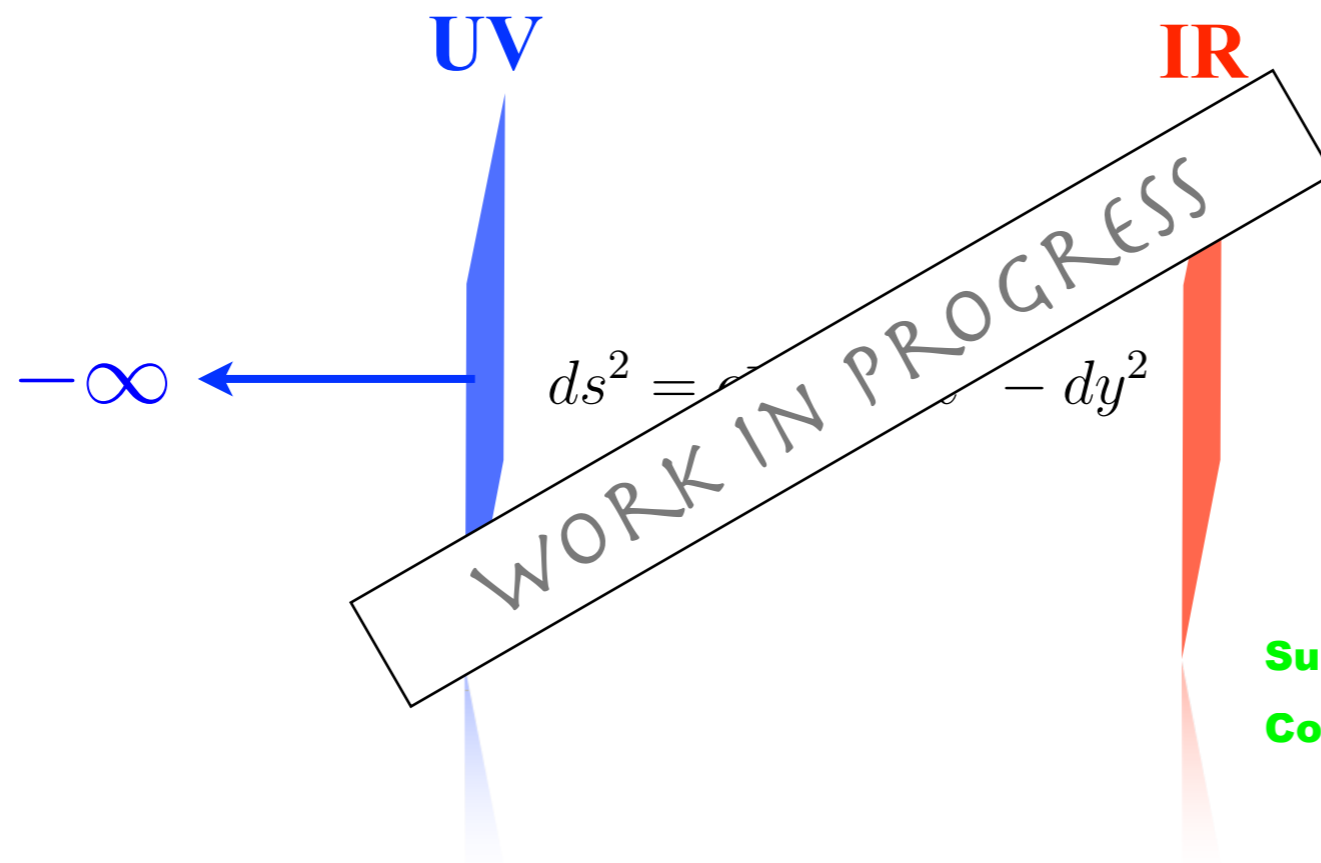
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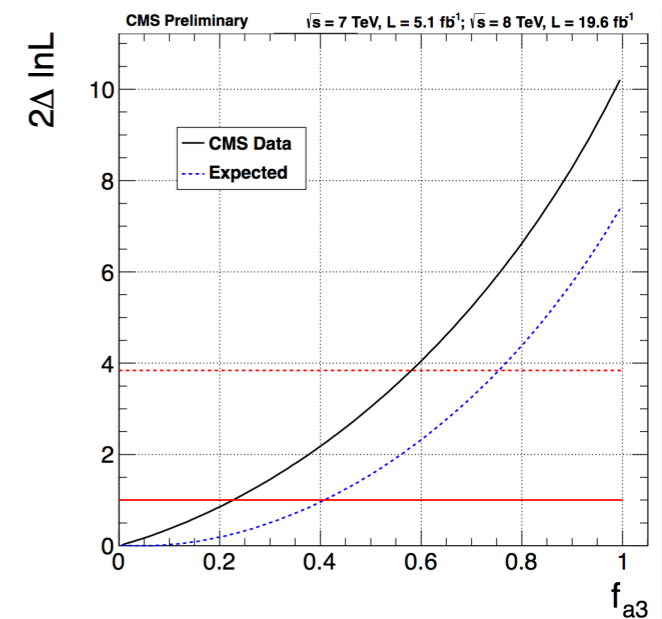
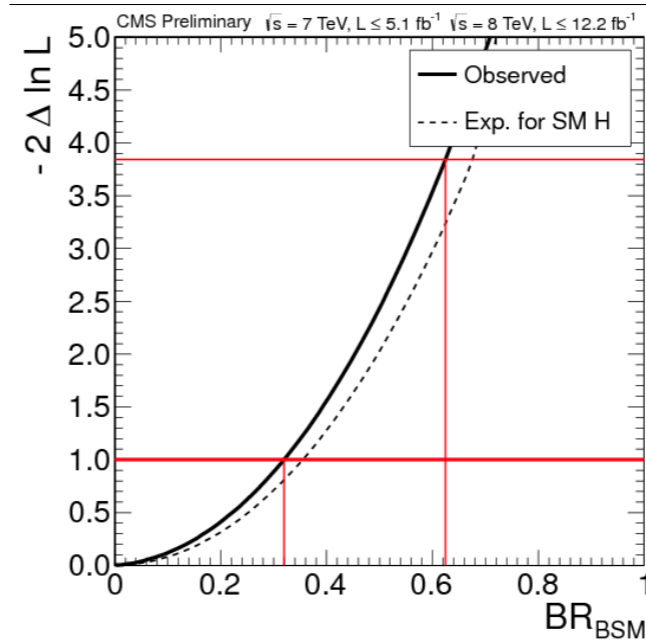
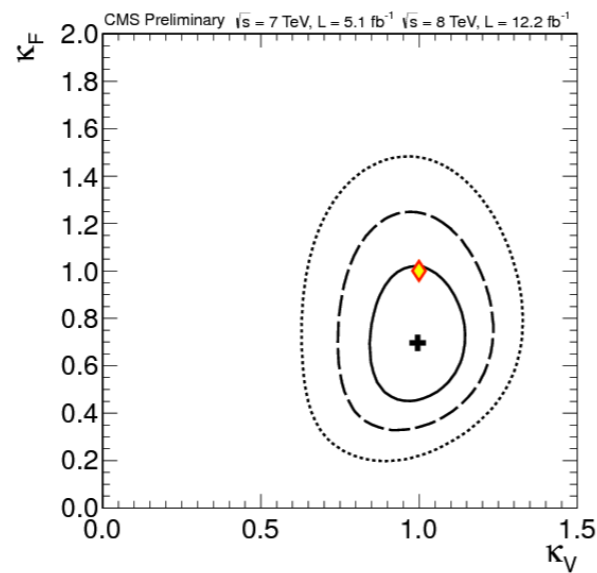
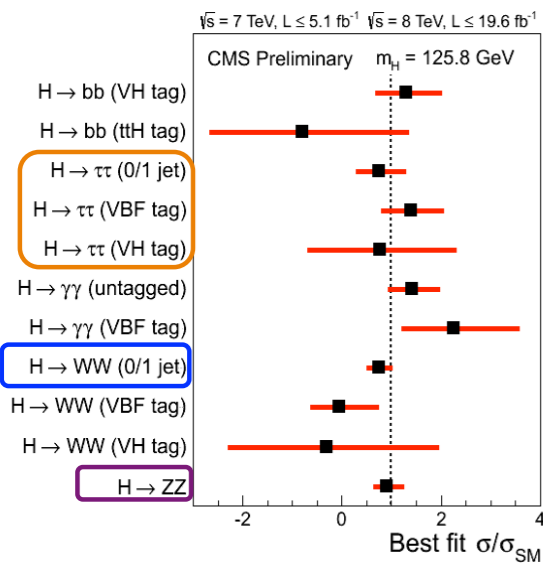
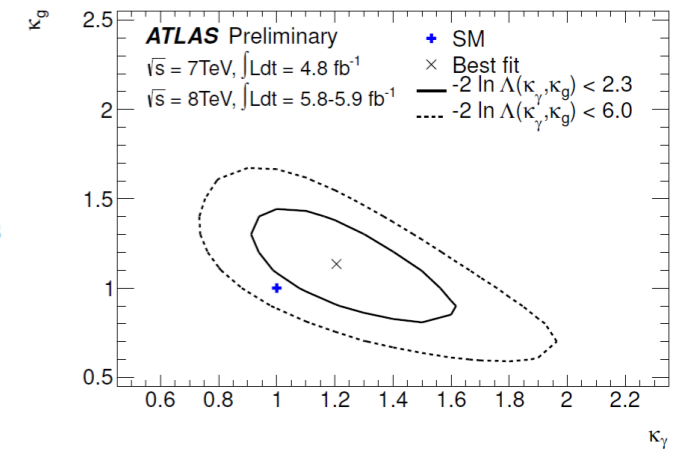
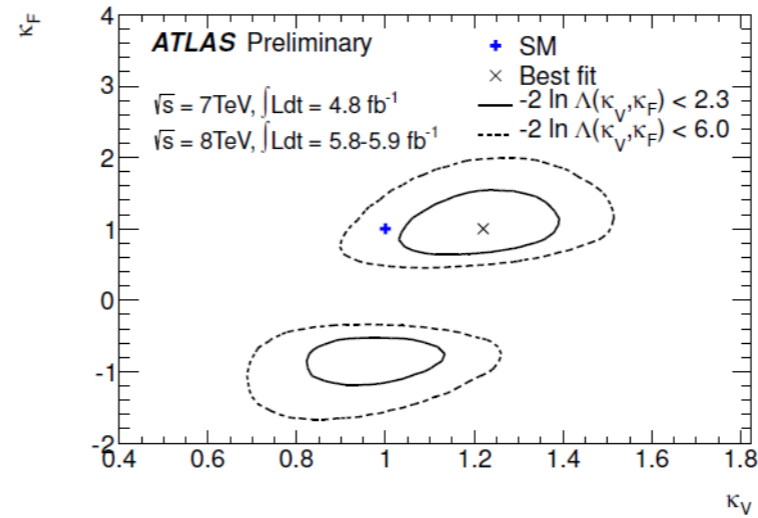
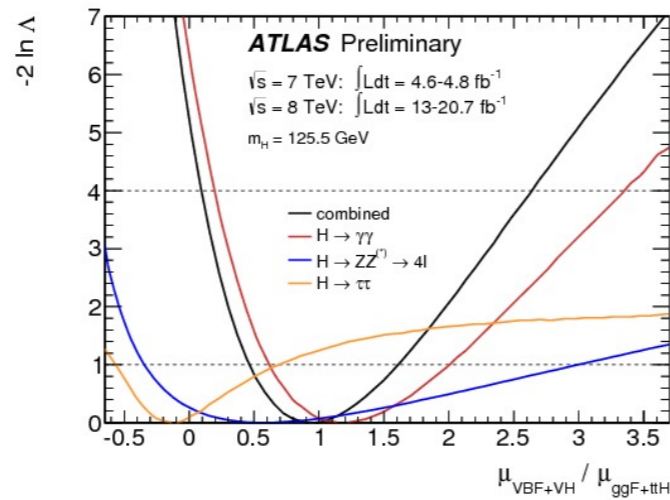
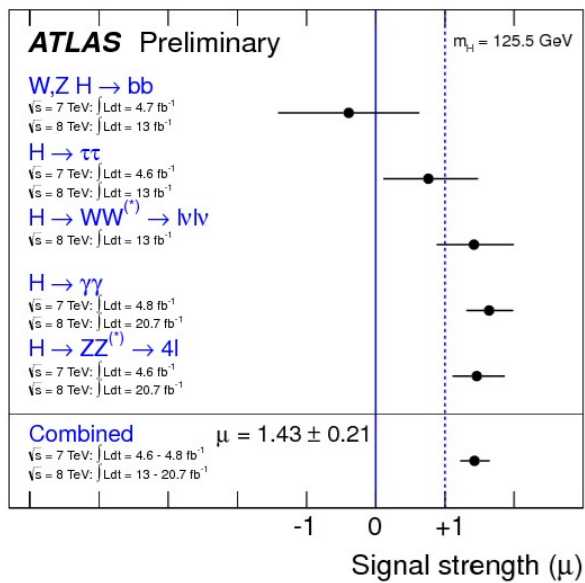
Sundrum '04

Contino, Pomarol, Rattazzi, '10

Still one needs to accomplish: $v/f \simeq 1$

Goldstone-Higgs couplings @ the LHC

More data on EWSB than ever!



$$\mathcal{L}_{(0)} = \frac{h}{v} \left[c_V (2m_W^2 W_\mu^\dagger W^\mu + m_Z^2 Z_\mu Z^\mu) - c_t \sum_{f=u,c,t} m_f \bar{f} f - c_b \sum_{f=d,s,b} m_f \bar{f} f - c_\tau \sum_{f=e,\mu,\tau} m_f \bar{f} f \right]$$

$$\mathcal{L}_{(2)} = -\frac{h}{4v} \left[2c_{WW} W_{\mu\nu}^\dagger W^{\mu\nu} + c_{ZZ} Z_{\mu\nu} Z^{\mu\nu} + 2c_{Z\gamma} A_{\mu\nu} Z^{\mu\nu} + c_{\gamma\gamma} A_{\mu\nu} A^{\mu\nu} - c_{gg} G_{\mu\nu}^a G_{\mu\nu}^a \right]$$

$$c_{WW} = c_{\gamma\gamma} + \frac{g_L}{g_Y} c_{Z\gamma}, \quad c_{ZZ} = c_{\gamma\gamma} + \frac{g_L^2 - g_Y^2}{g_L g_Y} c_{Z\gamma}$$

Standard Model

$$c_V = c_t = c_b = c_\tau = 1$$

$$c_{\gamma\gamma} = c_{Z\gamma} = c_{gg} = 0$$

SO(5)/SO(4)

$$c_V = \sqrt{1 - v^2/f^2}$$

$$c_f = \frac{1 - (1 + n)v^2/f^2}{\sqrt{1 - v^2/f^2}}$$

$$c_{\gamma\gamma,gg} \sim \frac{(g'^2, g_S^2) v^2 y_t^2}{16\pi^2 f^2 g_\rho^2}$$

$$c_{Z\gamma} \sim \frac{g^2 v^2}{16\pi^2 f^2}$$

dilaton

$$c_V = \frac{v}{f}$$

$$c_f = \frac{v}{f}(1 + \gamma_f)$$

$$c_{\gamma\gamma,gg} = \frac{(g'^2, g_S^2) v}{16\pi^2 f} \left(b_{IR}^{(EM,3)} - b_{UV}^{(EM,3)} \right)$$

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dilaton

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< 1 (model independent)



SO(5)/SO(4)

$$c_V = \sqrt{1 - v^2/f^2}$$

$$c_f = \frac{1 - (1 + n)v^2/f^2}{\sqrt{1 - v^2/f^2}}$$

< 1 (m.i.)

$$c_{\gamma\gamma,gg} \sim \frac{(g'^2, g_S^2) v^2 y_t^2}{16\pi^2 f^2 g_\rho^2}$$

$$c_{Z\gamma} \sim \frac{g^2 v^2}{16\pi^2 f^2}$$

dilaton

$$c_V = \frac{v}{f}$$

< 1 / > 1 (m.d.)

$$c_f = \frac{v}{f} (1 + \gamma_f)$$

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SO(5)/SO(4)

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$$c_{Z\gamma} \sim \frac{g^2}{16\pi^2} \frac{v^2}{f^2}$$

SM-like

dilaton

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$$c_f = \frac{v}{f} (1 + \gamma_f)$$

$$c_{\gamma\gamma,gg} = \frac{(g'^2, g_S^2)}{16\pi^2} \frac{v}{f} \left(b_{IR}^{(EM,3)} - b_{UV}^{(EM,3)} \right)$$

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suppression
(m.i.)

dilaton

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SO(5)/SO(4)

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**Goldstone
suppression**

dilaton

$$c_V = \frac{v}{f}$$

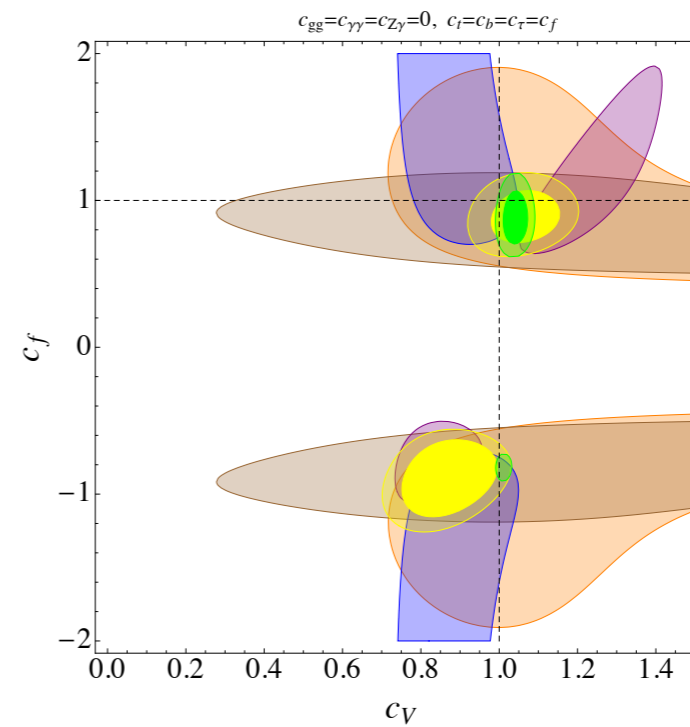
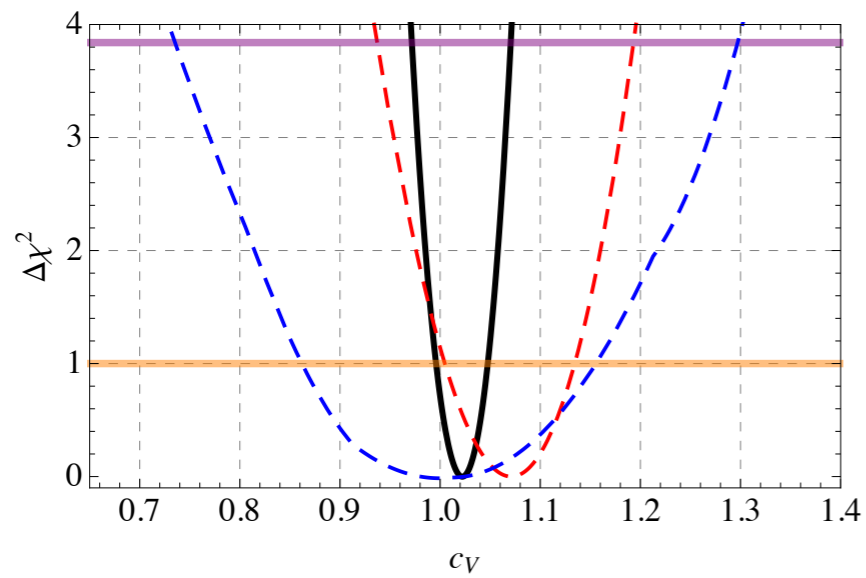
$$c_f = \frac{v}{f} (1 + \gamma_f)$$

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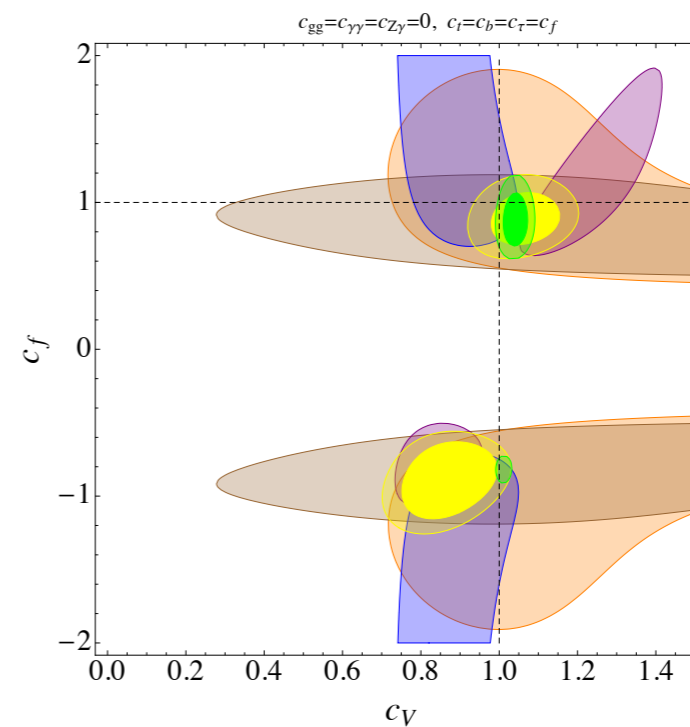
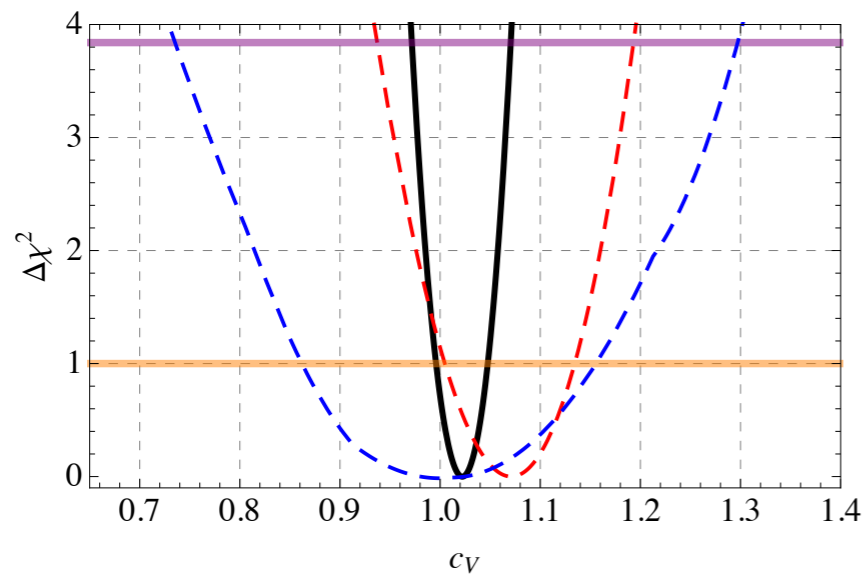
$$c_{Z\gamma} \sim \frac{g^2}{16\pi^2} \frac{v}{f} \left(b_{IR}^{(2)} - b_{UV}^{(2)} \right)$$

**Scale
anomaly**

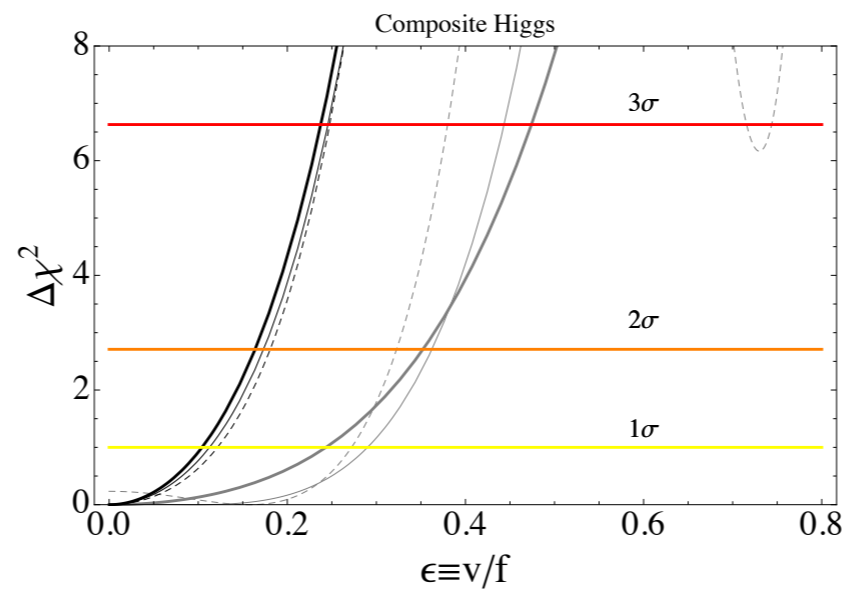
EW precision tests & Higgs couplings:



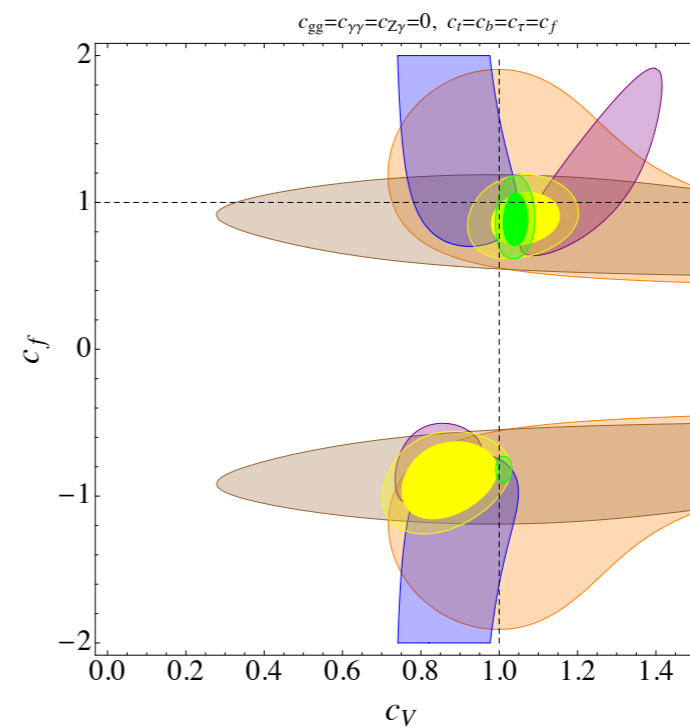
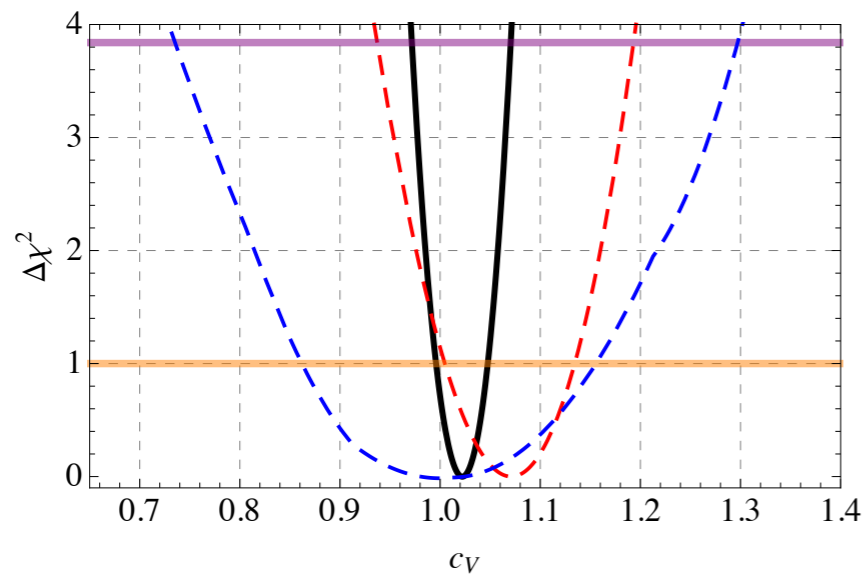
EW precision tests & Higgs couplings:



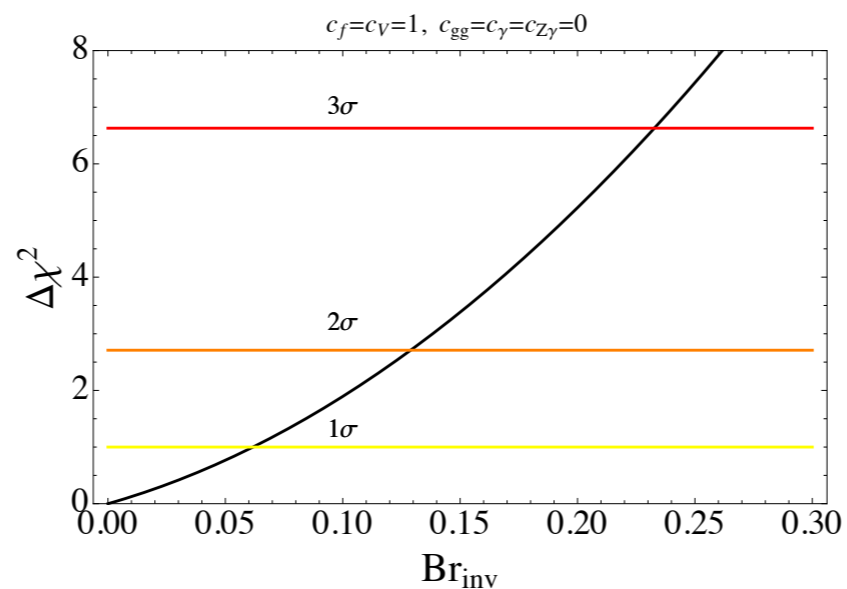
SO(5)/SO(4)



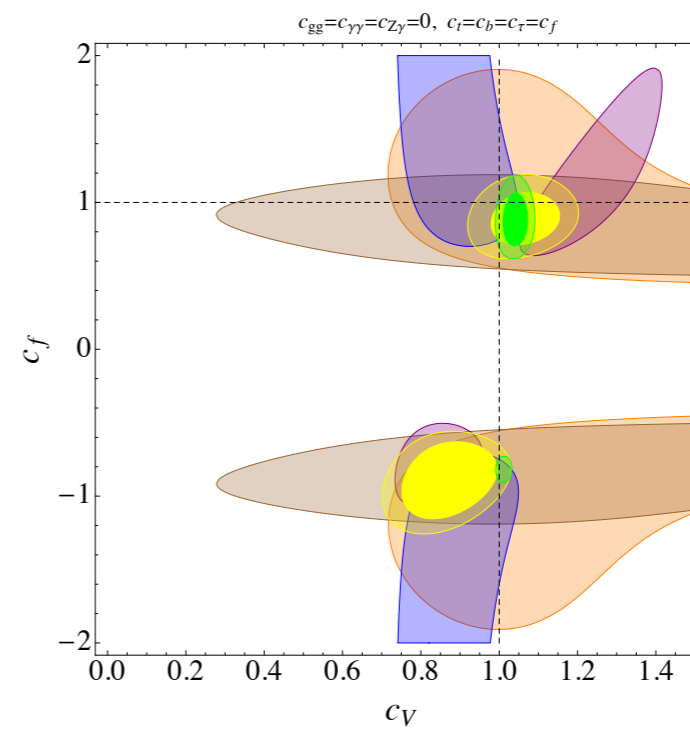
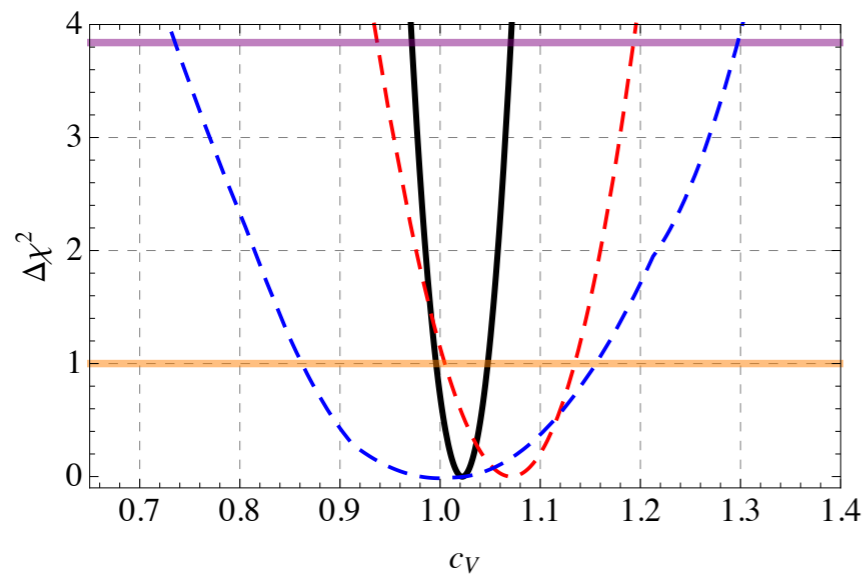
EW precision tests & Higgs couplings:



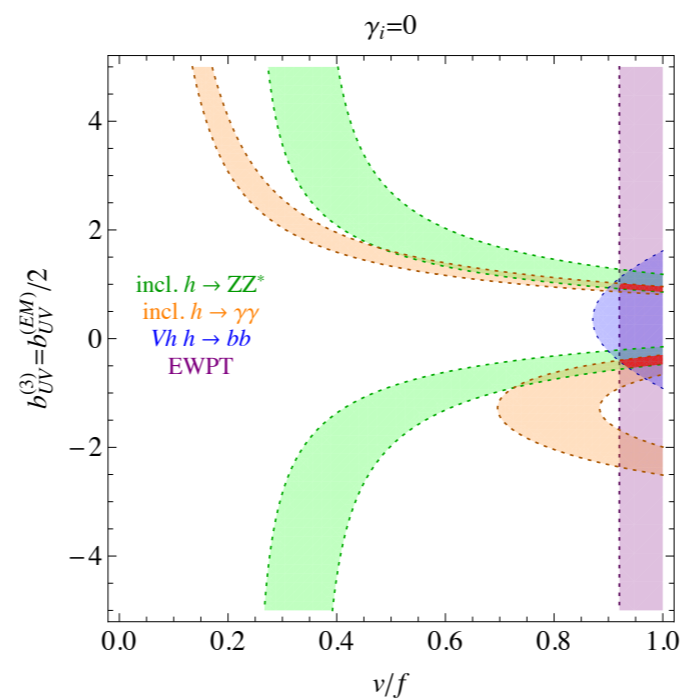
SO(6)/SO(5) $h \rightarrow \eta\eta = \cancel{E}_T$



EW precision tests & Higgs couplings:

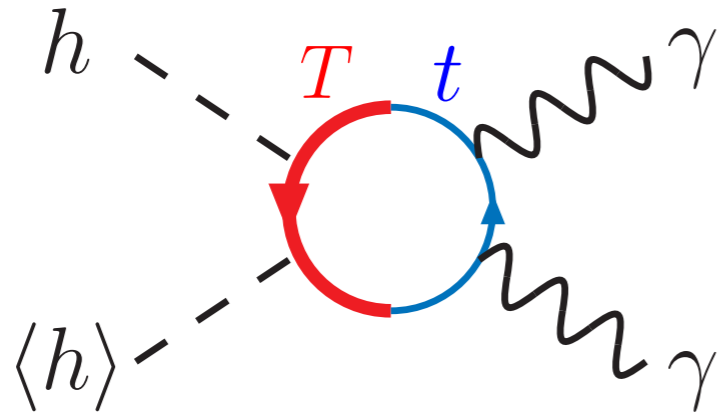


dilaton



Non-minimal Higgs sectors & Higgs couplings

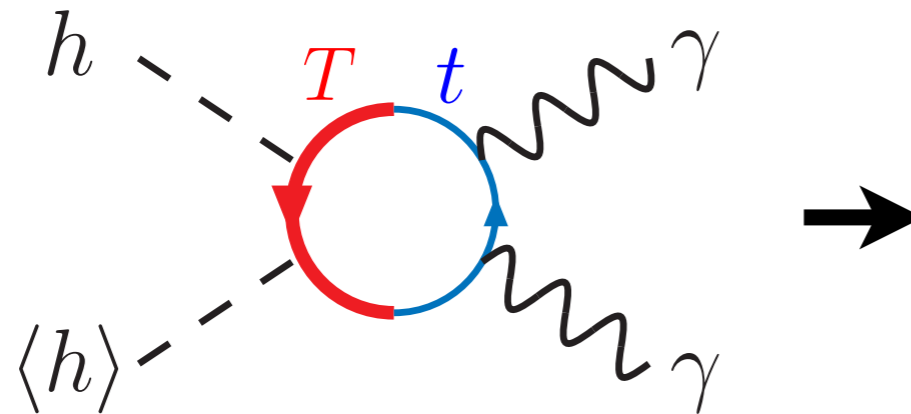
h to photons from composite resonance:



$$\rightarrow c_\gamma \frac{g'^2}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} \frac{g_{SM}^2}{g_\rho^2} H^\dagger H B_{\mu\nu} B^{\mu\nu}$$

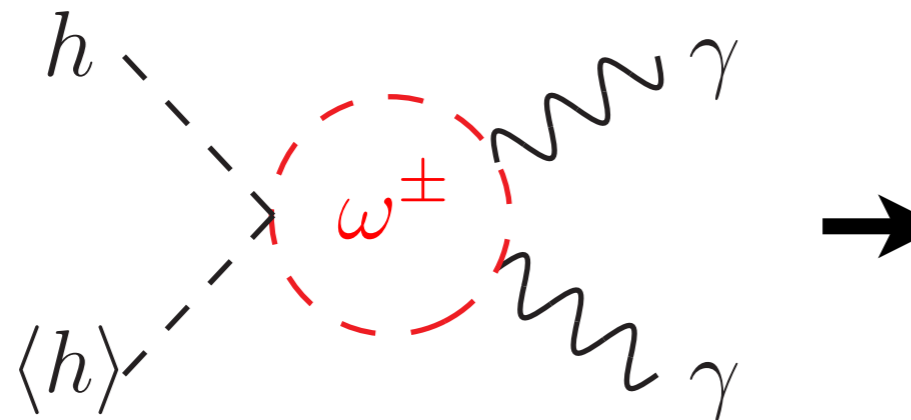
Non-minimal Higgs sectors & Higgs couplings

h to photons from composite resonance:



$$c_\gamma \frac{g'^2}{m_\rho^2} \frac{g_\rho^2}{16\pi^2} \frac{g_{SM}^2}{g_\rho^2} H^\dagger H B_{\mu\nu} B^{\mu\nu}$$

h to photons from **extra Goldstone's**:



$$\tilde{c}_\gamma \frac{g'^2}{m_\Pi^2} \frac{g_\Pi^2}{16\pi^2} H^\dagger H B_{\mu\nu} B^{\mu\nu}$$

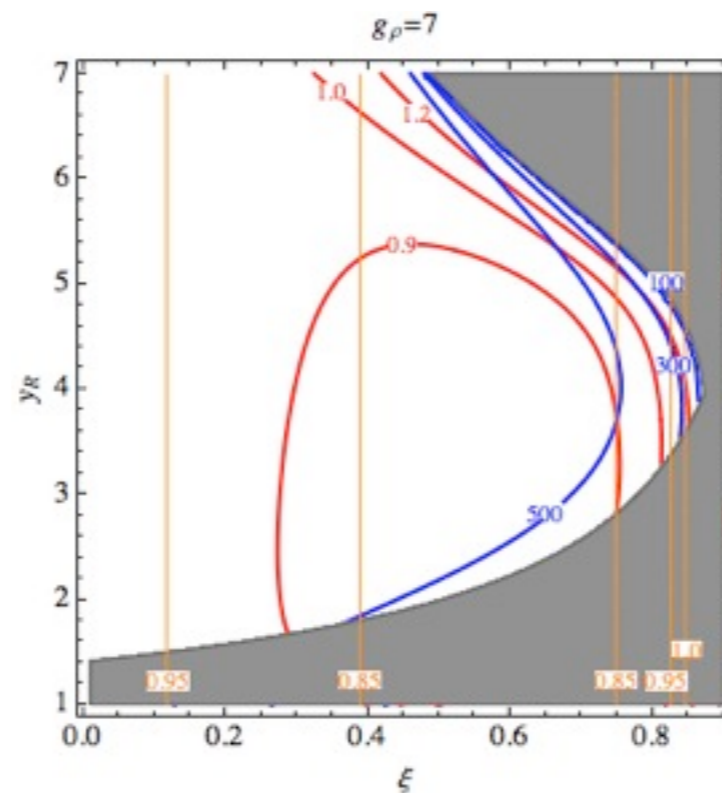
$$m_\Pi^2 \sim \frac{g_\rho^2}{16\pi^2} g_{SM}^2 f^2 \quad \& \quad g_\Pi^2 \sim \frac{g_\rho^2}{16\pi^2} g_{SM}^2 \quad \rightarrow \quad c_\gamma \sim \tilde{c}_\gamma \frac{g_\rho^2}{g_{SM}^2}$$

E.g.: $SO(8)/SO(7)$ & Higgs to photons

$$SO(8)/SO(7) \cong SO(7)/G_2 \quad \longrightarrow \quad \mathbf{7} = (\mathbf{2}, \mathbf{2}) + (\mathbf{3}, \mathbf{1}) = H + \omega$$

Sigma-model:
$$\frac{f^2}{2} \partial_\mu \Sigma^T \partial^\mu \Sigma = \frac{f^2}{2} \left\{ (\partial h)^2 + (\partial \omega)^2 + \frac{(h \partial h + \omega \partial \omega)^2}{1 - h^2 - \omega^2} \right\}$$

Potential:
$$V = m_1^2 h^2 + m_2^2 \omega^2 + \lambda_1 h^4 + \lambda_2 \omega^4 + \lambda_3 h^2 \omega^2$$

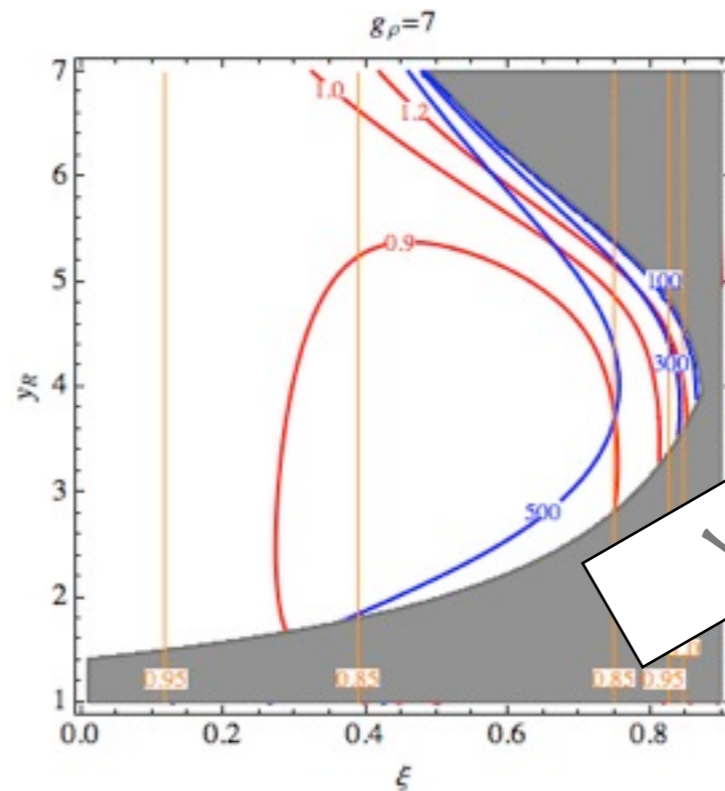


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Nature has given us a light higgs for EWSB

- ◆ If a composite Higgs, the expectation is that it behaves as a Goldstone boson.
- ◆ A 125 GeV composite Higgs implies light and weakly coupled top resonances, with masses around the current bound 700 GeV.
- ◆ Light W and Z resonances are disfavored by EW precision data and Higgs couplings measurements.
- ◆ We have clear predictions for composite Higgs couplings (deviations), which we should look for.
- ◆ Extra Goldstone's might play an important role and deserve further study.

Thank you for your attention