

Technicolor at Criticality

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Motivations

The SM with a fundamental Higgs remarkably explains the EW physics: the EW precision parameters are compatible with "zero" ($S, T \approx 0$).

This suggests that **the Higgs sector of the SM is weakly coupled**.
If so, what about naturalness, then?

More fundamental descriptions:

- Supersymmetry is technically natural, but...
its perturbative formulation (though predictive) does not solve the hierarchy problem
- Technicolor (potentially) solves the hierarchy problem but...
does it have an IR weakly coupled Higgs?

Dynamical EW Symmetry Breaking¹

- Start with a chirally invariant strong dynamics (Technicolor = TC) and “weakly” gauge an $SU(2) \times U(1)$ subgroup of the flavor group.
- Spontaneous Chiral Symmetry Breaking, i.e. $\langle \bar{\psi}\psi \rangle \sim \Lambda_\chi^3$, implies EWSB.
- Choose appropriate boundary conditions so that the dynamical scale is set to $\Lambda_\chi = O(1)$ TeV.

YOU GET:

- a natural explanation, and stabilization, of the hierarchy $\Lambda_\chi \ll \Lambda_{UV}$
- W^\pm, Z^0 masses at the right scale (and $\rho = 1$)

BUT:

- what about Fermion Masses ?!
- what about Precision Tests ?!

¹S. Weinberg '76, Susskind '79

Fermion Mass Generation (1)

We would need to couple the SM fermions q to the Higgs operator $\bar{\psi}\psi$. This is generally accomplished with an Extended TC framework², and leads to ($f, y, G = O(1)$)

$$f \frac{(\bar{\psi}\psi)(\bar{\psi}\psi)}{\Lambda_{ETC}^2} \quad y \frac{(\bar{q}q)(\bar{\psi}\psi)}{\Lambda_{ETC}^2} \quad G \frac{(\bar{q}q)(\bar{q}q)}{\Lambda_{ETC}^2}$$

- $f \neq 0$: masses for the (pseudo) NGBs;
- $y \neq 0$: SM Fermion Masses;
- $G \neq 0$: FCNC !

²Dimopoulos and Susskind '79, Eichten and Lane '80

Fermion Mass Generation (2)

The typical SM fermion mass $m_f(\mu \sim \Lambda_{ETC})$ strongly depends on the scaling dimension $\Delta(\bar{\psi}\psi)$ of the Higgs:

$$m_f = y\Lambda_\chi \left(\frac{\Lambda_\chi}{\Lambda_{ETC}} \right)^{\Delta-1} \quad \Lambda_{ETC} > 10^3 \text{ TeV (FCNC)}$$

- with $\Delta(\bar{\psi}\psi) \sim 3$ (QCD-like) we have $m_f \sim 1 \text{ MeV}$
we cannot explain the 2nd and 3rd generations;
- with $\Delta(\bar{\psi}\psi) \sim 2$ we could explain the 2nd generation³
(still, the top is too heavy...)
- with $\Delta(\bar{\psi}\psi) \sim 1$ we could explain also the 3rd generation
(hierarchy hidden in y ...)

³Holdom '81

EW Precision Tests

The S parameter tends to be too large in models of Dynamical EW Symmetry Breaking.

- with $\Delta(\bar{\psi}\psi) \sim 3$ the Higgs $\bar{\psi}\psi$ is a loose bound state of N_{dof} techni-quarks and we expect

$$S \sim \frac{N_{dof}}{6\pi}$$

- with $\Delta(\bar{\psi}\psi) < 3$ in the UV, the perturbative estimates are not reliable (2nd WSR is not satisfied, AdS/CFT) and the S parameter decreases⁴

$$S \sim ???$$

⁴Sundrum and Hsu '93, Appelquist et al. '99, ...

Asymptotic Non-Freedom ?!

The bottom line of the above discussion is that models with

- $\Delta(\bar{\psi}\psi) < 3$ in the UV: **asymptotic NON-freedom**
- $\Delta(\bar{\psi}\psi) \sim 1$ in the IR: **"weakly coupled" Higgs**

are phenomenologically very compelling (m_f, S, \dots)

Nice. But:

- (i) **Are there explicit examples?** (main criticism to Holdom's)
- (ii) **What about Naturalness?** (main motivation for Technicolor)

In order to answer (i) and (ii), a deeper understanding of the IR structure of non-abelian gauge theories is required.

This aim motivates the present talk.

I will assume that

- the TC physics is analytic in N_f (number of massless flavors)
- Chiral Symmetry Breaking (χ SB) is responsible for confinement and the Schwinger-Dyson (SD) equation approach is a sensible tool

and conjecture that

- non-abelian gauge theories possess an asymptotically non-free phase where χ SB is induced by an order parameter with scaling dimension

$$\text{(IR)} \quad 1 \lesssim \Delta \leq 2 \quad \text{(UV)}$$

- and that such a theory (TC at criticality) admits a description in terms of a NJL-like model

Outline

- 1 Basic idea behind TC at Criticality
- 2 Phases of non-abelian gauge theories
 - The Banks-Zaks (BZ) fixed point and the Conformal Window
 - Confinement without χ SB or Asymptotic Non-Freedom?
- 3 Asymptotic Non-Freedom?!
 - Lattice?
 - Schwinger-Dyson equation and Quenched QED
 - An effective (dual) approach
- 4 TC at Criticality
 - The Composite Higgs
 - Flavor Physics
- 5 Conclusions

The Basic Ideas

The Nambu Jona-Lasinio (NJL) model

$$\bar{\psi}i\partial\psi + \frac{f}{2}(\bar{\psi}\psi)^2$$

nicely describes dynamical chiral symmetry breaking.

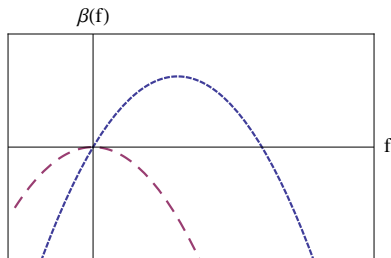
However, it suffers from 2 big problems:

- it is non-renormalizable (a scalar d.o.f. is hidden in the description...)
- it is unnatural: if defined at a scale Λ , then χ SB occurs at $\Lambda_\chi \sim \Lambda$ unless fine-tuning is allowed

NJL in $d = 2$ dimensions

The problems of the NJL model can be solved by defining the theory in a generic space-time dimension d :

- renormalizability (Taylor expansion in $1/N$) for $d < 4^5$
- naturalness in $d = 2$ (Gross-Neveu model): $\Lambda_\chi = \Lambda e^{-1/f(\Lambda)}$



⁵[Parisi '75, Gross '75]

Lessons from the NJL in $d = 2$ dimensions

- The theory is natural (namely, the IR scale depends only very mildly on the UV cutoff) because it is defined (at the UV cutoff!) in terms of marginally relevant operators:

the mass term of the Higgs field $\bar{\psi}\psi$ is marginally relevant

- It might be phenomenologically interesting (in a $d = 2$ dimensional world...) because the order parameter $\bar{\psi}\psi$ behaves as a "weakly coupled" scalar in the IR:

the scale dimension of the order parameter is $\Delta(\bar{\psi}\psi) = O\left(\frac{1}{4\pi}\right)$ at $\mu \sim \Lambda_\chi$ (recall that $\Delta = 0$ for a free scalar and $1/4\pi$ is the loop factor in $d = 2$)

Can we construct a similar model in $d = 4$ dimensions?

Interestingly, it turns out that
the large class of theories defined as

$$CFT + f\mathcal{O}^2$$

(where CFT is a large N conformal field theory, and $\mathcal{O} \in CFT$ with arbitrary scaling dimension Δ)

has an universal behavior at leading order in a planar analysis⁶.

Examples include:

- the NJL model with $\mathcal{O} = \bar{\psi}\psi$ and massless L σ M with $\mathcal{O} = \phi^2$ (where the CFT is trivial)
- quenched QED with $\mathcal{O} = \bar{\psi}\psi$ and orb. proj. of $\mathcal{N} = 4$ with $\mathcal{O} = \phi^2$ (where the CFT is nontrivial)

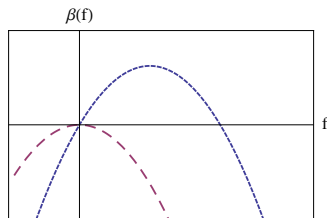
⁶[LV '10]

Universal properties

These models have the same phase structure:

$$\mu \frac{df}{d\mu} = -f^2 + (2\Delta - d)f$$

$$\Delta(\mathcal{O}) = \Delta - f$$



Focusing on $d = 4$:

- for $\Delta = 2$ we have $\beta_f = -f^2$ and the theory is natural ($\Lambda_\chi \ll \Lambda$)
- $\Delta(\mathcal{O}) < 2$ at scales $\mu > \Lambda_\chi$

Idea:

If we are able to find a CFT such that $\Delta(\bar{\psi}\psi) = 2$, and place on top of it the 4-fermion deformation $f(\bar{\psi}\psi)^2$, then we would have

- (i) a natural model for dynamical symmetry breaking: $\Lambda_\chi = \Lambda e^{-1/f}$
- (ii) a "weakly coupled" Higgs field in the IR: $\Delta(\bar{\psi}\psi) < 2$ for $\mu > \Lambda_\chi$

NOW: Is there any candidate CFT?

The Conformal Window

Technicolor at Criticality (TCC) is based on the well established existence of the Conformal Window (CW) in non-abelian gauge theories:

CW: a region in flavor space in which the UV-free dynamics flows towards an interacting IRFP. In the CW the IR dimension satisfies

$$2 \leq \Delta(\bar{\psi}\psi) < 3 \quad (1)$$

In particular, there exists $N_f = N_f^c$ such that $\Delta(\bar{\psi}\psi) = 2$

TC at Criticality

TC at Criticality is defined via

$$\langle e^{i \int f (\bar{\psi}\psi)^2} \rangle_{CFT} \quad \text{with} \quad \Delta(\bar{\psi}\psi) = 2$$

with $\langle \dots \rangle_{CFT}$ the Green's functions of the $SU(N)$ gauge theory at $\lambda = \lambda_{IR}$ and $N_f = N_f^c$:

- in the broken phase ($f > 0$) we have

$$\Lambda_\chi = \Lambda e^{-1/f(\Lambda)}$$

- and the scaling dimension of the quark bilinear (for $f \neq 0$) satisfies

$$1 \lesssim \Delta(\bar{\psi}\psi) \leq 2$$

What is the physical meaning of this construction?

Phases of non-abelian gauge theories

Consider a non-supersymmetric $SU(N)$ gauge theory with a number N_f of massless fermions and 't Hooft coupling λ .

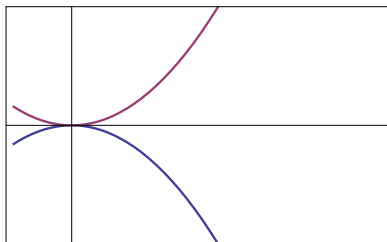
1-loop analysis and the QCD example tell us that:

- (i) if N_f is "large" asymptotic freedom is lost ($\lambda \rightarrow 0$ in the IR)
- (ii) if N_f is "small" the theory manifests χ SB and confines

The Banks-Zaks fixed point and the conformal window

More precisely:

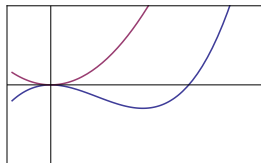
- for $N_f > N_f^{af}$ asymptotic freedom is lost: positive beta function β_λ . ($\lambda = 0$ is an IR fixed point)
- for $N_f < N_f^{af}$ asymptotic freedom sets in: negative beta function. ($\lambda = 0$ is an UV fixed point)



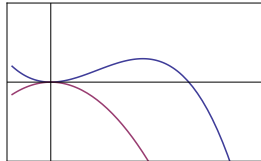
Q: Is the physics smooth at $N_f = N_f^{af}$?

Banks and Zaks⁷ assumed the physics is smooth (analytic) in N_f .
Continuity of β_λ requires a zero: fixed point. There are 2 possibilities:

- IR fixed point approaching
 $\lambda_* = 0$ with $N_f \rightarrow N_f^{af} - 0$:



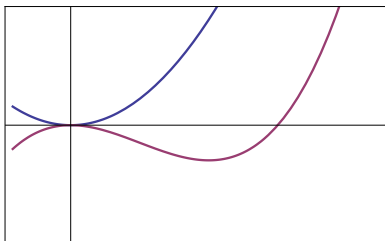
- UV fixed point approaching
 $\lambda_* = 0$ with $N_f \rightarrow N_f^{af} + 0$:



Since in both cases we expect $\lambda_* \rightarrow 0$ we can use perturbation theory to verify our guess.

⁷Banks and Zaks '81

It turns out that Nature has chosen the first possibility: $\lambda_* = \lambda_{IR}$

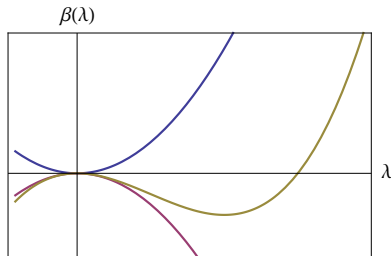


Continuity of β_λ requires the BZ fixed point

Conformality lost

The existence of the BZ IR fixed point has been established. Still, we expect confinement to occur for "small" N_f . Hence:

- for $N_f > N_f^{af}$ the theory is IR-free
- for $N_f^c < N_f < N_f^{af}$ the theory is IR-conformal: **conformal window**.
- for $N_f < N_f^c$ we expect confinement and χ SB: negative beta function.

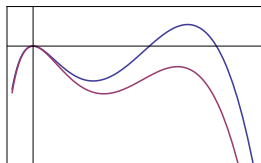
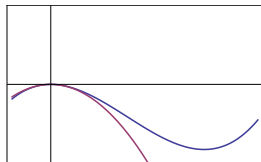


Q: Is the physics smooth at $N_f = N_f^c$?

Assume the physics is smooth (analytic) in N_f .

There are 2 possibilities ⁸ :

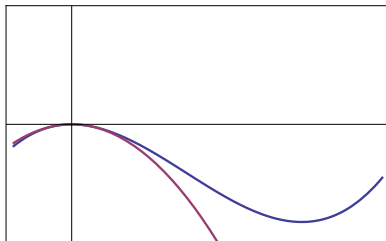
- the Banks-Zaks IR fixed point approaches $\lambda_{IR} = \infty$ for $N_f \rightarrow N_f^c + 0$:
- there exists a nontrivial UV fixed point $\lambda_{UV} \neq 0$ approaching λ_{IR} as $N_f \rightarrow N_f^c + 0$:



**In both cases λ can be "large":
perturbation theory may not be reliable.**

⁸D.B. Kaplan et al. '09

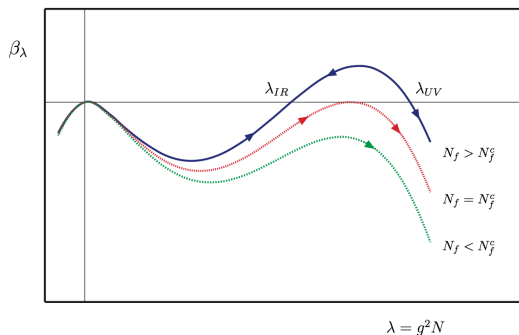
The first possibility



there are reasons to believe it is realized in SUSY QCD:

- existence of a weakly coupled ($\lambda_{mag} \sim 1/\lambda_{IR} \rightarrow 0$) "magnetic" dual theory.
- at $N_f = N_f^c$ the dual theory is weakly coupled:
confinement without χ SB!

The second possibility



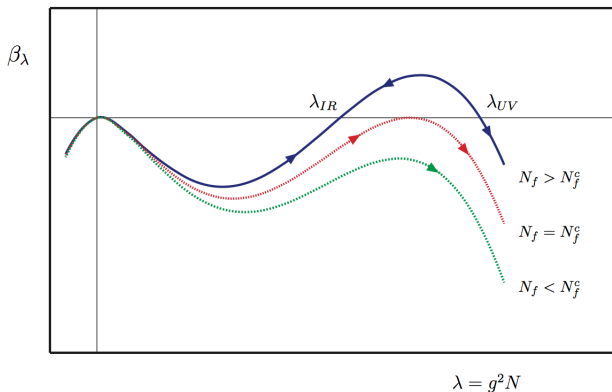
- there exists an asymptotically non-free branch $\lambda \geq \lambda_{UV}$ with χ SB
- for $N_f \leq N_f^c$ χ SB becomes visible to the UV-free phase:
 χ SB drives the theory away from conformality!

We cannot prove analytically either the first nor the second guess (lattice!).
Yet, in both cases we expect remarkable implications:

- if the first possibility is realized we might hope that a magnetic QCD dual actually exists (this would solve the strongly coupled theory!)
- if the second possibility is realized we would have at our disposal an *asymptotically non-free* phase with new, and potentially interesting, phenomenological properties (realization of Holdom's idea ⁹)

⁹Holdom '81

I will propose a number of arguments in favor of the second possibility



and **conjecture TC at Criticality to be a dual description of the strong branch $\lambda > \lambda_{IR}$ for $N_f \sim N_f^c$**

Main features of this physics:

- ① there exists an asymptotically non-free branch $\lambda \geq \lambda_{UV}$ with χ SB.
- ② for $N_f = N_f^c$ the two nontrivial fixed points merge.
The order parameter for χ SB has the form characterizing a Conformal Phase Transition¹⁰ ($c > 0$):

$$\Lambda_\chi = \theta(N_f^c - N_f) \Lambda e^{-c/|\Delta(N_f) - \Delta_c|}$$

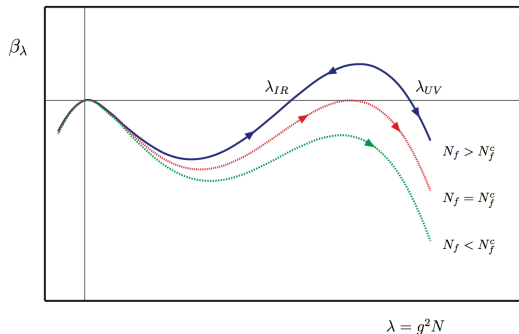
with $\Delta_c = \Delta(N_f^c)$ the dimension of the quark bilinear $\bar{\psi}\psi$ at the IR fixed point ($\Delta_c = 2$ in¹¹)

- ③ for $N_f < N_f^c$ χ SB becomes visible to the UV-free phase if $\lambda > \lambda_c$

¹⁰Miransky and Yamawaki '97

¹¹Cohen and Georgi '89

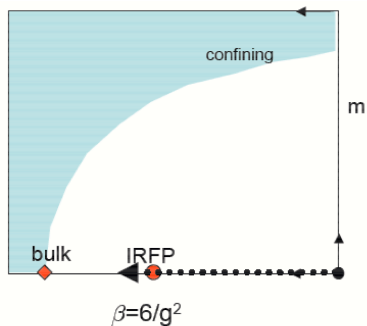
Q: Can we confirm this picture?



- LATTICE (?!)
- ANALYTICAL TOOLS

Lattice

Lattice simulations seem to suggest that χ_{SB} and confinement are tightly connected (no indication of confinement without χ_{SB}). In this sense, the second possibility seems more appropriate... Now:



- does the confining phase extends all the way to the chiral limit?
- is the bulk transition 2nd order?

SD approach

If the conjectured picture is right χ SB is expected to play a crucial role (as opposed to the SUSY case...)

A study of the Schwinger-Dyson equations in this case would provide useful information, but requires approximations in order to be handled.

For example, in the "rainbow approximation":

The diagram illustrates the rainbow approximation for the fermion self-energy. It shows an equation where a fermion line with a wavy loop (representing a photon) is equal to a simple fermion line. The wavy loop is attached to the fermion line, and the entire expression is set equal to a simple fermion line with an arrow pointing right.

A solution of the equation gives the dynamical fermion mass $\Sigma(p)$: χ SB occurs if $\Sigma(0) \neq 0$ in the chiral limit.

Quenched QED (1)

Consider massless QED

$$\mathcal{L}_{CFT} = -\frac{1}{4\lambda} F^2 + \bar{\psi} i D \psi$$

In the quenched limit (fermion loops are suppressed as in large N QCD) the rainbow approximation is justified.

An analysis of the SD equation reveals that

$$\Sigma(0) \simeq \Lambda e^{-\pi/\sqrt{\frac{\lambda}{\lambda_c}-1}} \quad \lambda_c = \text{number.}$$

- (i) χ SB requires $\lambda > \lambda_c$
- (ii) $\beta_\lambda \propto -\left(\frac{\lambda}{\lambda_c} - 1\right)^{3/2} \neq 0$ (Miransky scaling¹²) with λ_c an UVFP.
- (iii) Conformal Phase Transition (CPT) at $\lambda = \lambda_c$, where $\Delta(\bar{\psi}\psi) = 2$

¹²Miransky '85

Quenched QED (2)

Note that:

- $\beta_\lambda \neq 0$ is not consistent with the quenched approximation (not true in the non-abelian case...)
- for $\lambda = \lambda_c$ the 4-fermion deformation $(\bar{\psi}\psi)^2$ is marginal

We are thus led to consider¹³

$$-\frac{1}{4\lambda}F^2 + \bar{\psi}iD\psi + f(\bar{\psi}\psi)^2$$

This theory belongs to the general class introduced earlier:

- (i) $\lambda = \text{const}$ in the leading quenched approximation
- (ii) $\beta_f = -f^2 + (2\Delta - 4)f$ and χ SB for $f > f_{UV}$.
- (iii) CPT at $\lambda = \lambda_c$, where $\Delta(\bar{\psi}\psi) = 2$ and $\Lambda_\chi = \Lambda e^{-1/f} \propto \Sigma(0)$.

¹³[W.A.Bardeen et al. '86]

Extrapolating these results to the non-abelian case, χ SB requires:

- either a strong coupling $\lambda > \lambda_c$ and $f = 0$

OR

- $\lambda = \text{const}$ and a $f(\bar{\psi}\psi)^2$ deformation

Are these theories

2 equivalent descriptions of the same dynamics ?!

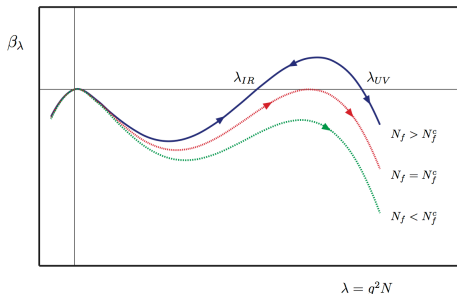
If this is true the dynamical mass (and phase structure) must be the same:

$$\underline{\text{IF:}} \quad \Lambda e^{-\pi/\sqrt{\frac{\lambda}{\lambda_c}-1}} \equiv \Lambda e^{-1/f} \quad \Leftrightarrow \quad f \propto \sqrt{\frac{\lambda}{\lambda_c}-1} \quad ???$$

$$\underline{\text{THEN:}} \quad \beta_f = -f^2 \quad \Leftrightarrow \quad \beta_\lambda \propto -\left(\frac{\lambda}{\lambda_c}-1\right)^{3/2} \quad !!!$$

Where do the "equivalence" come from?

Assume we would like to model the strong branch defined at $\lambda = \lambda_{UV}$:



How can this be done? There are two equivalent ways:

1. Study the Yang Mills action at strong coupling (this is $\lambda = large$ and $f = 0...$)
2. Use an effective approach! Sit at λ_{IR} and add CFT deformations (this is $\lambda = const$ and $f \neq 0...$)

Conformal Perturbation Theory:

introduce on the top of the CFT all operators compatible with the symmetries. The theory is now defined by the path integral

$$\langle e^{i \int \mathcal{L}_{pert}} \rangle_{CFT} = \int \mathcal{D}[CFT] e^{i \int \mathcal{L}_{pert}}$$

In order for this theory to describe the strong, asymptotically non-free branch:

- The CFT must be defined in terms of the Green's functions of the $SU(N)$ gauge theory with $\lambda = \lambda_{IR}$.
- $\mathcal{L}_{pert} = \sum_n f_n \mathcal{O}_n$ must include the CFT deformations responsible for the flow $\lambda_{UV} \rightarrow \lambda_{IR}$ (\mathcal{L}_{pert} is relevant at λ_{UV}).
Because \mathcal{L}_{pert} is "dynamical" we expect $f_n = f_n(\lambda)$

What is \mathcal{L}_{pert} ???. The SD approach strongly suggests that

$$\mathcal{L}_{pert} = f(\bar{\psi}\psi)^2 + \dots \quad \text{with} \quad f = f(\lambda)$$

At leading order in the planar expansion we can consistently assume the 4-fermion operator is the ONLY deformation and consider the path integral ¹⁴

$$\langle e^{i \int f(\bar{\psi}\psi)^2} \rangle_{CFT}$$

CONJECTURE: This generalized formulation of the Nambu-Jona Lasinio model represents an effective (dual) description of the asymptotically non-free phase of non-abelian gauge theories

¹⁴LV '10

Q: Is there any indications in favor of the conjecture?

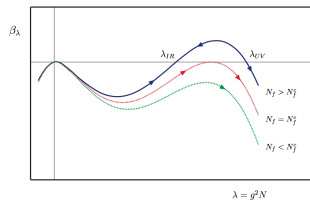
Yes. From a large N (colors) analysis of

$$\langle e^{i \int f(\bar{\psi}\psi)^2} \rangle_{CFT}$$

we find

- 2 fixed points $f = f_{IR,UV}$ only if $2 \leq \Delta < 3$
(namely if the CW of the gauge theory is there)
- f_{IR} is mapped into λ_{IR} via $f_{IR} = f(\lambda_{IR})$. The same for f_{UV}
(λ_{UV} is predicted ONLY if the CW exists!)
- The fixed points $f_{IR,UV}$ merge when $\Delta = 2$:
Conformal Phase Transition and $\Lambda_\chi = \Lambda e^{-1/f}$
(agreement with the SD equation approach)

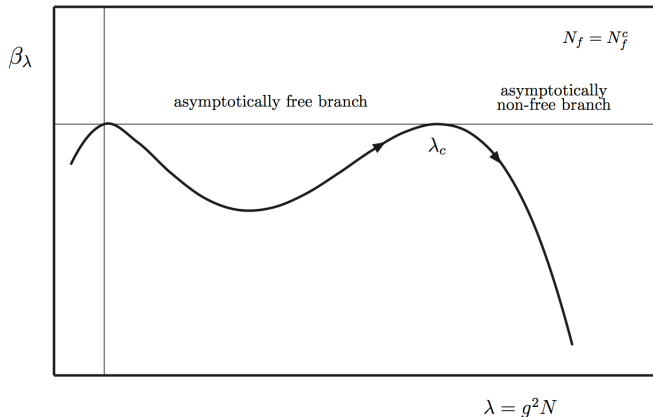
The emerging physical picture is the following:



- the UV free phase is described by the Yang-Mills action
- the UV non-free phase ($\lambda > \lambda_{IR}$) is dual to $\text{CFT} + f(\bar{\psi}\psi)^2$,
where $\lambda = \lambda_{IR}$ is mapped into $f_{IR} = 0$, while $\lambda = \lambda_{UV}$ into $f = f_{UV}$.
- When $N_f = N_c^c$ the fixed points merge $\lambda_{IR} = \lambda_{UV} \equiv \lambda_c$ ($f_{IR} = f_{UV}$)
 - the dual model consistently predicts a CPT at $\Delta = 2$.
 - λ_c must be identified as the Miransky UV fixed point.

TC at Criticality: the physical meaning

Technicolor at Criticality is expected to describe the non-abelian dynamics defined at $\lambda > \lambda_{IR} = \lambda_{UV} = \lambda_c$



The Composite Higgs

A "weakly coupled" Higgs $\bar{\psi}\psi$ is anticipated by analogy with the Gross-Neveu model (the natural version of the NJL).

The Higgs physics can be understood by identifying H with a dilaton, i.e. the pseudo NGB of dilatation invariance

(in analogy with the η' of QCD, in our framework the Higgs/dilaton mixing is maximal...)

- if $\Delta = 1 + \epsilon$ is the IR dimension of the Higgs ($\epsilon \lesssim O(0.1)$ from NJL), then ϵ is the explicit CFT breaking ($\Lambda_\chi = 0$ for $\epsilon = 0$)
- by symmetry arguments $m_{Higgs}^2 \sim \epsilon \Lambda_\chi^2$.
More generally, $g_{\bar{\psi}\psi} = g_{SM\ Higgs}(1 + O(\epsilon))$ for any coupling

The phenomenology is analogous to that of CH models¹⁵:

The Higgs in TCC is a pseudo-NGB of an Approximate Dilatation Invariance of the Strong Dynamics

¹⁵D.B. Kaplan and Georgi '84

The Flavor Sector

The renormalization effects from the scale Λ_{ETC} (at which the Yukawa operator is generated) down to Λ_χ (at which the chiral condensate is formed) gives

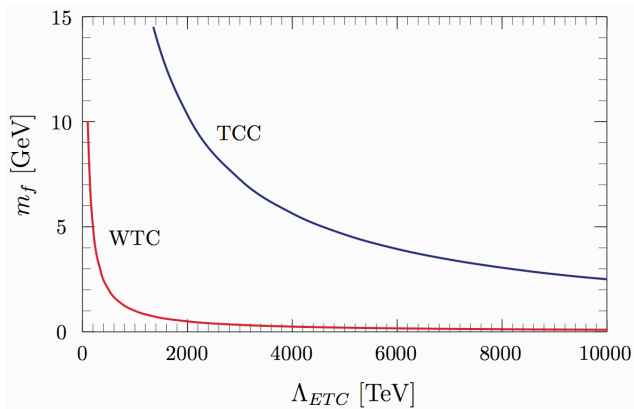
$$\begin{aligned}
 m_f &= y \frac{\Lambda_\chi^3}{\Lambda_{ETC}^2} \exp \left(\int_{\Lambda_\chi}^{\Lambda_{ETC}} \gamma \, d \log \mu \right) \\
 &= y \frac{\Lambda_\chi^2}{\Lambda_{ETC}} \left[e \log \left(\frac{\Lambda_{ETC}}{\Lambda_\chi} \right) \right].
 \end{aligned}$$

There are two competing contributions:

- $\Lambda_\chi/\Lambda_{ETC}$ suppression typical of $\Delta(\bar{\psi}\psi) \sim 2$ (WTC)
- Log enhancement coming from $f(\mu)$ ($1 \sim \Delta(\bar{\psi}\psi) < 2$ in TCC)

The Flavor Sector: $i = 1, 2$

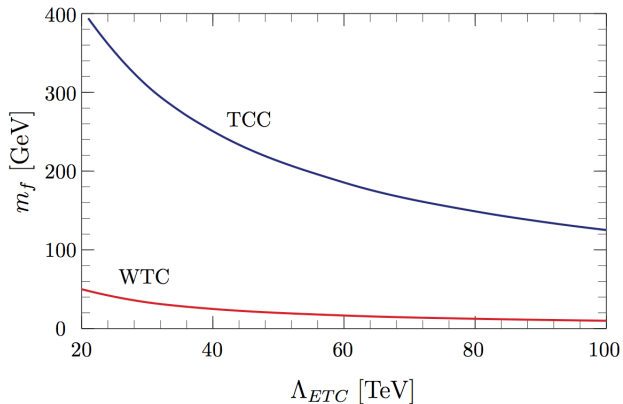
The fermion mass in TCC lies in between a WTC dynamics with $\Delta(\bar{\psi}\psi) \sim 2$ and a fundamental Higgs with $\Delta(\bar{\psi}\psi) \sim 1$



$\Lambda_{ETC}^{i=1,2} > O(10^4)$ TeV for 1st and 2nd generations

The Flavor Sector: $i = 3$

The fermion mass in TCC lies in between a WTC dynamics with $\Delta(\bar{\psi}\psi) \sim 2$ and a fundamental Higgs with $\Delta(\bar{\psi}\psi) \sim 1$



$\Lambda_{ETC}^{i=3} = O(10^2)$ TeV for the top

Summery

- the well established phases of QCD with many massless flavors N_f :
 - 1) $N_f > N_f^{af}$: the theory is in an IR-free phase
 - 2) $N_f^c < N_f < N_f^{af}$: the theory is IR conformal
 - 3) $N_f < N_f^c$: the theory develops a chiral condensate and confines
- the Conformal Window exists because the beta function β_λ is continuous at $N_f = N_f^{af}$
- continuity of the beta function β_λ at $N_f = N_f^c$ admits two scenarios:
 - a) the theory manifests confinement without χ SB
(and possibly a magnetic dual)
 - b) the theory has an asymptotically non-free phase

Lattice simulations are needed!!!

Conclusions (1)

- (1) **I presented a number of argument in support of the existence of an asymptotically non-free phase for ordinary (non SUSY) non-abelian theories.** In particular I (re)interpreted the analysis of Miransky as an indication in favor of this physics:
- the Miransky scaling would be the running close to the non-trivial UV fixed point
 - the (unphysical) statement " χ_{SB} occurs at $\lambda > \lambda_c$ " would be replaced by the (physical) statement " χ_{SB} occurs in the phase $\lambda > \lambda_{UV}$ "
- (2) **I speculated on the existence of a dual description of the strong branch.** The physics agrees with that extracted from the SD equation approach:
- χ_{SB} becomes visible to the UV-free phase when $\Delta(\bar{\psi}\psi) = 2$ (agreement with Georgi and Cohen)
 - at that critical point the theory undergoes a Conformal Phase Transition (the asymptotically non-free theory is natural!)

Conclusions (2)

- (3) **I proposed a class of asymptotically non-free theories**
 (these exist irrespective of the validity of the above conjectures on non-abelian gauge theories!)
strong coupling throughout the RG flow: dual AdS/CFT description?!
- (4) **Technicolor at Criticality** represents one such example:
- TCC solves the hierarchy problem ($\Delta(\bar{\psi}\psi) = 2$ in the UV)
 - TCC predicts the existence of a "weakly coupled" Higgs in the IR (i.e. a dilaton $\Delta(\bar{\psi}\psi) \simeq 1$ in the IR)
- strong impact on Flavor Physics and (potentially) on EW physics

Thank You

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