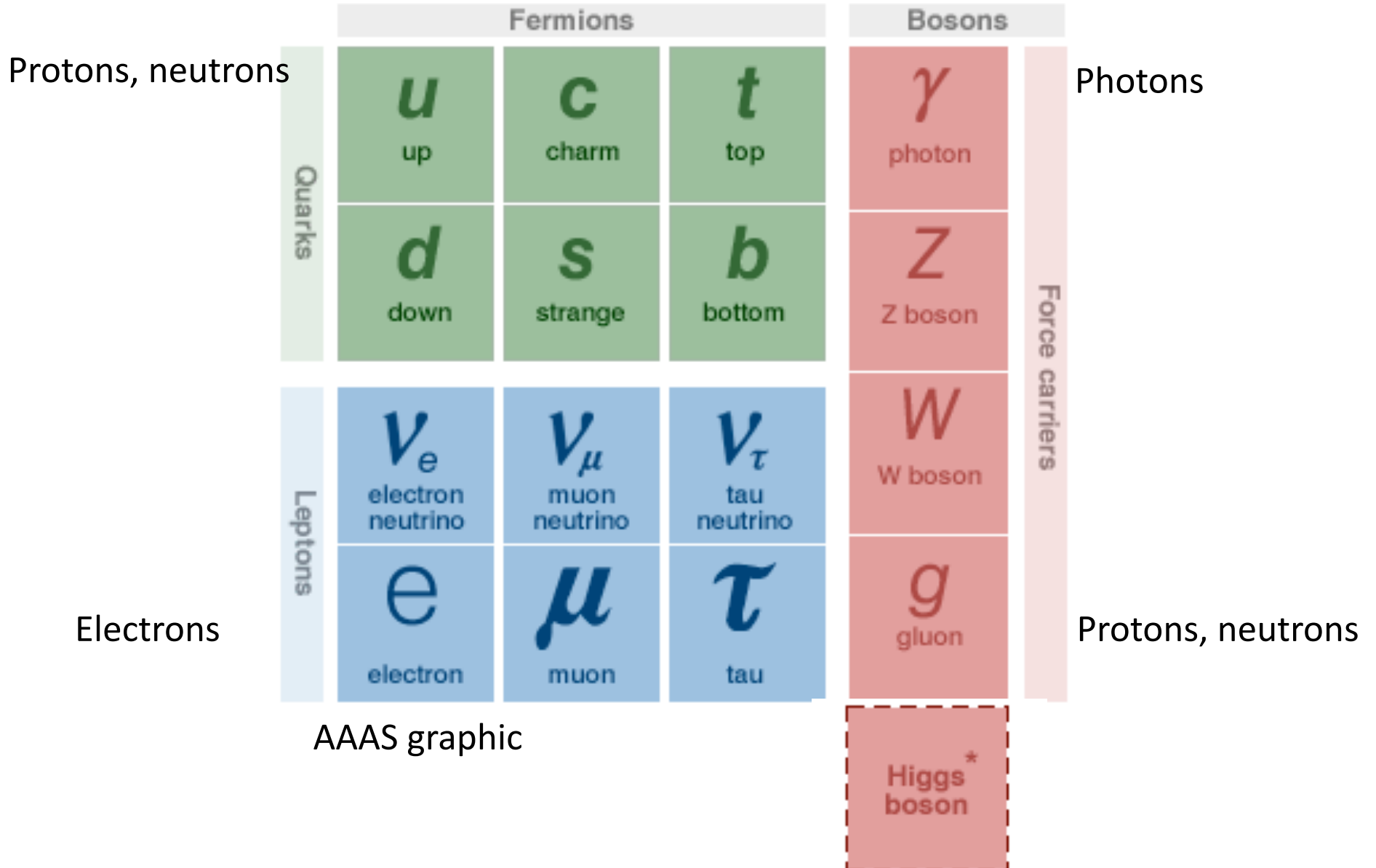


Results from the neutrino experiment

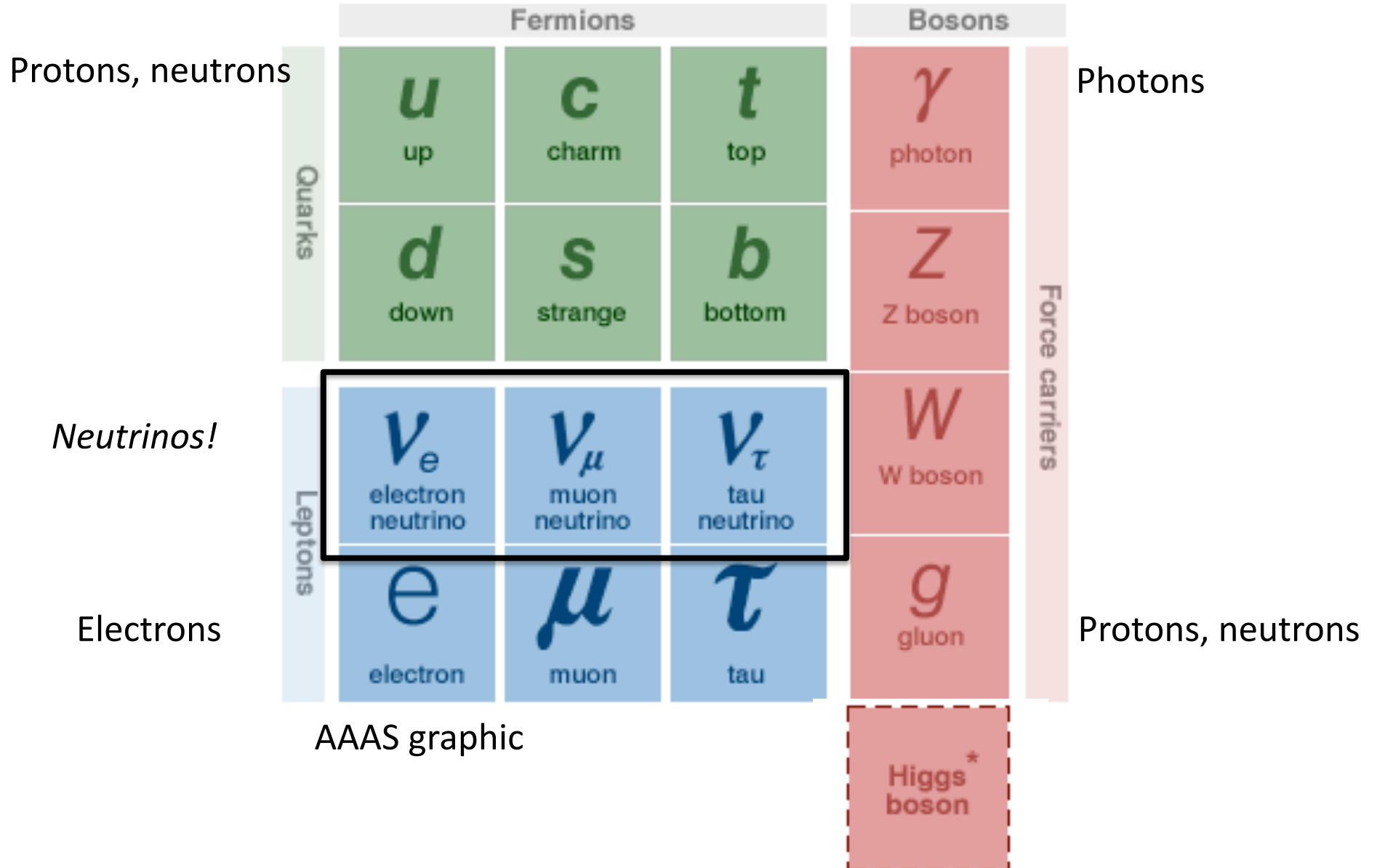
Kendall Mahn, TRIUMF



The Standard Model



The Standard Model



What we now know about neutrinos

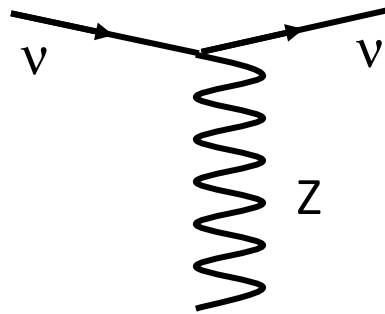
- Three flavors: ν_e , ν_μ , ν_τ

Leptons	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino
	e electron	μ muon	τ tau

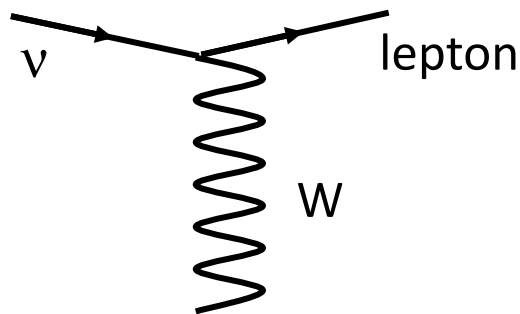
What we now know about neutrinos

- Three flavors: ν_e , ν_μ , ν_τ
- Neutral
- Interact via the weak force

Neutral Current (NC)



Charged Current (CC)



$$\nu_e \rightarrow e$$

$$\nu_\mu \rightarrow \mu$$

$$\nu_\tau \rightarrow \tau$$

Leptons	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino
	e electron	μ muon	τ tau

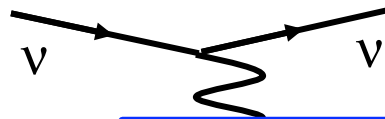
Z Z boson	Force carriers
W W boson	

What we now know about neutrinos

- Three flavors: ν_e , ν_μ , ν_τ
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Leptons	ν_e electron neutrino	ν_μ muon neutrino	ν_τ tau neutrino
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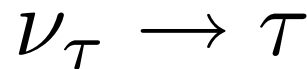
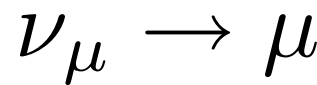
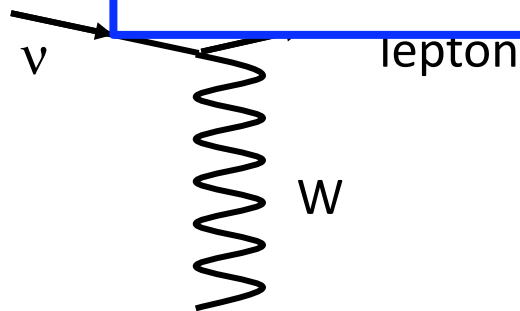
Neutral Current (NC)



At neutrino energy (E_ν) ~ 1 GeV, $\sigma_{CC} \sim 10^{-38}$ cm²

Mean free path through lead is 1 light year

Charge

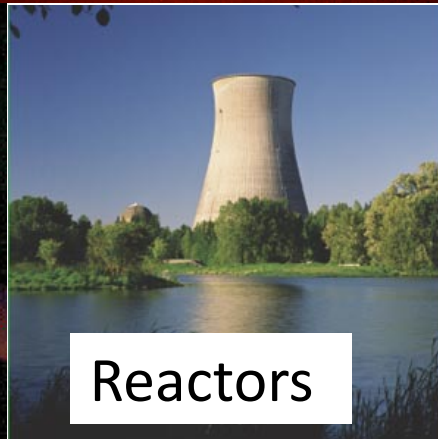
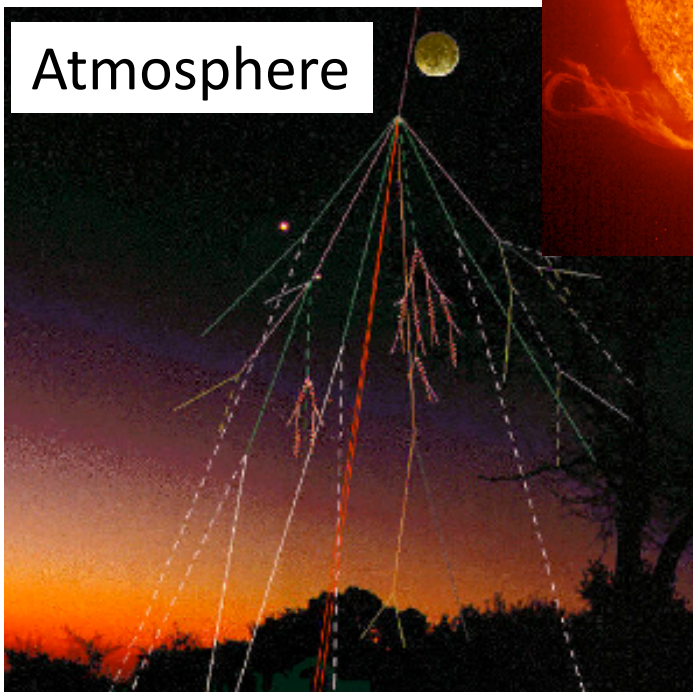


W boson

lepton

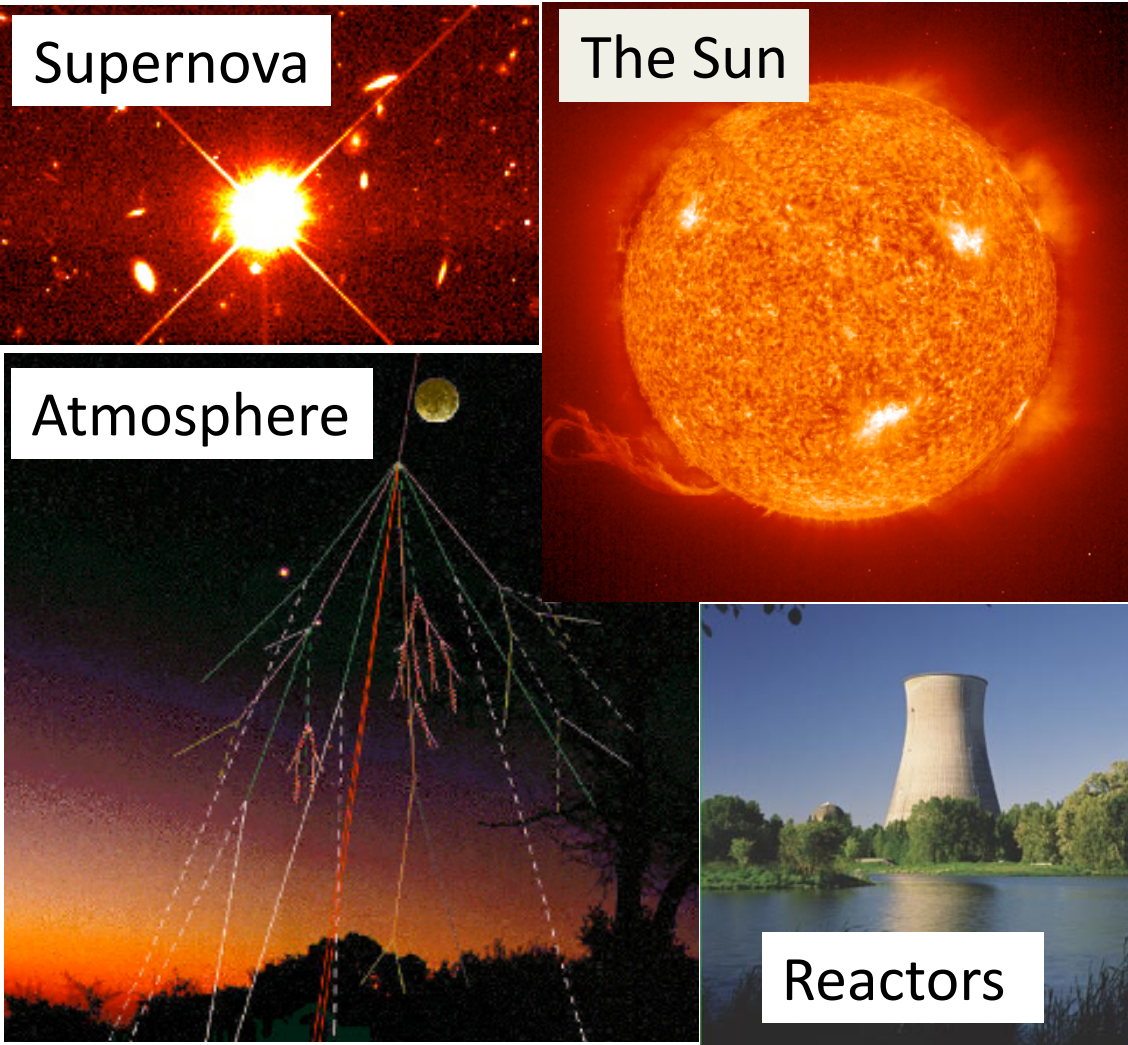
What we now know about neutrinos

- Three flavors: ν_e , ν_μ , ν_τ
- Neutral
- Interact via the weak force
- **Abundant**

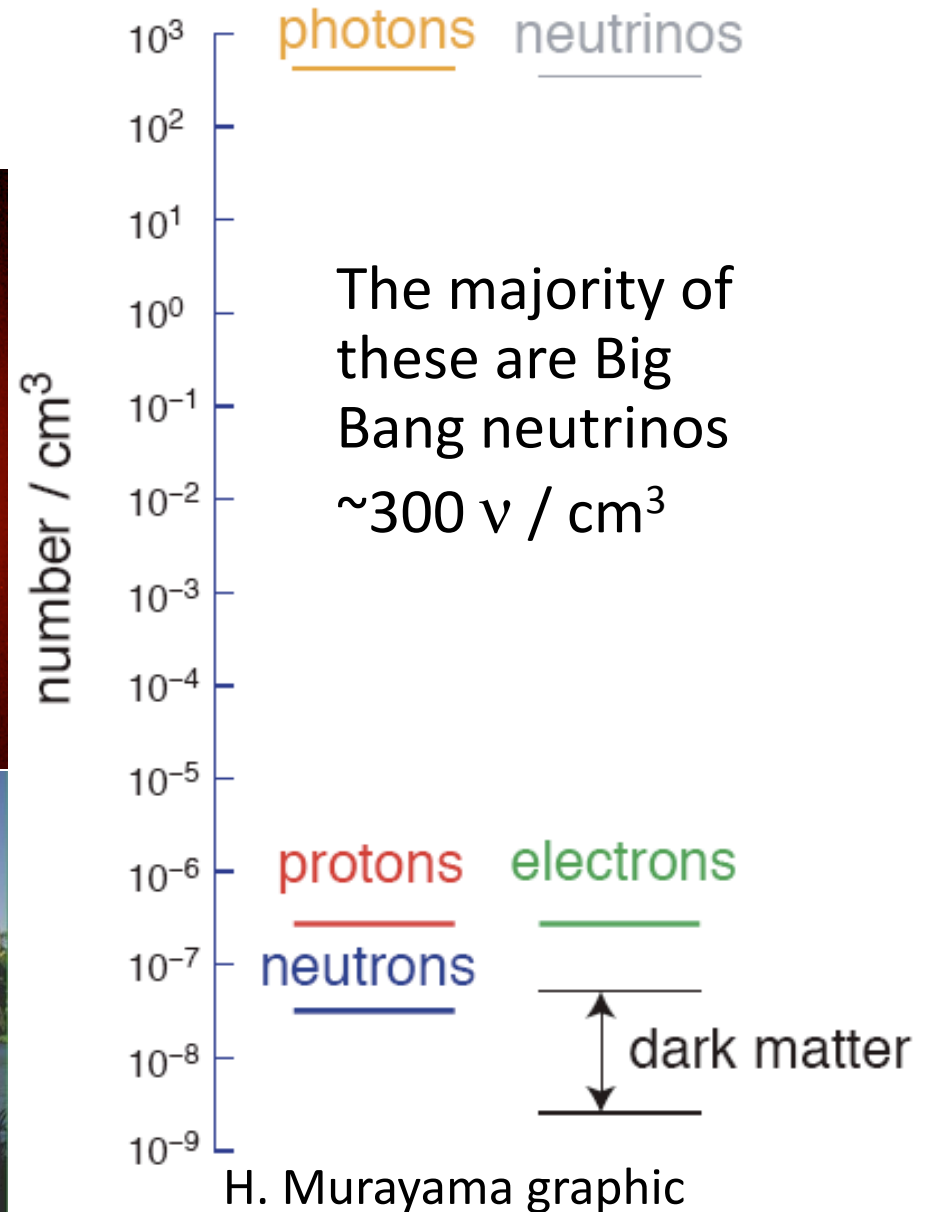


What we now know about neutrinos

- Three flavors: ν_e , ν_μ , ν_τ
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- Interact via the weak force
- **Abundant**



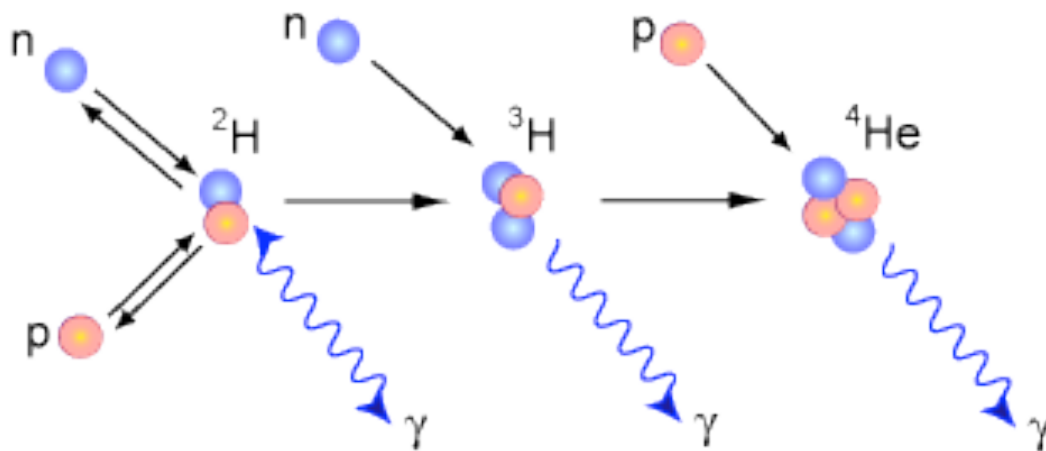
The Particle Universe



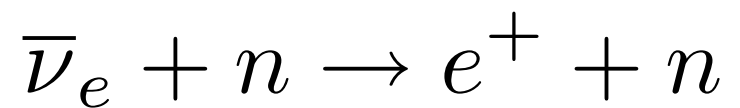
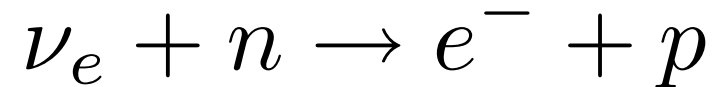
What we now know about neutrinos

- Three flavors: ν_e , ν_μ , ν_τ
- Neutral
- Interact via the weak force
- **Abundant**

The amount of neutrinos and antineutrinos affects the formation of elements in the early universe:



CSIRO graphic



What we now know about neutrinos

- Three flavors: ν_e , ν_μ , ν_τ
- Neutral
- Interact via the weak force
- Abundant
- **Massive**

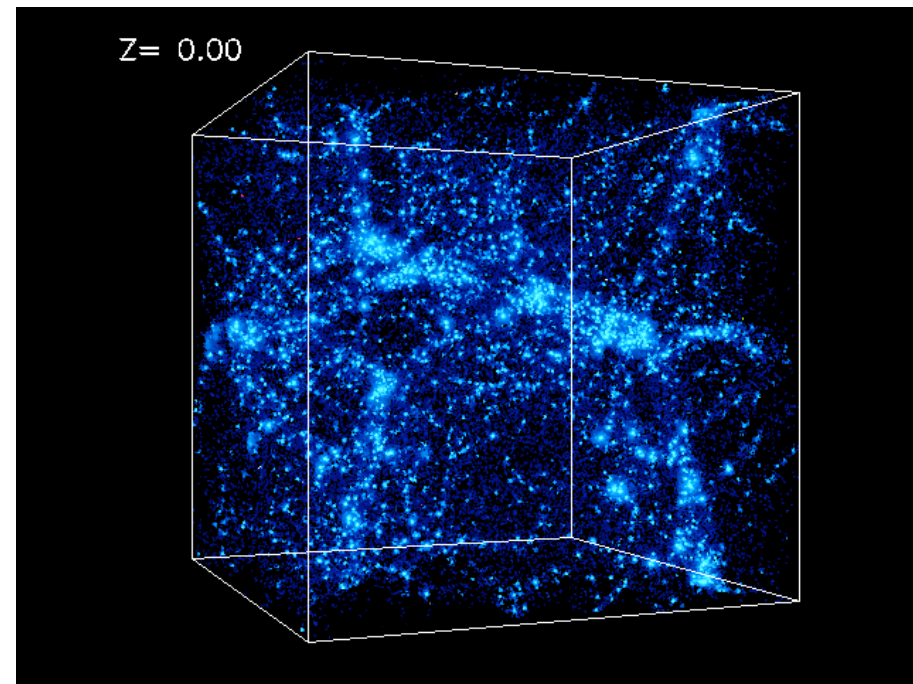
The mass of the neutrino is small but it has a big impact in the early universe

At early times, neutrinos behave like radiation

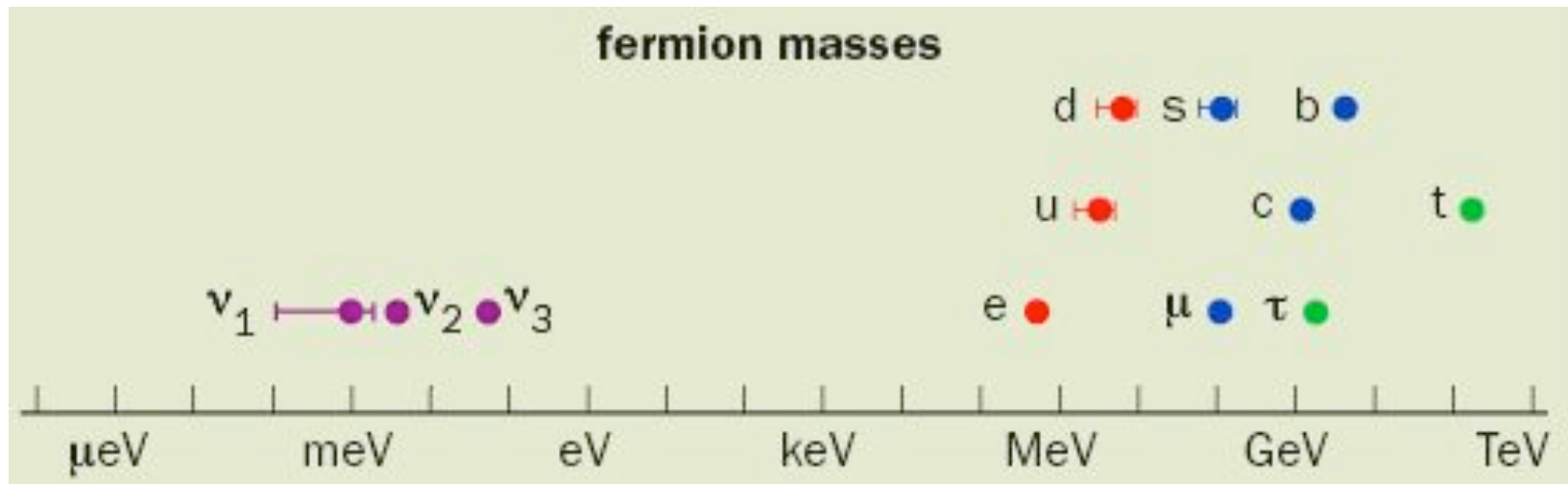
At late times, neutrinos behave like matter

Affects large scale structure formation

Center for Cosmological Physics graphic



Neutrino mass is SMALL



H. Murayama graphic

While we know neutrinos have mass, we don't know the origin of neutrino mass

- Neutrinos are unlike other particles in the Standard Model because they are neutral and only interact with the weak force (and gravity)

Why is neutrino mass non-zero?

Why is it so much smaller than the other particles?

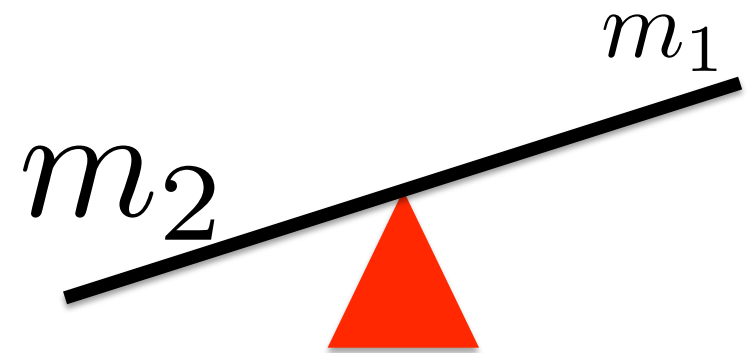
Neutrino mass

The “see saw mechanism” explains the lightness of the neutrino mass by adding a (very heavy) neutrino which doesn’t interact

If we have one neutrino which interacts in the Standard Model (m_D) and a heavy partner (m_R) then:

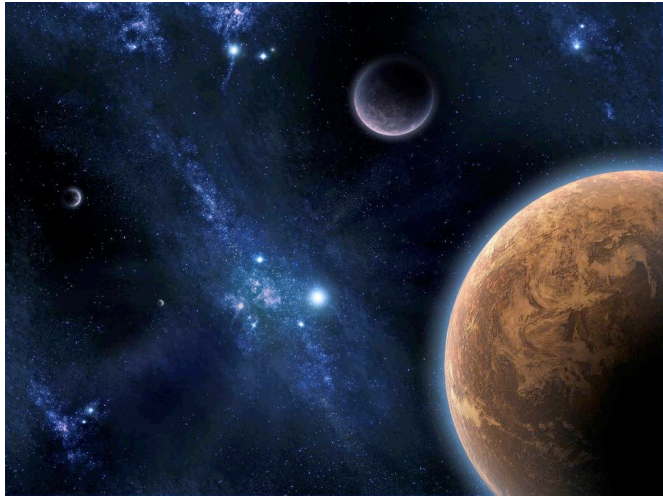
$$m_1 \simeq \frac{(m_D)^2}{m_R} \ll m_D,$$

$$m_2 \simeq m_R,$$

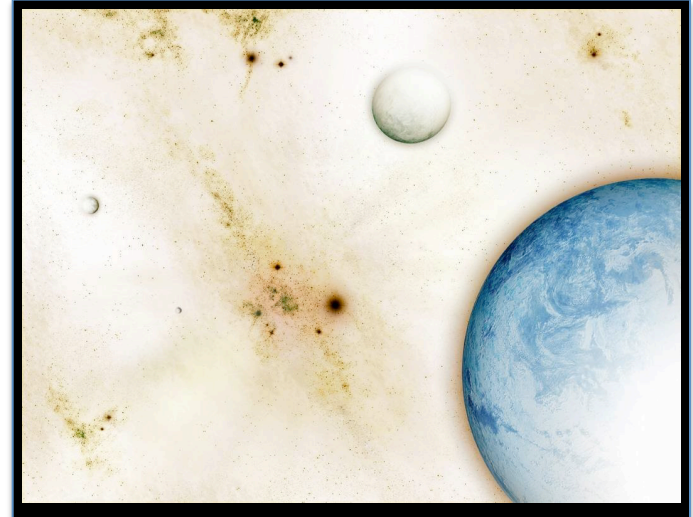


To get the observed neutrino mass, then $m_2 \sim m_R$ is very heavy (10^{15} GeV)

Neutrinos and the matter-antimatter asymmetry



?
≠

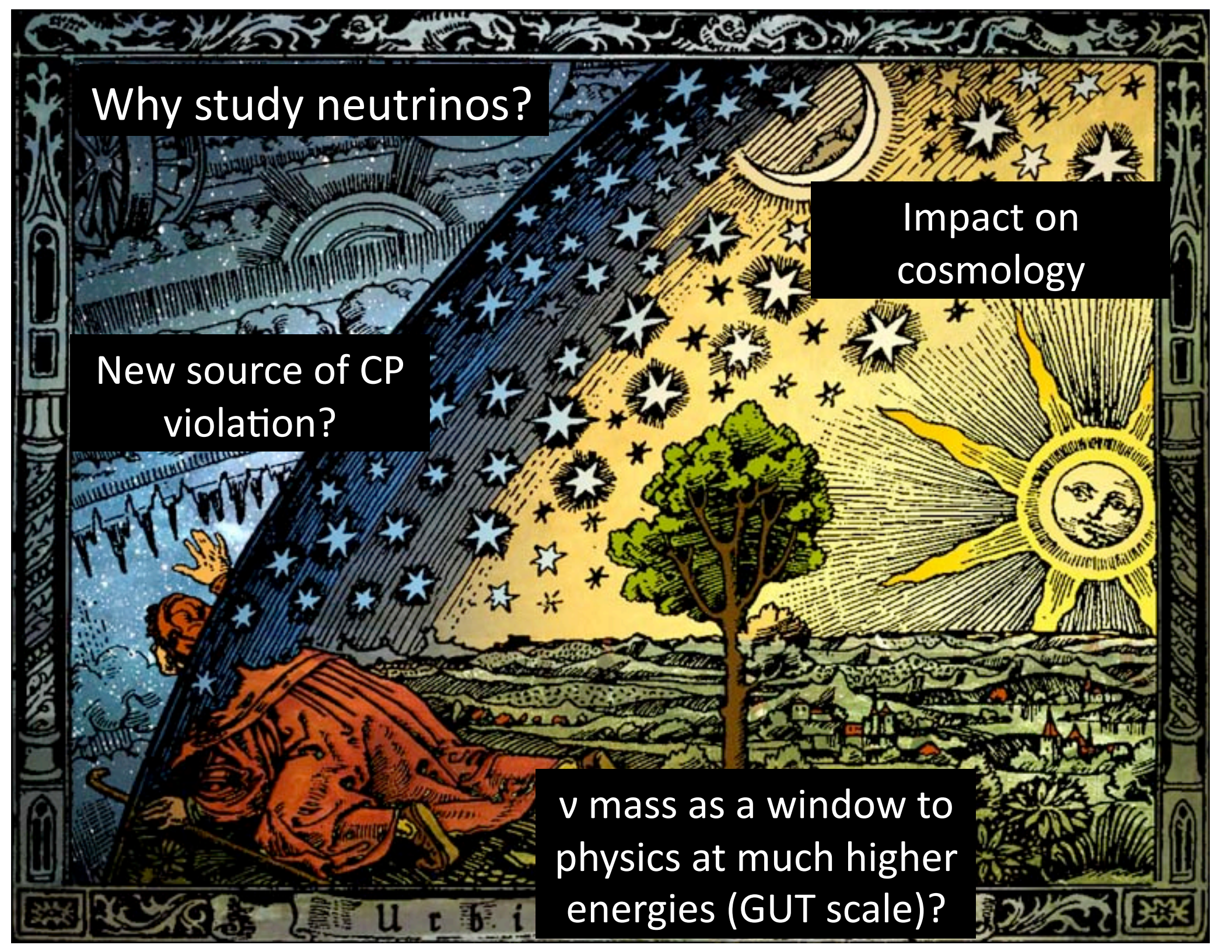


How do we explain the observed matter-antimatter asymmetry in the universe?

- To create this asymmetry, we need: non-thermal equilibrium, CP violation and baryon number violation
- So far, there is no sufficient source of CP violation in the Standard Model

If there is CP violation with neutrinos, CP violating decays of the heavy neutrino can create the baryon number violation

Searching for CP violation with neutrinos may lead to insights about this mechanism

A medieval manuscript illustration of a landscape. The scene is framed by a decorative border. In the foreground, a man in a red robe is shown from the back, looking towards a landscape. The landscape features a large green tree, a small town with a church, and rolling hills. The sky is filled with a large sun with a human face, a crescent moon, and numerous stars. A diagonal line divides the sky into a blue upper half and a yellow lower half. The overall style is characteristic of a medieval manuscript illumination.

Why study neutrinos?

Impact on cosmology

New source of CP violation?

ν mass as a window to physics at much higher energies (GUT scale)?

What is neutrino oscillation?

We know neutrinos have mass because of we observe neutrino “oscillation”: the interference between the flavor and mass eigenstates of the neutrino

If we start with two neutrino flavor (ν_e, ν_μ) and two mass states (ν_1, ν_2) then:

$$\begin{pmatrix} \nu_e \\ \nu_\mu \end{pmatrix} = \begin{pmatrix} \cos \theta & \sin \theta \\ -\sin \theta & \cos \theta \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \end{pmatrix}$$

The flavor state evolution in time is like an elliptically polarized wave:

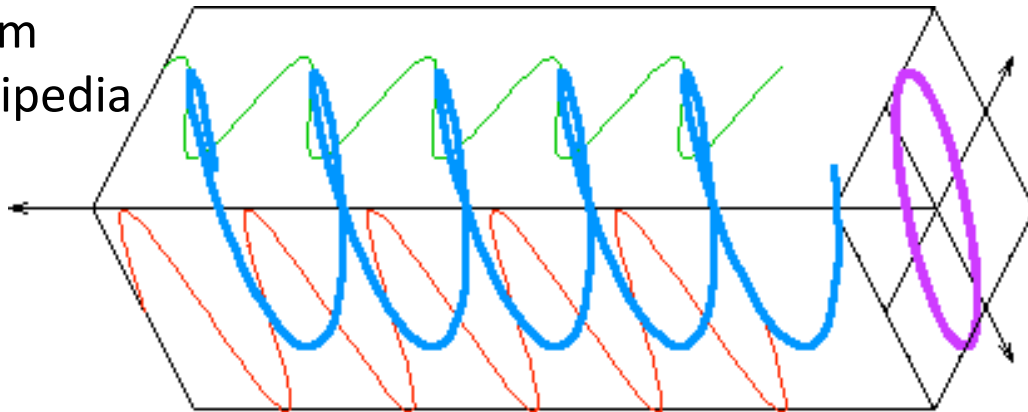
$$|\nu_e(t)\rangle = \cos \theta e^{-iE_1 t} |\nu_1\rangle - \sin \theta e^{-iE_2 t} |\nu_2\rangle$$

What is neutrino oscillation?

The flavor state evolution in time is like an elliptically polarized wave:

$$|\nu_e(t)\rangle = \cos \theta e^{-iE_1 t} |\nu_1\rangle - \sin \theta e^{-iE_2 t} |\nu_2\rangle$$

From
wikipedia



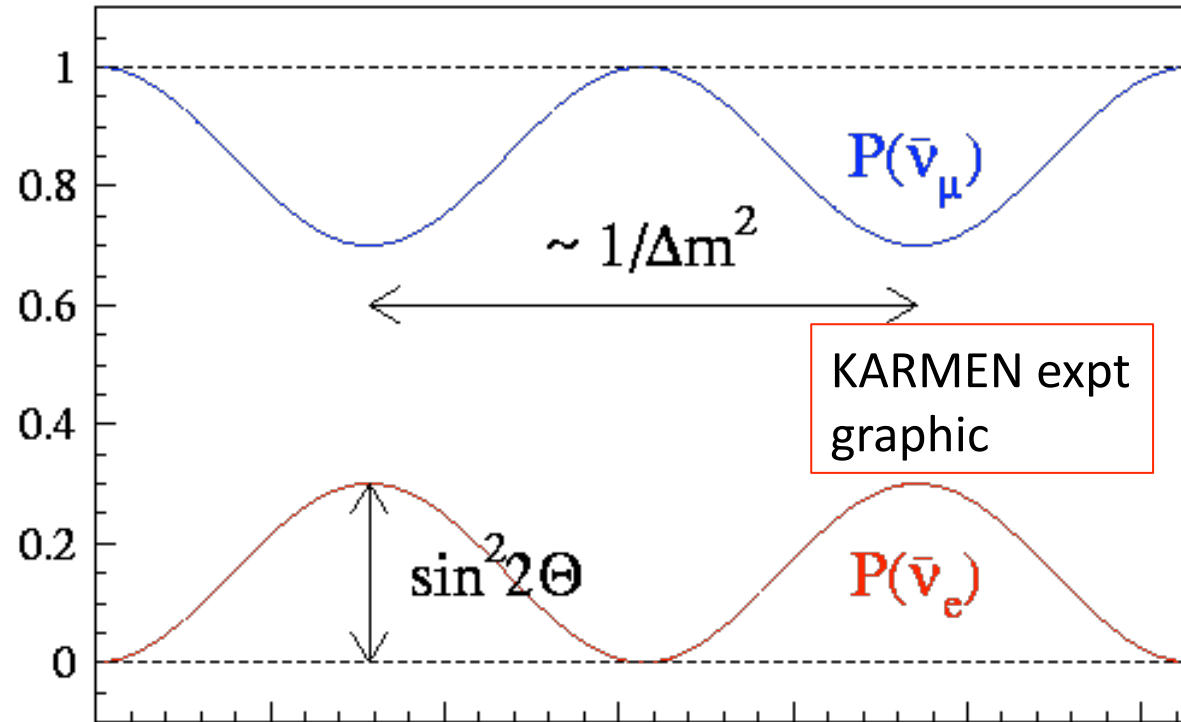
Starting polarized along the x-axis
(like starting in ν_μ state) then:

- Some time later polarization is along y-axis (ν_e)
- Or back to the x-axis (ν_μ)

No mass, no oscillation

Neutrino oscillation

$$P_{\mu e} = \sin^2 2\theta \sin^2 \left(\frac{1.27 \Delta m_{ij}^2 L}{E} \right)$$



Probability to observe ν_μ after starting in flavor state ν_e depends on:

- θ : Mixing angle
- L (km): Distance the neutrino has travelled
- E (GeV): Energy of the neutrino
- Δm^2 (eV^2): mass splitting

Difference of the square of the mass eigenvalues

$$\Delta m_{ij}^2 = m_i^2 - m_j^2$$

If neutrinos have no mass, or degenerate masses, no interference is possible

Open questions about neutrino mixing

$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Flavor eigenstates (coupling to the W) Mass eigenstates (definite mass)

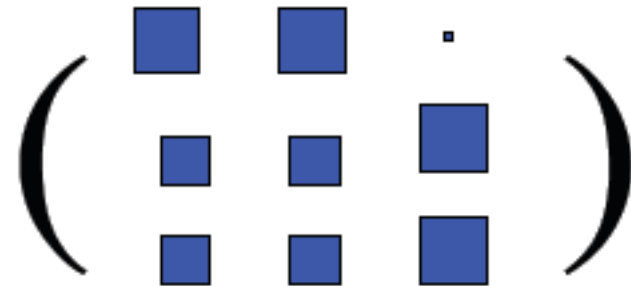
Unitary PMNS mixing matrix

Three observed flavors of neutrinos (ν_e, ν_μ, ν_τ) means U is represented by **three independent mixing angles** ($\theta_{12}, \theta_{23}, \theta_{13}$) and a CP violating phase δ

$$\theta_{12} = 33.6^\circ \pm 1.0^\circ$$

$$\theta_{23} = 45^\circ \pm 6^\circ \quad (90\% \text{CL})$$

$$\theta_{13} = 9.1^\circ \pm 0.6^\circ$$



Is θ_{23} mixing maximal (45°)?

Open questions about neutrino mixing

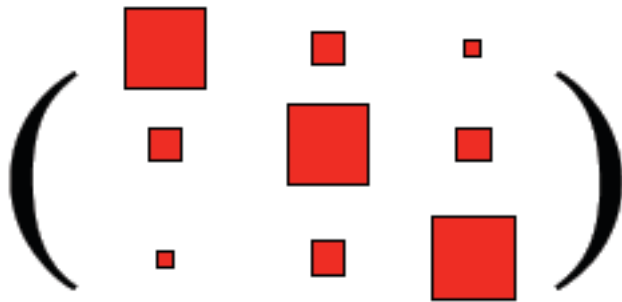
$$\begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix}$$

Flavor eigenstates (coupling to the W) Mass eigenstates (definite mass)

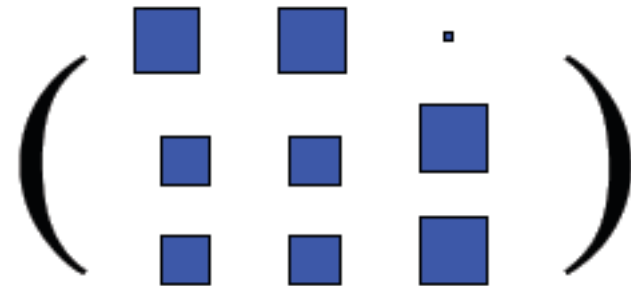
Unitary PMNS mixing matrix

Three observed flavors of neutrinos (ν_e, ν_μ, ν_τ) means U is represented by **three independent mixing angles** ($\theta_{12}, \theta_{23}, \theta_{13}$) and a CP violating phase δ

Quark mixing angles are small:



Neutrino mixing angles are large:



Why are quark and lepton mixing so different?

Open questions about neutrino mixing

$$\begin{array}{l} \text{Flavor eigenstates} \\ \text{(coupling to the W)} \end{array} \begin{pmatrix} \nu_e \\ \nu_\mu \\ \nu_\tau \end{pmatrix} = \begin{pmatrix} U_{e1} & U_{e2} & U_{e3} \\ U_{\mu1} & U_{\mu2} & U_{\mu3} \\ U_{\tau1} & U_{\tau2} & U_{\tau3} \end{pmatrix} \begin{pmatrix} \nu_1 \\ \nu_2 \\ \nu_3 \end{pmatrix} \begin{array}{l} \text{Mass eigenstates} \\ \text{(definite mass)} \end{array}$$

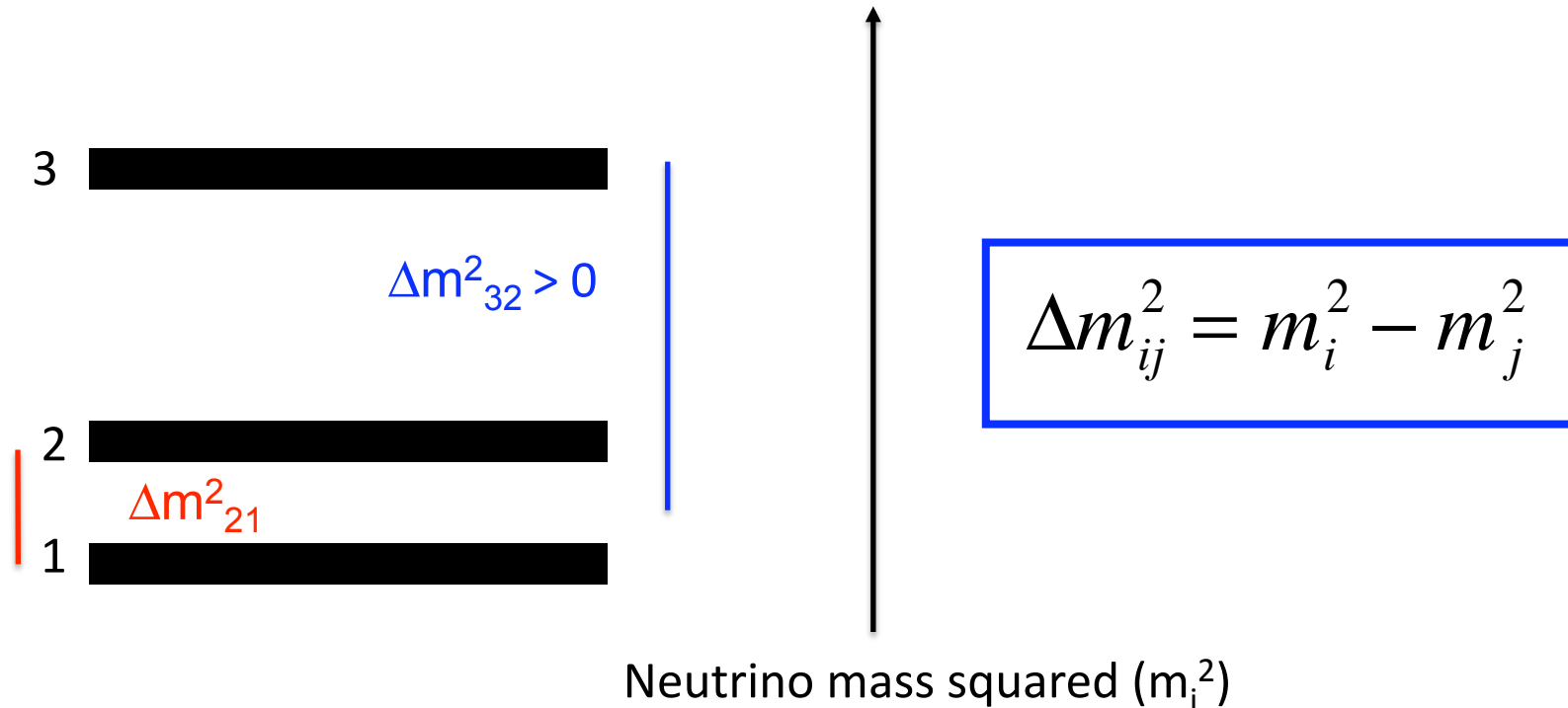
Unitary PMNS mixing matrix

Three observed flavors of neutrinos (ν_e, ν_μ, ν_τ) means U is represented by three independent mixing angles ($\theta_{12}, \theta_{23}, \theta_{13}$) and a **CP violating phase δ**

$$\delta_{\text{CP}} = ??$$

*Is there CP violation in the neutrino sector?
Is it large?*

Neutrino mass differences

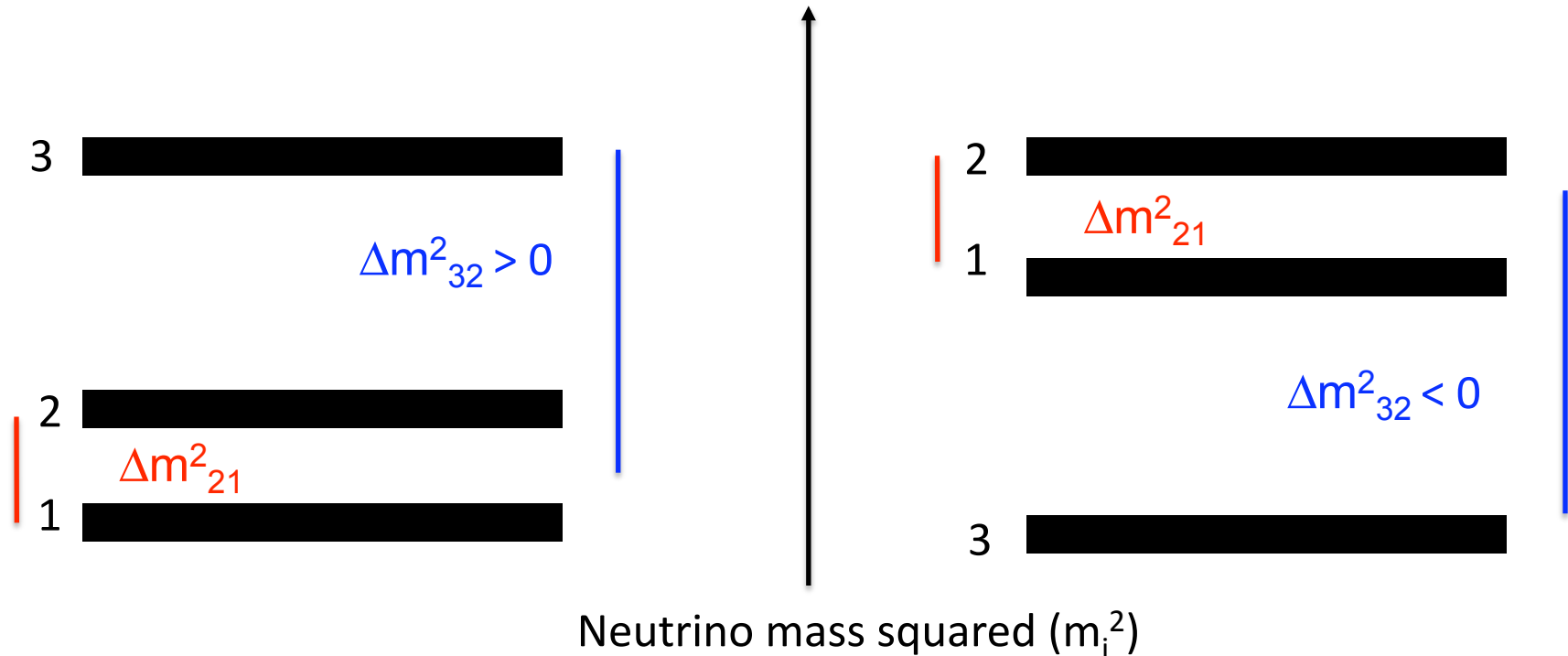


Three neutrino mass eigenstates mean two independent mass differences

Two observed mass “splittings”, determined from atmospheric and solar neutrino experiments, respectively

- $\Delta m^2(\text{atmospheric}) = |\Delta m_{32}^2| \sim 2.4 \times 10^{-3} \text{ eV}^2$
- $\Delta m^2(\text{solar}) = \Delta m_{21}^2 \sim 7.6 \times 10^{-5} \text{ eV}^2$

Open questions about neutrino mixing



The sign of Δm^2_{32} , or the “mass hierarchy” is still unknown

- Normal “hierarchy” is like quarks (m_1 is lightest, $\Delta m^2_{32} > 0$)
- Inverted hierarchy has m_3 lightest ($\Delta m^2_{32} < 0$)

Neutrino oscillation, revisited

$\Delta m_{32}^2 \gg \Delta m_{21}^2$, producing high frequency and low frequency oscillation terms

$$P_{\alpha\beta} = \delta_{\alpha\beta} - 4 \sum_{i>j} \text{Re}[U_{\beta i} U_{\alpha i}^* U_{\beta j}^* U_{\alpha j}] \sin^2 \left(\frac{\Delta m_{ij}^2 L}{4E} \right) + 2 \sum_{i>j} \text{Im}[U_{\beta i} U_{\alpha i}^* U_{\beta j}^* U_{\alpha j}] \sin \left(\frac{\Delta m_{ij}^2 L}{2E} \right)$$

If choose L, E, such that $\sin^2(\Delta m_{32}^2 L/E)$ is of order 1, then Δm_{21}^2 terms will be small. Then...

ν_μ "disappear" into ν_e, ν_τ

$$P(\nu_\mu \rightarrow \nu_\mu) \cong 1 - \sin^2 2\theta_{23} \sin^2 \left(\frac{\Delta m_{32}^2 L}{4E} \right)$$

A small fraction of ν_e will "appear"

$$\Delta m_{31}^2 \sim \Delta m_{32}^2$$

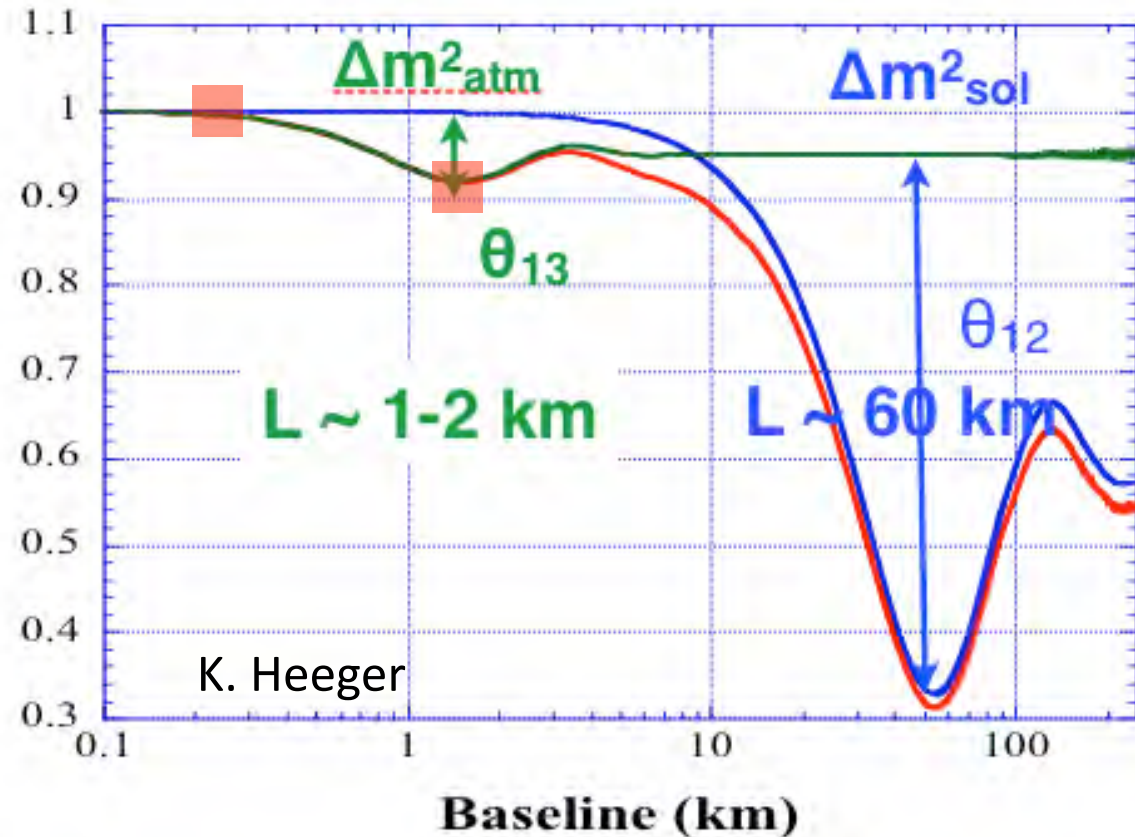
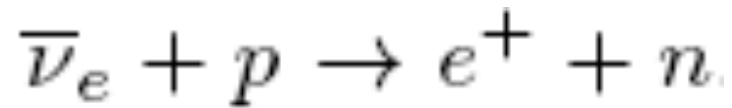
Only leading order term shown

$$P(\nu_\mu \rightarrow \nu_e) \cong \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right)$$

Disappearance measurements: reactors

Antineutrino disappearance from
(a group of) reactors

Measure rate with inverse beta decay:



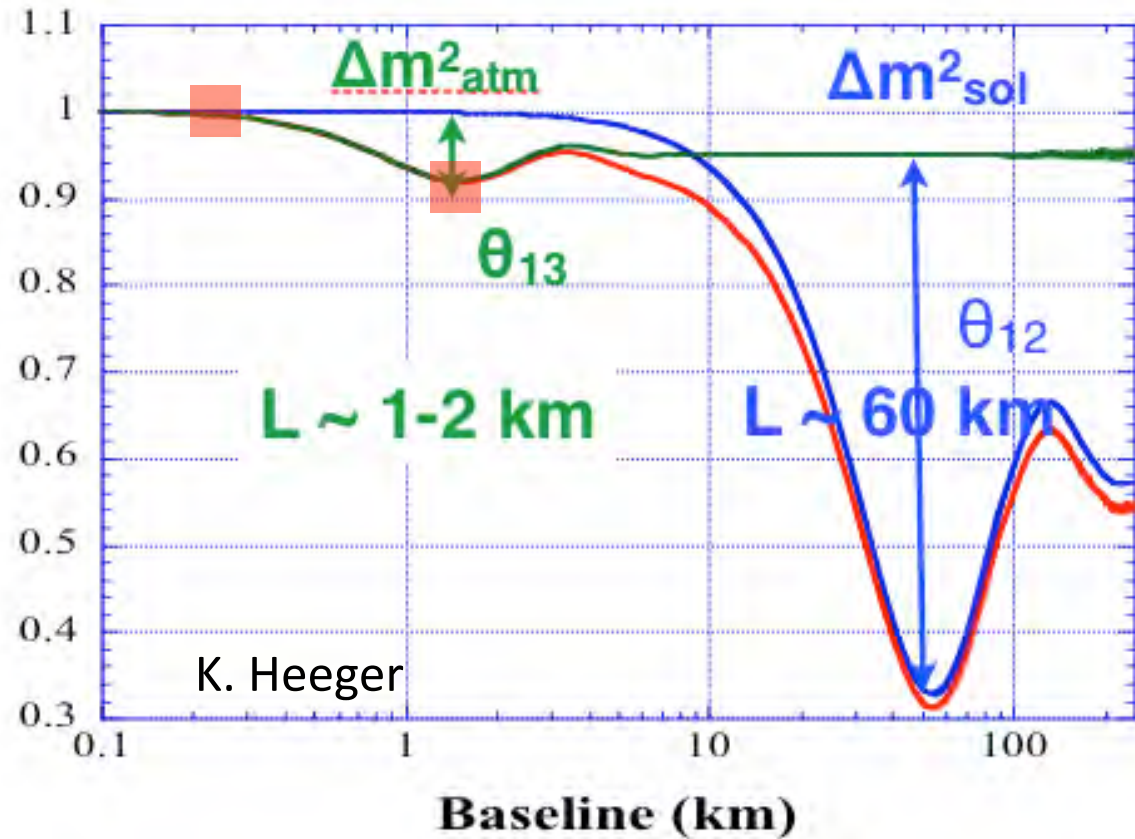
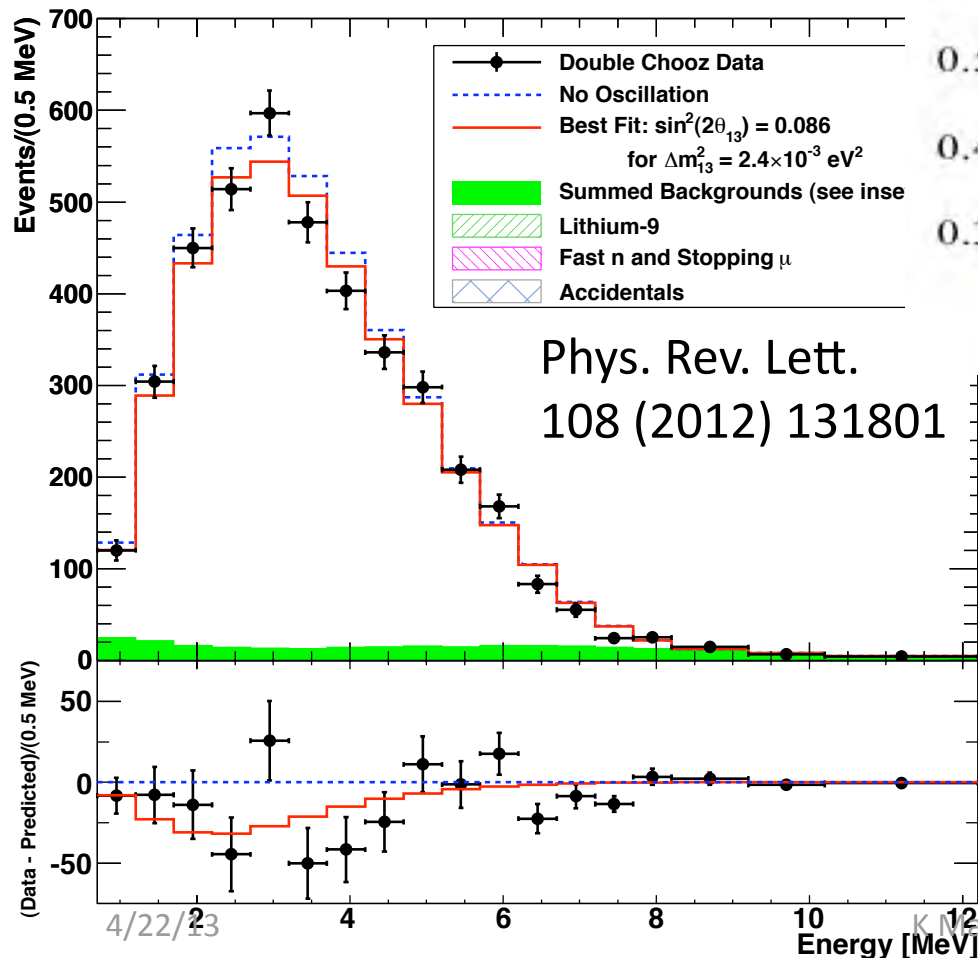
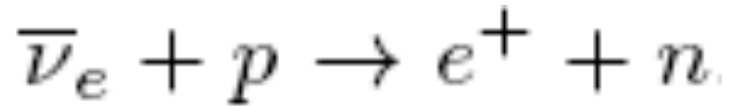
Determine θ_{13} from difference between near and far detectors from the reactor complex

$$P(\nu_e \rightarrow \nu_{x \neq e}) \approx \sin^2 2\theta_{13} \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right)$$

Disappearance measurements: reactors

Antineutrino disappearance from
(a group of) reactors

Measure rate with inverse beta decay:



Determine θ_{13} from difference between near and far detectors from the reactor complex

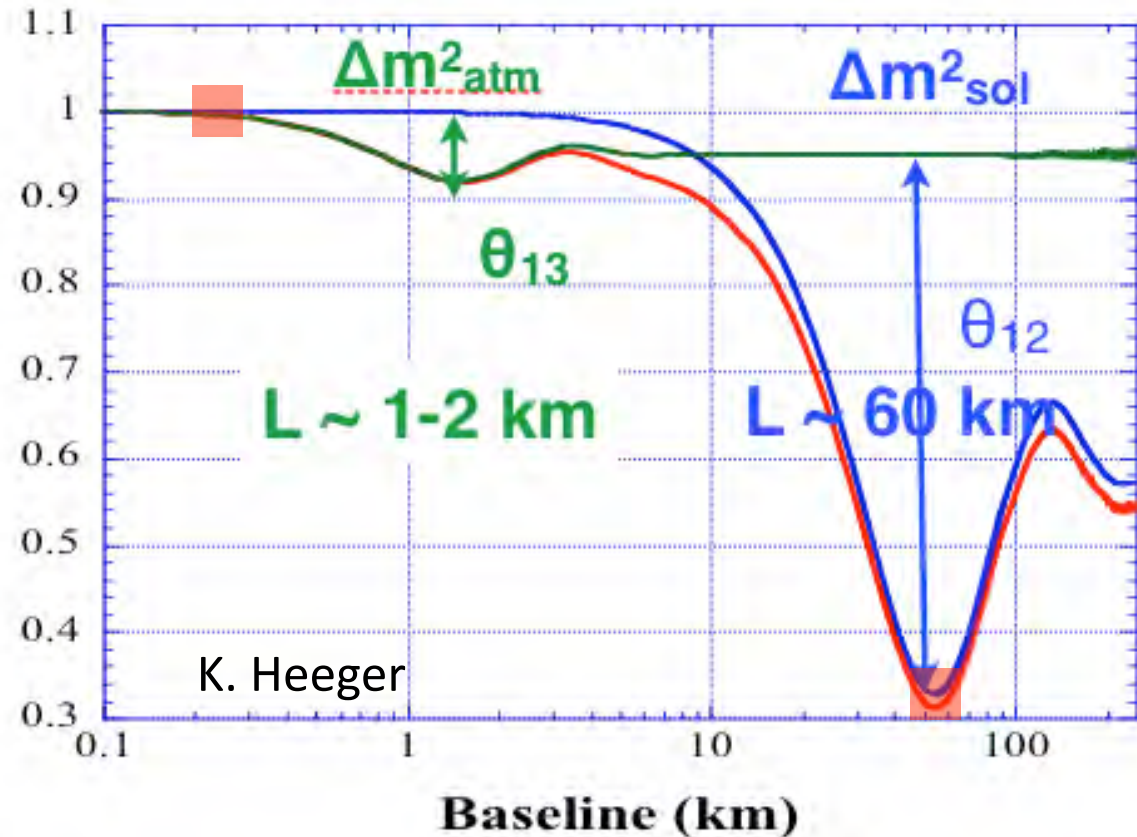
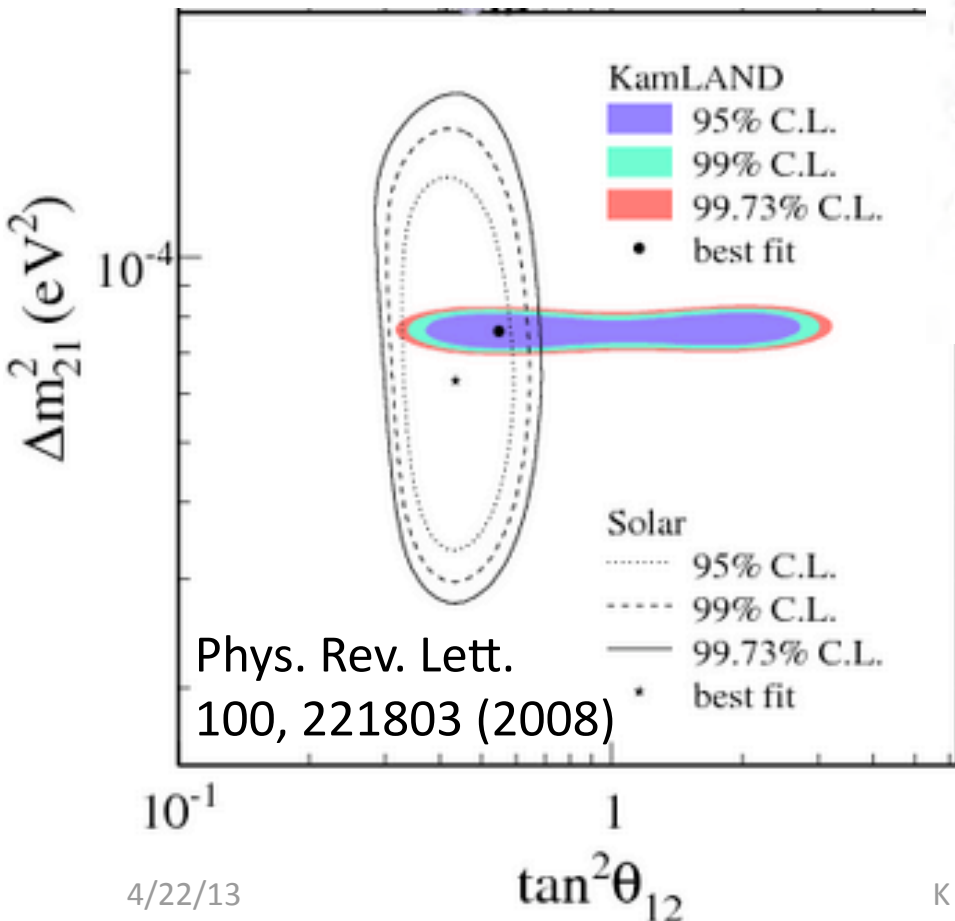
$$\theta_{13} = 9.1^\circ \pm 0.6^\circ \quad \text{PDG2012}$$

Daya Bay, RENO, Double Chooz collaborations

Disappearance measurements

Can also use reactor sources to measure solar mixing parameter (KamLAND)

Complementary to solar neutrino experiments (e.g. SNO)



Determine Δm_{21}^2 , θ_{12} from the distorted energy spectrum

$$\Delta m_{21}^2 = 7.6 \times 10^{-5} eV^2$$

$$\theta_{12} = 33.6^\circ \pm 1.0^\circ \quad \text{PDG2012}$$

Disappearance with atmospheric sources

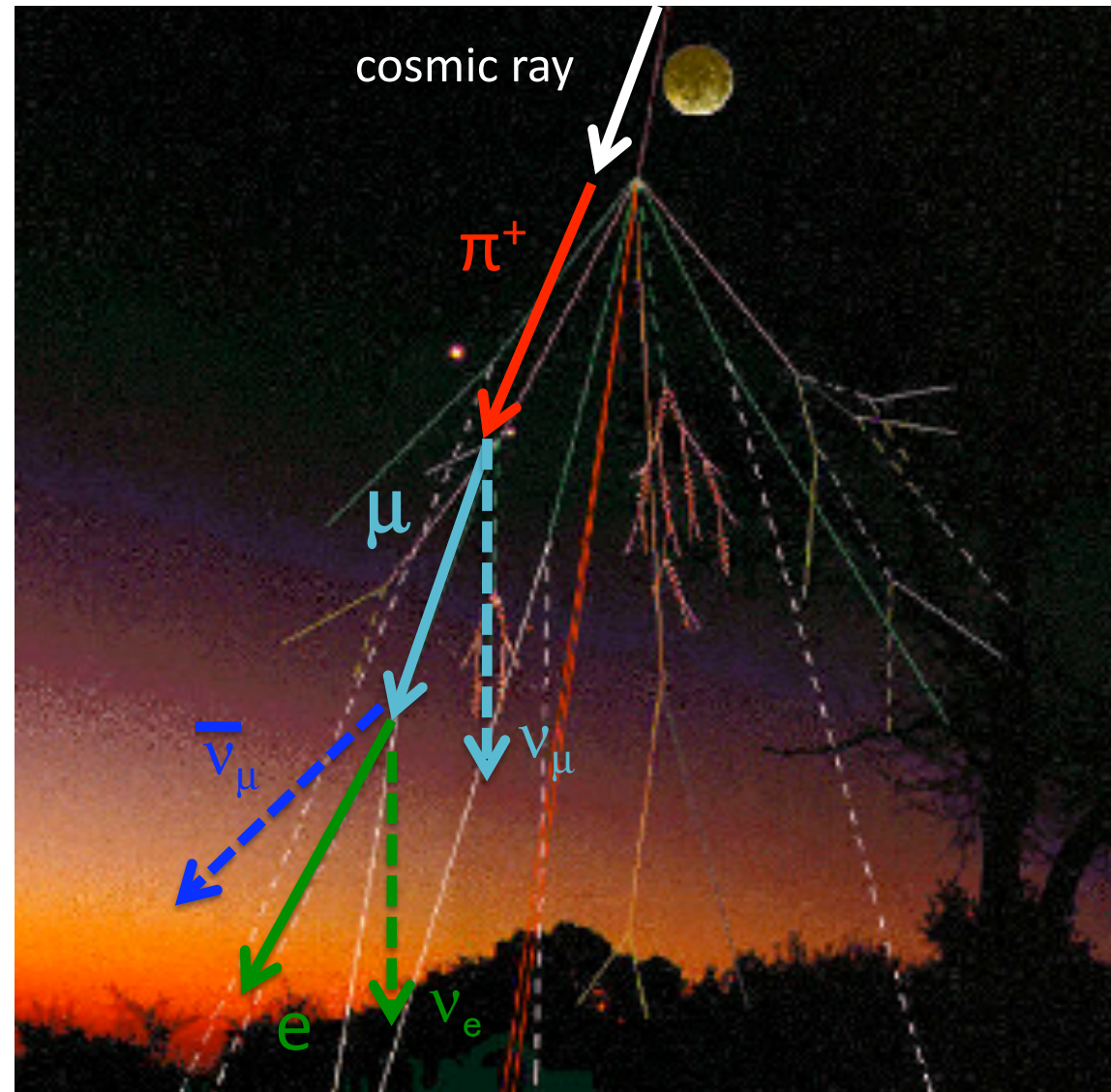
Muon neutrino disappearance from atmospheric neutrinos

Cosmic rays (protons, He, etc) hit nuclei in atmosphere:

- Produces muon neutrinos, muon antineutrinos and electron neutrinos

Need a large detector and time:

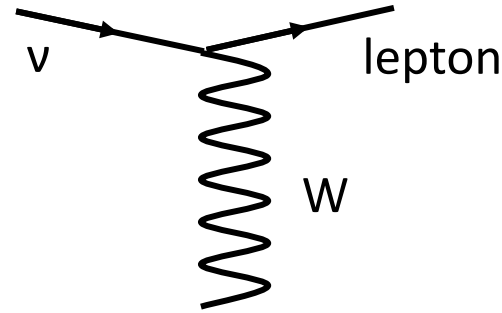
- MINOS
- IceCube
- Super-Kamiokande



Detecting atmospheric neutrinos

Detect neutrino interactions with charged current interactions

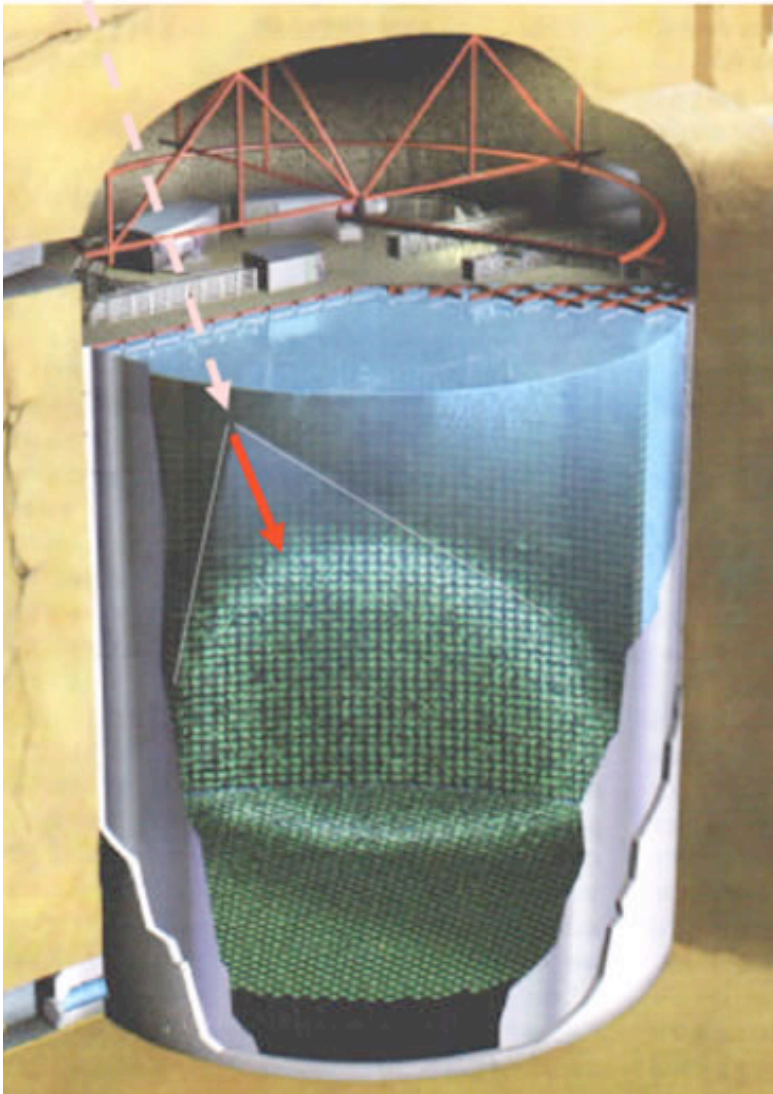
Charged Current (CC)



$$\nu_e \rightarrow e$$

$$\nu_\mu \rightarrow \mu$$

$$\nu_\tau \rightarrow \tau$$



Super-Kamiokande: 22.5kton fiducial volume
water Cherenkov detector

Charged particles emit Cherenkov light

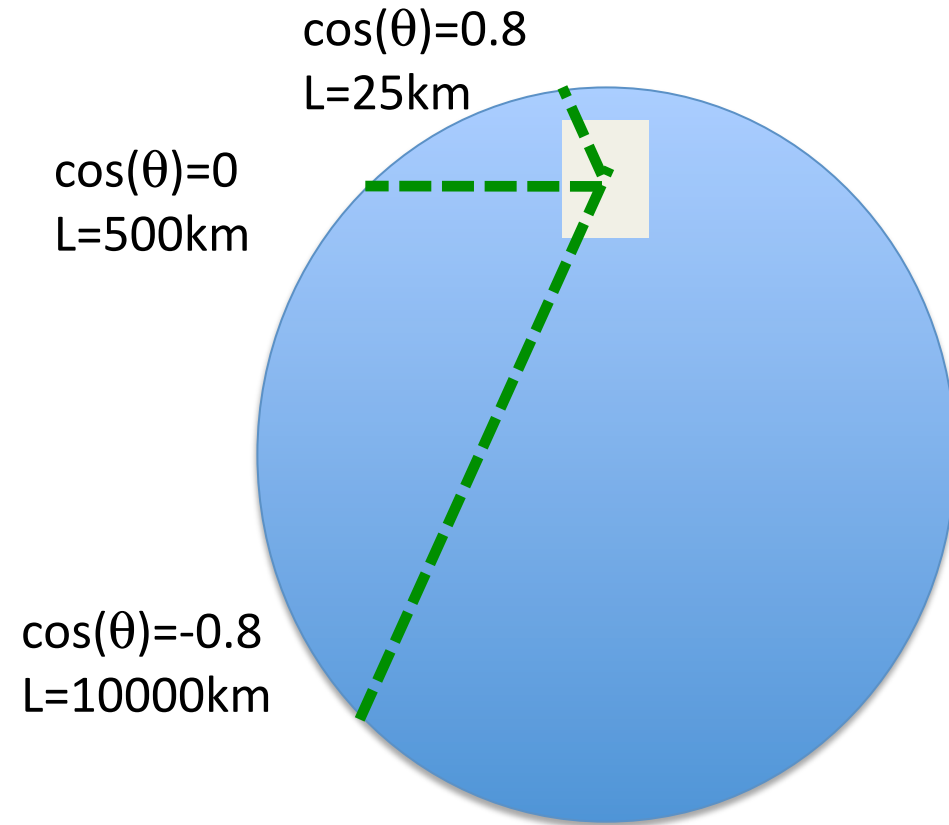
- Ring is imaged by 11,129 PMTs; ring is used to determine the lepton direction and momentum
- Entering (non-neutrino) events are rejected by outer veto region
- Select ν_e or ν_μ events from ring shape and topology

Disappearance measurements: atmospheric nu

Oscillation probability changes with L:

- Distance from production to detector
- As a function of angle from the zenith $\cos(\theta)$

$$P(\nu_\mu \rightarrow \nu_\mu) \cong 1 - \sin^2 2\theta_{23} \sin^2 \left(\frac{1.27 \Delta m_{32}^2 L}{E} \right)$$

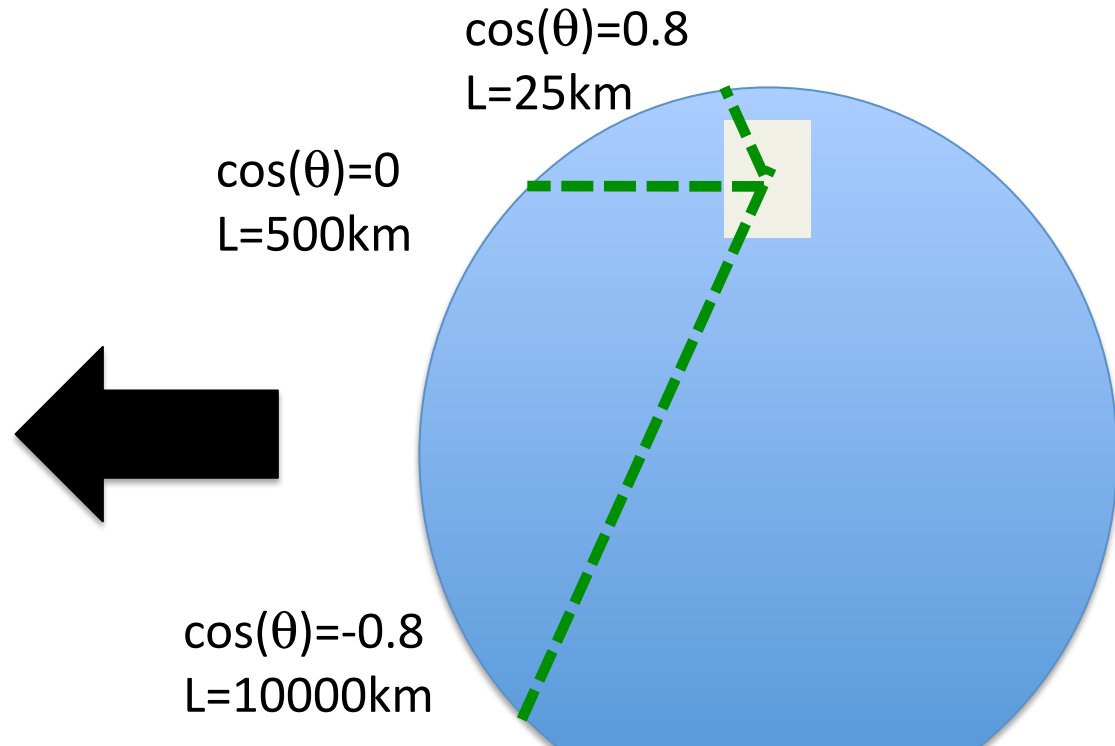
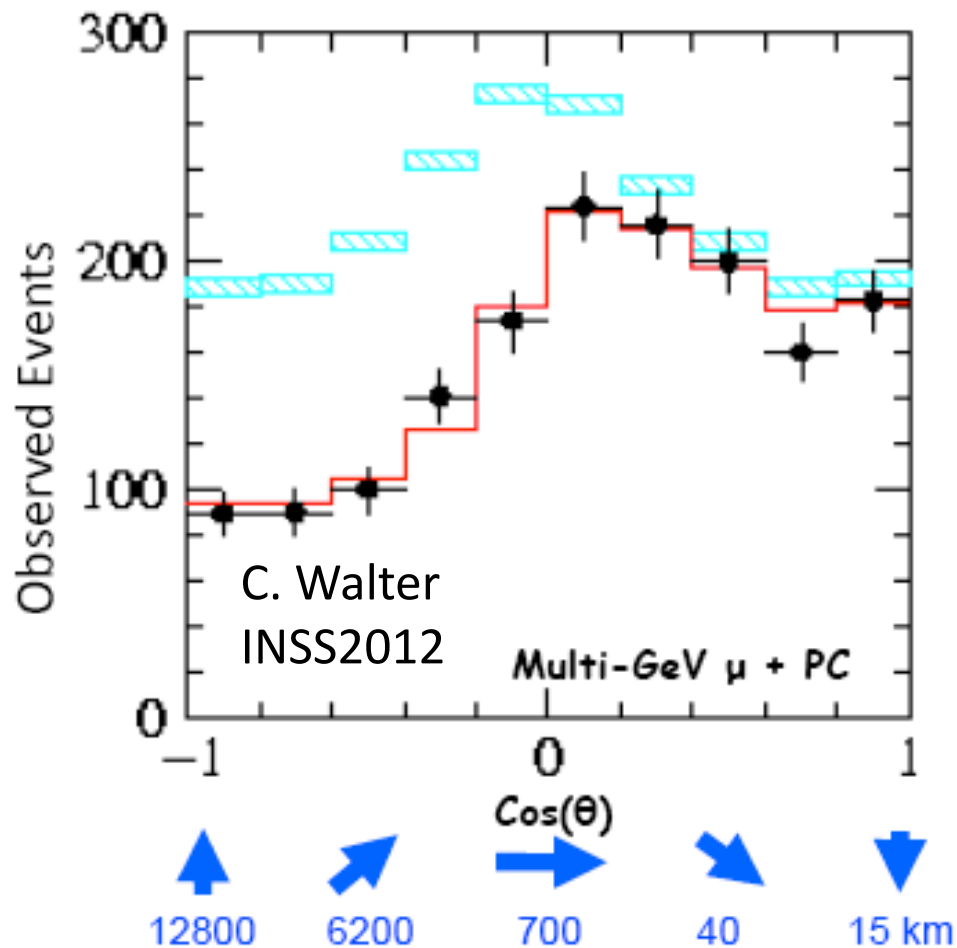


Disappearance with atmospheric sources

Oscillation probability changes with L:

- Distance from production to detector
- As a function of angle from the zenith $\cos(\theta)$

$$P(\nu_\mu \rightarrow \nu_\mu) \cong 1 - \sin^2 2\theta_{23} \sin^2 \left(\frac{1.27 \Delta m_{32}^2 L}{E} \right)$$



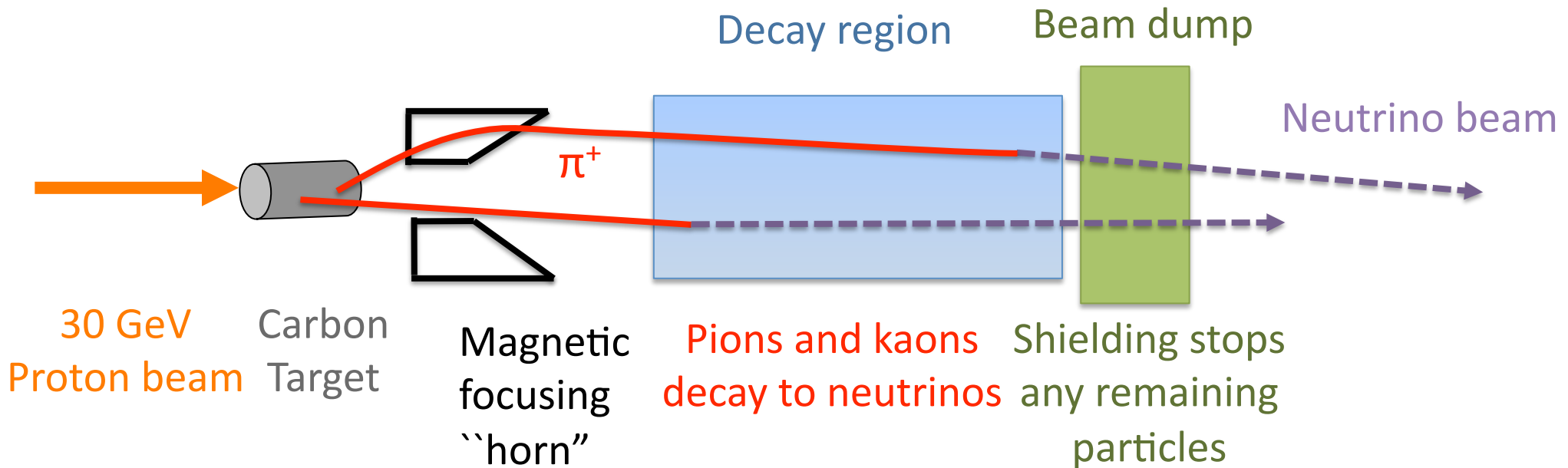
Determine $|\Delta m_{32}^2|$, θ_{23} from atmospheric and accelerator neutrinos:

$$\Delta m_{32}^2 = 2.35 \times 10^{-3} eV^2$$

$$\theta_{23} = 45^\circ \pm 6^\circ$$

PDG2012

Accelerator-based neutrino sources

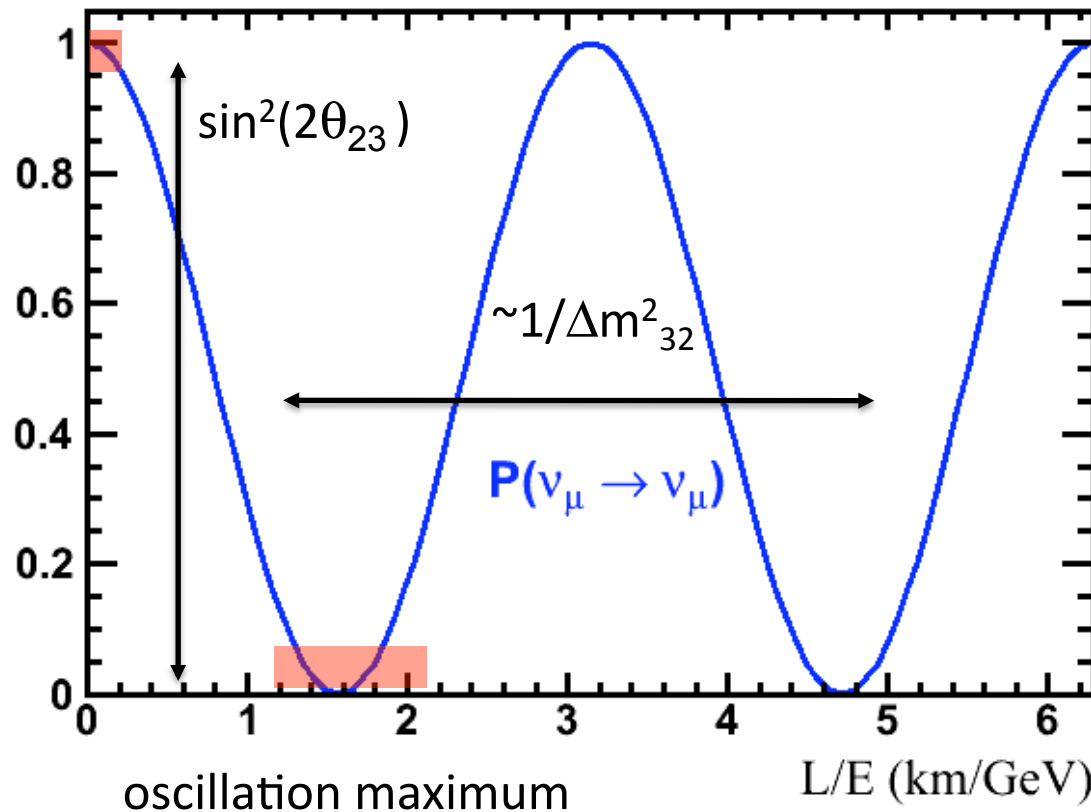


Advantages of an accelerator-based neutrino source:

1. >99% muon neutrino flavor, small ν_e component from muon, kaon decay
2. Intensity of proton beam increases neutrino rate
3. Switch magnetic horn polarization to focus π^- and produce an antineutrino beam
4. Tunable neutrino energy spectrum optimized for oscillation

Disappearance with accelerator sources

$$P(\nu_\mu \rightarrow \nu_\mu) \cong 1 - \sin^2 2\theta_{23} \sin^2 \left(\frac{\Delta m_{32}^2 L}{4E} \right)$$

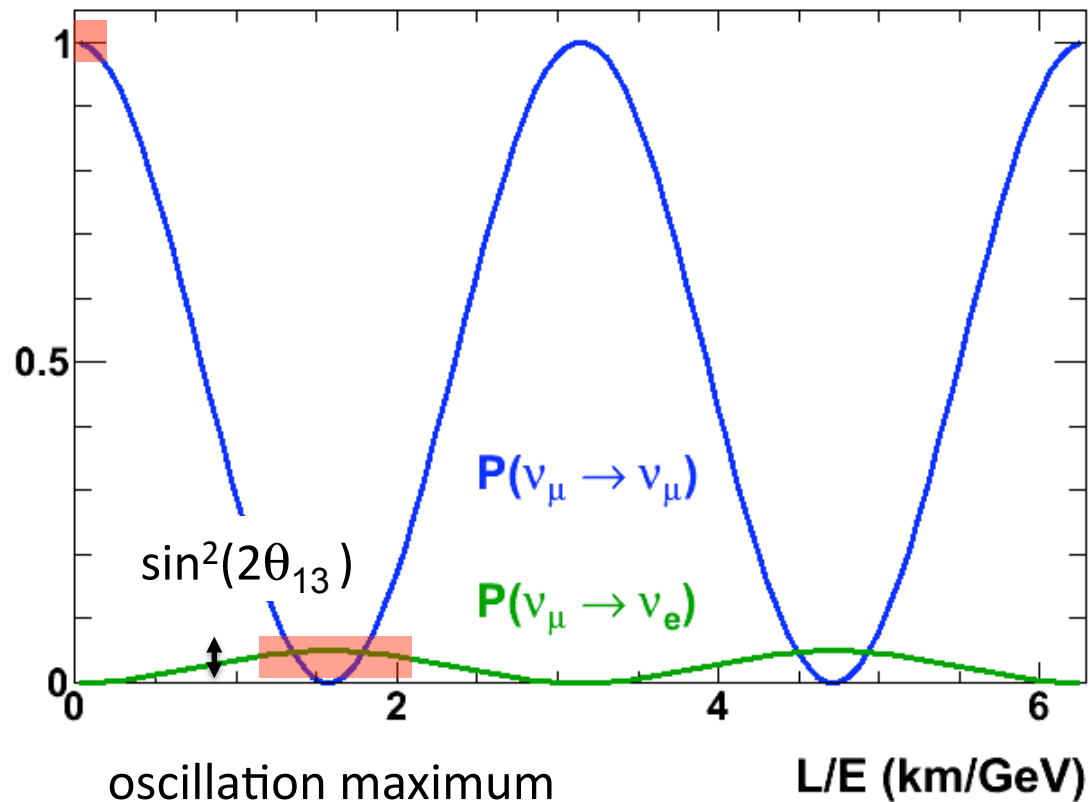


Typical experimental setup:

- Measure ν_μ rate at $L=0$
- Measure ν_μ rate at $L \sim$ oscillation maximum
- Infer oscillation parameters from rate change (θ_{23}) and distortion of spectrum (Δm_{32}^2)

Appearance with accelerator sources

$$P(\nu_\mu \rightarrow \nu_e) \cong \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right)$$

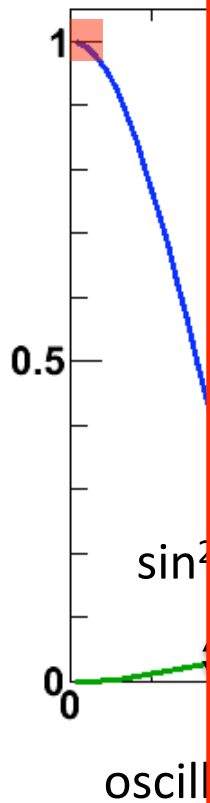


Typical experimental setup:

- Measure ν_μ rate* at $L=0$
*In practice also measure any ν_e background rates at $L=0$
- Measure ν_e rate at $L \sim$ oscillation maximum
- Infer oscillation parameters from rate change (θ_{13})

Appearance with accelerator sources

$$P(\nu_\mu \rightarrow \nu_e) \cong \sin^2 2\theta_{13} \sin^2 \theta_{23} \sin^2 \left(\frac{\Delta m_{31}^2 L}{4E} \right)$$



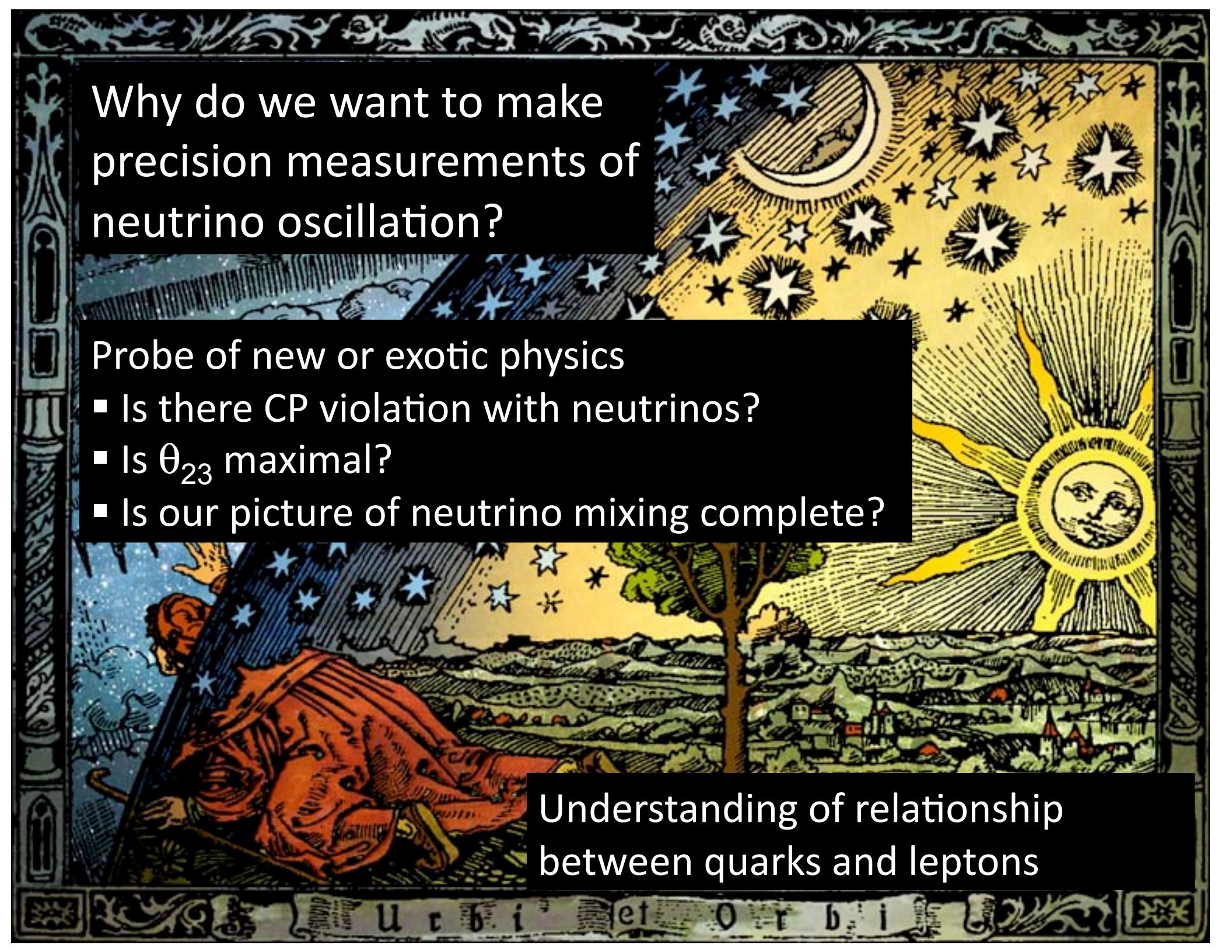
Subleading terms of ν_μ to ν_e appearance depend on δ_{CP} , mass hierarchy

Requires precision measurements of:

$$\Delta m_{32}^2, \theta_{23}, \Delta m_{21}^2, \theta_{12} \text{ and } \theta_{13}$$

Measurements of ν_μ to ν_e appearance are sensitive to new or exotic physics

rs



Why do we want to make precision measurements of neutrino oscillation?

Probe of new or exotic physics

- Is there CP violation with neutrinos?
- Is θ_{23} maximal?
- Is our picture of neutrino mixing complete?

Understanding of relationship between quarks and leptons

The Tokai-to-Kamioka (T2K) experiment

“Long baseline” ($L \sim 295\text{km}$) neutrino experiment designed to measure ν_e appearance (θ_{13}) and ν_μ disappearance (Δm^2_{32} , θ_{23})

Far detector

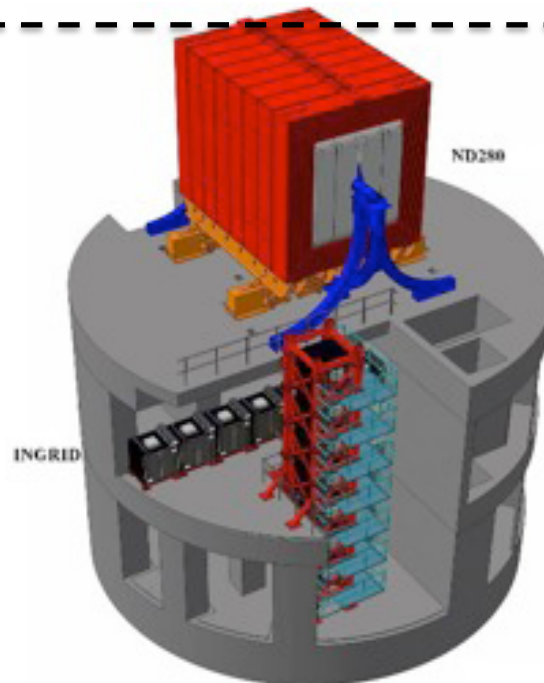
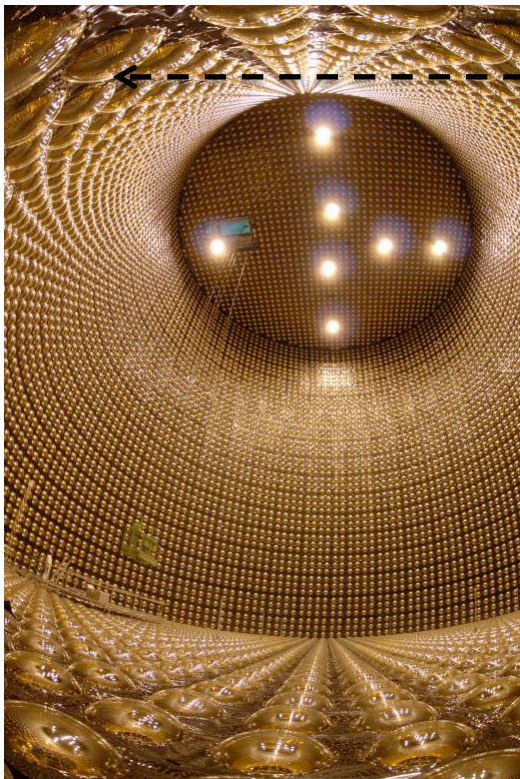
Super-Kamiokande

Near detectors

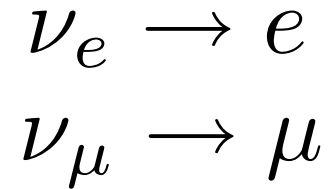
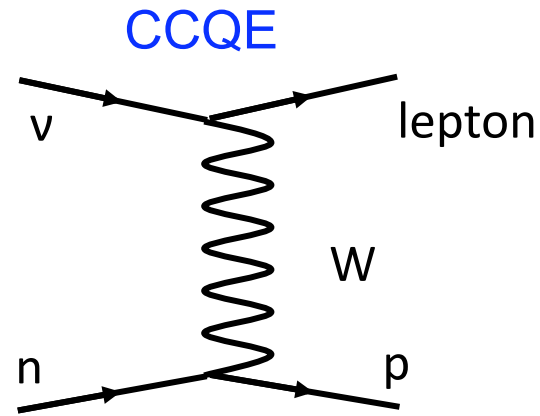
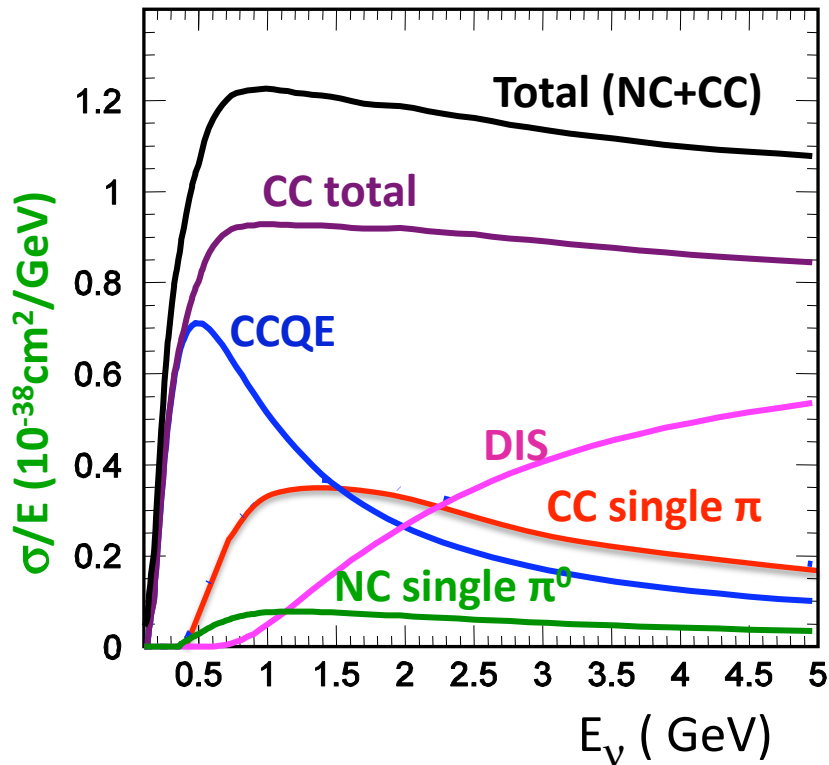
ND280

Neutrino beam

Peak $E_\nu \sim 0.6\text{ GeV}$



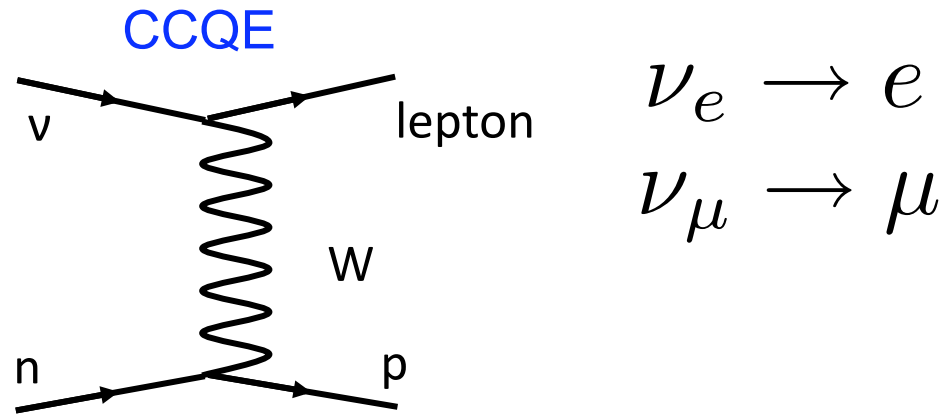
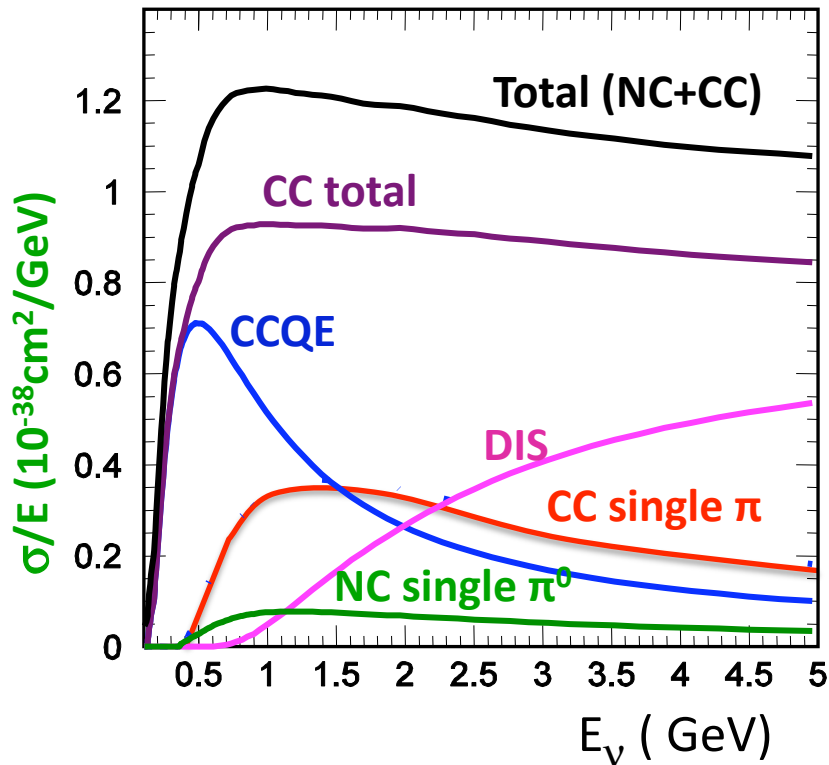
Neutrino interactions at T2K



At $E_\nu \sim 0.6$ GeV, most neutrino interactions are **Charged Current Quasi Elastic (CCQE)**

- Neutrino flavor determined from flavor of outgoing lepton

Neutrino interactions at T2K



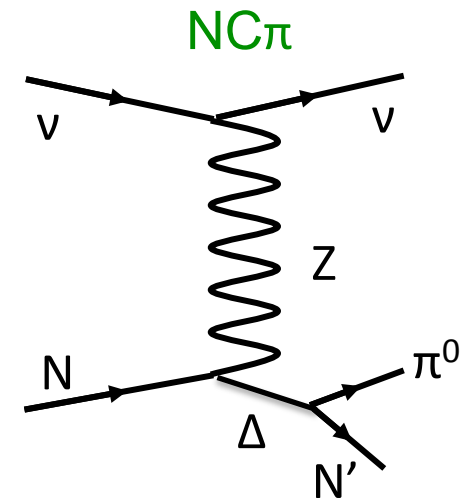
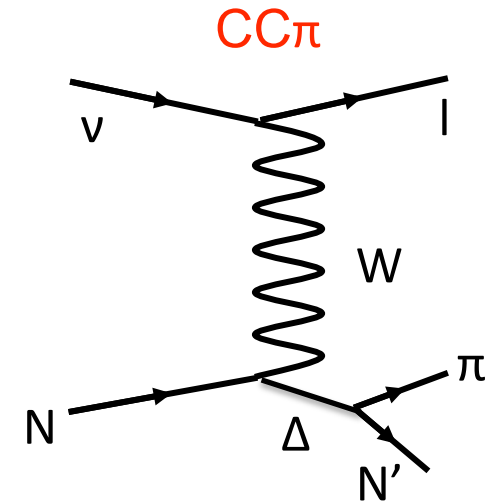
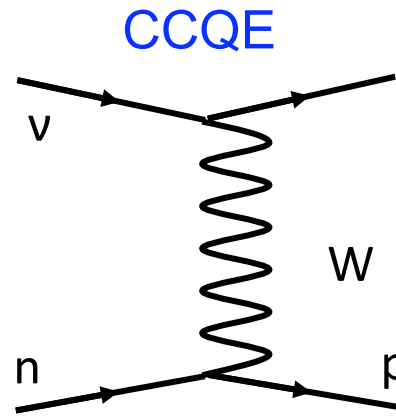
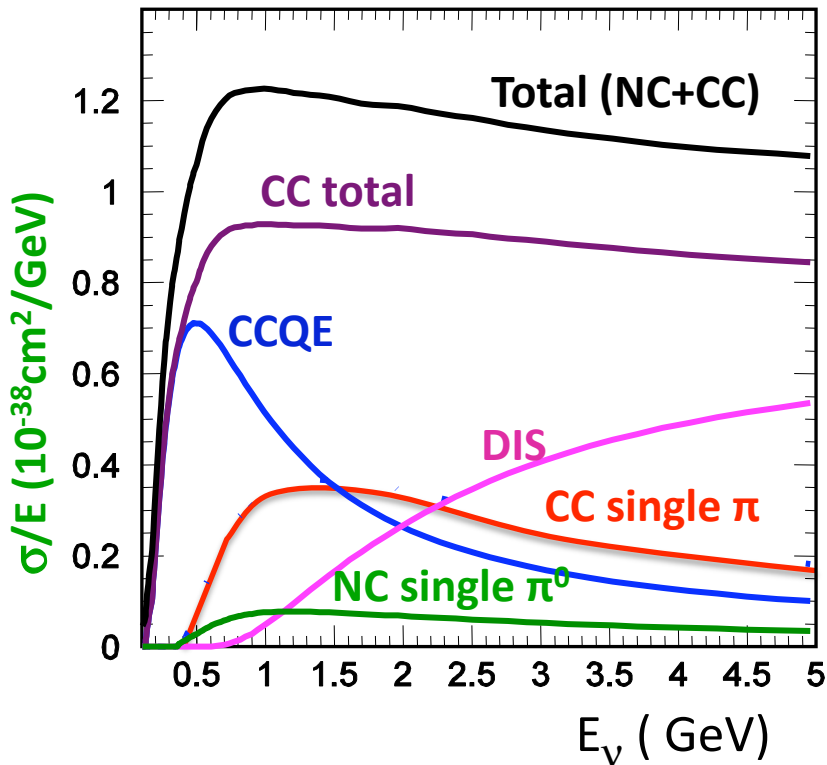
At $E_\nu \sim 0.6$ GeV, most neutrino interactions are **Charged Current Quasi Elastic (CCQE)**

- Neutrino flavor determined from flavor of outgoing lepton
- Infer neutrino properties from the muon (or electron) momentum and angle:

$$E_\nu^{QE} = \frac{m_p^2 - m_n'^2 - m_\mu^2 + 2m_n' E_\mu}{2(m_n' - E_\mu + p_\mu \cos \theta_\mu)}$$

*2 body kinematics
Assumes the target
nucleon is at rest*

Neutrino interactions at T2K



Other interactions important for T2K analysis:

- Charged current single pion production (**CC π**)
 - Lepton and pion (charged or neutral) produced
- Neutral current single pion production (**NC π^0**)
 - No lepton in final state (happens for all flavors)
 - Only neutral pion (π^0) produced in detector
 - Can mimic ν_e signal at Super-Kamiokande

ν_e appearance analysis

$$N(\nu_e) = \Phi(E_\nu) \sigma(E_\nu) \epsilon P(\nu_\mu \rightarrow \nu_e)$$

Fit the observed rate to determine $\sin^2 2\theta_{13}$ Also depends on:

Neutrino flux
prediction

Neutrino cross section
model

Far detector selection,
efficiency

ν_e appearance analysis

$$N(\nu_e) = \Phi(E_\nu) \sigma(E_\nu) \epsilon P(\nu_\mu \rightarrow \nu_e)$$

Fit the observed rate to determine $\sin^2 2\theta_{13}$ Also depends on:

Neutrino flux prediction

Neutrino cross section model

Far detector selection, efficiency

We reduce the error on the rate of ν_e with the near detector:

$$N(\nu_\mu) = \Phi(E_\nu) \sigma(E_\nu) \epsilon$$

Neutrino flux prediction

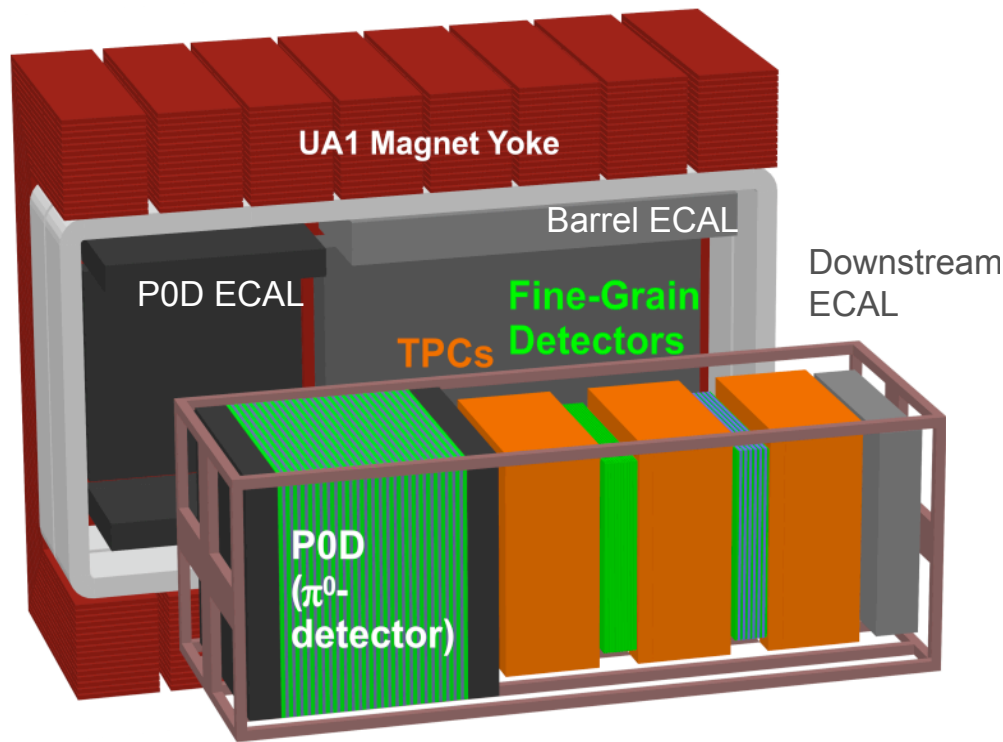
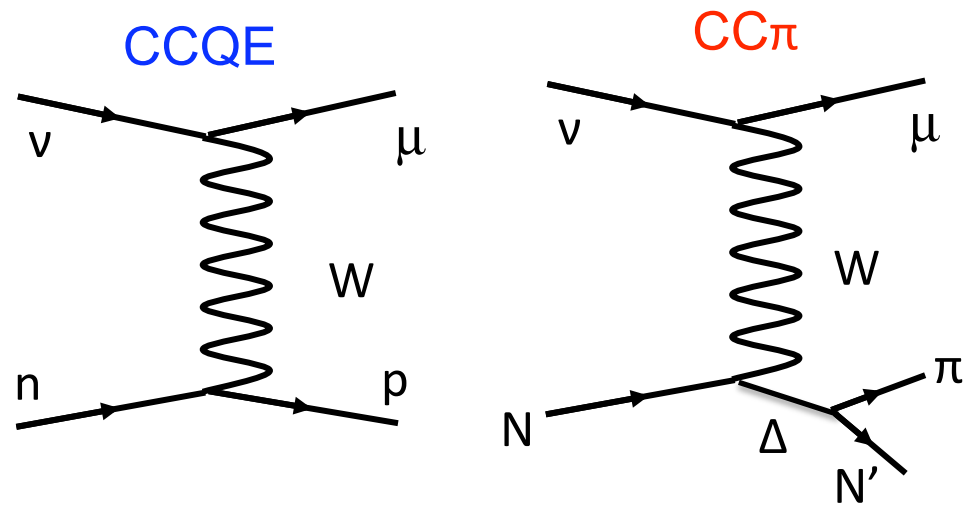
Neutrino cross section model

Near detector selection, efficiency

*Challenge as osc analysis co-convenor:
correlate the physics, coordinate the students, convince the physicists*

Near detectors (ND280)

Measure unoscillated ν_μ (CC) rate:
Select nothing coming in (neutrino)
and muons coming out (ν_μ)



Analysis this year relies on “Tracker”,
constructed at TRIUMF

- 2 scintillator based tracking detectors (FGDs)
- 3 time projection chambers (TPCs)
- Placed inside the UA1 magnet

Additional detectors include:

- P0D (π^0 detector)
- Electromagnetic calorimeters
- Muon range detectors

Selecting CC ν_μ interactions

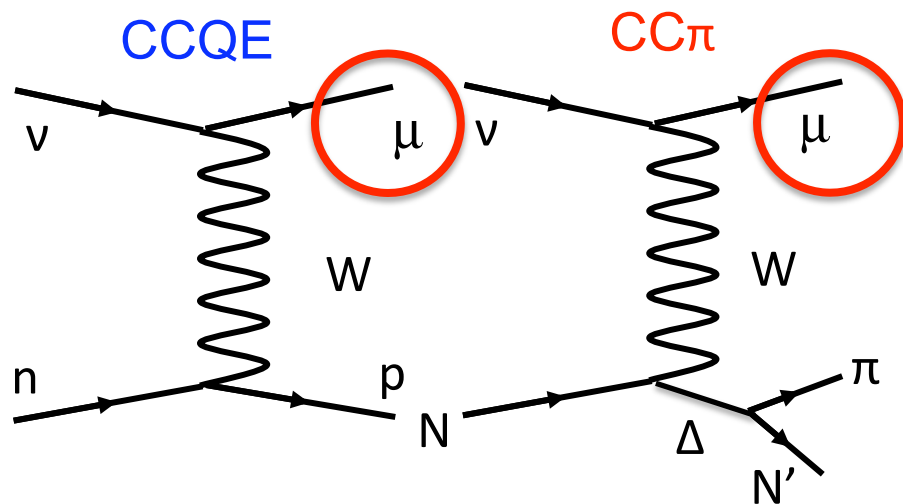
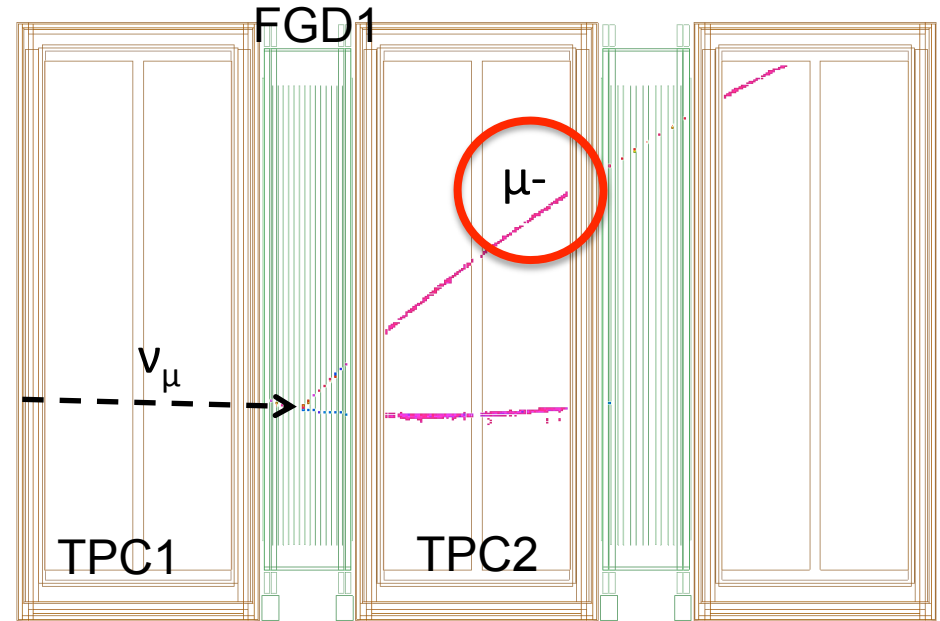
Measure unoscillated ν_μ (CC) rate

1. Neutrino interaction in FGD1

- Veto events with TPC1 tracks
- Events within FGD1 fiducial volume

2. Select highest momentum, negative curvature track as μ^- candidate

- Energy loss of the track in TPC also consistent with muon hypothesis



Selecting CC ν_μ interactions

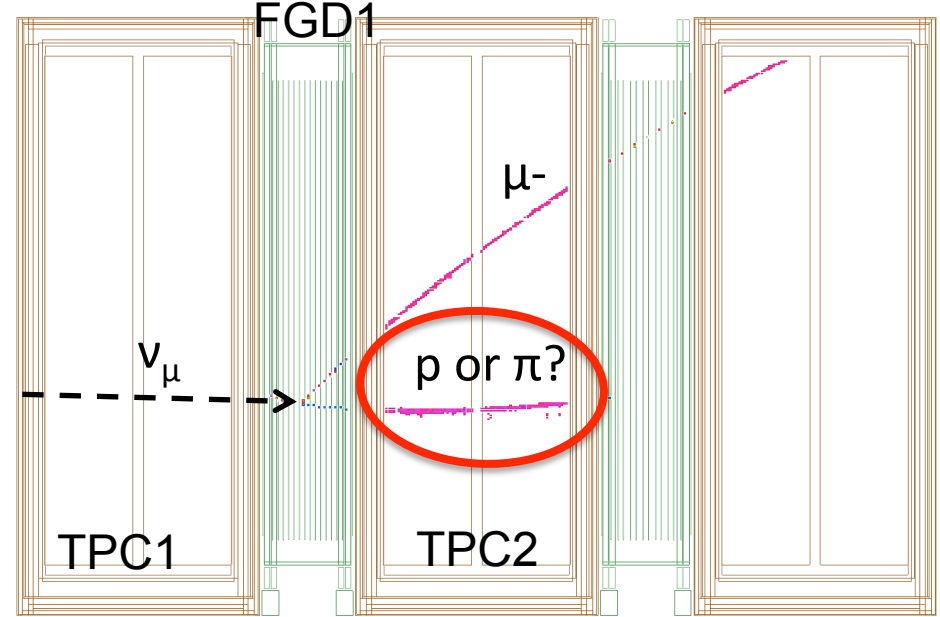
Measure unoscillated ν_μ (CC) rate

1. Neutrino interaction in FGD1

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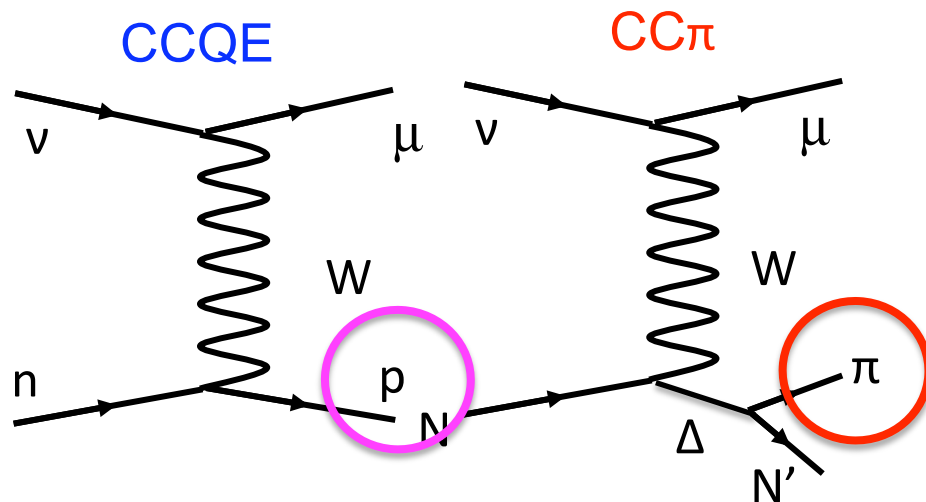
Further separate sample into two categories to increase sensitivity to cross section:

CCQE enhanced:

- 1 TPC-FGD1 matched track
- no decay electron in FGD1

CCnonQE enhanced:

- all other CC interactions



Near detector rate constraint

Tune flux, cross section models with a likelihood fit

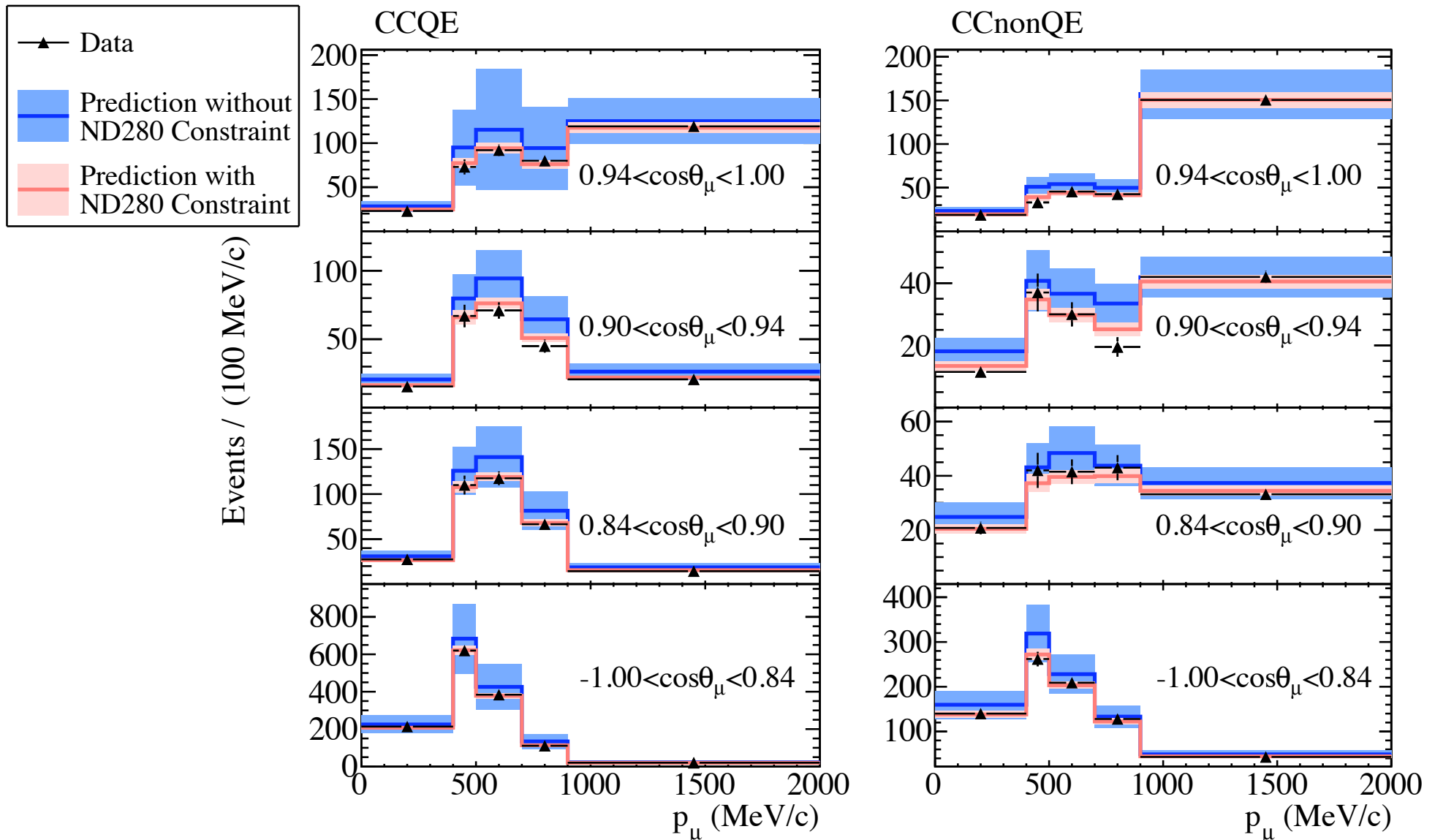
- p - θ distribution is sensitive to rate ($\Phi \times \sigma$)

$$E_\nu^{QE} = \frac{m_p^2 - m_n'^2 - m_\mu^2 + 2m_n' E_\mu}{2(m_n' - E_\mu + p_\mu \cos \theta_\mu)}$$

- Fit includes information on flux, cross sections from external measurements (e.g. beam monitors, neutrino cross section measurements)
- Shared flux, similar CC cross section composition of near and far detector selections

$$N(\nu_e) = \Phi(E_\nu) \sigma(E_\nu) \epsilon P(\nu_\mu \rightarrow \nu_e)$$
$$N(\nu_\mu) = \Phi(E_\nu) \sigma(E_\nu) \epsilon$$

Results of near detector rate fit



- Rate changed by no more than 10% across all energies
- CC cross sections, ν_μ flux uncertainties reduced substantially
- $\Delta\chi^2 = 29.1, p=0.925$

Expected number of ν_e candidates

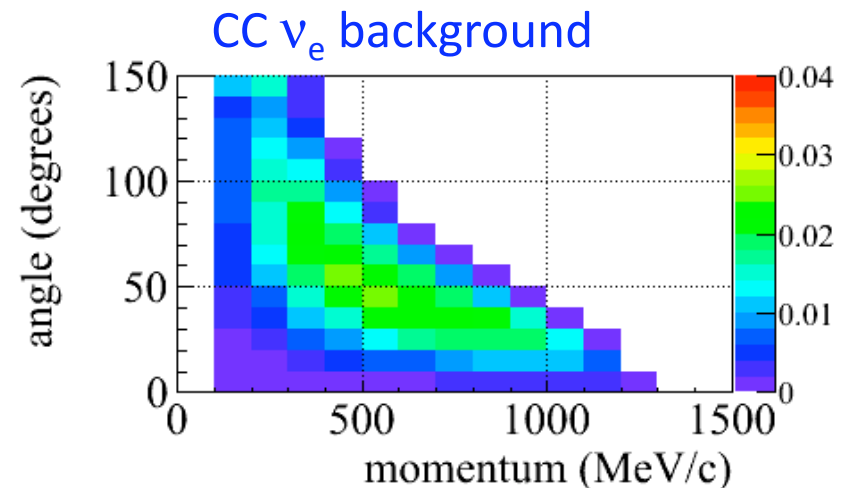
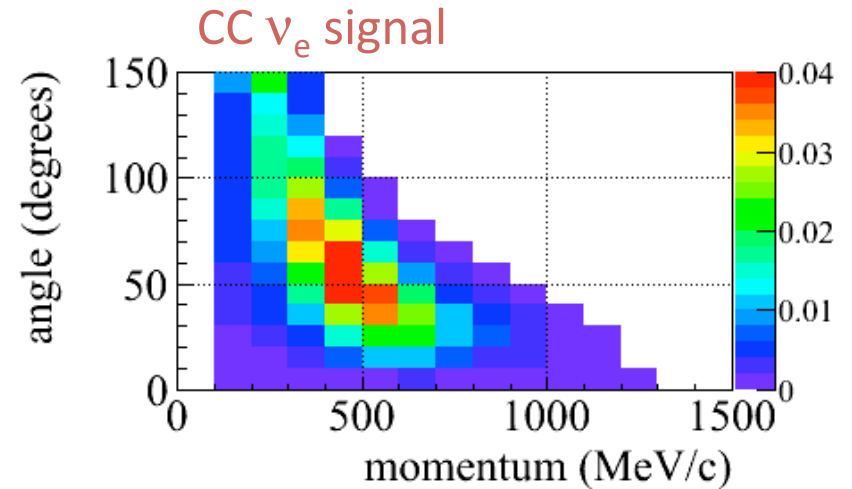
After ND280 tuning, expect ~ 11 events with ν_μ to ν_e oscillation, 3 without

- Rate, p - θ kinematics of events distinguishes signal from background

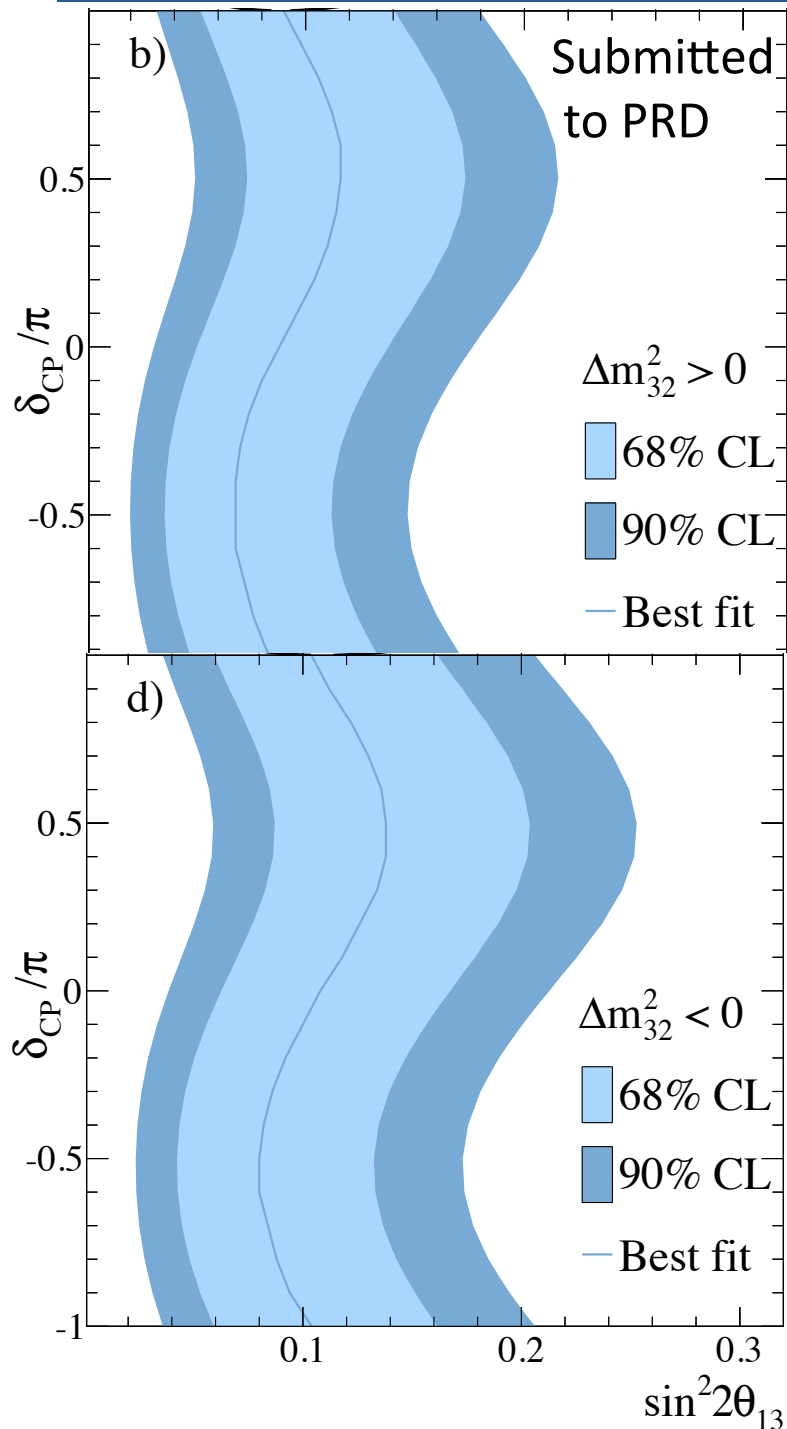
Signal (ν_μ to ν_e osc)	# events
@ $\sin^2 2\theta_{13}=0.1, \delta_{cp}=0$	8.2

ν_e signal @ $\Delta m_{32}^2 = 2.4 \times 10^{-3} \text{ eV}^2, \sin^2 2\theta_{23}=1.0$

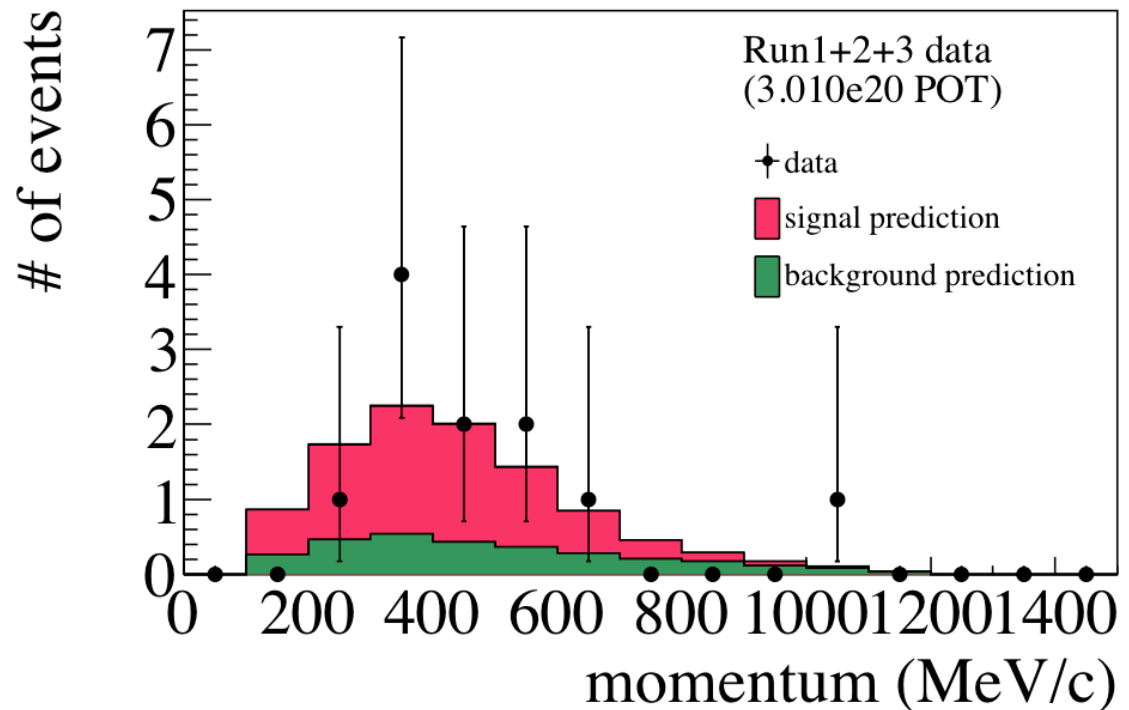
Background	# events
beam $\nu_e + \bar{\nu}_e$	1.8
$\nu_\mu + \bar{\nu}_\mu$ (mainly NC) background	1.3
osc through θ_{12}	0.2
total:	3.3 ± 0.4 (sys)



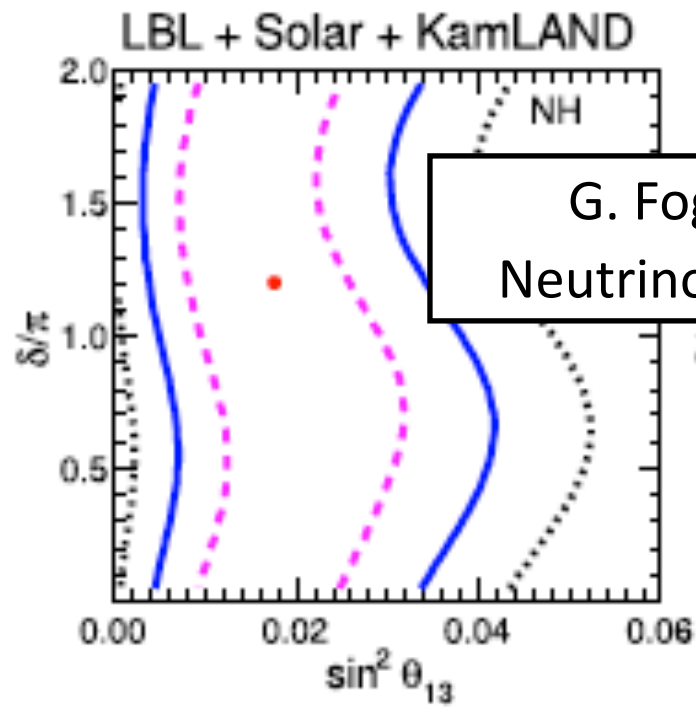
ν_e appearance results



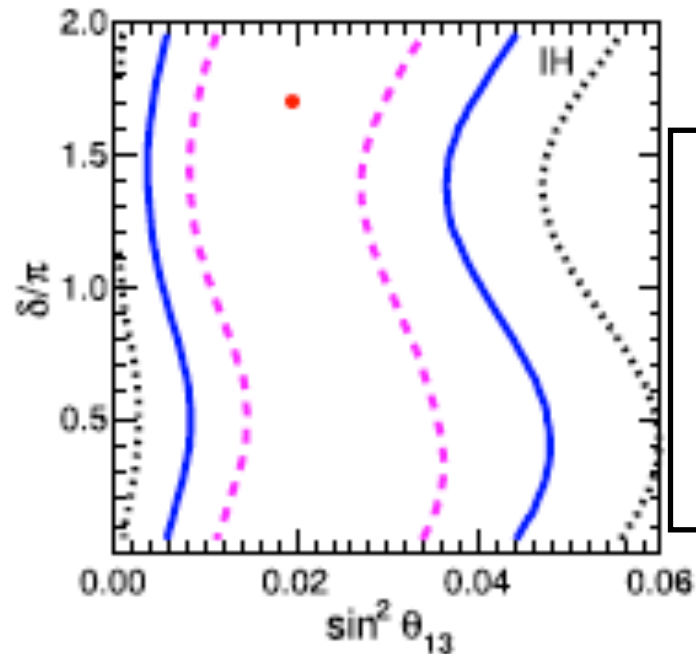
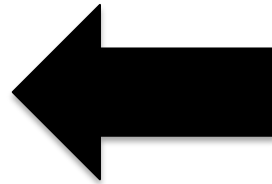
- 11 candidate events observed for background of 3.3 ± 0.4
- Probability to see 11 events or more for $\sin^2 2\theta_{13} = 0$ is 0.0009 (3.1σ equivalent)
- Fit assumes $|\Delta m_{32}^2| = 2.4 \times 10^{-3} \text{ eV}^2$ and $\sin^2 2\theta_{23} = 1$
- For normal hierarchy, best fit:
 $\sin^2 2\theta_{13} = 0.088 +0.049 -0.039$



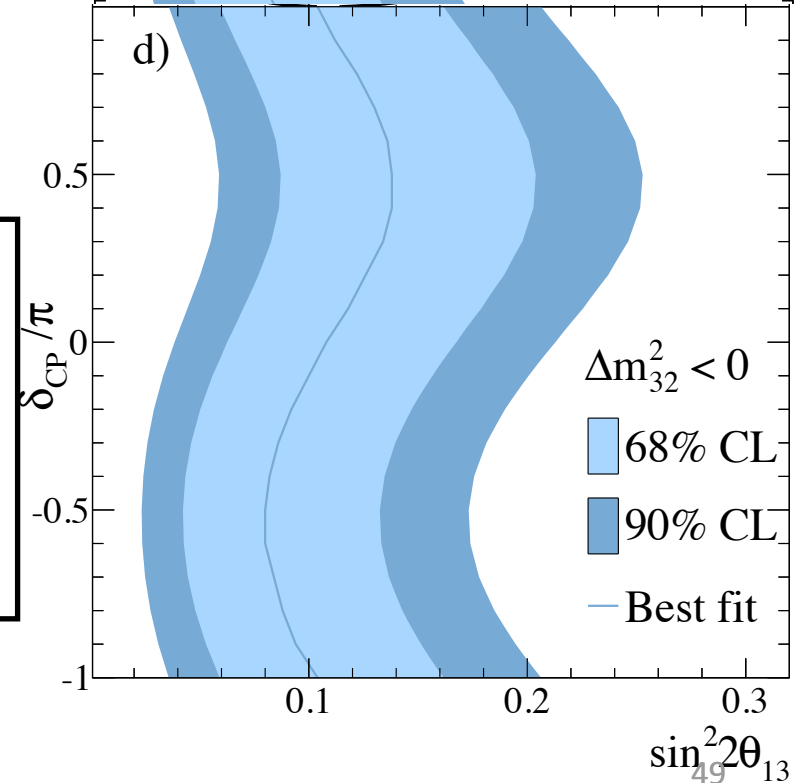
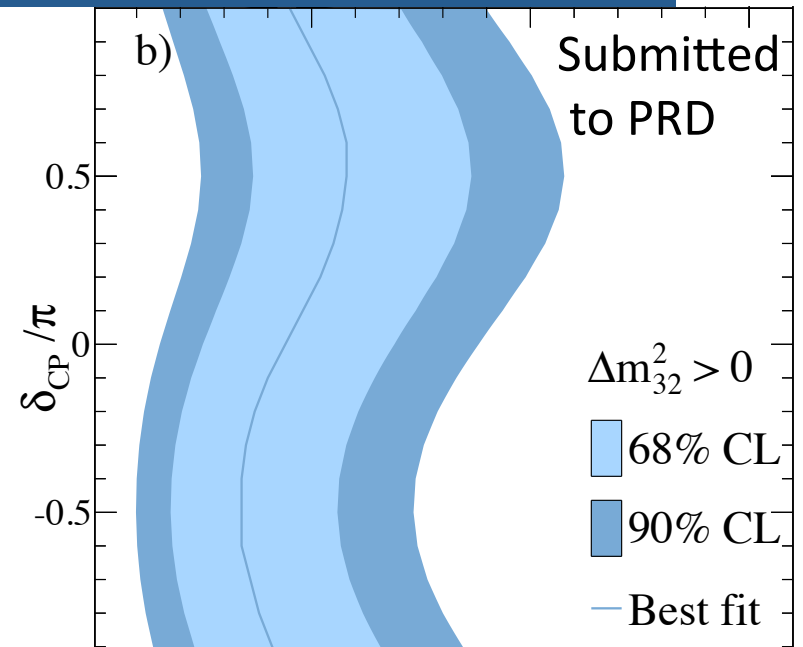
Implications of a large θ_{13}



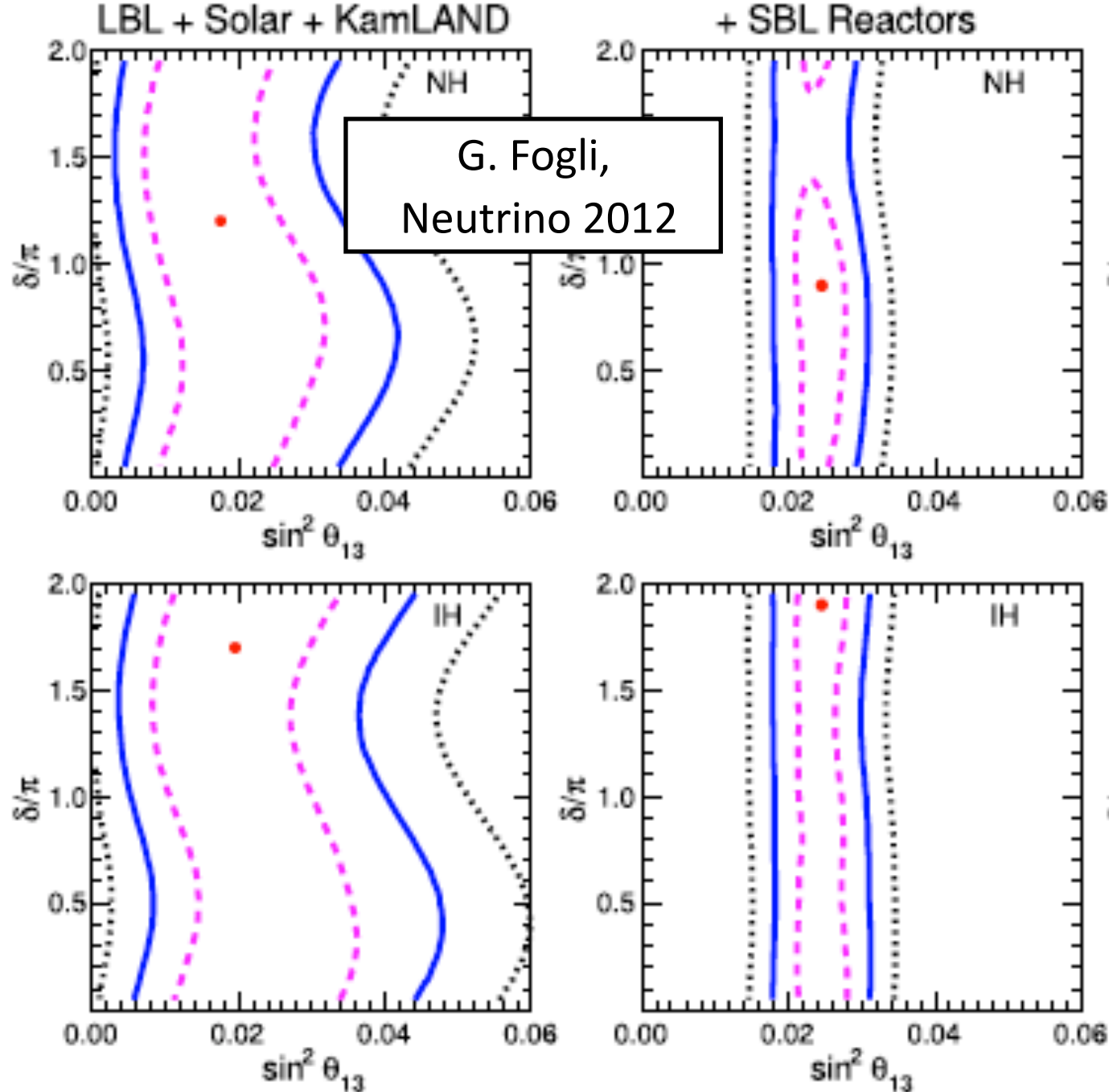
G. Fogli,
Neutrino 2012



Long baseline (LBL) appearance depends on all the mixing parameters, including δ_{CP}, θ_{13}



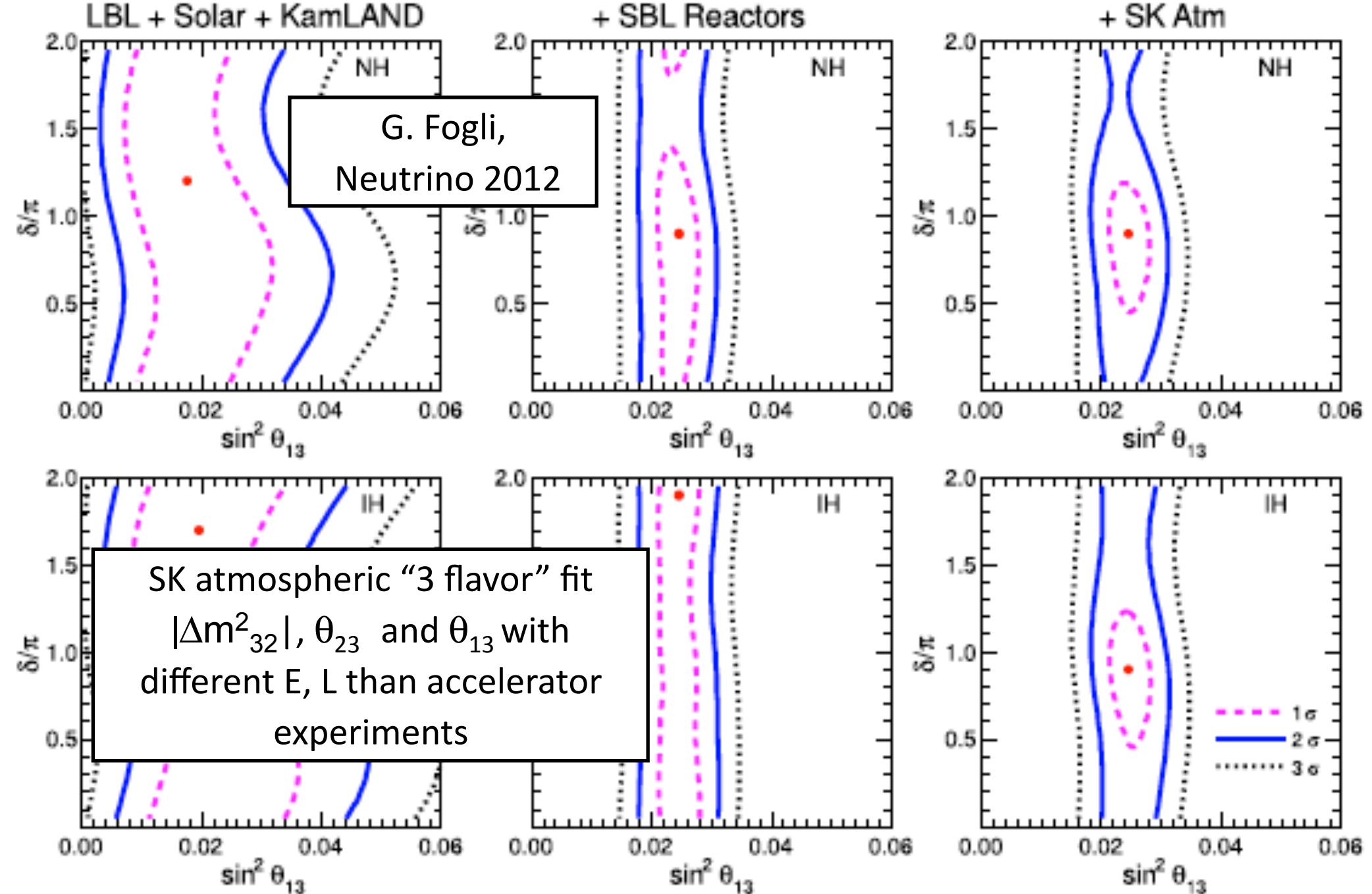
Implications of a large θ_{13}



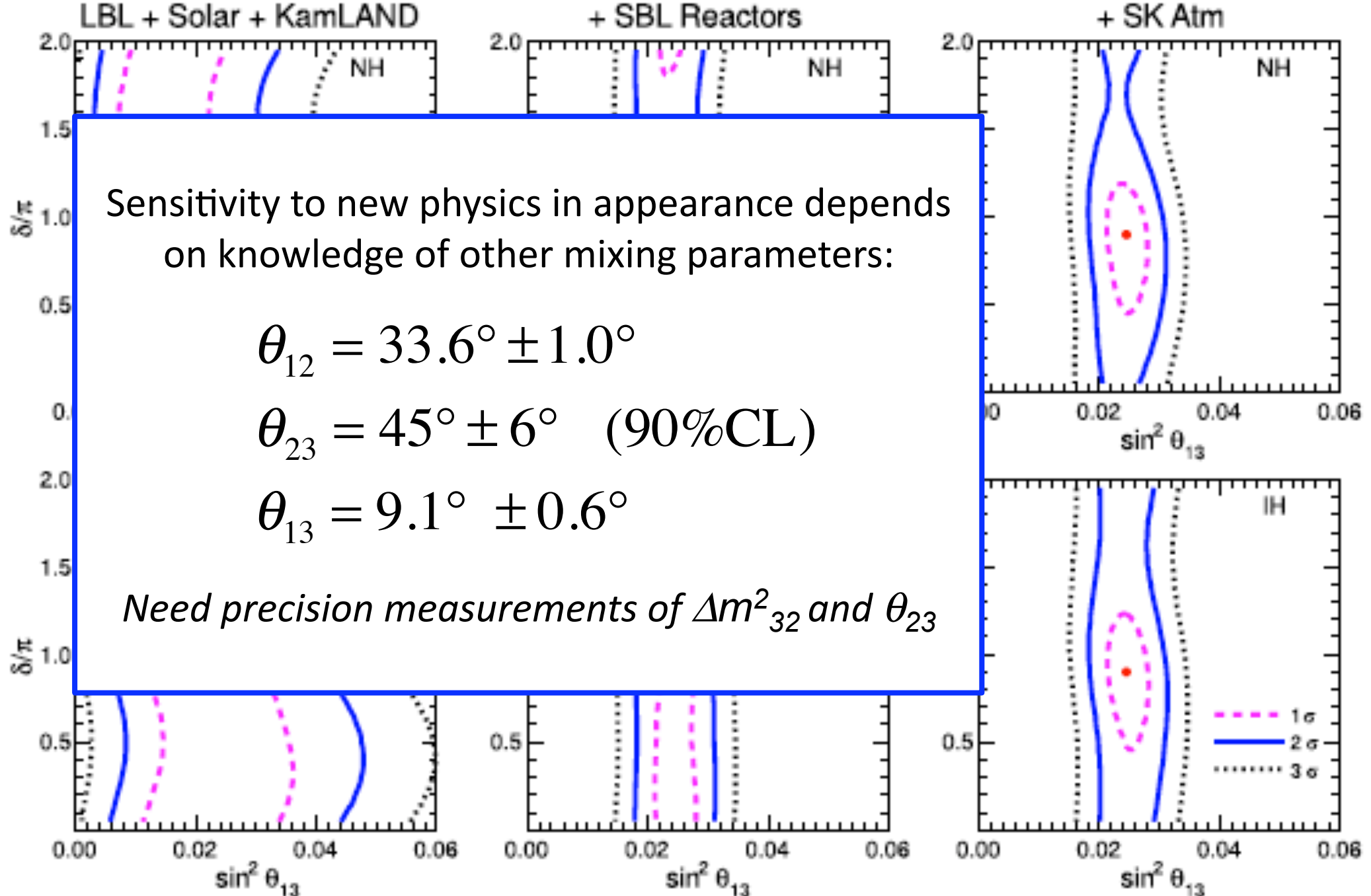
G. Fogli,
Neutrino 2012

Reactor experiments
are a pure
measurement of θ_{13}

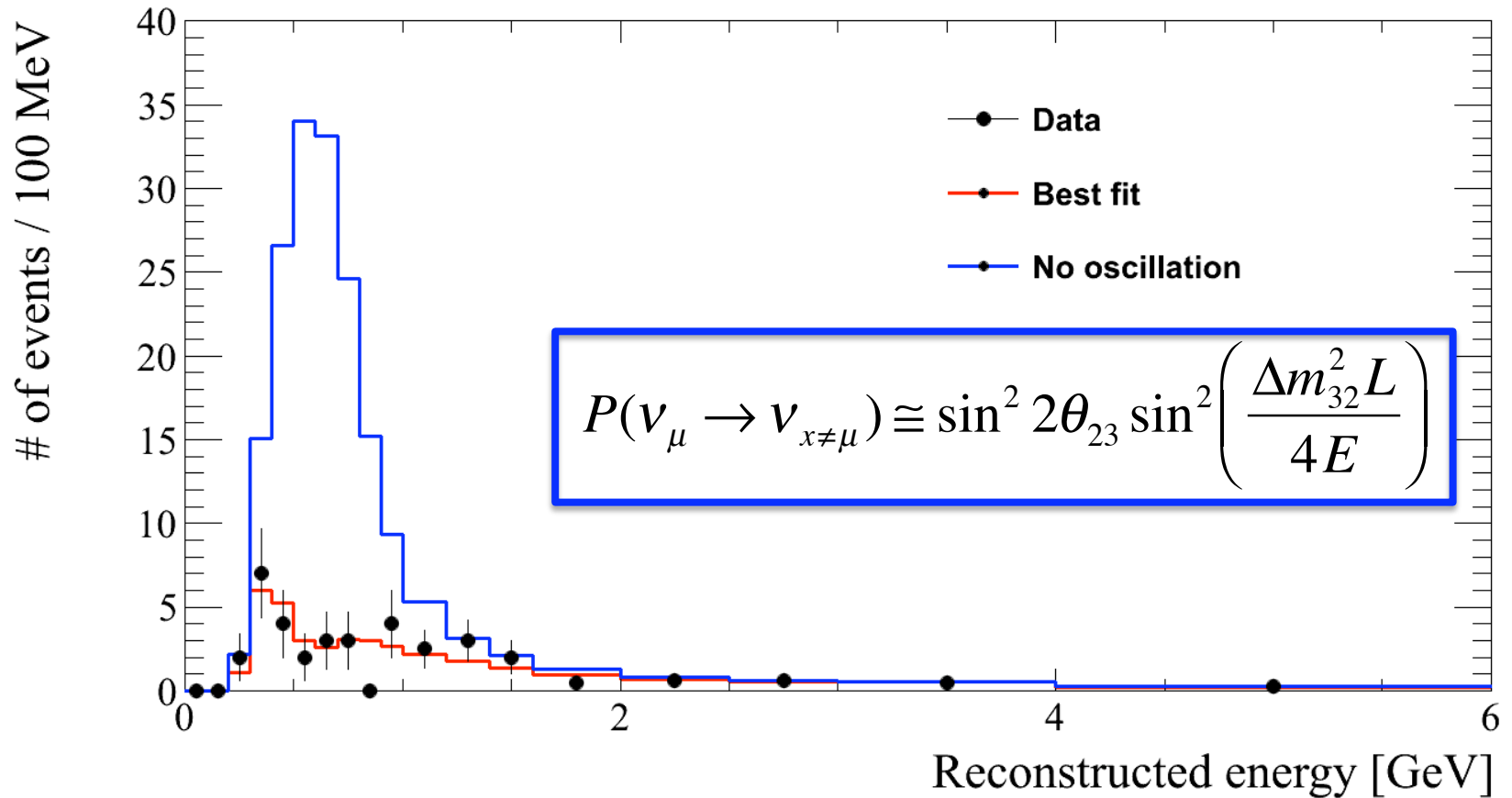
Implications of a large θ_{13}



Implications of a large θ_{13}



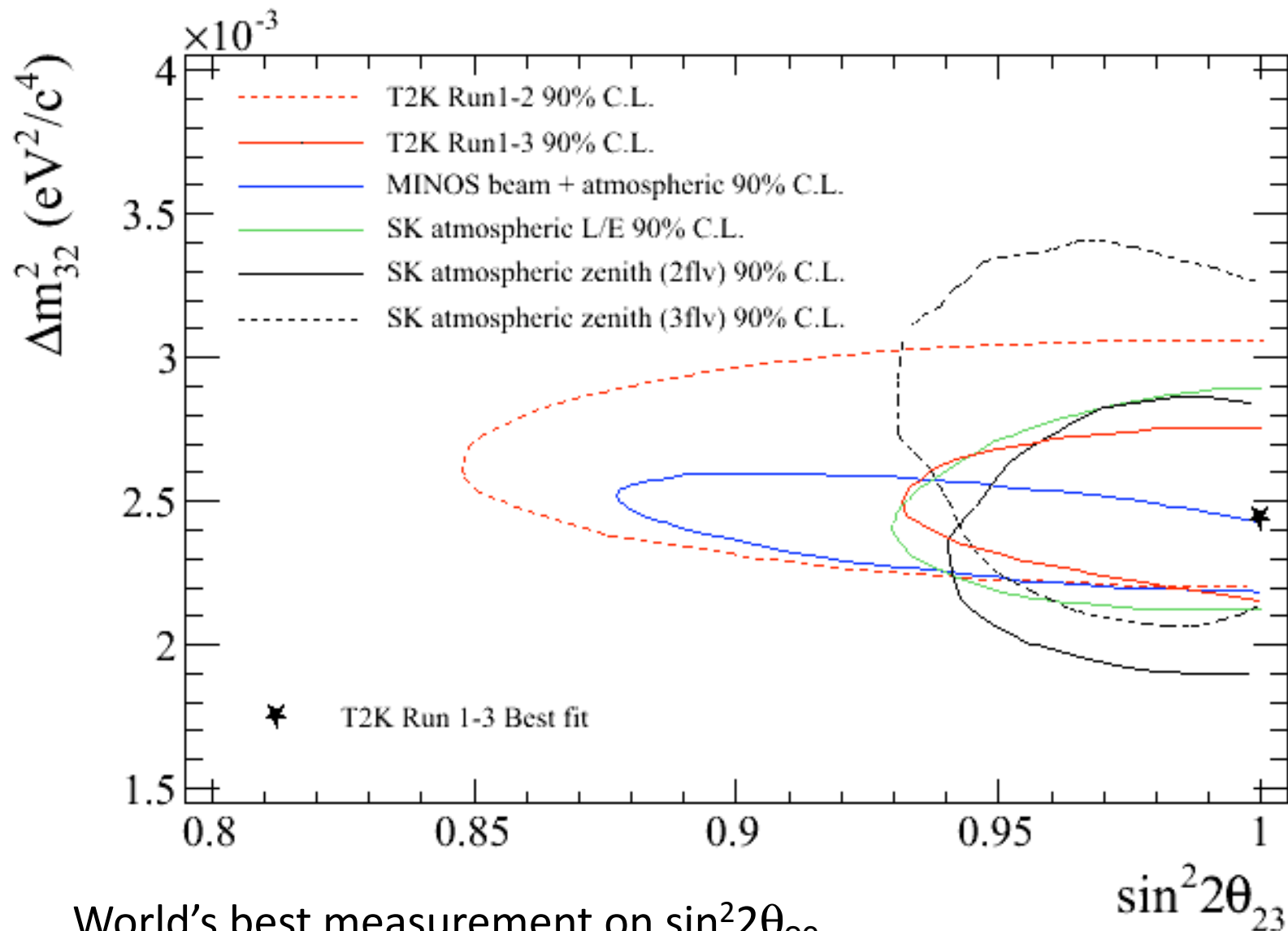
T2K ν_μ disappearance



Disappearance distorts energy spectrum and rate of ν_μ candidates

- Select CCQE ν_μ candidates at SK
- Reconstruct neutrino energy from muon kinematics
- Apply same near detector tuning as for ν_e appearance

ν_μ disappearance results



World's best measurement on $\sin^2 2\theta_{23}$

- Best fit is consistent with maximal mixing ($\theta_{23} = 45^\circ$)
- Expect to ~double statistics with this year's data set ending in July

Why T2K?

Evidence for ν_e appearance is the first step towards searches of CP violation in the lepton sector

- Do we see hints of new physics?

New world's best limits on θ_{23} from ν_μ disappearance

- Will θ_{23} continue to be maximal?
- If not, what is the θ_{23} octant?

What is needed to measure δ_{CP} ?

Compare ν_e appearance to $\bar{\nu}_e$ appearance to determine an asymmetry:

$$A_{CP} = \frac{P(\nu_\mu \rightarrow \nu_e) - P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)}{P(\nu_\mu \rightarrow \nu_e) + P(\bar{\nu}_\mu \rightarrow \bar{\nu}_e)} \simeq \frac{\Delta m_{12}^2 L}{4E_\nu} \cdot \frac{\sin 2\theta_{12}}{\sin \theta_{13}} \cdot \sin \delta$$

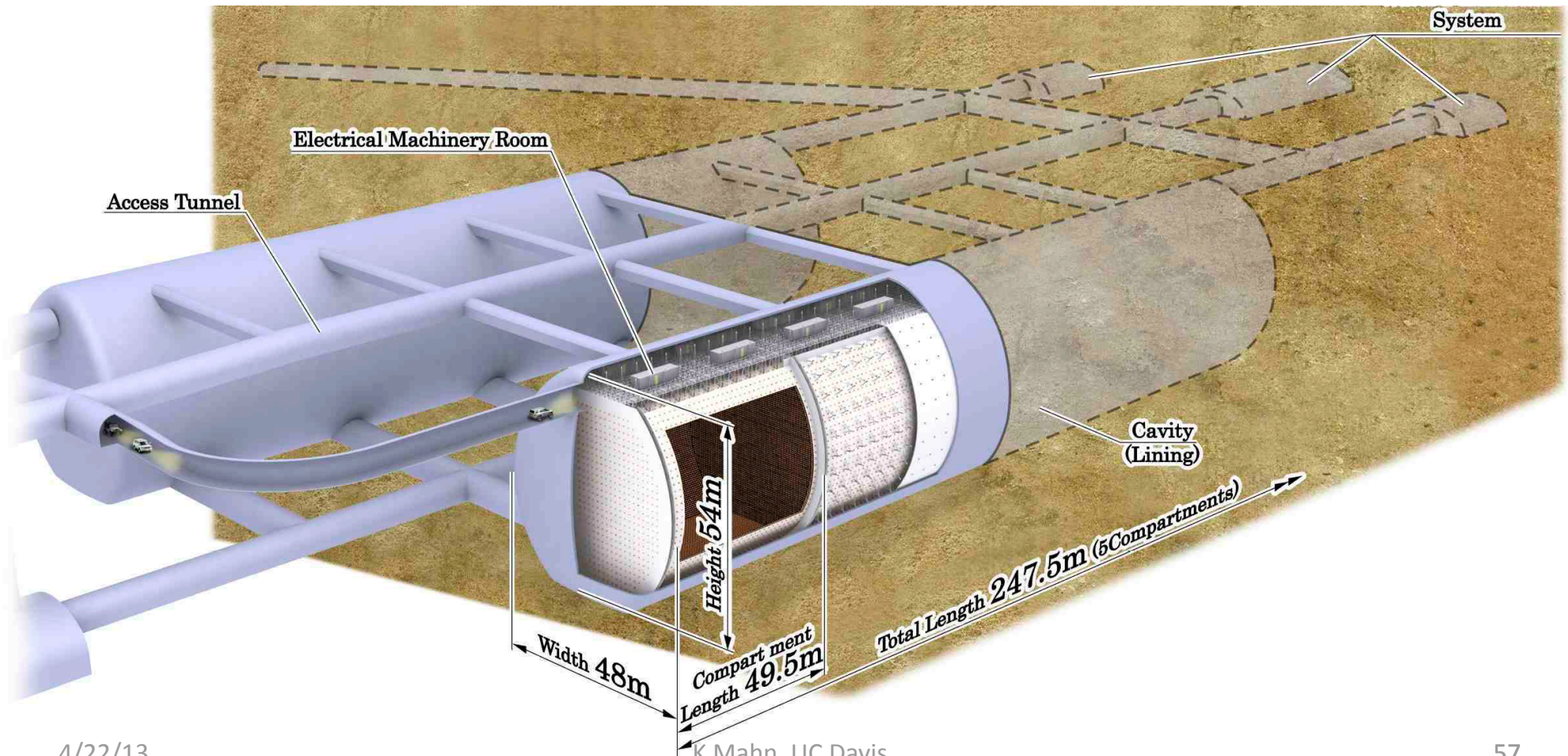
With θ_{13} “large”, then A_{CP} is small ($\sim 20\text{-}30\%$), so the measurement of δ_{CP} need systematic uncertainties of $<5\%$ or better

- T2K’s current statistics: **11 events** (ν_e appearance probability)
- Need more raw event rate, with a larger detector

Hyper-Kamiokande

~1Mton detector, approximately 25x Super-Kamiokande

- 99,000 inner PMTs, 25,000 veto region PMTs (10 compartments)
- Same neutrino beamline as T2K, different cavern
- Other physics reach: solar neutrinos, atmospheric neutrinos, astrophysical neutrinos (supernova), geo-neutrinos and proton decay



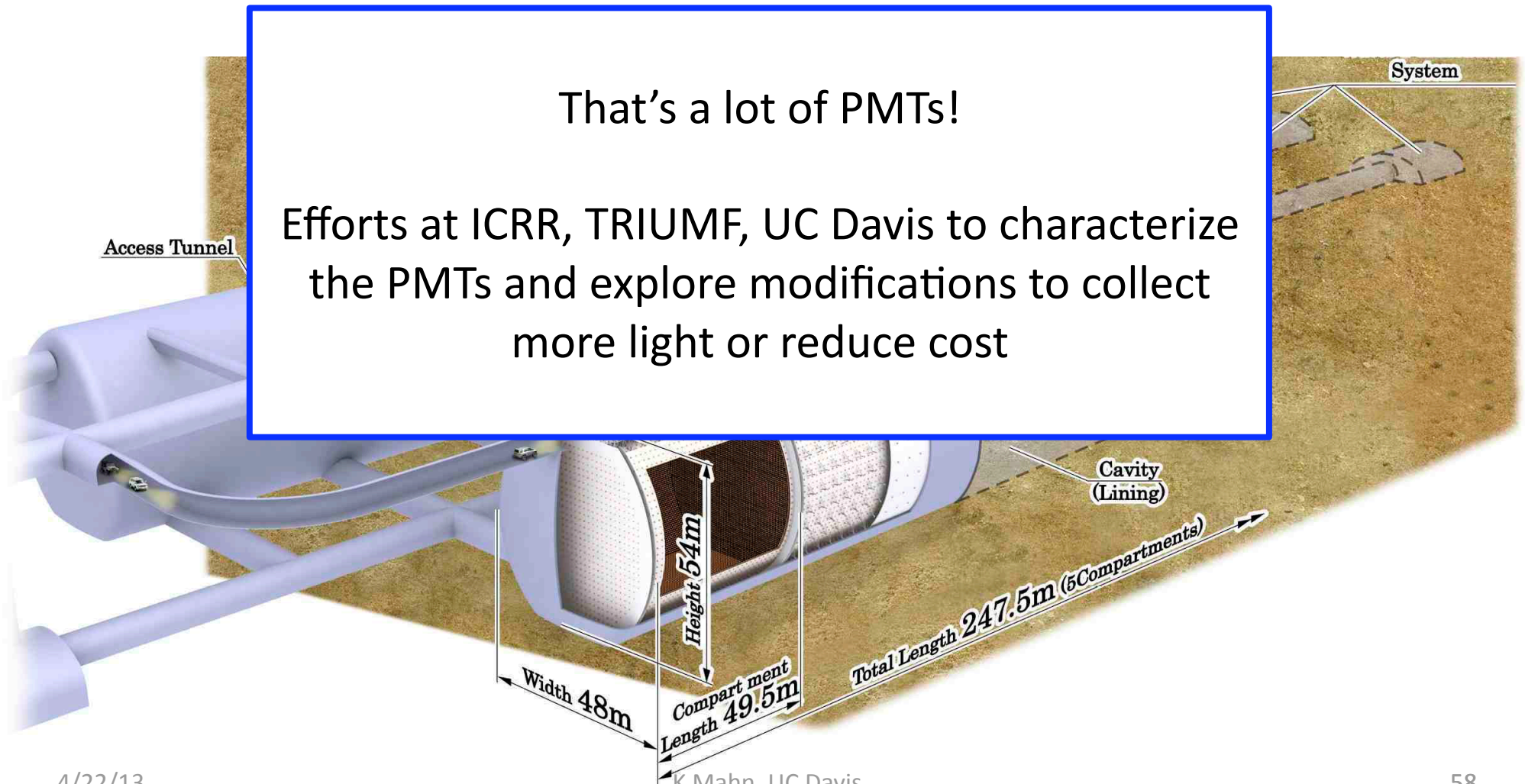
Hyper-Kamiokande

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That's a lot of PMTs!

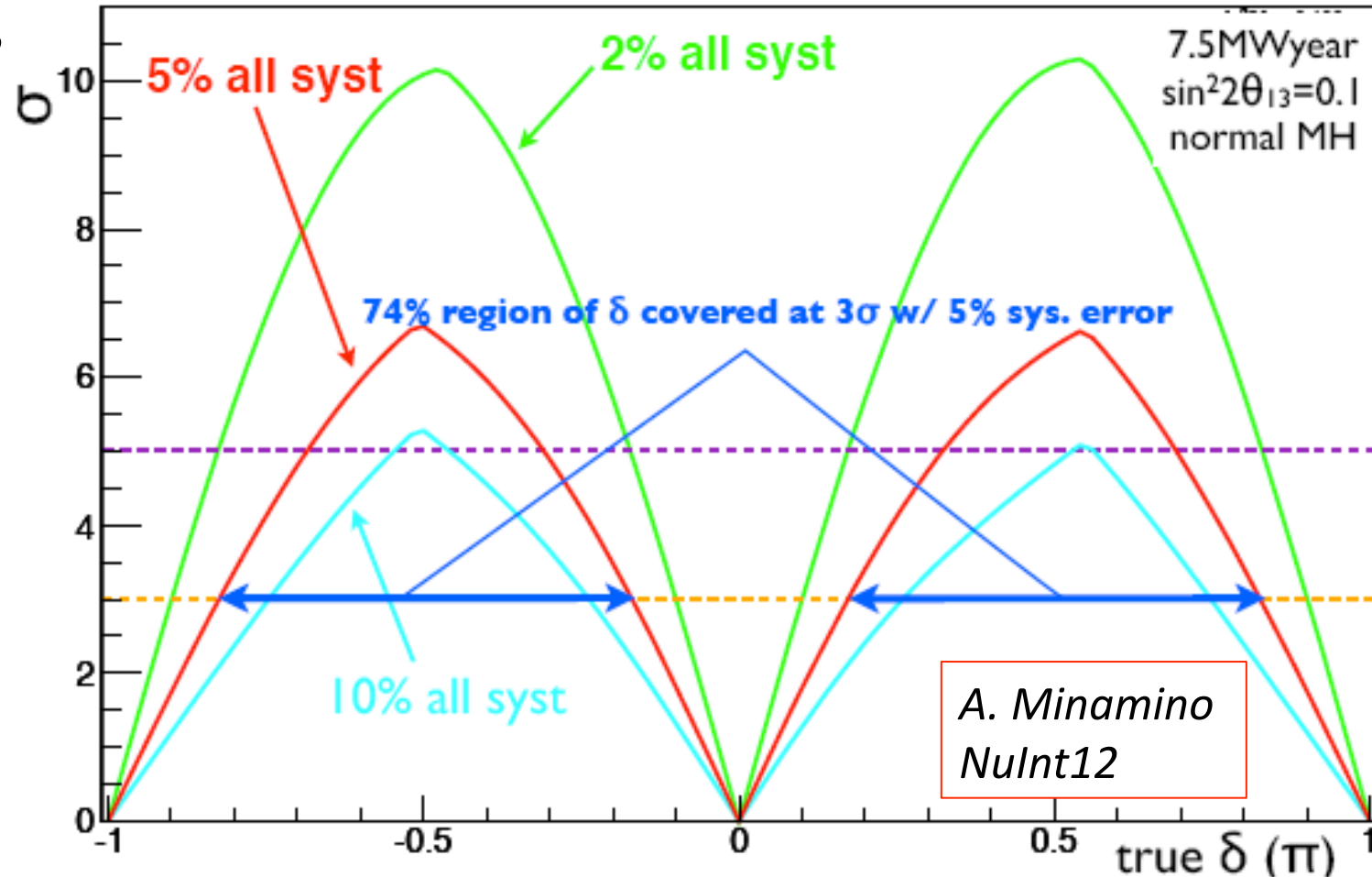
Efforts at ICRR, TRIUMF, UC Davis to characterize the PMTs and explore modifications to collect more light or reduce cost



δ_{CP} discovery sensitivity

HK LOI: hep-ex 1109.3262

	v run	v run
Signal ν_e, ν_e	3560	1959
NC	649	678
CC ν_e ν_e	880	878
Other	81	403

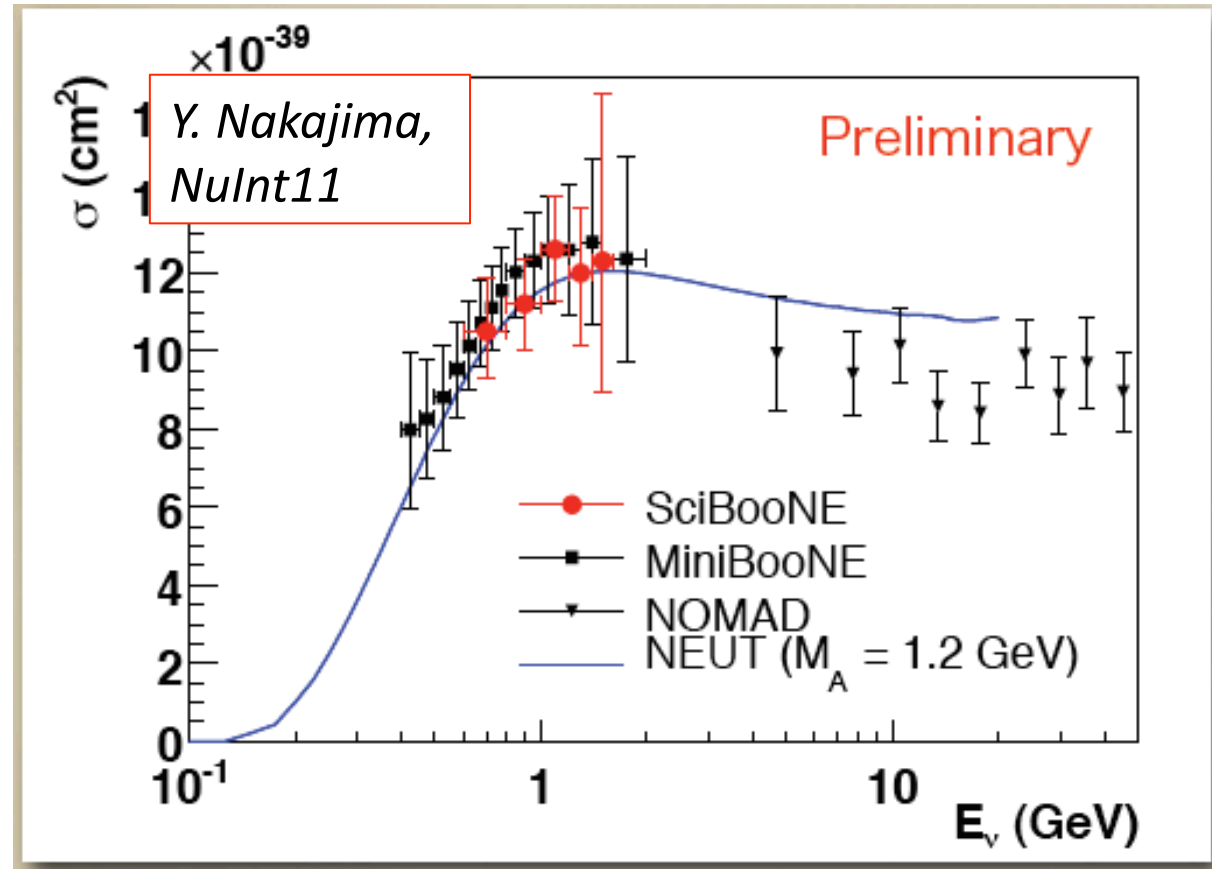


With $<5\%$ overall systematic uncertainty, HK could observe evidence of nonzero δ_{CP}

- Statistical uncertainty $\sim 2\%$
- Improved control of systematic uncertainties corresponds to increased physics impact

How do we achieve <5% systematics?

Uncertainties	ν_e sig+bkrd
ν flux+xsec (constrained by ND280)	$\pm 5.7\%$
ν xsec (unconstrained by ND280)	$\pm 7.5\%$
Far detector	$\pm 3.9\%$
Total	$\pm 10.3\%$

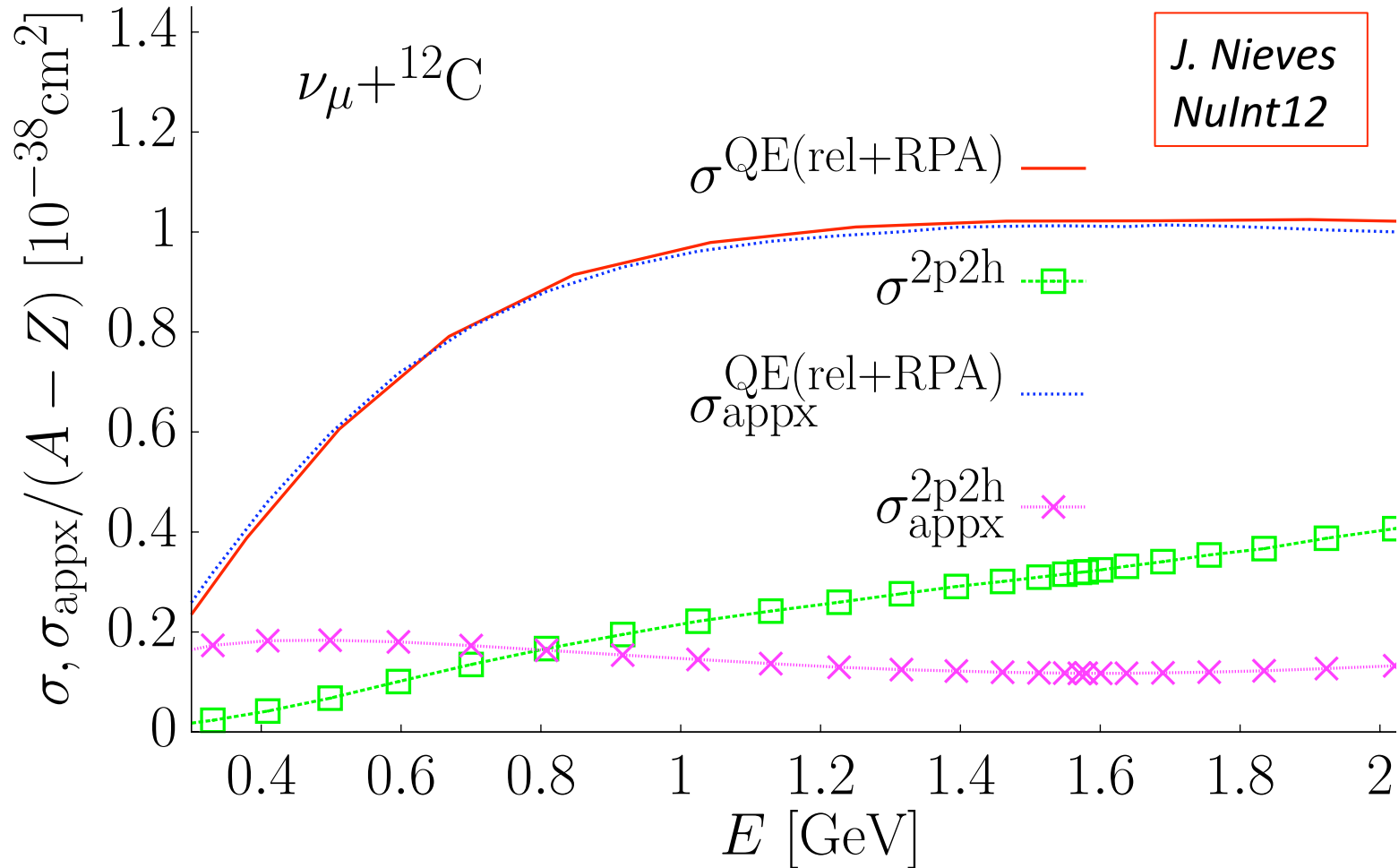


The largest systematic uncertainties currently on the T2K ν_e appearance analysis are neutrino interaction model uncertainties

- Disagreements between data and neutrino interaction model with other neutrino experiments (e.g. MiniBooNE, SciBooNE)
- Differences between alternate interaction models than those currently used by T2K

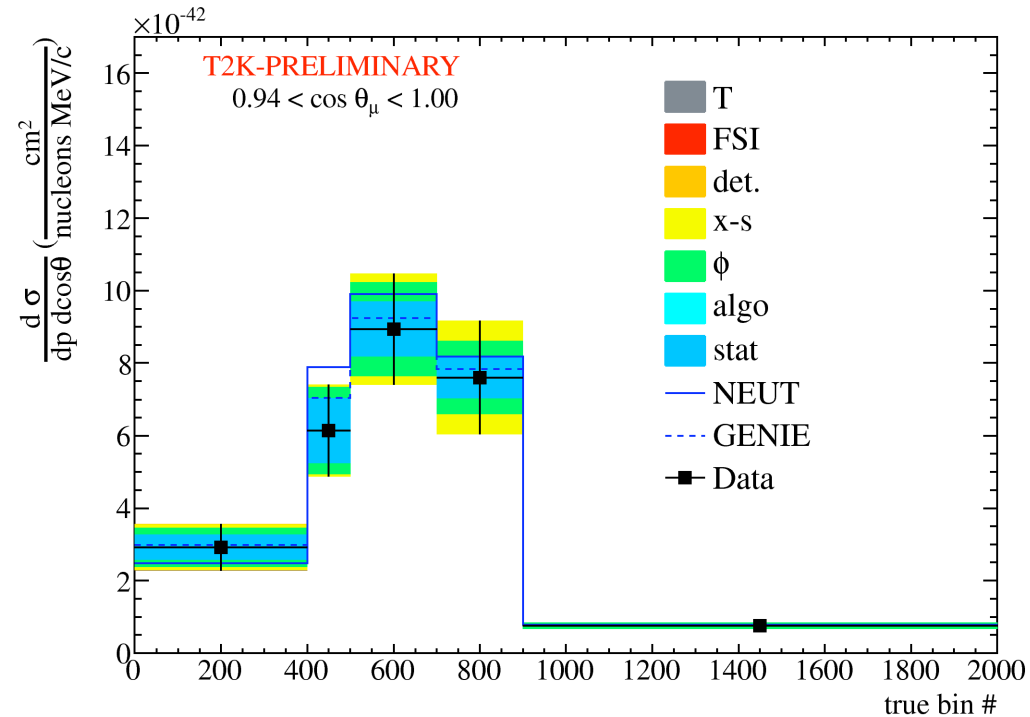
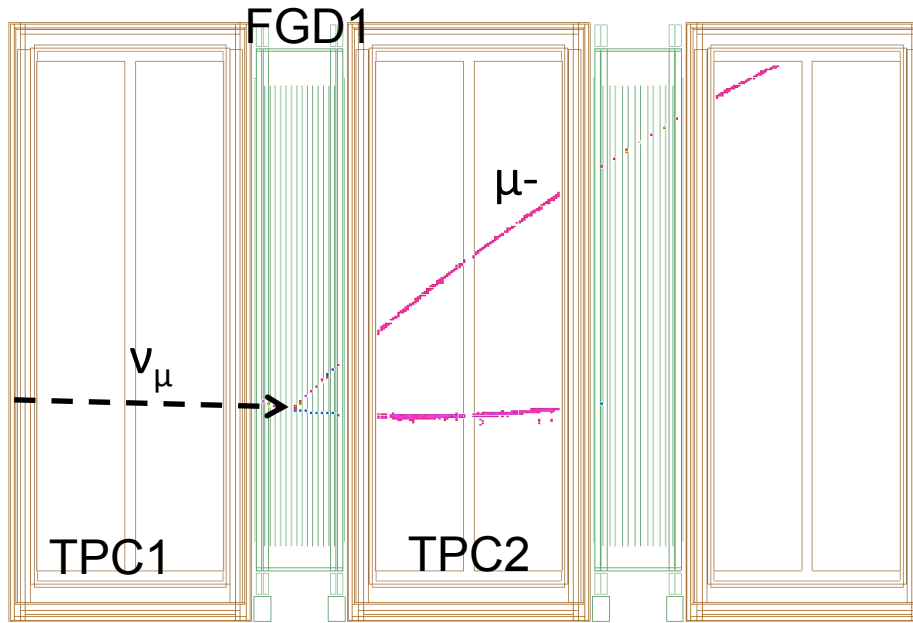
Also challenges faced by LBNE, LBNO, other proposed long baseline neutrino experiments

T2K's efforts to reduce cross section uncertainties



- 1) Incorporate alternate or updated neutrino interaction models into our simulations
 - Validate existing models with electron, pion scattering data
 - Add new models which help resolve disagreements with neutrino data to MC

T2K's efforts to reduce cross section uncertainties



2) Test the agreement of new models with ND280, as ND280-XSEC co-convenor:

- Detailed information (particle type, kinematics) out of the interaction
- Provide cross section measurements for community to further develop models

Produced T2K's first cross section measurement (CC inclusive)

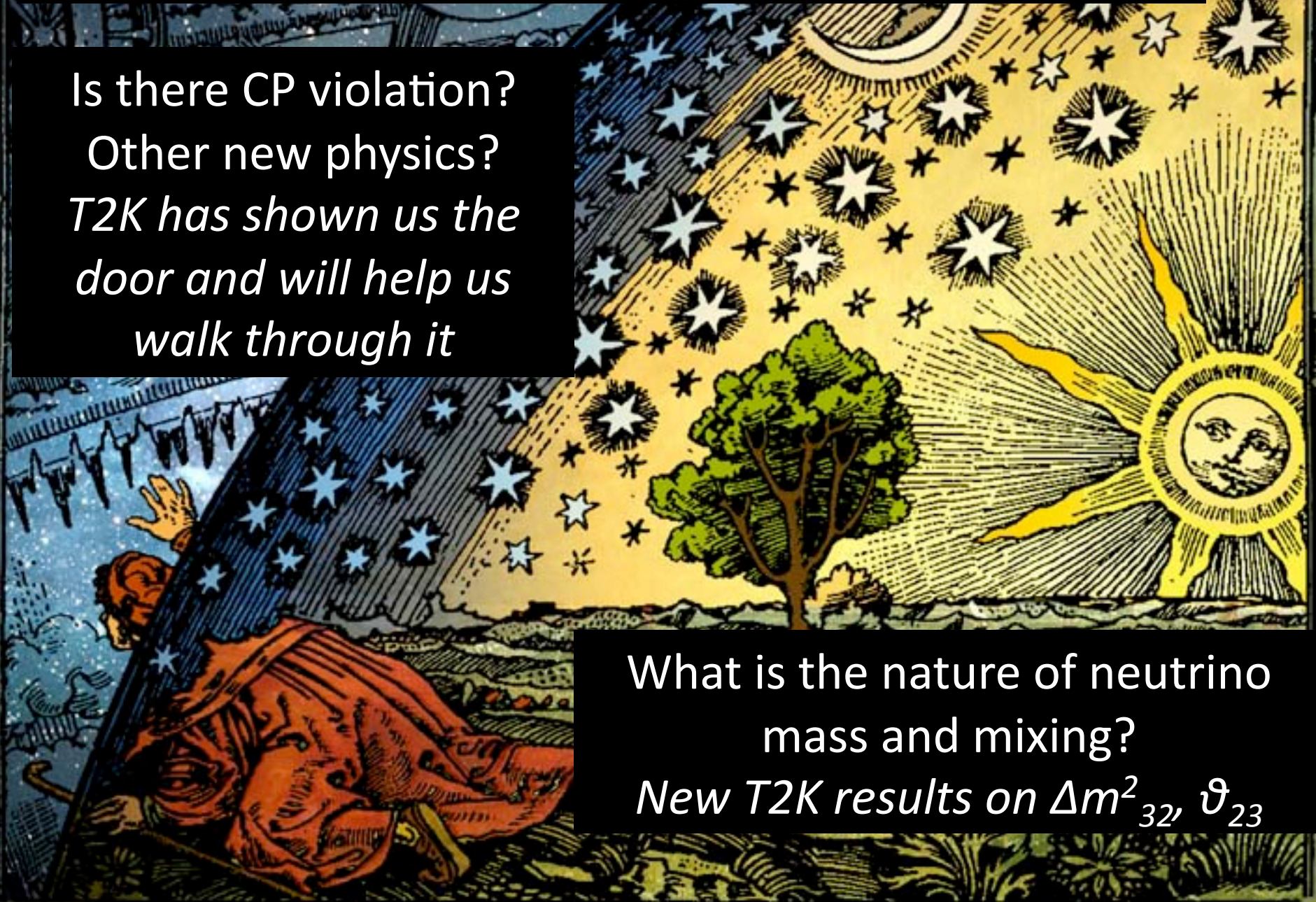
Accepted for publication in PRD

- ND280 performance, limitations important to determine what is needed for a HK near detector program

What will neutrinos tell us in the next 10 years?

Is there CP violation?
Other new physics?
*T2K has shown us the
door and will help us
walk through it*

What is the nature of neutrino
mass and mixing?
New T2K results on Δm^2_{32} , ϑ_{23}

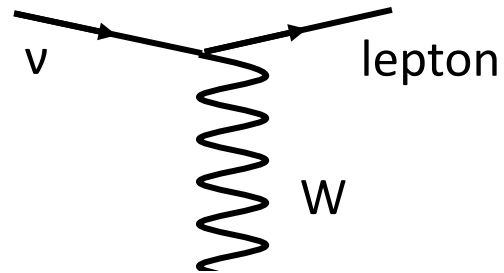


Backup slides

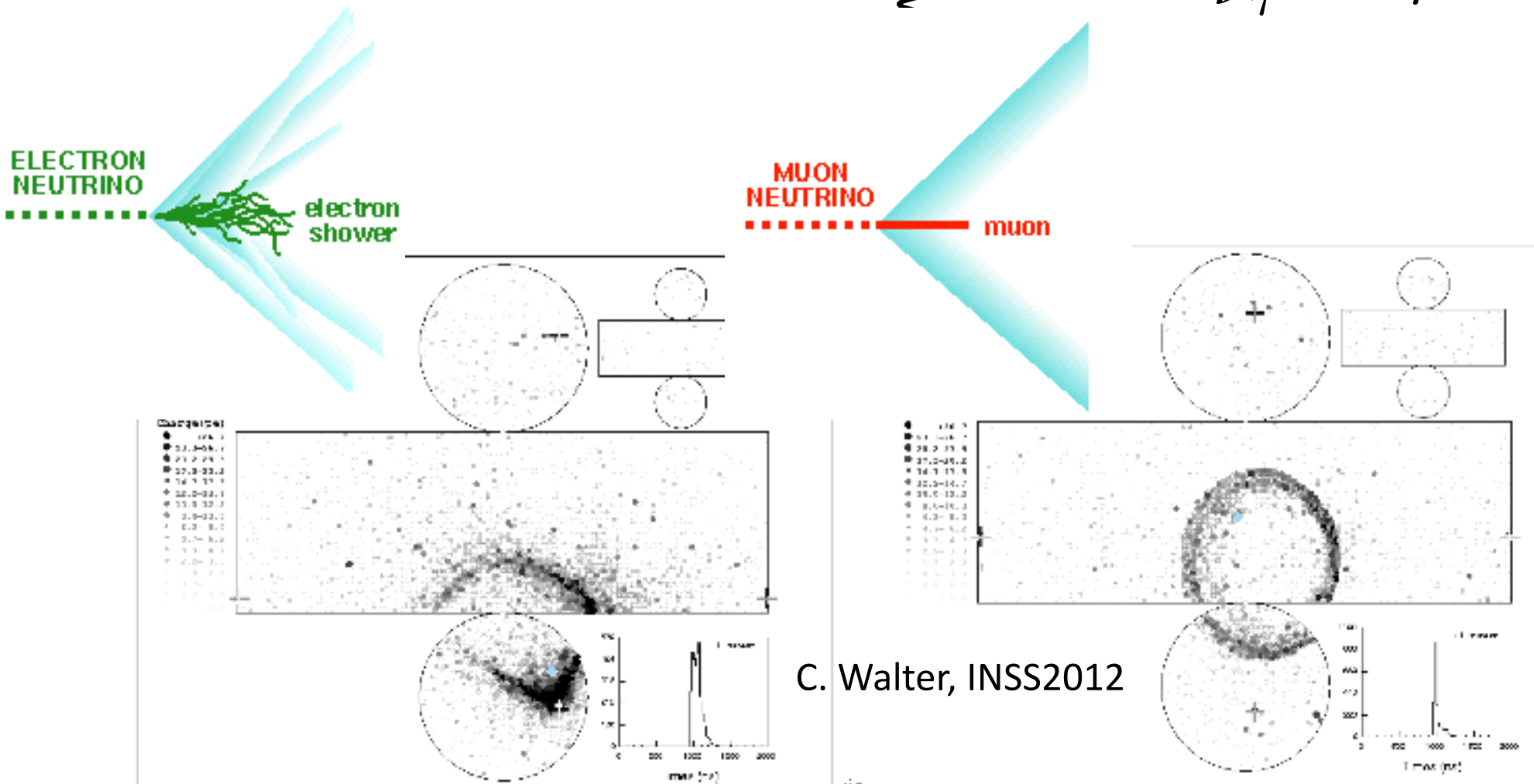
Detecting atmospheric neutrinos

Select ν_e or ν_μ events from ring shape and topology

Charged Current (CC)



$$\begin{aligned} \nu_e &\rightarrow e \\ \nu_\mu &\rightarrow \mu \\ \nu_\tau &\rightarrow \tau \end{aligned}$$



C. Walter, INSS2012

Selecting CC ν_e interactions

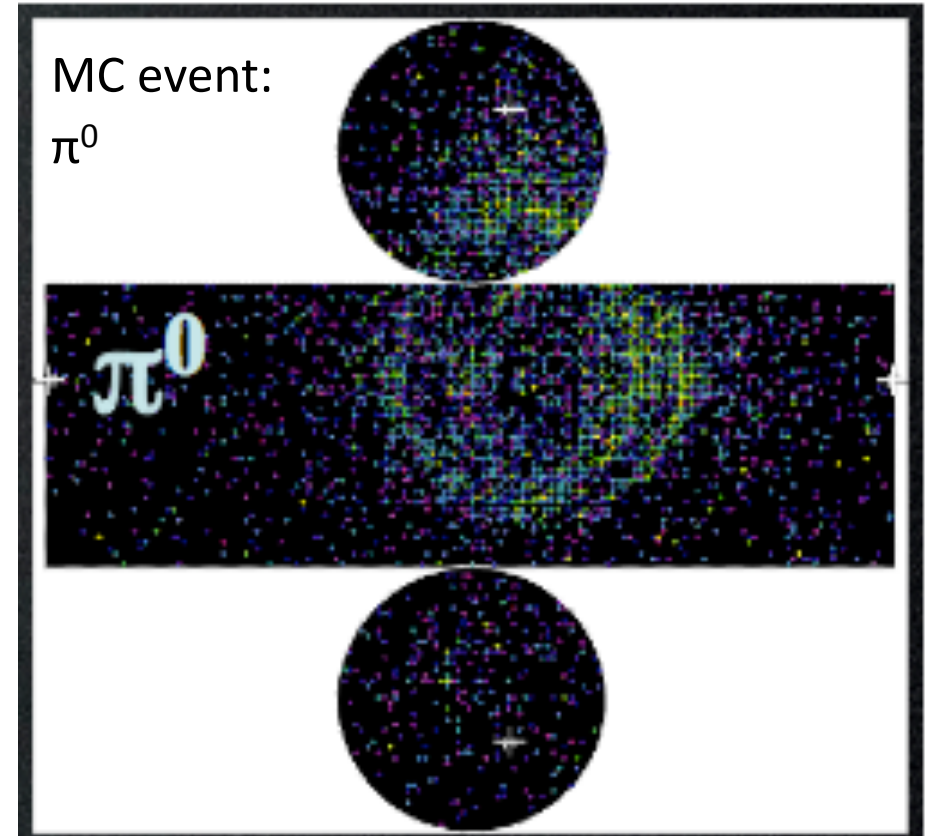
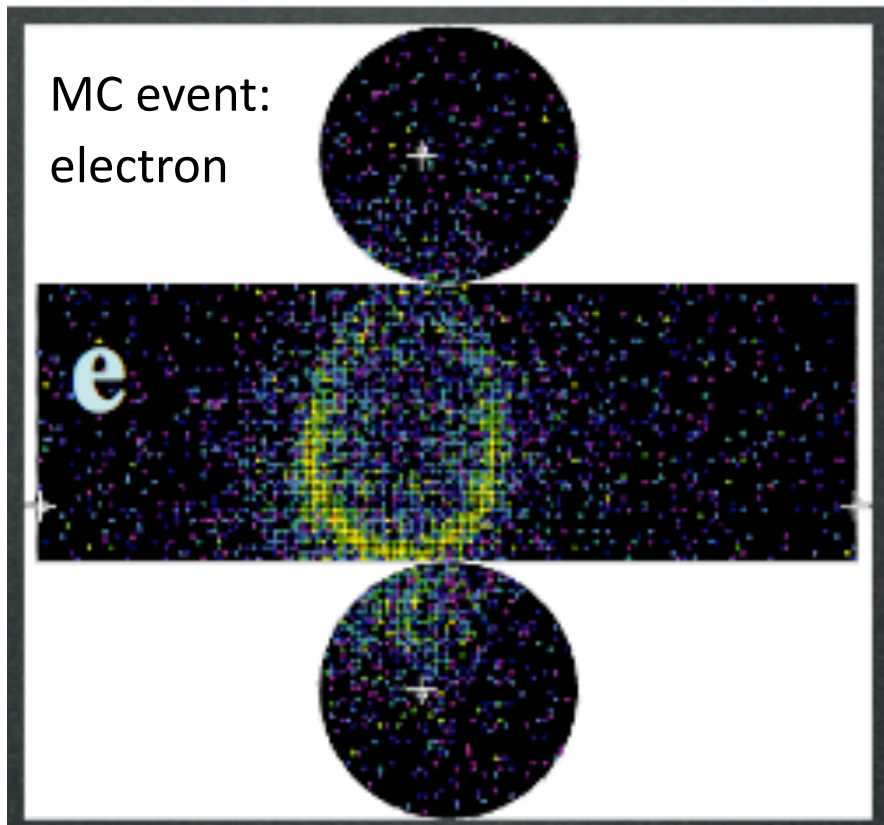
Signal: CC ν_e from ν_μ to ν_e oscillation

Background: CC ν_e Irreducible beam ν_e

Background: NC $\pi^0 \nu_\mu$ Mimics CC ν_e

A π^0 from a NC interaction will decay to two photons (two electron-like rings)

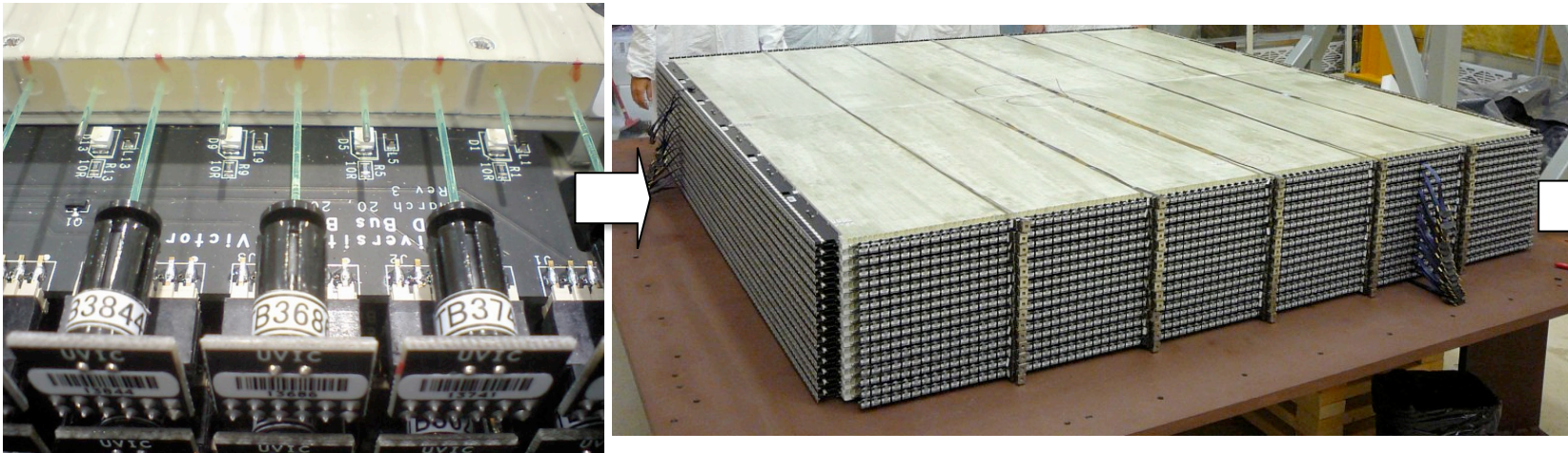
- Search for 2nd ring
- Calculate invariant mass
- Reject events consistent with π^0 invariant mass



Fine Grained Detectors (FGDs)

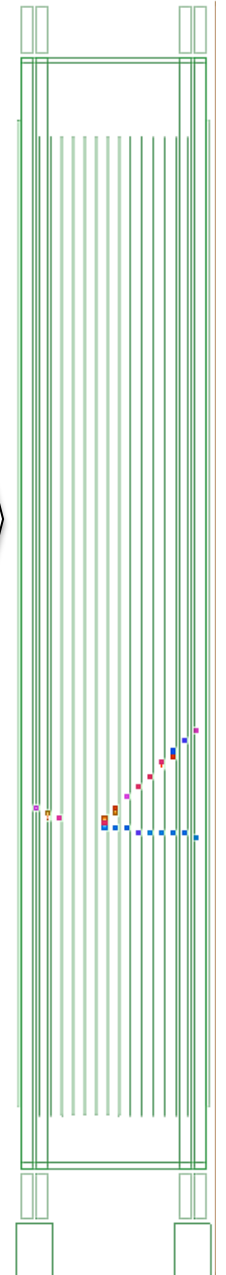
Scintillation light (from charged particles) is sent down a wavelength shifting fibre connected to a multi-pixel-photon-counter (MPPC)

- MPPCs function in a magnetic field
- First large scale use



X and Y scintillator layers can be used for 3D tracking
1cm² bar size provides detailed vertex information

P.-A. Amaudruz et al,
“The T2K fine-grained detectors”,
NIM A (2012) 10.1016/j.nima.2012.08.020



Time projection chambers (TPCs)

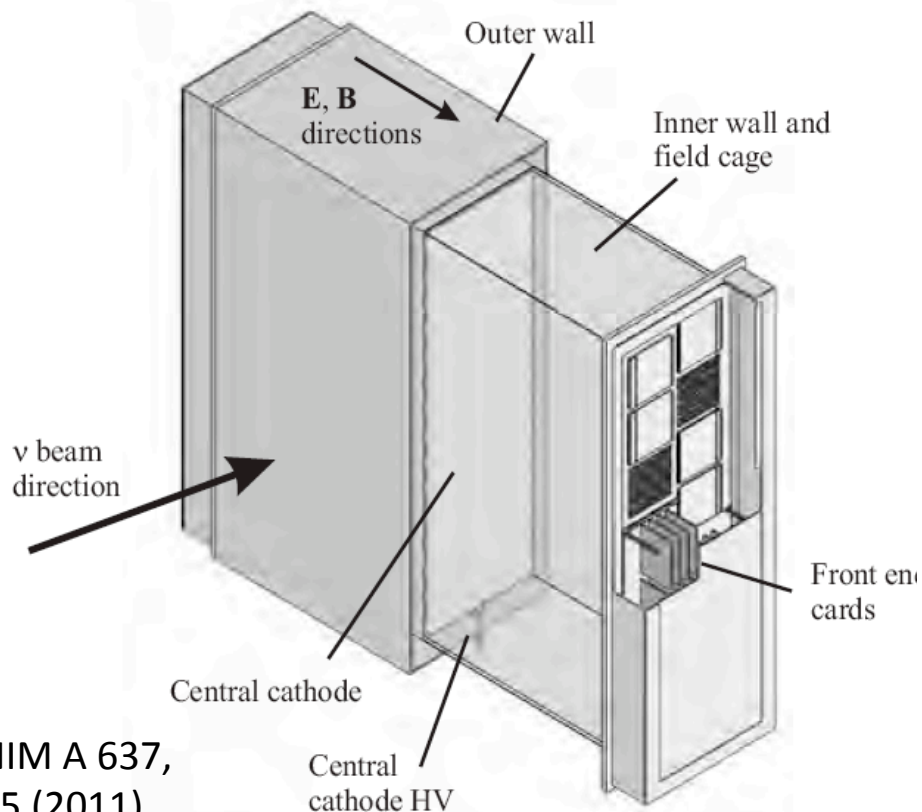
Charged particle ionizes gas; electrons drift to readout plane ($E \sim 25\text{kV}$)

“Wireless” TPC: Use of bulk micromegas detectors in readout

3D tracks are reconstructed provided drift velocity in the gas and timing of entry from other subdetectors

Momentum of the particle can be determined from curvature

- 0.2T B field; $p_{\mu} \sim 1 \text{ GeV}/c$ has $<10\%$ momentum resolution



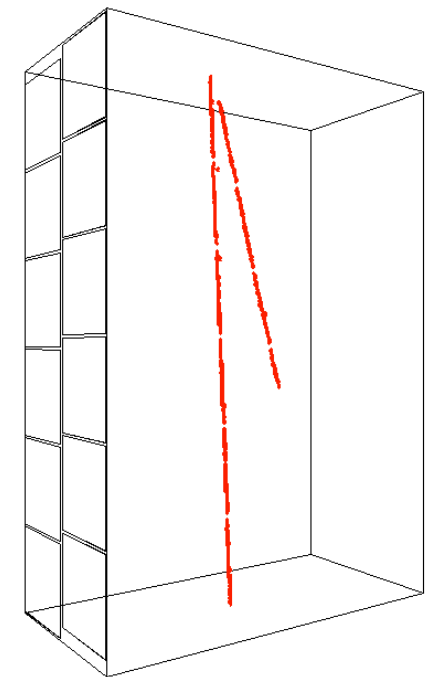
NIM A 637,
25 (2011)

4/22/13



K Mahn, UC Davis

*Built DQ system,
alignment convener*



68

Overall systematic uncertainty

After ND tuning, systematic uncertainties reduced to $\sim 10\%$ on signal+ background

- Overall uncertainty halved with use of the near detector data

Signal (ν_μ to ν_e osc)	# events
@ $\sin^2 2\theta_{13}=0.1, \delta_{cp}=0$	7.81

Background	# events
beam $\nu_e + \bar{\nu}_e$	1.73
$\nu_\mu + \bar{\nu}_\mu$ (mainly NC) background	1.31
osc through θ_{12}	0.18
total:	3.22 $\pm 0.43(\text{sys})$

Uncertainties	ν_e bkrd	ν_e sig+bkrd
ν flux+xsec (constrained by ND280)	$\pm 8.7\%$	$\pm 5.7\%$
ν xsec (unconstrained by ND280)	$\pm 5.9\%$	$\pm 7.5\%$
Far detector	$\pm 7.7\%$	$\pm 3.9\%$
Total	$\pm 13.4\%$	$\pm 10.3\%$
No ND measurement	26%	22%

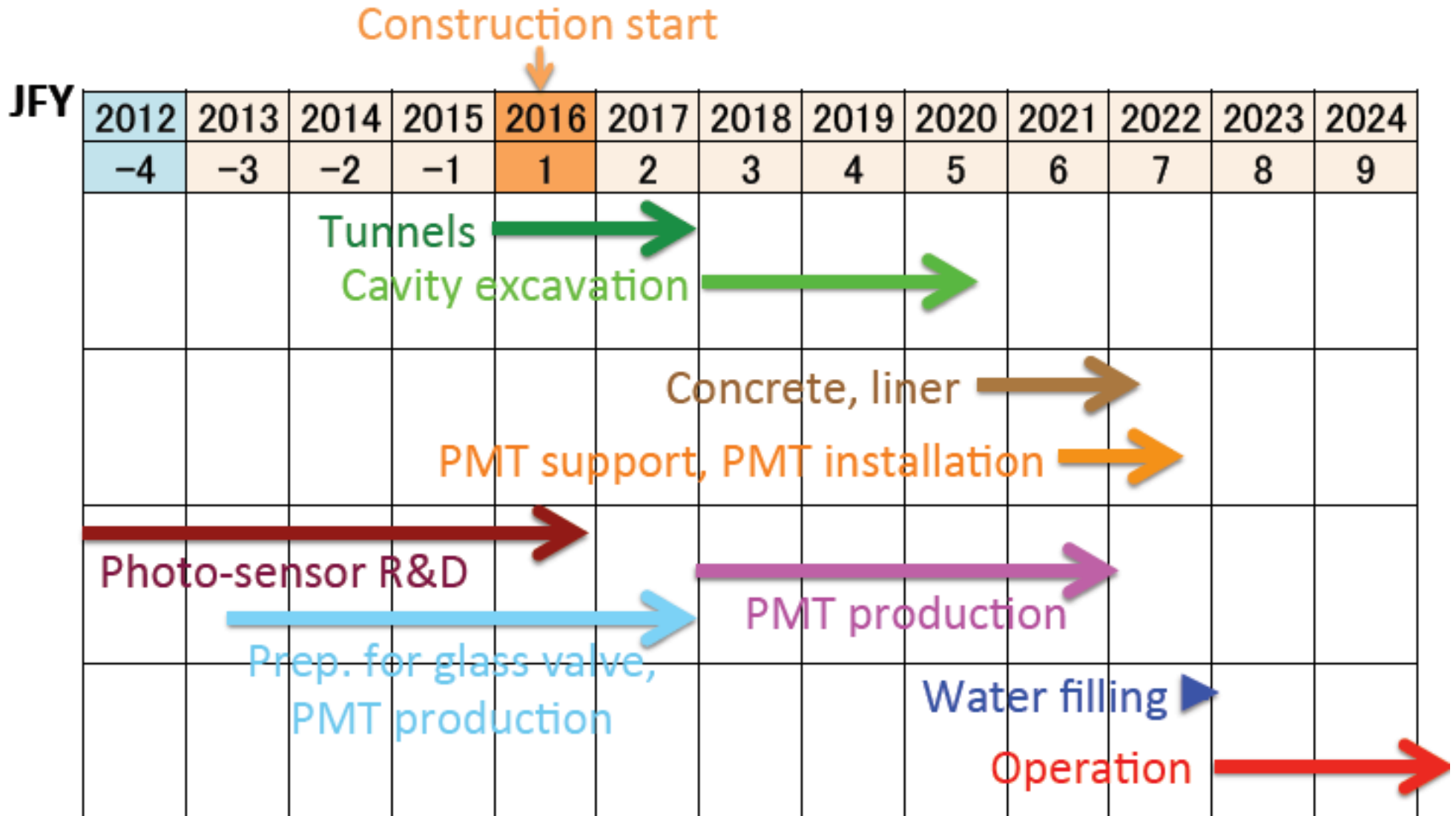
ν_e signal @ $\Delta m_{32}^2 = 2.4 \times 10^{-3} \text{ eV}^2, \sin^2 2\theta_{23} = 1.0$

Hyper-K timeline

Schedule

assuming budget being approved from JPY2016

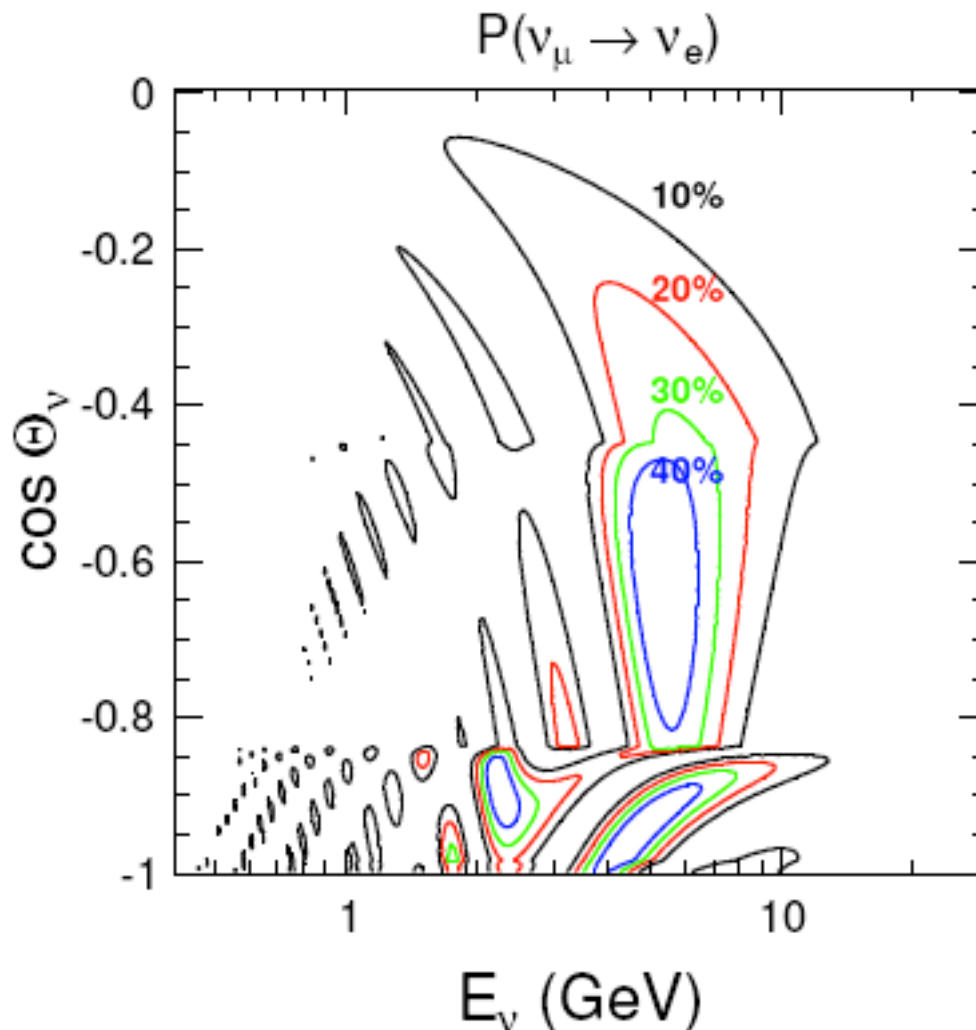
A. Minamino
NuInt12



Appearance measurements: atmospheric nu

Electron neutrino rate is altered by ν_μ to ν_e appearance and survival probability of ν_e

- Contours of equal probability as a function of E_ν and $\cos(\theta)$

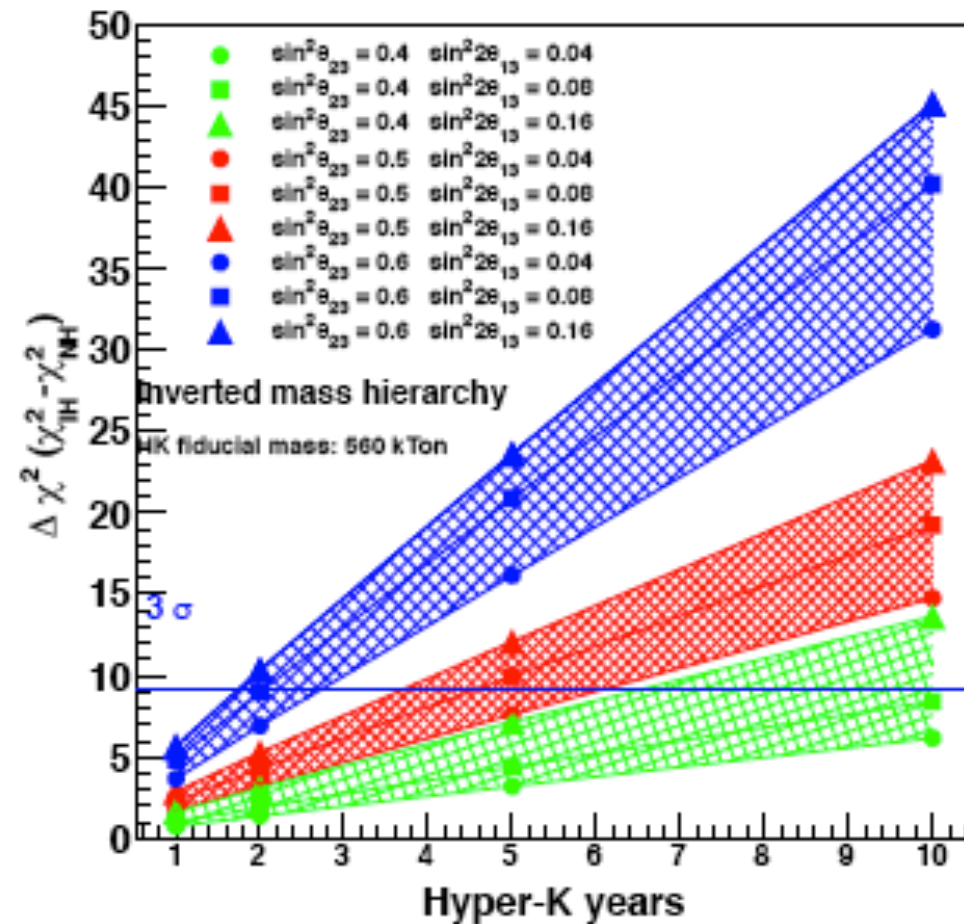
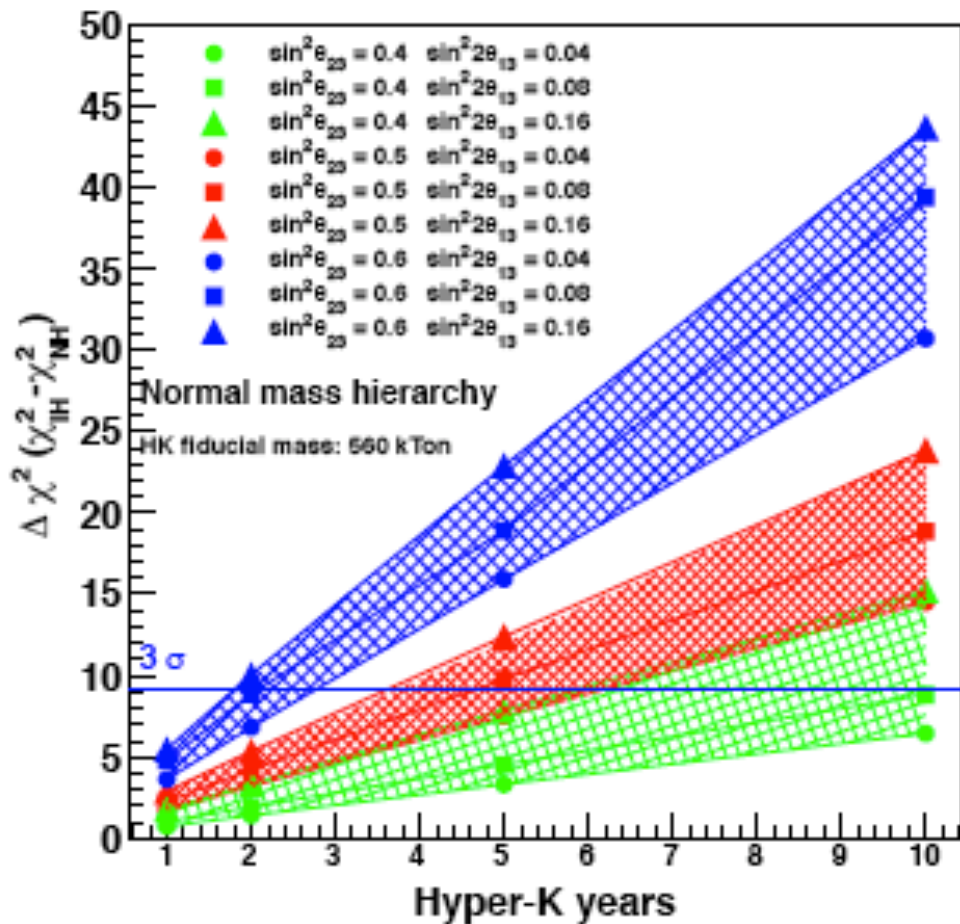


Appearance probability depends on all mixing parameters, including δ_{CP} , θ_{13}

- $\theta_{23} < 45$ degrees amplifies lower energy ν_e rate through the Earth's core
- normal hierarchy ($\Delta m_{32}^2 > 0$) increases higher energy ν_e rate through Earth's core

Super-Kamiokande collaboration
Phys Rev D81 092004,2010

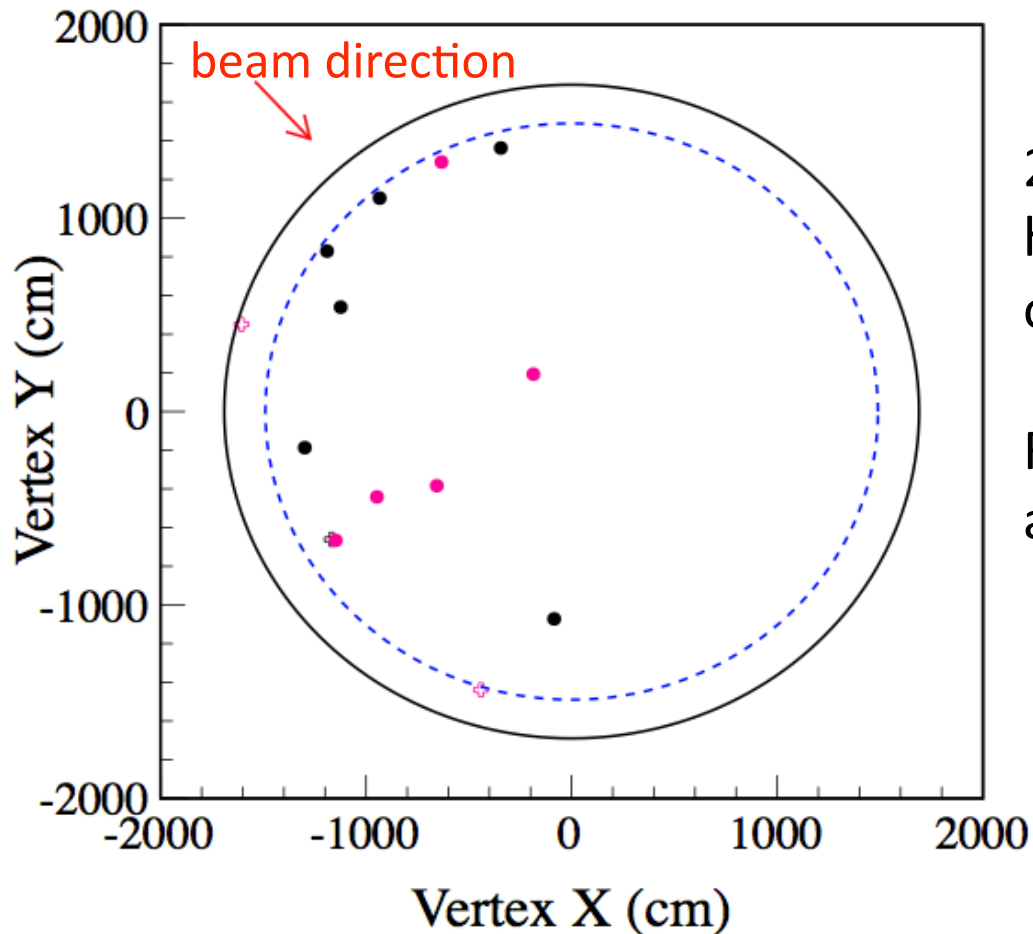
Hyper-K and mass hierarchy



Delta χ^2 for the true normal hierarchy (left) and inverted (right) for HK (atmospheric nu alone, $\sim 3\sigma$ across most of par space, better with T2HK)

- Nova resolves mass hierarchy at ~ 2 sigma for 40% of all values of delta
- Proposed Daya Bay II reactor experiments can be sensitive to MH
- PINGU 20: 3-11 sigma, depending on par space, systematics after 5 yrs
- Cosmology, or neutrinoless double beta decay may also provide indications

Vertex distribution of ν_e candidates



2011 analysis (Run 1+2, black points) had a discrepancy in radial distribution of event candidates

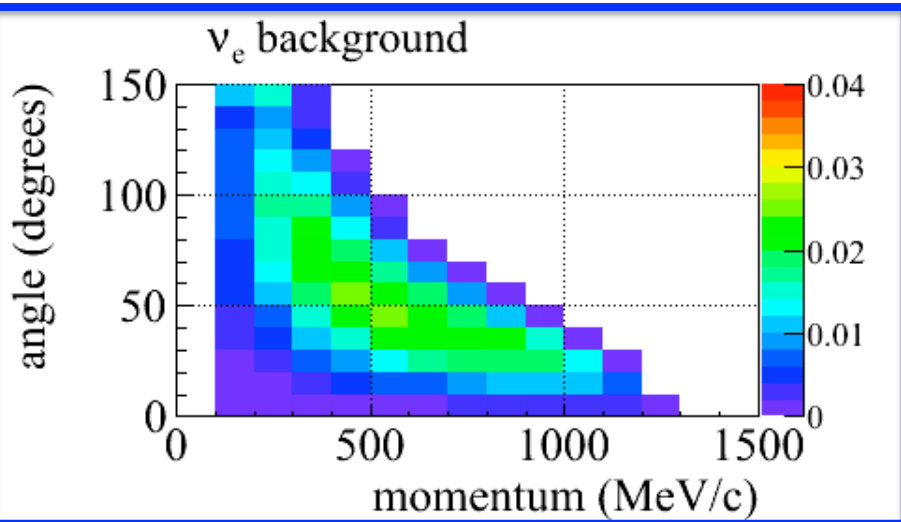
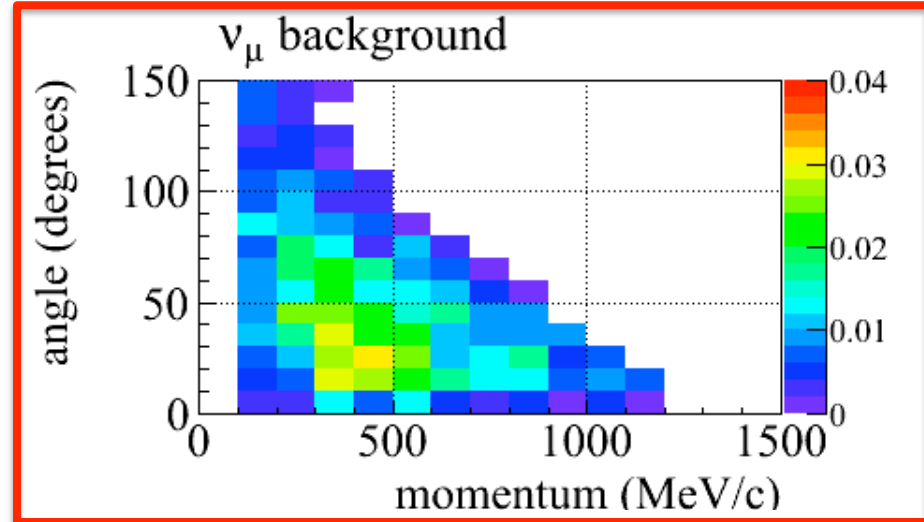
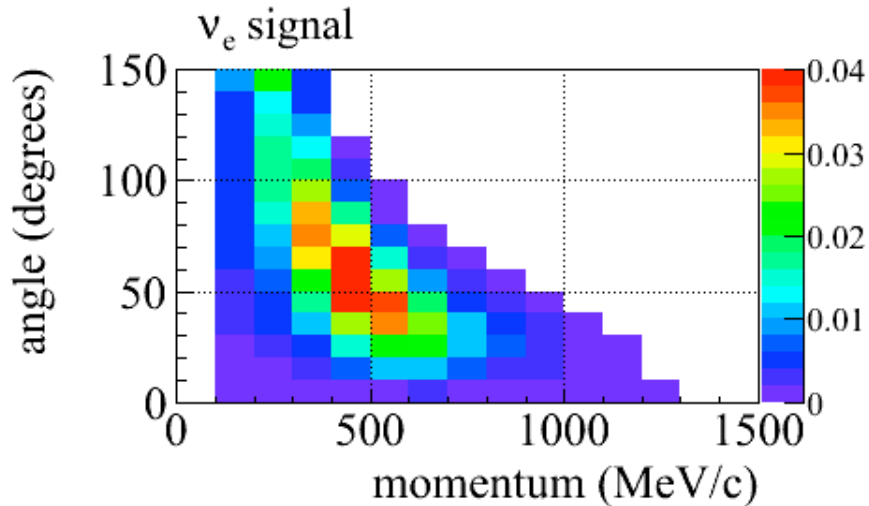
Radial distribution of new data (Run 3, pink) appears normal

KS test of radial distribution

Run 1+2: 10%

Run 3: 74.6%

Separating signal and background



Additional separation of signal, background events with CC ν_e candidate kinematics

- CC ν_e backgrounds come from higher energy neutrinos and populate signal and higher momentum region
- NC backgrounds are due to misID'd photons that reconstruct as electrons at low momentum and low angle (as well as the signal region)

Basic neutrino event selection (Run 1+2)

Basic neutrino selection (precuts)

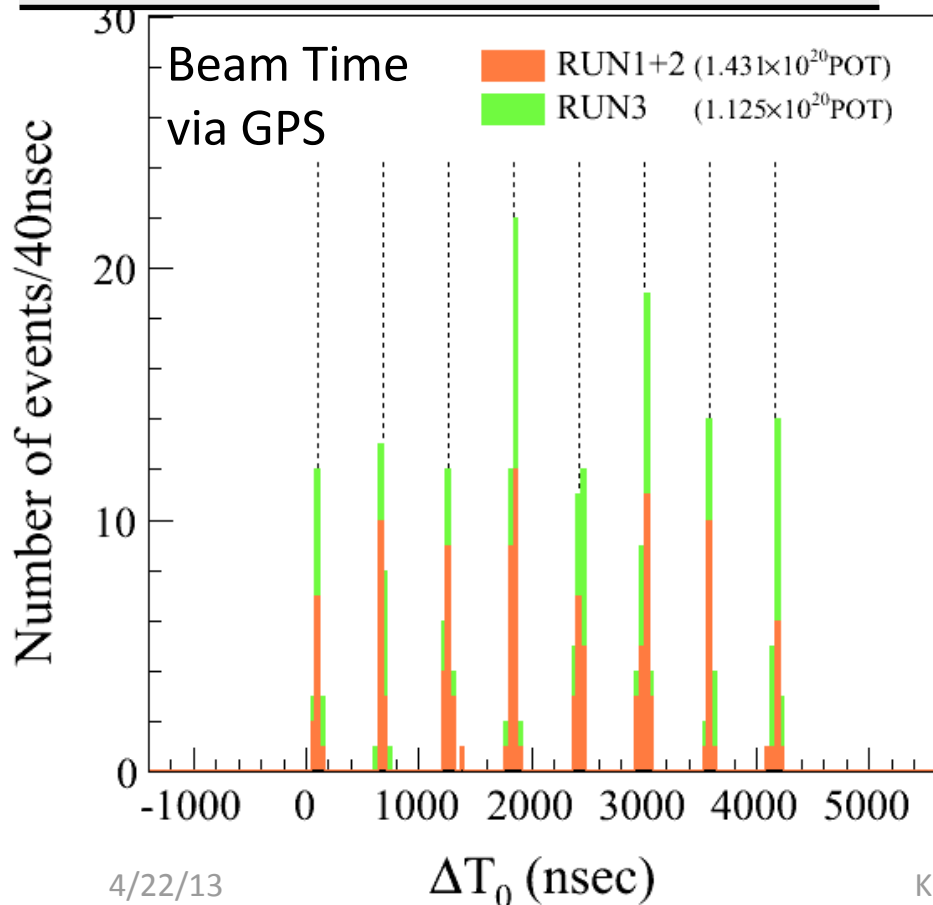
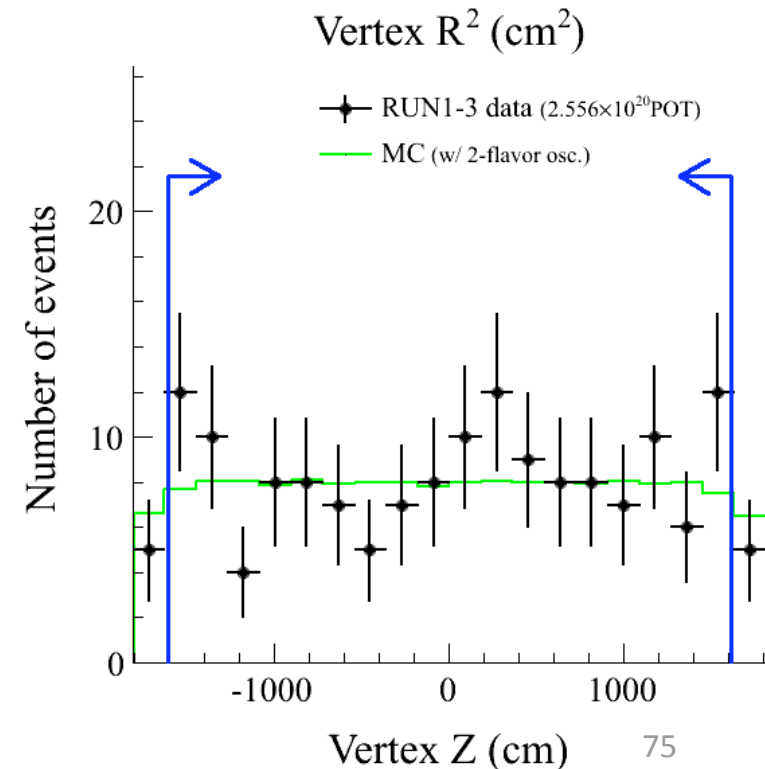
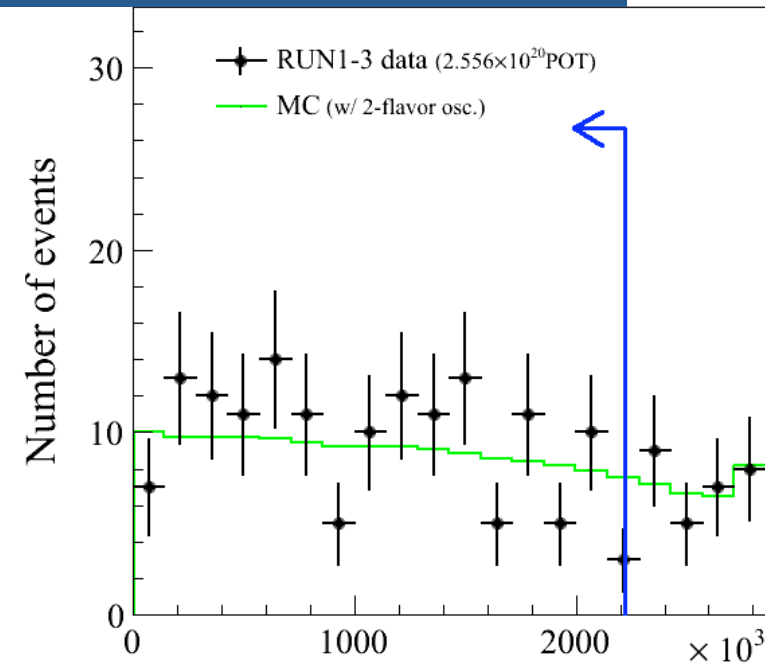
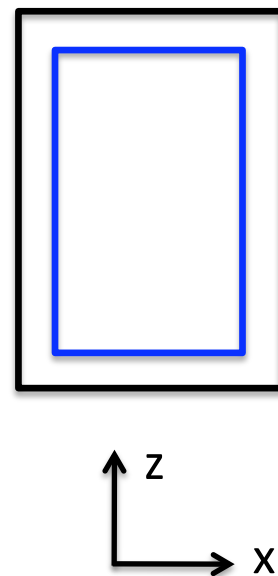
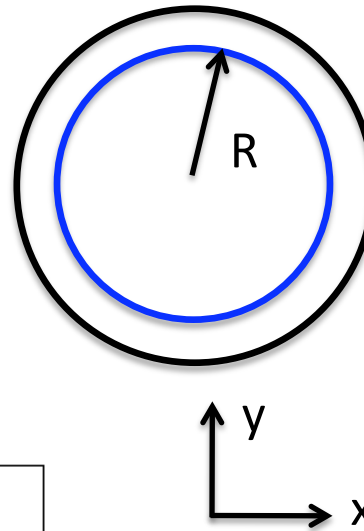
Event time within beam window

No activity in the veto

Visible $E > 30$ MeV

Reconstructed vertex > 2 m from wall

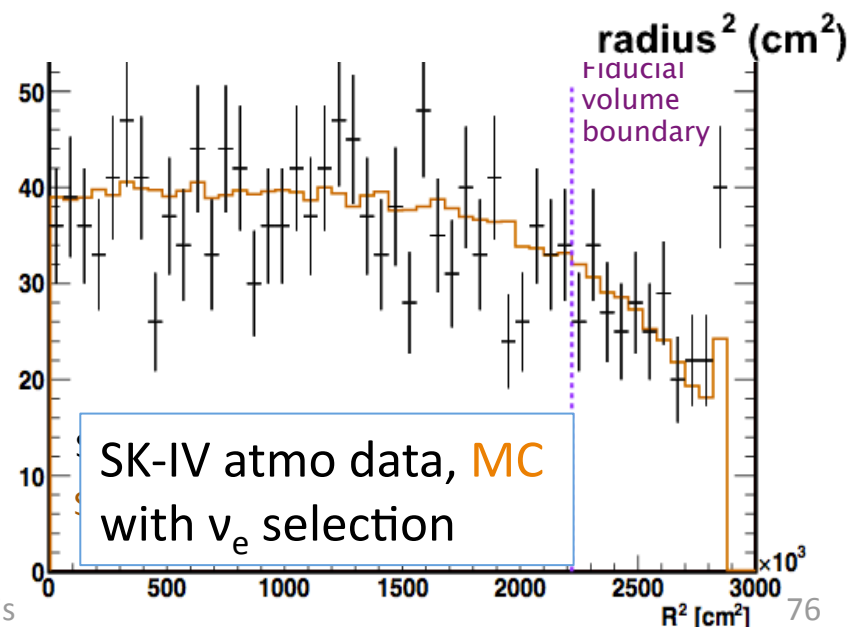
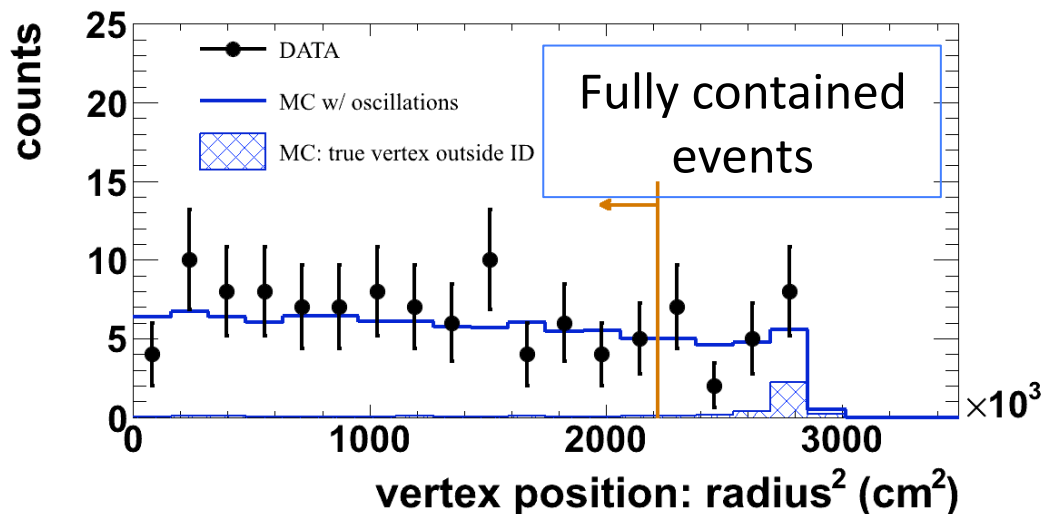
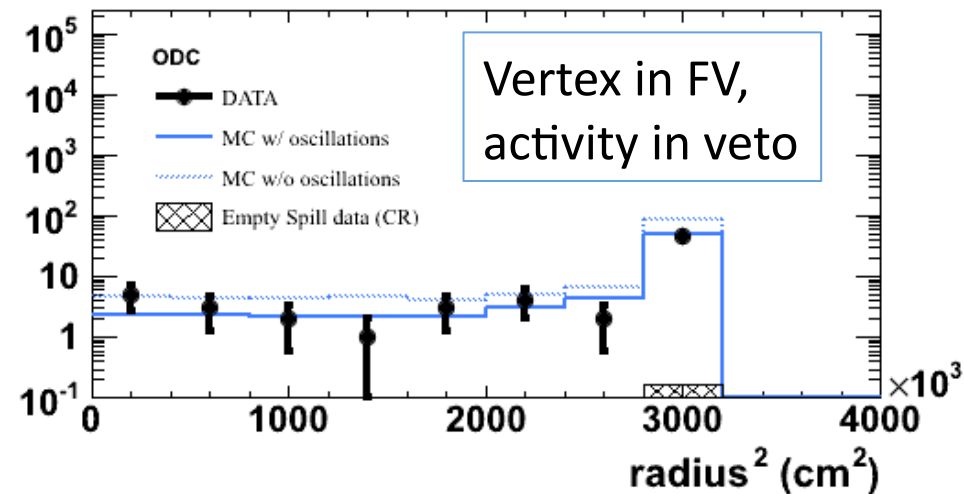
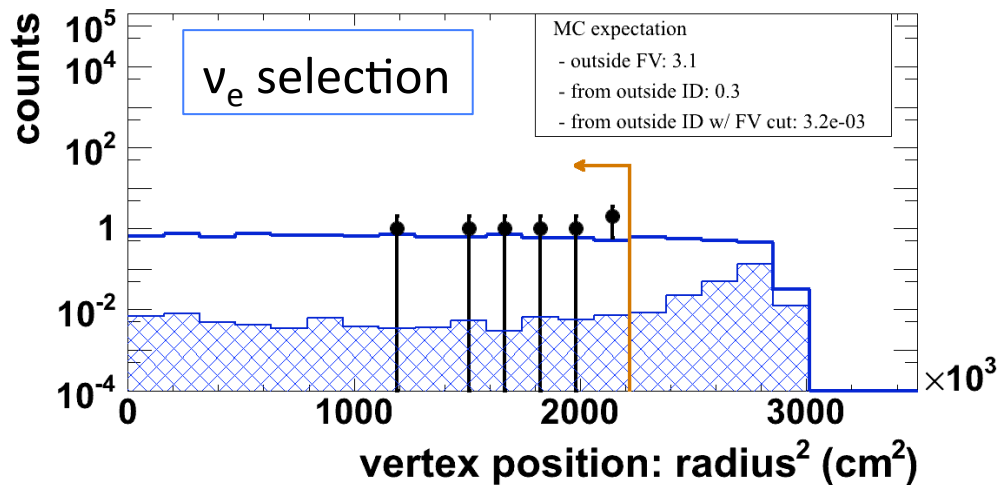
Single reconstructed ring



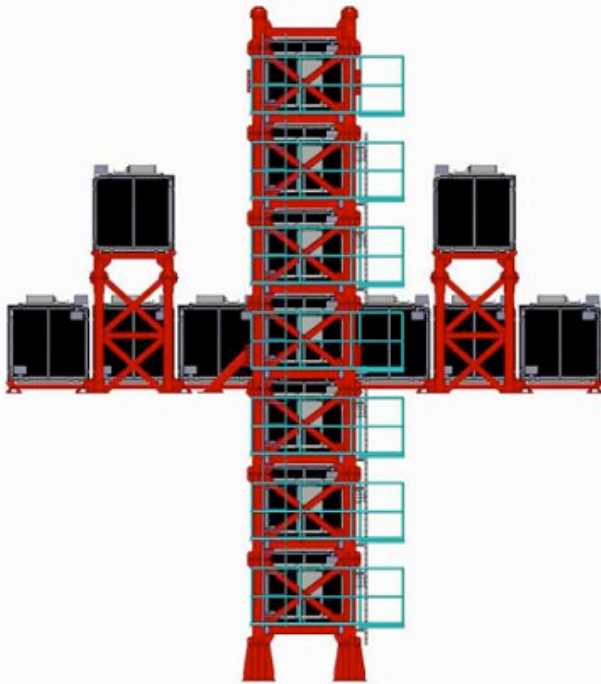
Beam backgrounds at high radius (Run 1+2)

MC simulates neutrino interactions upstream of the detector (e.g. π^0 production)

- Only 1 ν_e event cut by FV selection (no excess of ν_e events outside FV)
- Dedicated sample of events entering tank (with activity in veto) agree
- No bias to radial distribution of atmospheric sample under T2K ν_e selection



On-axis Interactive Neutrino GRID (INGRID)



16 modules arranged in a cross

- X-Y iron-scintillator layers, 7.1 tons each

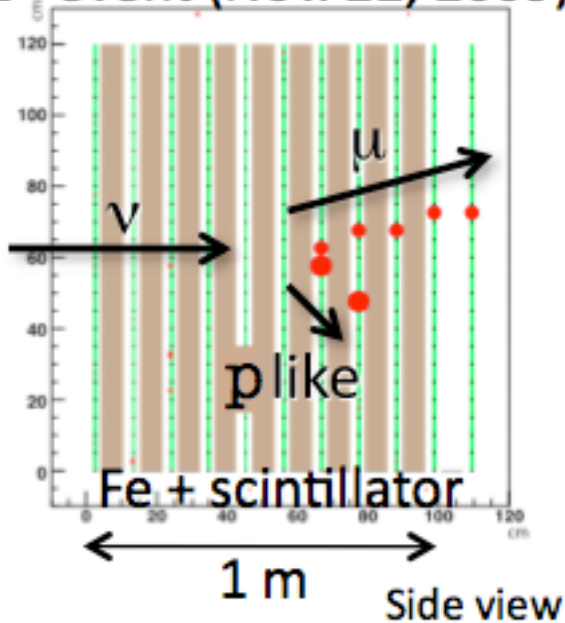
Count neutrino interactions in each module to determine neutrino rate vs. position

Extract beam direction better than 0.5 mrad

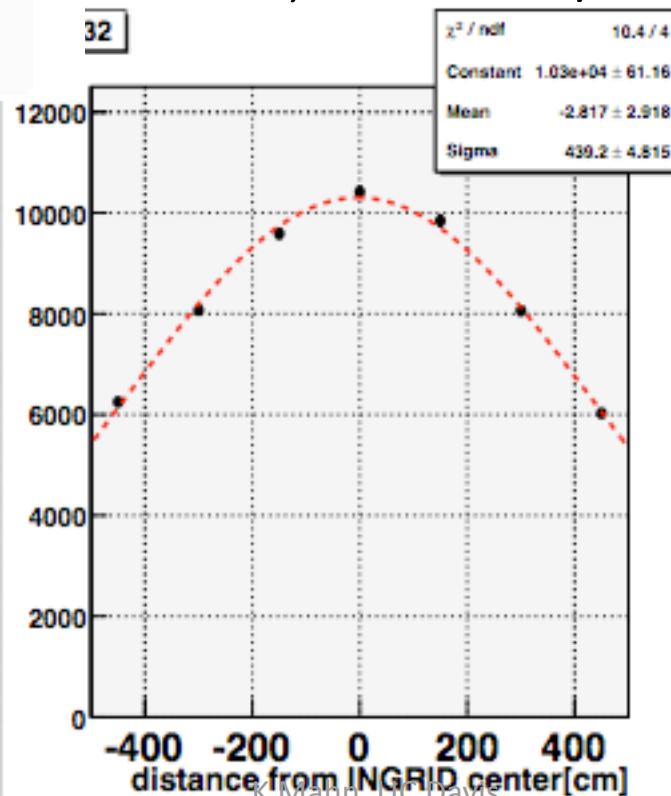
Monitor of neutrino beam vs. time

- $\sim 1.5 \nu / 10^{14}$ protons on target
- $\sim 10,000$ events / day

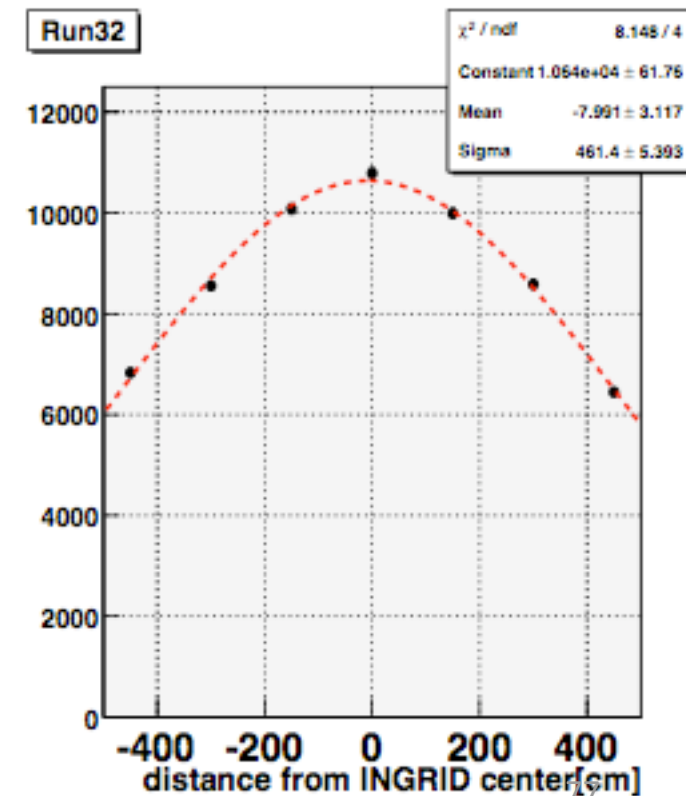
1st event (Nov. 22, 2009)



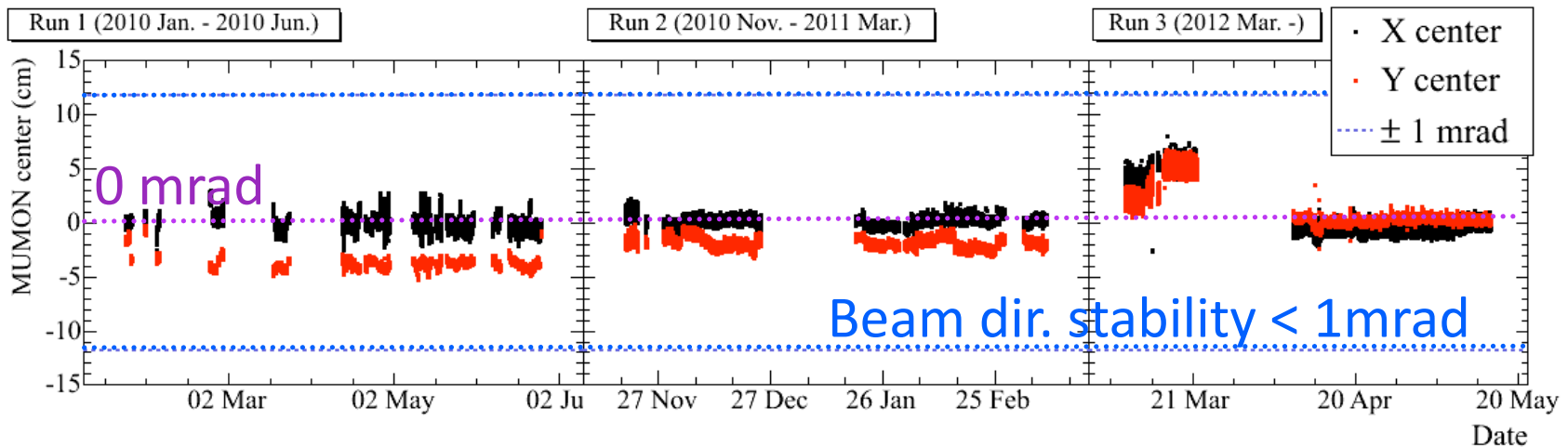
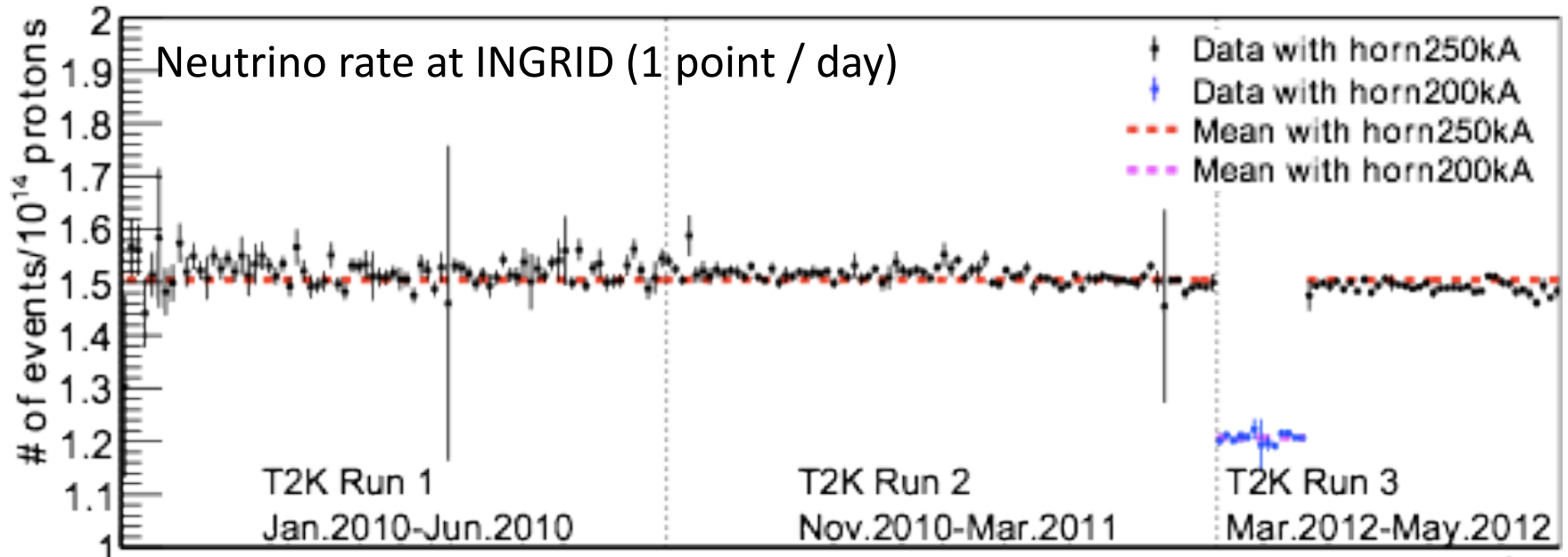
32



Run32

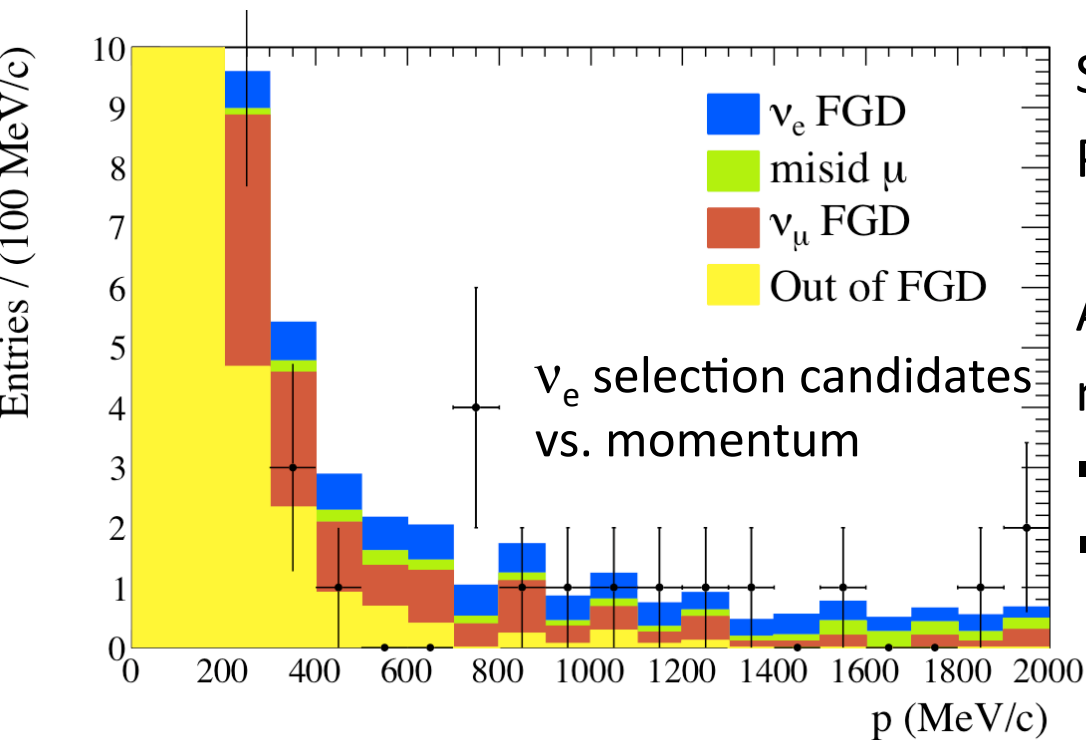


Neutrino beam stability



Beam direction (x and y)
with the muon monitor
Stable to <1 mrad

ND280 beam ν_e rate cross-check (I)



Select ν_e candidates at ND280 with TPC PID to check rate of intrinsic beam ν_e

Additional backgrounds to ν_e selection, measured via control samples

- μ misidentified as e
- e from photon conversion (photons emitted in ν_μ interactions in FGD and other subdetectors)

Ratio of observed ν_e / ν_μ events is consistent with untuned prediction

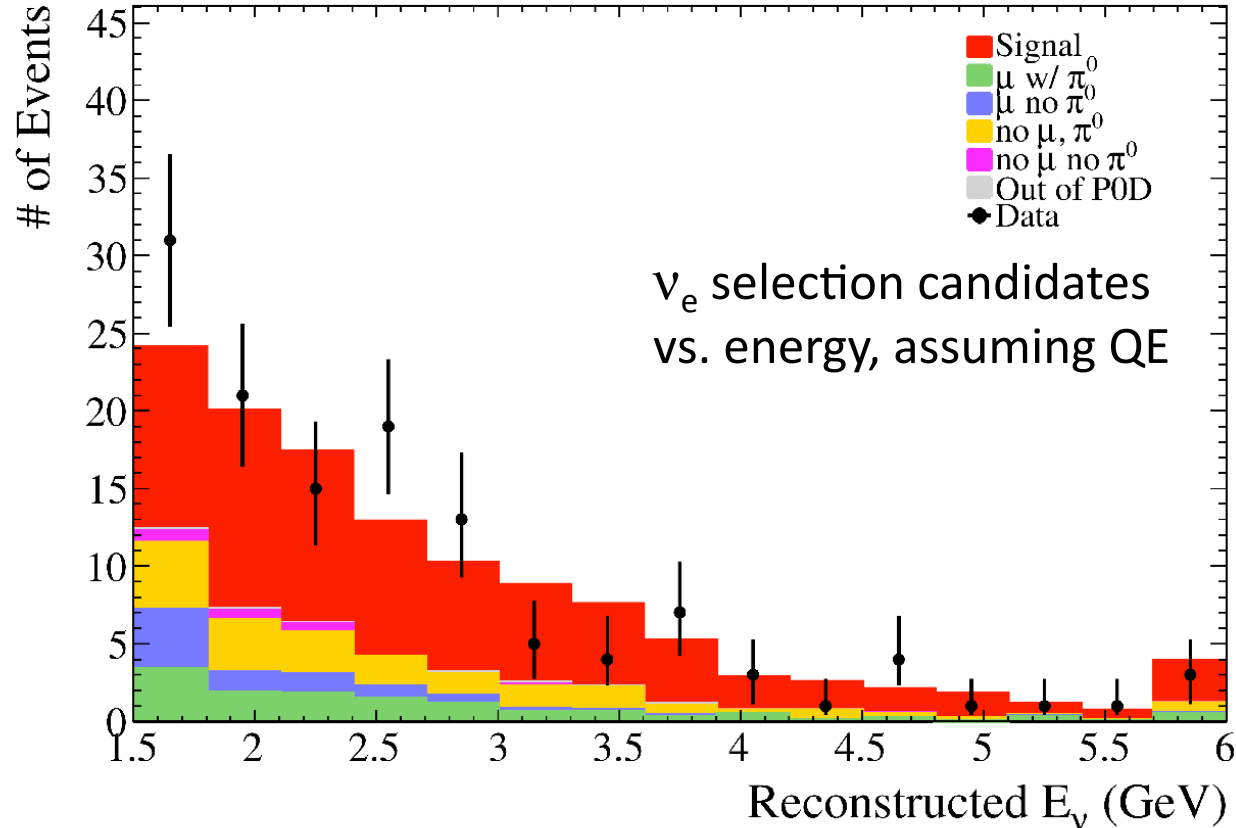
$$N(\nu_e) / N(\nu_\mu) = R(e:\mu) = 1.0\% \pm 0.7\% \text{ (statistics)} \pm 0.3\% \text{ (systematics)}$$

$$R(e:\mu, \text{data}) / R(e:\mu, \text{MC}) = 0.6 \pm 0.4 \text{ (statistics)} \pm 0.2 \text{ (systematics)}$$

Improvements to the analysis:

- Improved rejection of backgrounds with ECals
- More data: 2.88×10^{19} POT shown here

ND280 beam ν_e rate cross-check (II)



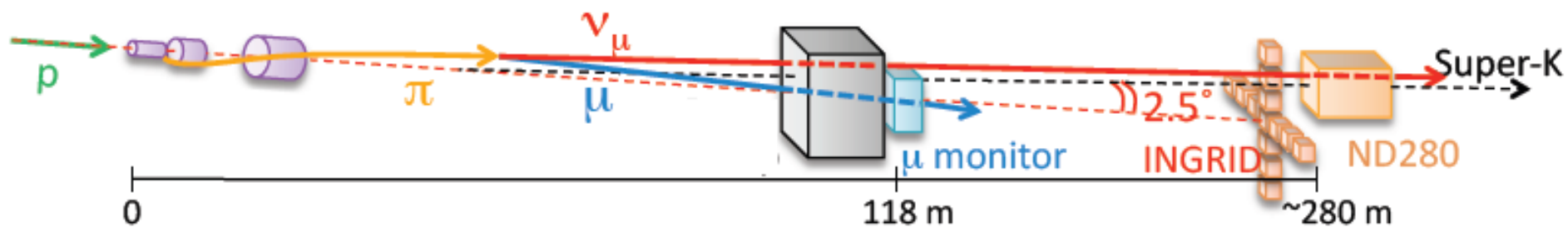
Select high energy CC ν_e candidates within the POD:

- Reconstructed track matched in x,y with vertex in FV consistent with an single EM shower (reject π^0 multiple photon showers and muons)
- Primary backgrounds are HE π^0 events

Consistent with current untuned MC:

$$\text{data-bkrd(MC)/sig(MC)} = R = 1.19 \pm 0.15(\text{statistics}) \pm 0.26(\text{systematics})$$

Neutrino flux prediction



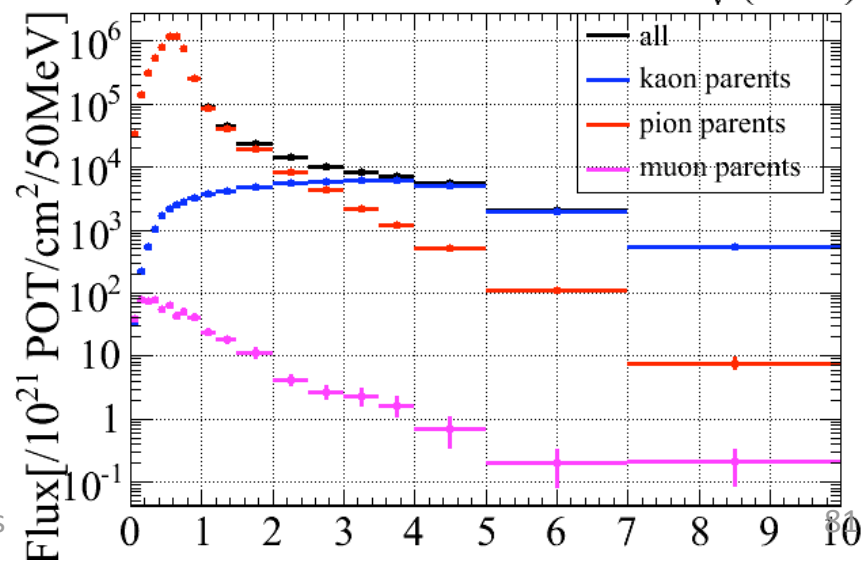
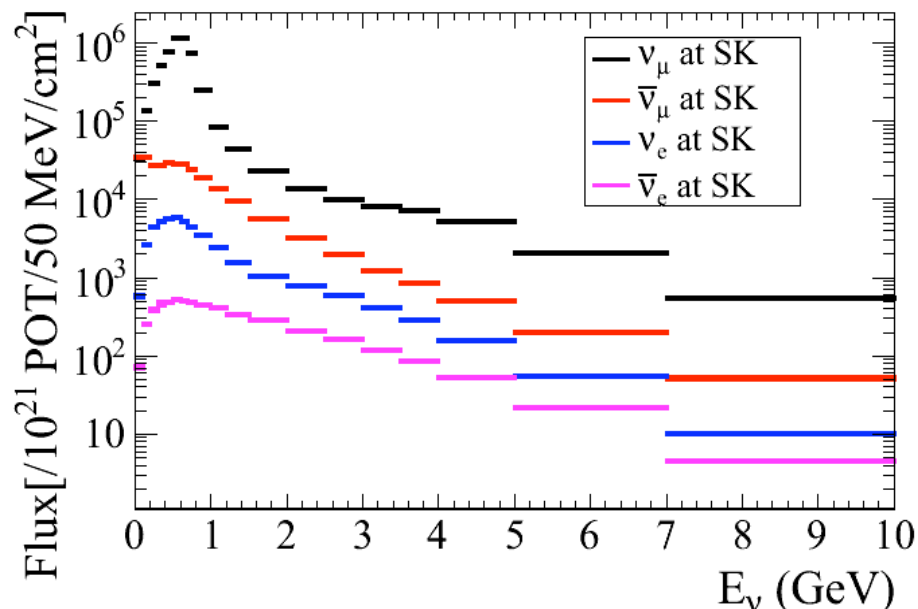
FLUKA/Geant3 beam simulation

Unoscillated flux at SK:

- ν_{μ} from π^+ , K decay
- $\sim 1\%$ ν_e from μ , K decay

Prediction and uncertainties determined by **external** or **in-situ** measurements of:

- proton beam
- π , K production from NA61 experiment
- Phys.Rev.C 84, 034604 (2011)
- Phys.Rev.C 85, 035210 (2012)
- alignment and off-axis angle

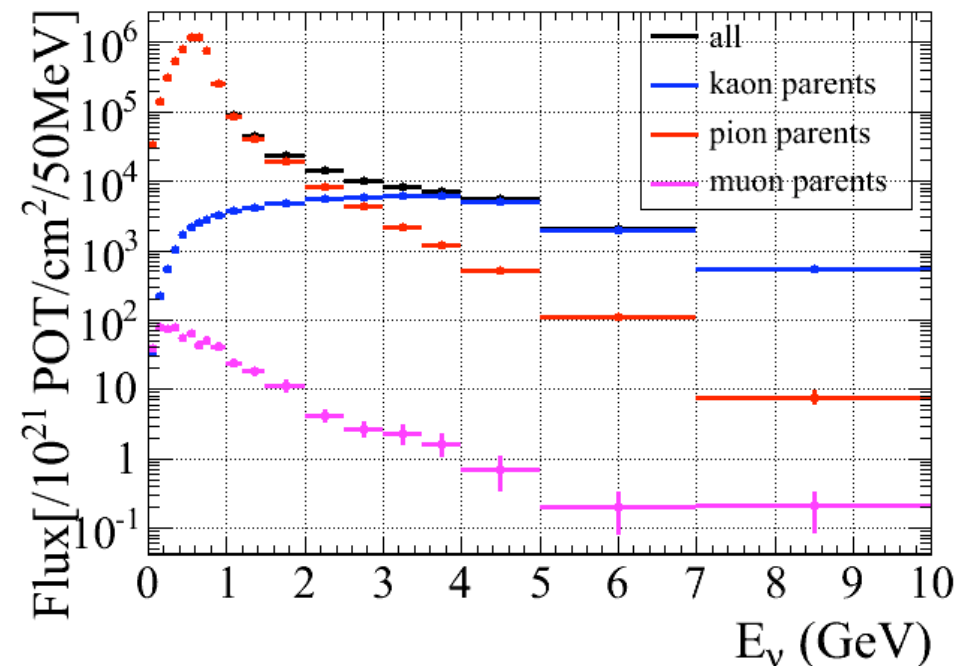
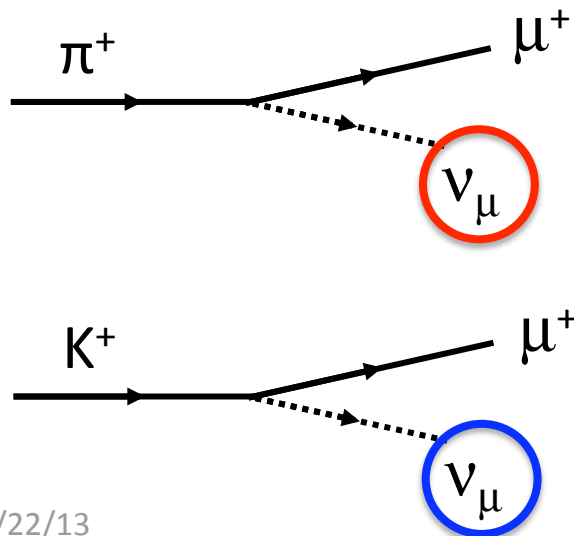


Neutrino flux at ND and SK

Neutrino Mode	Trkr. ν_μ	Trkr. ν_μ	SK ν_e	SK ν_e	SK ν_e
	CCQE	CCnQE	Sig.	CC intrinsic Bgnd.	NC Bgnd.
$\pi^+ \rightarrow \nu_\mu + \mu^+$	82.2%	45.8%	99.3%	1.1%	70.3%
$\mu^+ \rightarrow \nu_e + e^+ + \bar{\nu}_\mu$	<1%	<1%	<0.1%	66.0%	<0.1%
$K^{+,0} \rightarrow \nu_e + X$	<1%	<1%	<0.1%	33.0%	<0.1%
$K^{+,0} \rightarrow \nu_\mu + X$	17.4%	53.4%	0.7%	–	29.7%

ND samples represent ν_μ flux

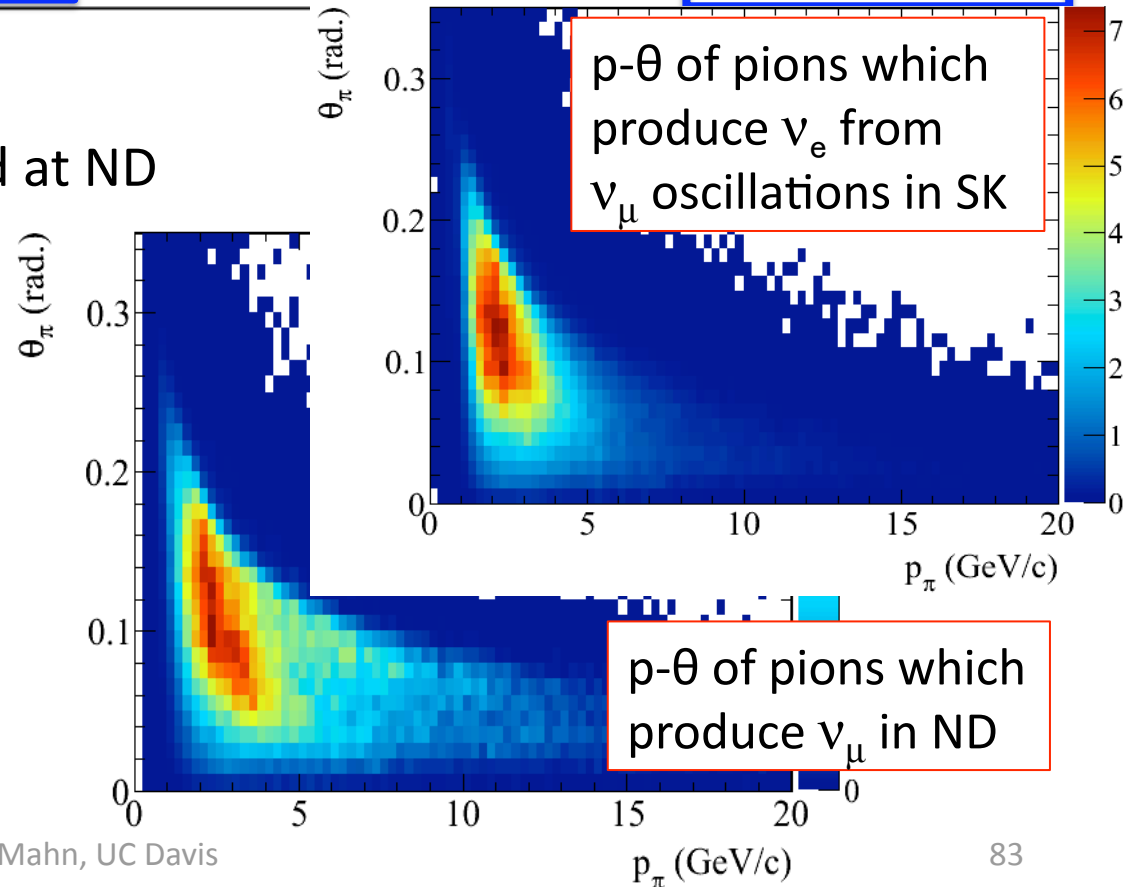
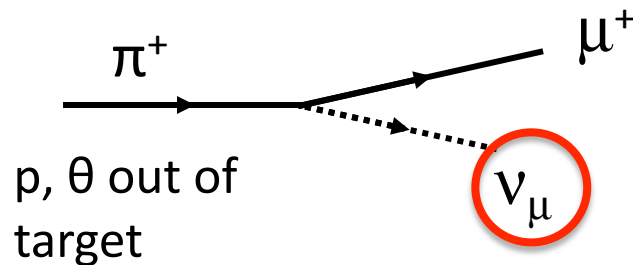
- ν_μ from π decay: CCQE, CCnQE samples
- ν_μ from K decay: CCnQE sample



Neutrino flux at ND and SK

Neutrino Mode	Trkr. ν_μ	Trkr. ν_μ	SK ν_e	SK ν_e	SK ν_e
	CCQE	CCnQE	Sig.	CC intrinsic Bgnd.	NC Bgnd.
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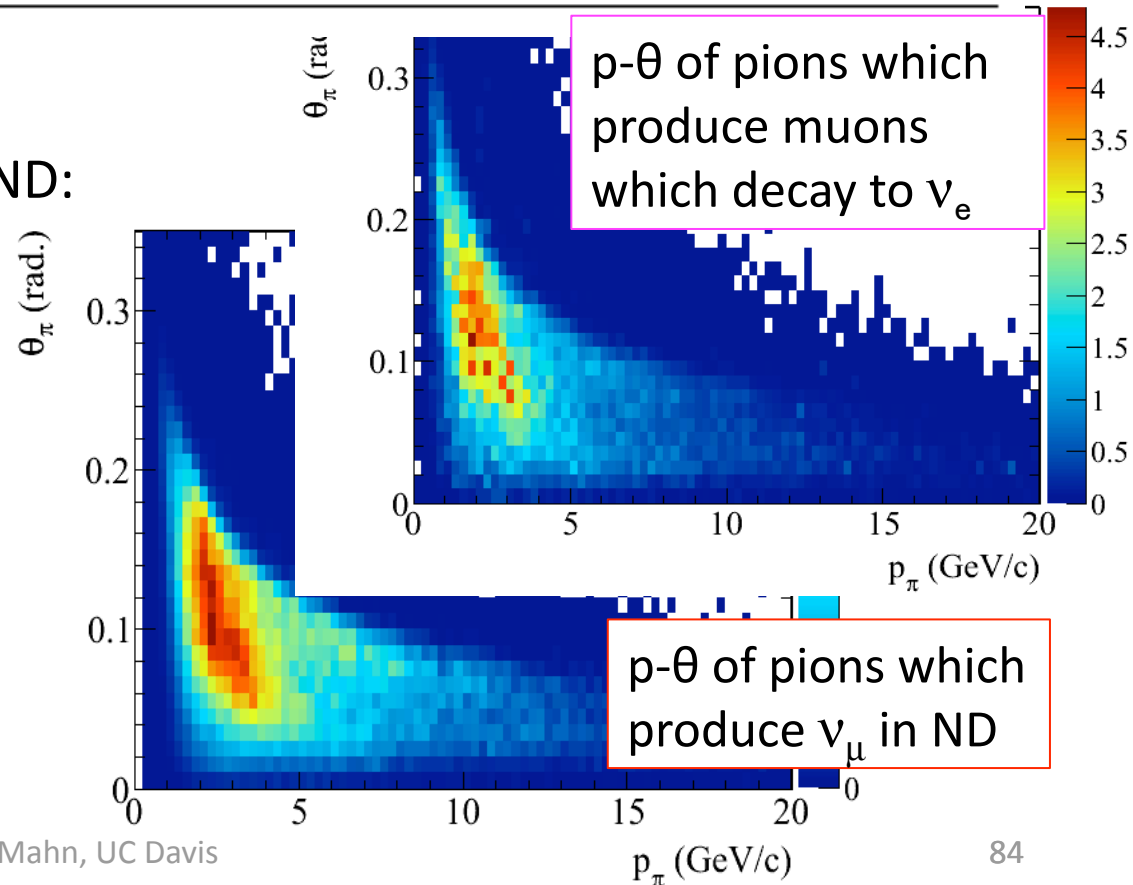
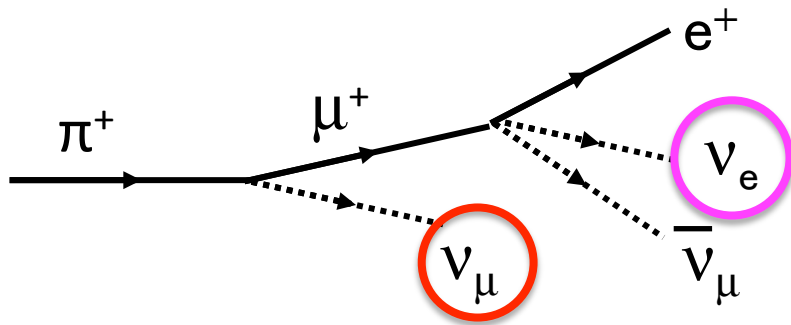
SK signal and NC background events
come from ν_μ flux directly measured at ND



Neutrino flux at ND and SK

Neutrino Mode	Trkr. ν_μ	Trkr. ν_μ	SK ν_e	SK ν_e	SK ν_e
	CCQE	CCnQE	Sig.	CC intrinsic Bgnd.	NC Bgnd.
$\pi^+ \rightarrow \nu_\mu + \mu^+$	82.2%	45.8%	99.3%	1.1%	70.3%
$\mu^+ \rightarrow \nu_e + e^+ + \bar{\nu}_\mu$	<1%	<1%	<0.1%	66.0%	<0.1%
$K^{+,0} \rightarrow \nu_e + X$	<1%	<1%	<0.1%	33.0%	<0.1%
$K^{+,0} \rightarrow \nu_\mu + X$	17.4%	53.4%	0.7%	–	29.7%

CC background from beam ν_e is strongly correlated with ν_μ flux at ND:



Neutrino interactions at ND and SK

Interaction Mode	Trkr. ν_μ CCQE	Trkr. ν_μ CCnQE	SK ν_e Sig.	SK ν_e Bgnd.
CCQE	76.6%	14.6%	85.8%	45.0%
CC1 π	15.6%	29.3%	13.7%	13.9%
CC coh.	1.9%	4.2%	0.3%	0.7%
CC other	4.1%	37.0%	0.2%	0.7%
NC	1.5%	5.3%	-	39.7%

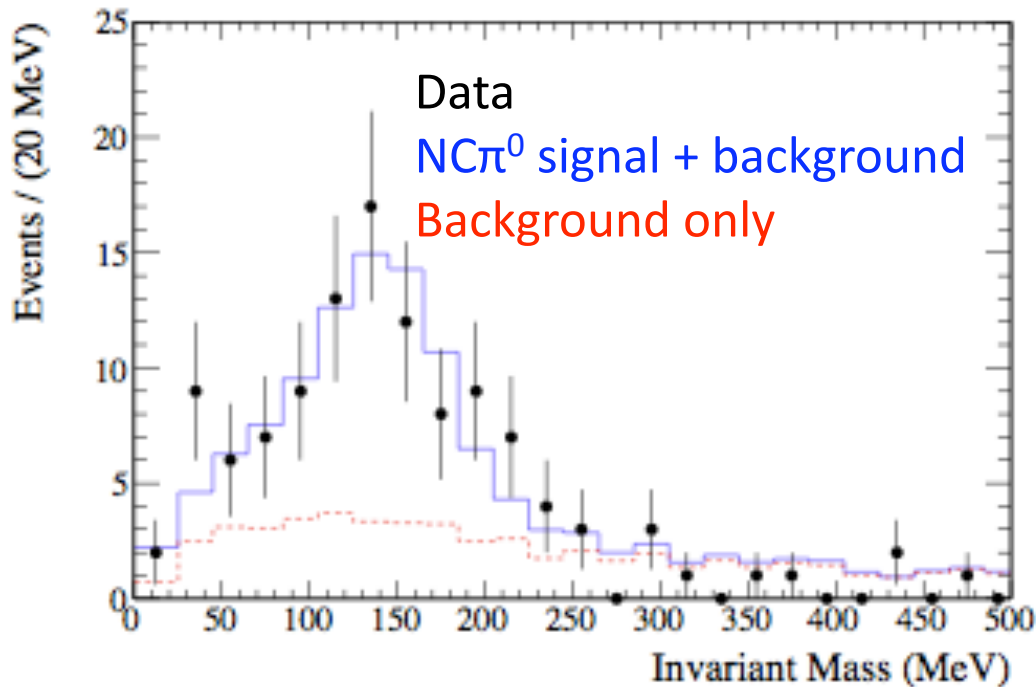
CCQE and CC1 π are the largest interaction mode in ND, SK samples

- Separation of CCQE and CCnQE ND samples gives additional power for fit to constrain cross section models
- Need to account for acceptance difference between ND (forward going selection) and SK (4 π selection) for identical changes to cross section to correlate the two samples

From experience with SciBooNE/MiniBooNE joint analysis, developed machinery to alter the cross section for each simulated event

Neutrino interactions at ND and SK

Interaction Mode	Trkr. ν_μ CCQE	Trkr. ν_μ CCnQE	SK ν_e Sig.	SK ν_e Bgnd.
CCQE	76.6%	14.6%	85.8%	45.0%
CC1 π	15.6%	29.3%	13.7%	13.9%
CC coh.	1.9%	4.2%	0.3%	0.7%
CC other	4.1%	37.0%	0.2%	0.7%
NC	1.5%	5.3%	-	39.7%

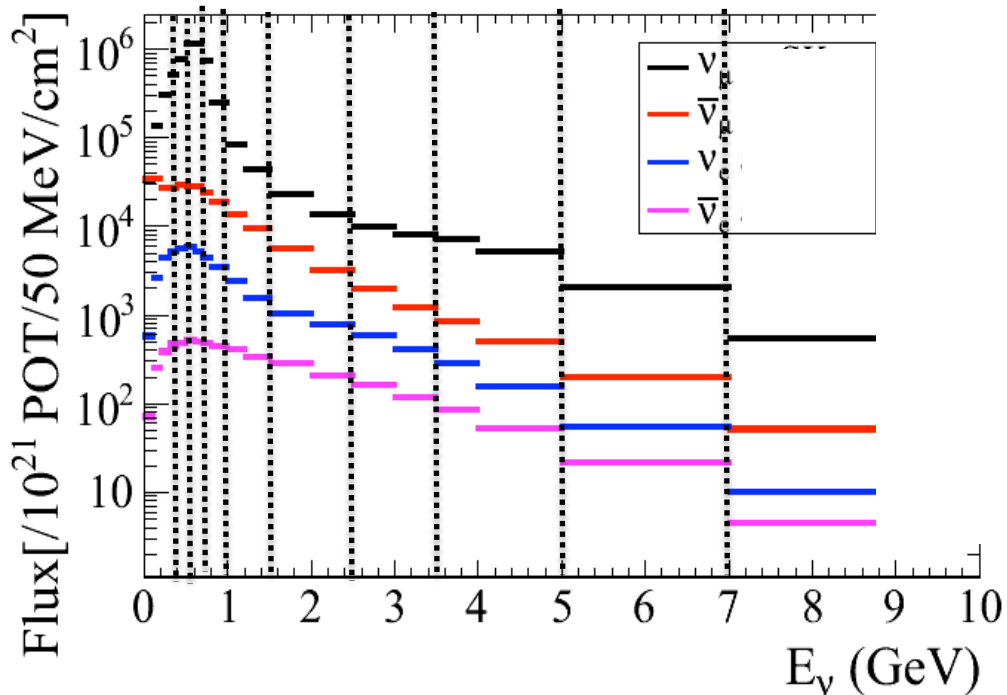


- Indirect constraint on NC ($1\pi^0$) through CC1 π in ND measurement
- Additional ND selection of NC π^0 with POD detector to cross check rate prediction

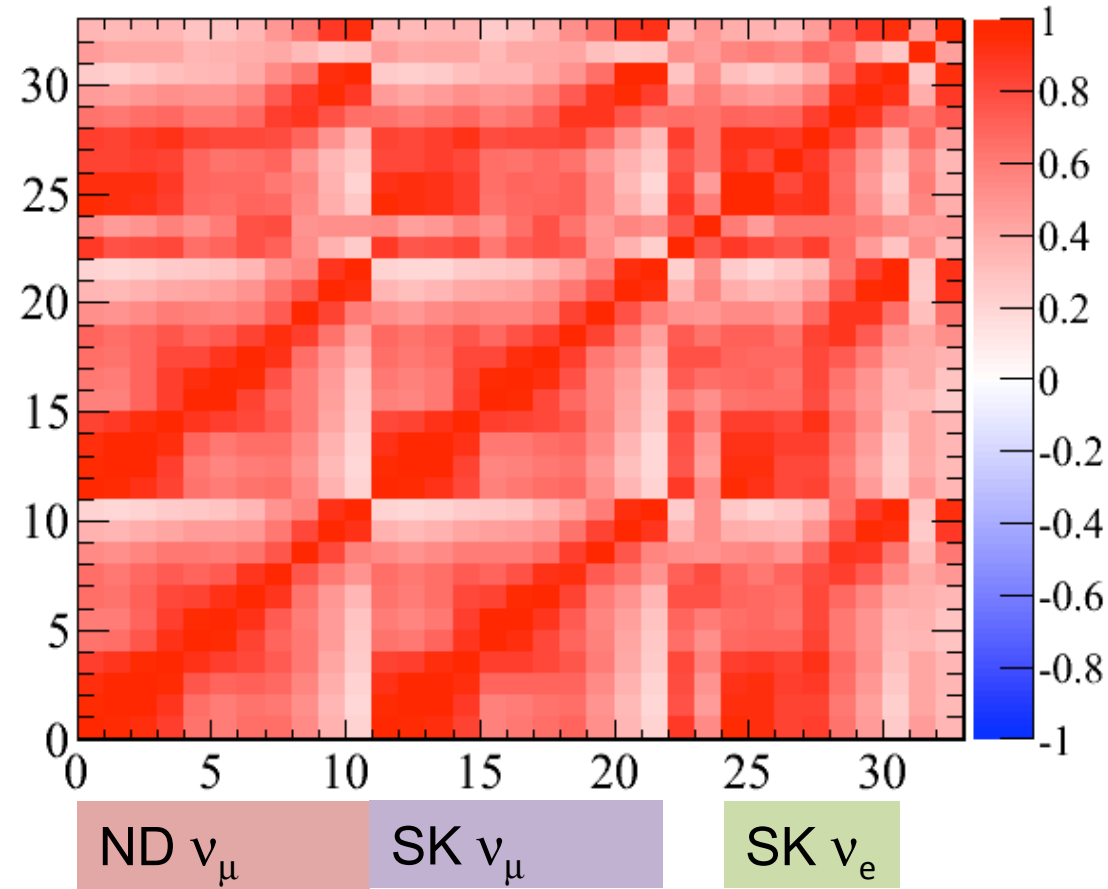
Flux parameterization

Neutrino flux prediction

Flux parameterization: f_i
 Normalization on E_ν bin i for SK
 and ND samples



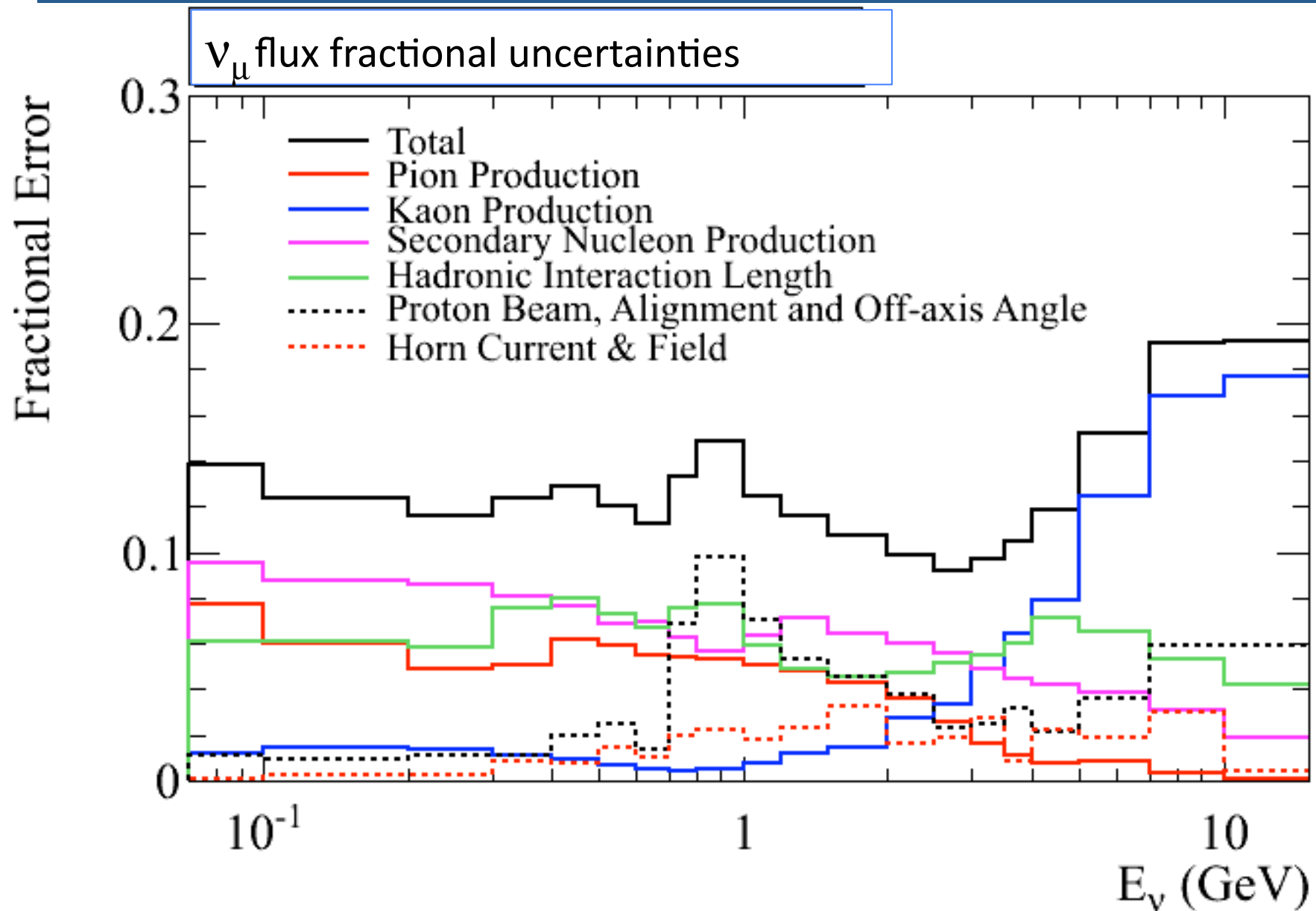
Correlations between flux bins



Correlations in flux covariance are shared
 hadron production uncertainties

Flux covariance built from measurements
 of beam or external data (e.g. NA61)

T2K neutrino flux uncertainties



Cross section parameterization

Cross section parameterization: X_k

Model parameters:

- MAQE and MARES (modify Q^2 distribution of QE and resonant 1π cross sections)
- Fermi momentum (pF) provides low Q^2 handle, and is target dependant (C vs. O)
- Spectral function – RFG model-model difference is also target dependant

Normalizations provide overall scaling independent of Q^2 on a particular interaction

Apply cross section to observables at ND, SK using reweighting techniques

M_A^{QE} (GeV)	1.21 ± 0.45	1.19 ± 0.19
M_A^{RES} (GeV)	1.162 ± 0.110	1.137 ± 0.095
CCQE Norm. 0-1.5 GeV	1.000 ± 0.110	0.941 ± 0.087
CCQE Norm. 1.5-3.5 GeV	1.00 ± 0.30	0.92 ± 0.23
CCQE Norm. >3.5 GeV	1.00 ± 0.30	1.18 ± 0.25
CC 1π Norm. 0-2.5 GeV	1.63 ± 0.43	1.67 ± 0.28
CC 1π Norm. >2.5 GeV	1.00 ± 0.40	1.10 ± 0.30
NC $1\pi^0$ Norm.	1.19 ± 0.43	1.22 ± 0.40
Fermi Momentum (MeV/c)	217 ± 30	224 ± 24
Spectral Function	$0(\text{off}) \pm 1(\text{on})$	0.04 ± 0.21
CC Other Shape (GeV)	0.00 ± 0.40	-0.05 ± 0.35

Parameter value, uncertainty is determined from MiniBooNE single pion samples

Parameter value, uncertainty is extrapolated to SK sample

ND280 likelihood

$$-2\ln L = 2 \sum_i^{p,\theta \text{ bins}} N_i^{\text{pred}}(\vec{f}, \vec{x}, \vec{d}) - N_i^{\text{data}} + N_i^{\text{data}} \ln[N_i^{\text{data}} / N_i^{\text{pred}}(\vec{f}, \vec{x}, \vec{d})]$$

Likelihood function, with Poisson statistics

$$+ \sum_j^{E_\nu \text{ bins}} \sum_k^{E_\nu \text{ bins}} (1 - f_j)(V_f^{-1})_{j,k}(1 - f_k)$$

$$+ \sum_l^{xsec \text{ pars}} \sum_m^{xsec \text{ pars}} (x_{nom} - x_l)(V_x^{-1})_{l,m}(x_{nom} - x_m)$$

$$+ \sum_i^{p,\theta \text{ bins}} \sum_n^{p,\theta \text{ bins}} (1 - d_i)(V_d^{-1})_{i,n}(1 - d_n)$$

$$+ \ln\left(\frac{|V_d(\vec{f}, \vec{x})|}{|V_d^{nom}|}\right)$$

Fit CCQE, CCnQE p_μ - θ_μ distribution (20x2 bins)

Sensitive to to rate ($\Phi \times \sigma$) changes:

$$E_\nu^{QE} = \frac{m_p^2 - m_n'^2 - m_\mu^2 + 2m_n' E_\mu}{2(m_n' - E_\mu + p_\mu \cos \theta_\mu)}$$

ND280 likelihood

$$-2\ln L = 2 \sum_i^{p,\theta \text{ bins}} N_i^{\text{pred}}(\vec{f}, \vec{x}, \vec{d}) - N_i^{\text{data}} + N_i^{\text{data}} \ln[N_i^{\text{data}} / N_i^{\text{pred}}(\vec{f}, \vec{x}, \vec{d})]$$

$$+ \sum_j^{E_\nu \text{ bins}} \sum_k^{E_\nu \text{ bins}} (1 - f_j)(V_f^{-1})_{j,k}(1 - f_k)$$

$$\ln L_{\text{flux}}(\vec{f})$$

$$+ \sum_l^{xsec \text{ pars}} \sum_m^{xsec \text{ pars}} (x_{nom} - x_l)(V_x^{-1})_{l,m}(x_{nom} - x_m)$$

$$\ln L_{xsec}(\vec{x})$$

$$+ \sum_i^{p,\theta \text{ bins}} \sum_n^{p,\theta \text{ bins}} (1 - d_i)(V_d^{-1})_{i,n}(1 - d_n)$$

$$+ \ln\left(\frac{|V_d(\vec{f}, \vec{x})|}{|V_d^{nom}|}\right)$$

Prior constraint terms for **flux**, **cross section** parameters

- V_f and V_x are covariance matrices
- Determined using in-situ and external datasets: beam monitors, NA61, MiniBooNE

ND280 likelihood

$$-2\ln L = 2 \sum_i^{p,\theta \text{ bins}} N_i^{\text{pred}}(\vec{f}, \vec{x}, \vec{d}) - N_i^{\text{data}} + N_i^{\text{data}} \ln[N_i^{\text{data}} / N_i^{\text{pred}}(\vec{f}, \vec{x}, \vec{d})]$$

$$+ \sum_j^{E_\nu \text{ bins}} \sum_k^{E_\nu \text{ bins}} (1 - f_j)(V_f^{-1})_{j,k}(1 - f_k)$$

$$+ \sum_l^{xsec \text{ pars}} \sum_m^{xsec \text{ pars}} (x_{nom} - x_l)(V_x^{-1})_{l,m}(x_{nom} - x_m)$$

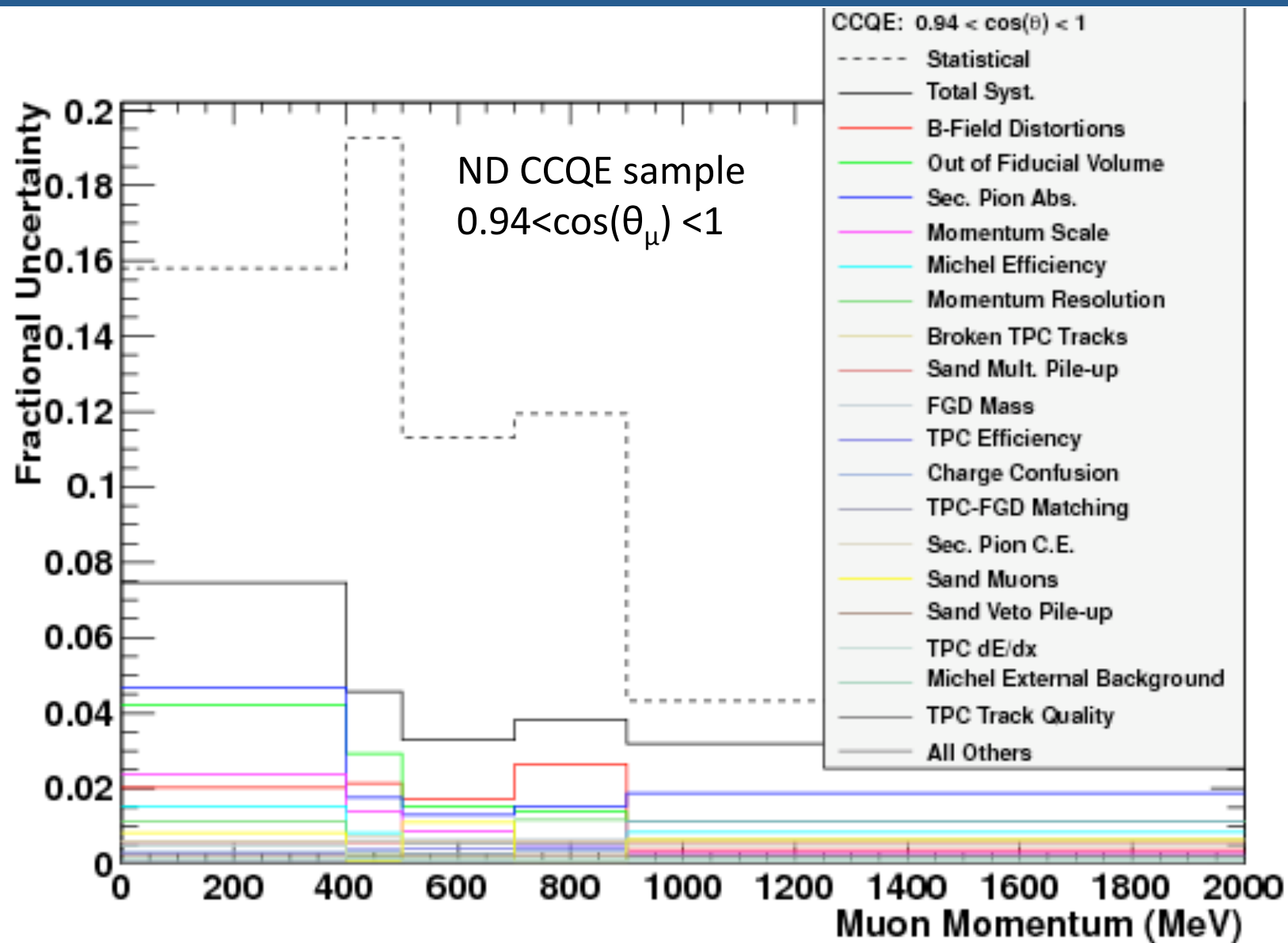
$$+ \sum_i^{p,\theta \text{ bins}} \sum_n^{p,\theta \text{ bins}} (1 - d_i)(V_d^{-1})_{i,n}(1 - d_n)$$

$$+ \ln\left(\frac{|V_d(\vec{f}, \vec{x})|}{|V_d^{nom}|}\right)$$

Prior constraint likelihood terms for
detector systematic errors

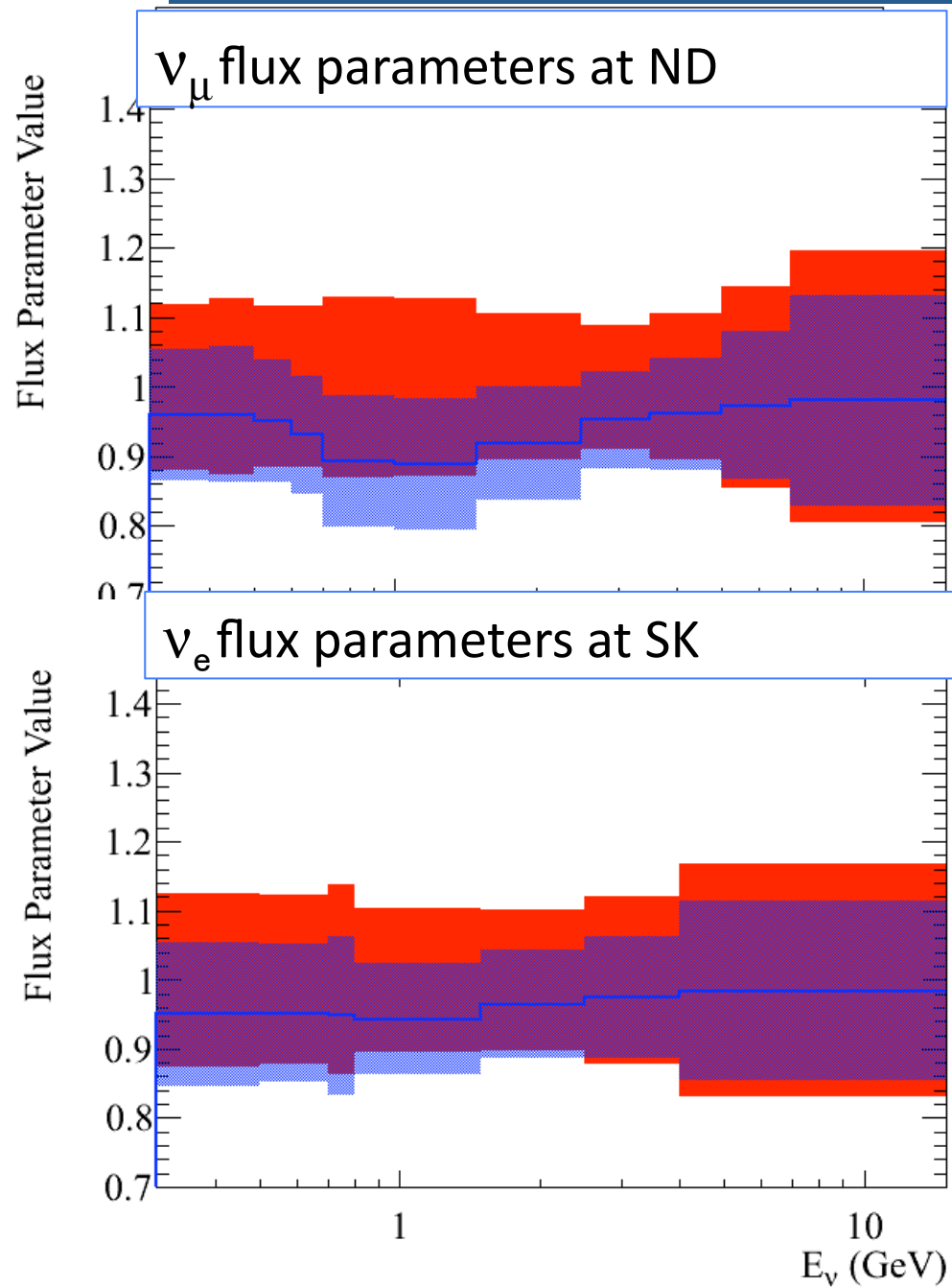
- Also includes uncertainties (e.g. FSI) which could not be otherwise easily parameterized
- Determined from control samples, calibration data, and external pion scattering data

Detector systematic errors

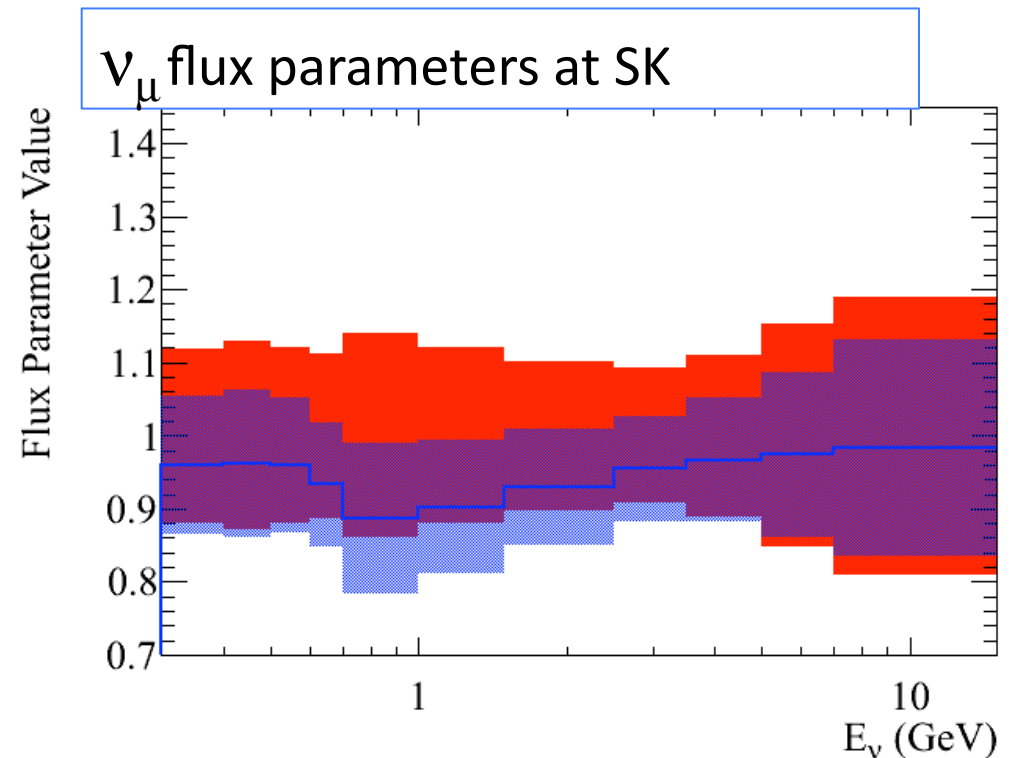


Fractional systematic uncertainty for vs. momentum

Flux parameters change after ND measurement



- Flux parameters without ND measurement and with ND measurement



Effect of ND measurement on ν_e signal, background

- Rate of ν_e signal and backgrounds **without ND measurement** and **with ND measurement**
- Uncertainty envelope from constrained flux, cross section parameters
- Includes correlation between flux and cross section at ND, SK

