

Quantum Magnetometry in Search of Dark Matter

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Outline

- Introduction:
 - Axions and ALPs
 - Spin-Based (Co)magnetometers
- Established Magnetometry Techniques for DM Research
- Novel Magnetometry Techniques
- Summary

QCD Axion

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- A solution to the strong CP problem, $\theta_{QCD} \rightarrow a/f_a$.

[Peccei, Quinn 1977; Weinberg 1978; Wilczek 1978]

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$$\partial_\mu a \bar{\psi} \gamma_5 \gamma^\mu \psi / f_a.$$

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- $m_a \propto \Lambda_{\text{QCD}}^2 / f_a$

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- Can be a CDM component (I assume all)

QCD Axion

Axion Like Particles (ALPs)

• A solution to the strong CP problem, $\theta_{QCD} \rightarrow a/f_a$

[Peccei, Quinn 1977; Weinberg 1978; Wilczek 1978]

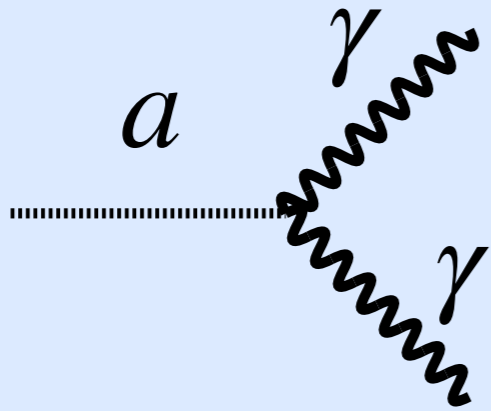
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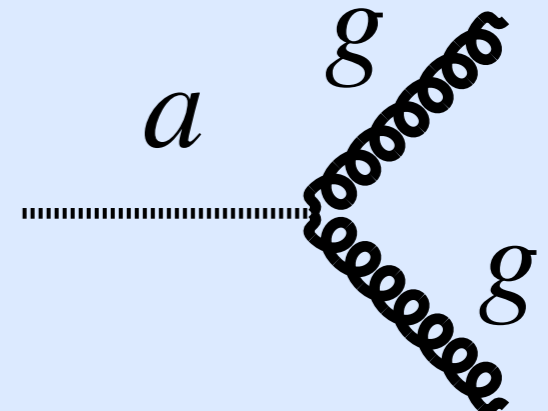
• ~~$m_a \sim \Lambda_{QCD}^2 / f_a$~~

• Can be a CDM component (I assume all)

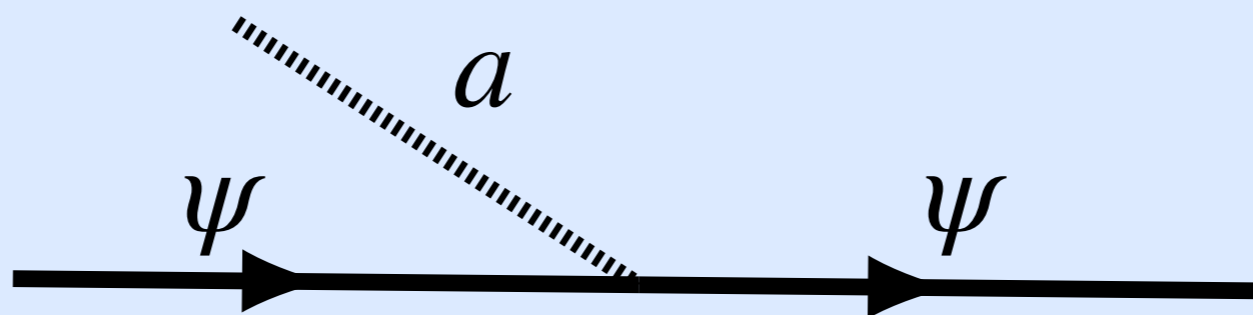
ALP-SM Interactions



$$-\frac{1}{4} g_{a\gamma\gamma} a F \tilde{F}$$

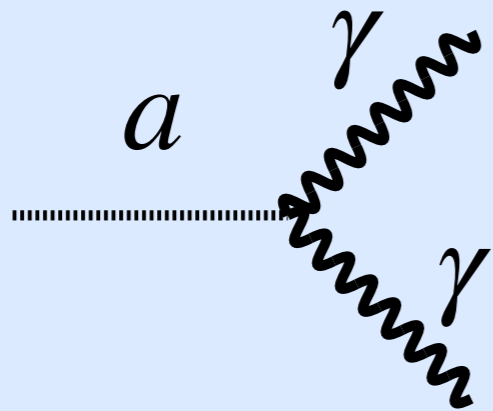


$$-\frac{a}{f_a} \frac{G \tilde{G}}{32\pi^2}$$



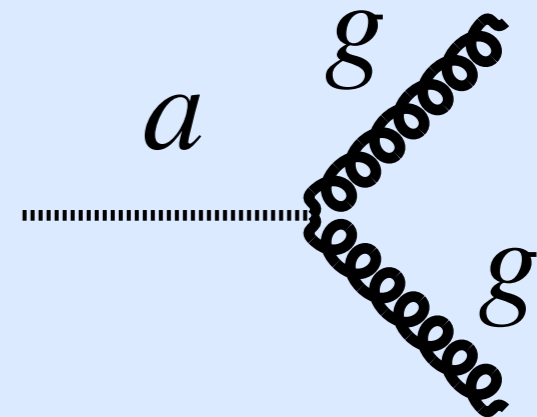
$$g_{a\psi\psi} \partial_\mu a \cdot \bar{\psi} \gamma^\mu \gamma_5 \psi$$

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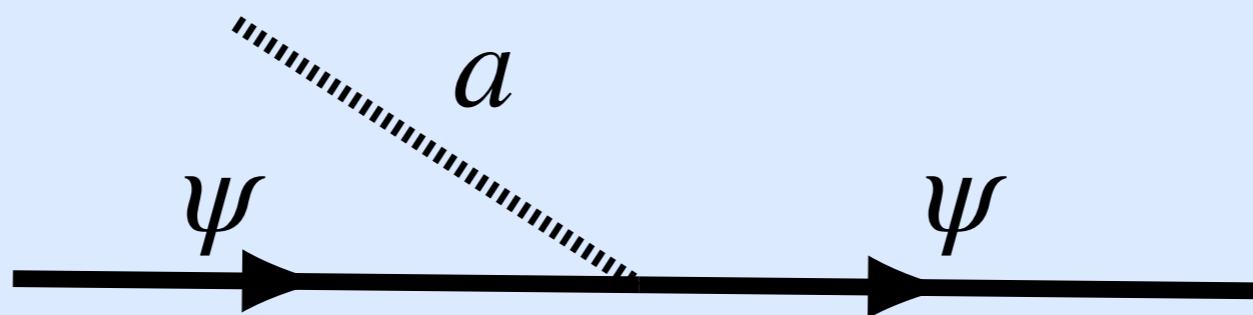


[2024, JHEP: IMB, Kalia],[2023 PRD, SNIPE Hunt (incl. IMB)], [several more in progress]

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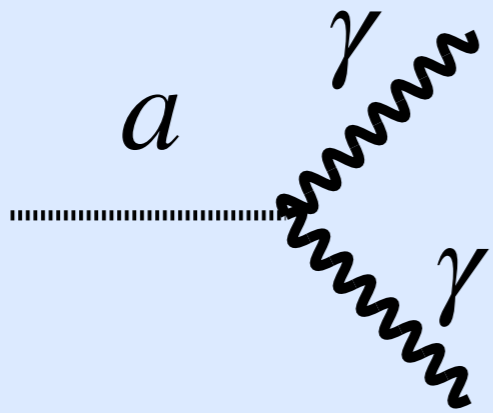


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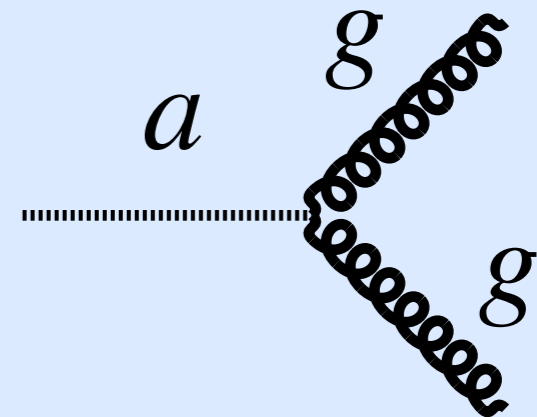
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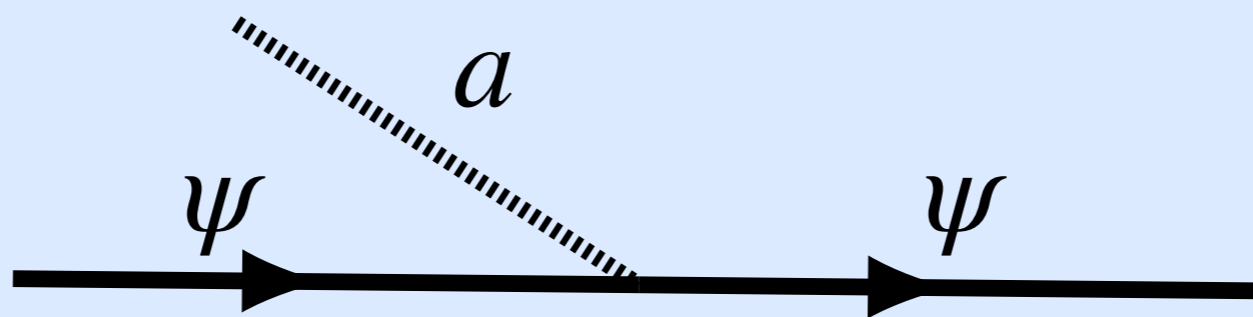
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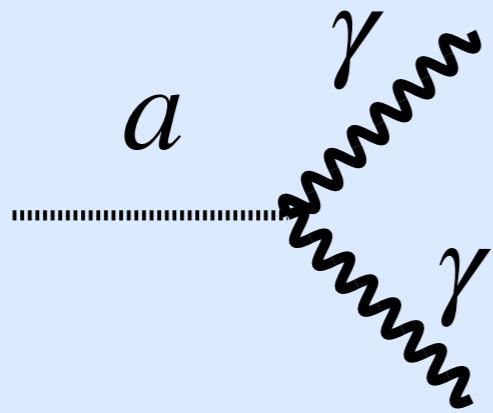
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[IMB et al (in progress)]



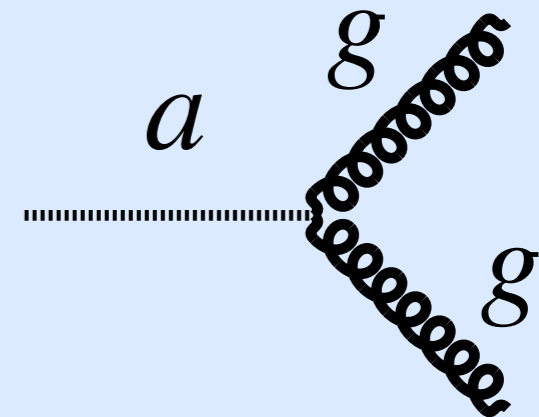
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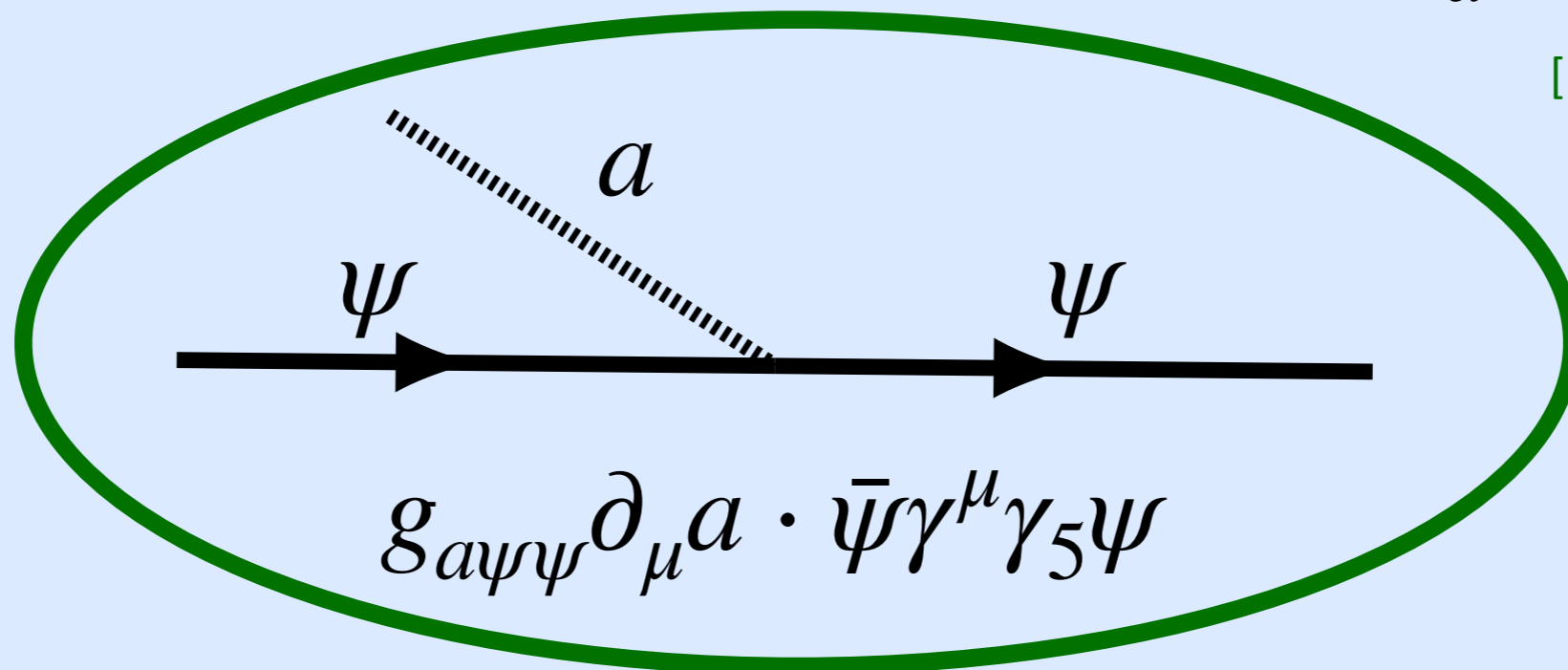
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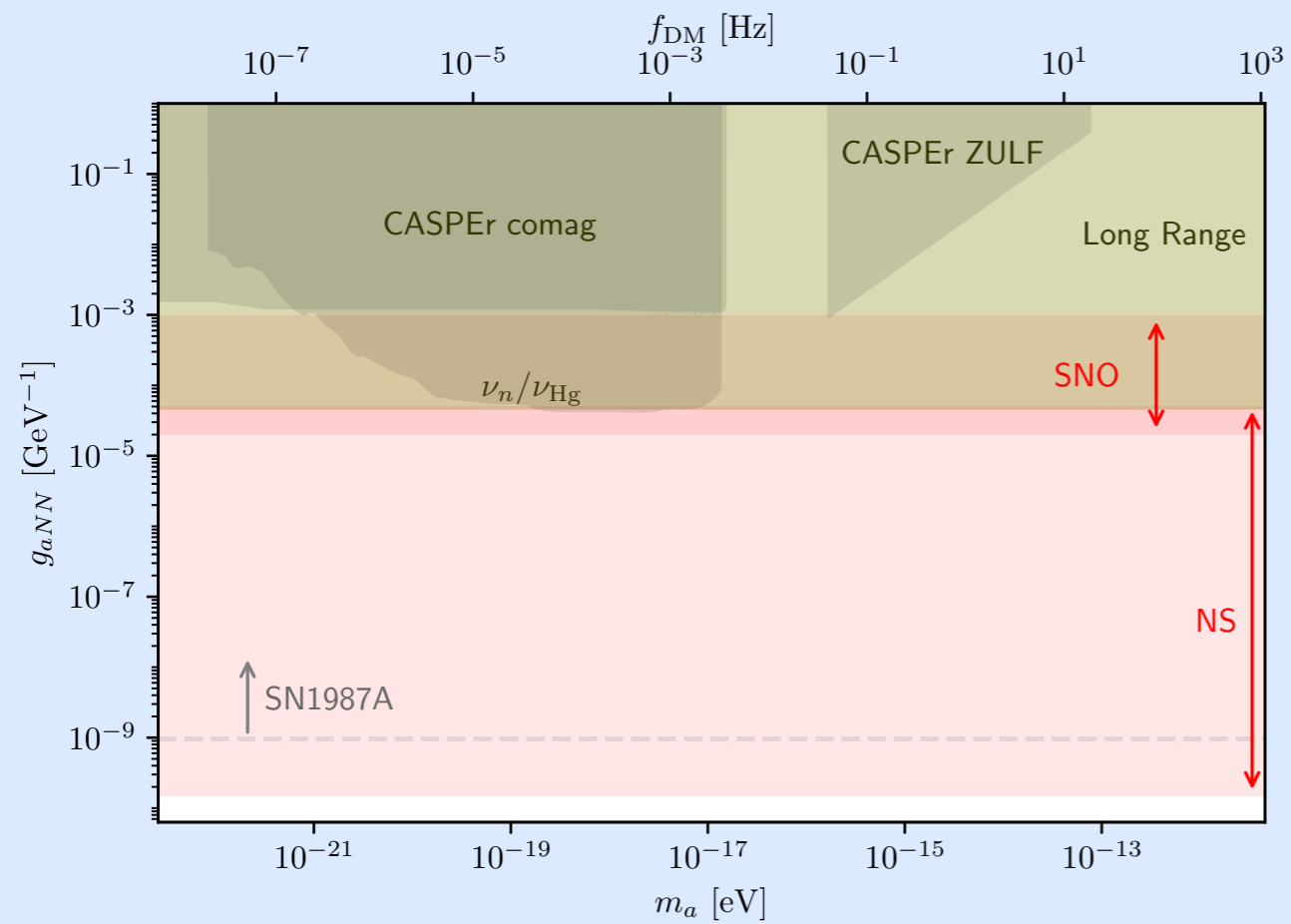
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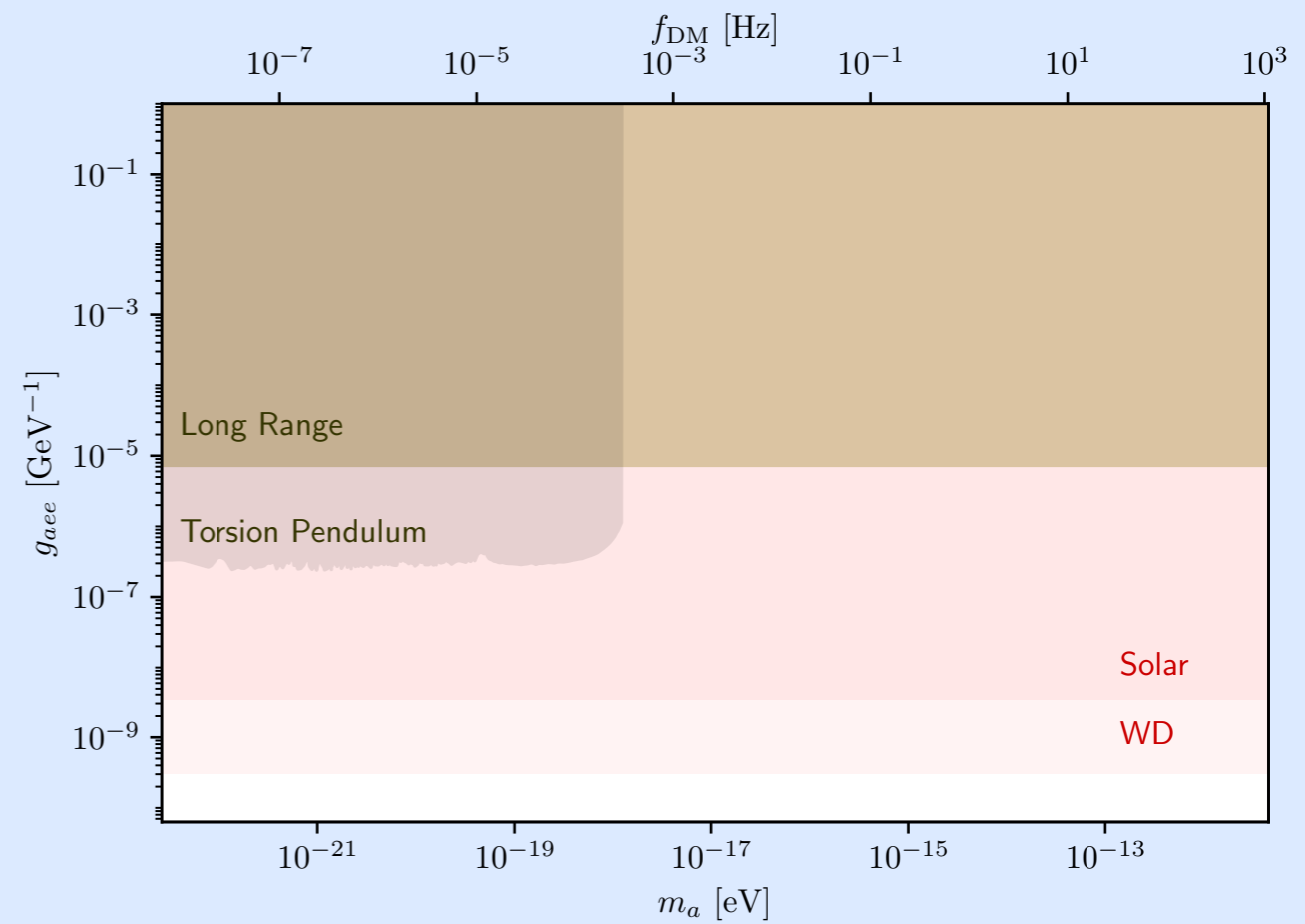


$$g_{a\psi\psi}\partial_\mu a \cdot \bar{\psi}\gamma^\mu\gamma_5\psi$$

ALP-Fermion parameter spaces (circa late 2019)



ALP-neutron



ALP-electron

ALP-Spin interaction

$$H_{a\psi\psi} = -g_{a\psi\psi} \vec{b}_a \cdot \vec{S}_\psi = -\vec{b}_{a-\psi} \cdot \vec{S}_\psi$$

$$\vec{b}_{a-\psi} = g_{a\psi\psi} \sqrt{2\rho_a} \cos(m_a t) \cdot \vec{v}_{a-\psi} \quad [\text{astro-ph/9501042}]$$

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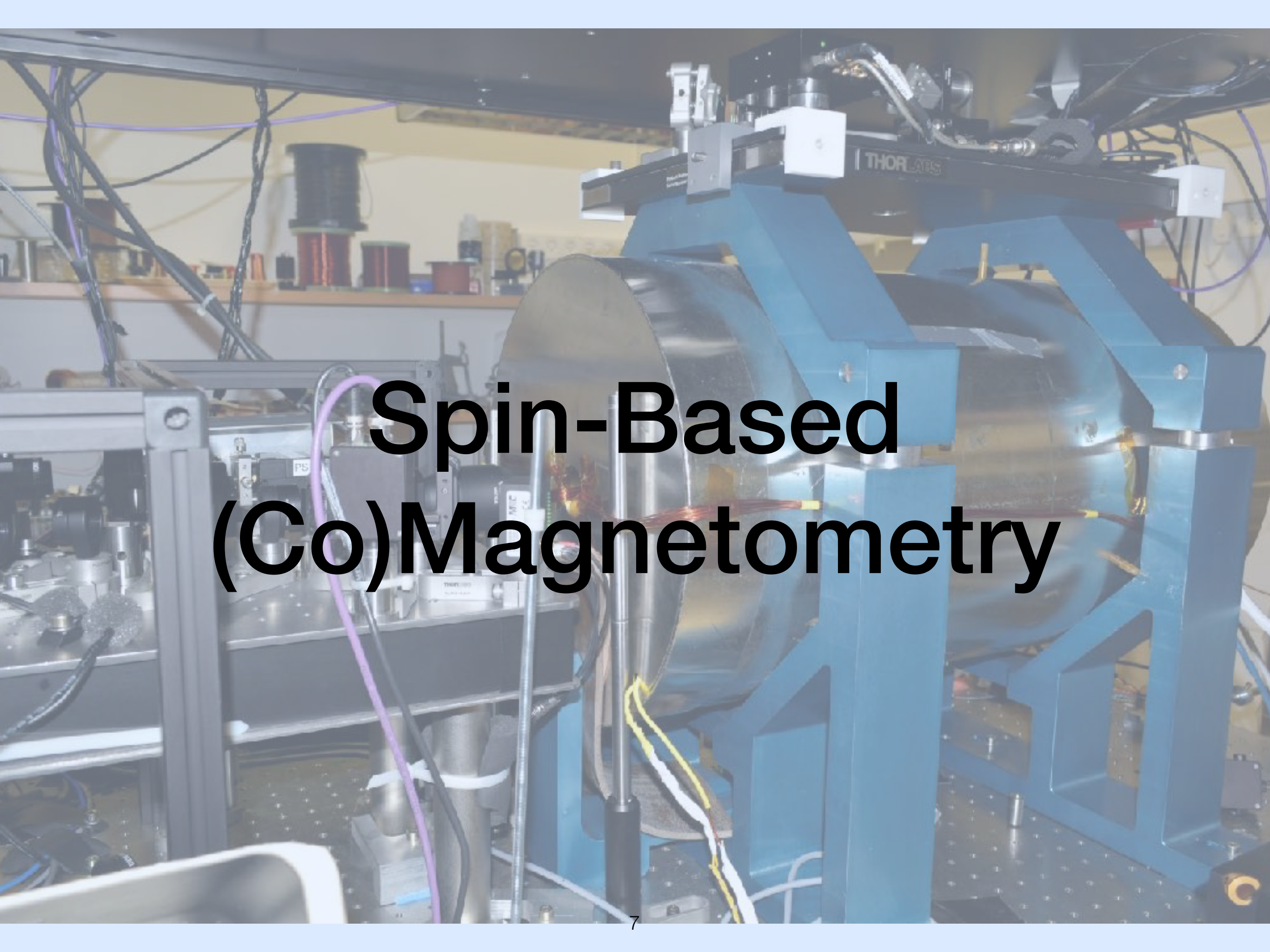
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But how to measure it?

$$(\text{Hint : } H_{zeeman} = -\gamma \vec{B} \vec{S})$$



Spin-Based (Co)Magnetometry

Bloch Equations

$$\dot{\vec{S}} =$$

Bloch Equations

* To leading order in important stuff

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Bloch Equations

- * To leading order in important stuff

$$\dot{\vec{S}} = \gamma \left(\vec{B} + \frac{\vec{b}}{\gamma} \right) \times \vec{S}$$

Torque

(generates transverse from
longitudinal)

Bloch Equations

- * To leading order in important stuff

$$\dot{\vec{S}} = \gamma \left(\vec{B} + \frac{\vec{b}}{\gamma} \right) \times \vec{S} - \Gamma \vec{S}$$

Torque

(generates transverse from longitudinal)

Decaying excitations
(causes stabilization)

Bloch Equations

* To leading order in important stuff

Creating macroscopic polarization
(generates a non-trivial steady state solution)

$$\dot{\vec{S}} = \gamma \left(\vec{B} + \frac{\vec{b}}{\gamma} \right) \times \vec{S} - \Gamma \vec{S} + R \hat{z}$$

Torque

(generates transverse from longitudinal)

Decaying excitations
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Transverse EOMs

We usually assume $\dot{S}_z = 0$ (also that $|\vec{S}| \approx |S_z|$),
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The transverse EOMs become

$$\dot{\vec{S}} = \gamma \left(\vec{B} + \frac{\vec{b}}{\gamma} \right) \times \vec{S} - \Gamma \vec{S} + R \hat{z}$$



$$\dot{S}_{\perp} = i\gamma \left(B_z + \frac{b_z}{\gamma} \right) S_{\perp} - i\gamma \left(B_{\perp} + \frac{b_{\perp}}{\gamma} \right) S_z - \Gamma S_{\perp}$$

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Solving the EOMs

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If B_z is constant



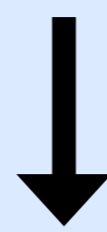
Fourier. From now on I'm going to ignore subtleties regarding $\cos(m_a t) \neq e^{im_a t}$

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$$S_{\perp}(\omega = m_a) = \frac{b_{\perp} + \gamma B_{\perp}(\omega = m_a)}{(\gamma B_z - m_a) + i\Gamma} S_z$$

The Result

$$S_{\perp} = \frac{b_{\perp} + \gamma B_{\perp}}{i\Gamma + (\gamma B_z - m_a)} S_z + \delta S_{\text{eff}}$$

The Result

The transverse
spin


$$S_{\perp} = \frac{b_{\perp} + \gamma B_{\perp}}{i\Gamma + (\gamma B_z - m_a)} S_z + \delta S_{\text{eff}}$$

The transverse spin:

Everything is encoded in the spin projections in the directions perpendicular to the pumping term.

The Result

The transverse
spin

Signal

$$S_{\perp} = \frac{b_{\perp} + \gamma B_{\perp}}{i\Gamma + (\gamma B_z - m_a)} S_z + \delta S_{\text{eff}}$$

Signal:

The thing we want to measure that an ALP generates

The Result

The transverse spin

Signal

Transverse magnetic fields

$$S_{\perp} = \frac{b_{\perp} + \gamma B_{\perp}}{i\Gamma + (\gamma B_z - m_a)} S_z + \delta S_{\text{eff}}$$

Transverse magnetic fields:

Can either be noise, or (as we will see) the effect of one atom species on the other. Note that it is proportional to γ .

The Result

The transverse spin

Signal

Transverse magnetic fields

Spin in the z direction

$$S_{\perp} = \frac{b_{\perp} + \gamma B_{\perp}}{i\Gamma + (\gamma B_z - m_a)} S_z + \delta S_{\text{eff}}$$

Spin in the z direction

Main demand: Don't be tiny

The Result

$$S_{\perp} = \frac{b_{\perp} + \gamma B_{\perp}}{i\Gamma + (\gamma B_z - m_a)} S_z + \delta S_{\text{eff}}$$

The transverse spin S_{\perp} is equal to the fraction of the signal $b_{\perp} + \gamma B_{\perp}$ (Transverse magnetic fields) over the denominator $i\Gamma + (\gamma B_z - m_a)$ (Spin in the z direction) multiplied by S_z plus δS_{eff} (Technical Noise).

Technical Noise:

In addition to the magnetic field noise, whatever system is used for readout introduces noise that does not “care” whether the spins are on or off resonant.

The Result

$$S_{\perp} = \frac{b_{\perp} + \gamma B_{\perp}}{i\Gamma + (\gamma B_z - m_a)} S_z + \delta S_{\text{eff}}$$

The transverse spin S_{\perp} is equal to the fraction of the signal $b_{\perp} + \gamma B_{\perp}$ (where b_{\perp} is the signal and γB_{\perp} are transverse magnetic fields) over the denominator $i\Gamma + (\gamma B_z - m_a)$ (where γB_z is spin in the z direction and m_a is ALP mass) multiplied by S_z (spin in the z direction) plus δS_{eff} (technical noise).

ALP Masses

Our experiments can only probe ultralight ALPs. Until now we focused mostly on things that are $< \text{neV}$, but in principle, can go as high as meVs .

The Result

$$S_{\perp} = \frac{b_{\perp} + \gamma B_{\perp}}{i\Gamma + (\gamma B_z - m_a)} S_z + \delta S_{\text{eff}}$$

The transverse spin

Signal

Transverse magnetic fields

Spin in the z direction

Resonance Frequency

ALP mass

Technical Noise

Resonance Frequency

Determined mostly by external magnetic fields (which we can control with coils). Note that it is proportional to γ .

The Result

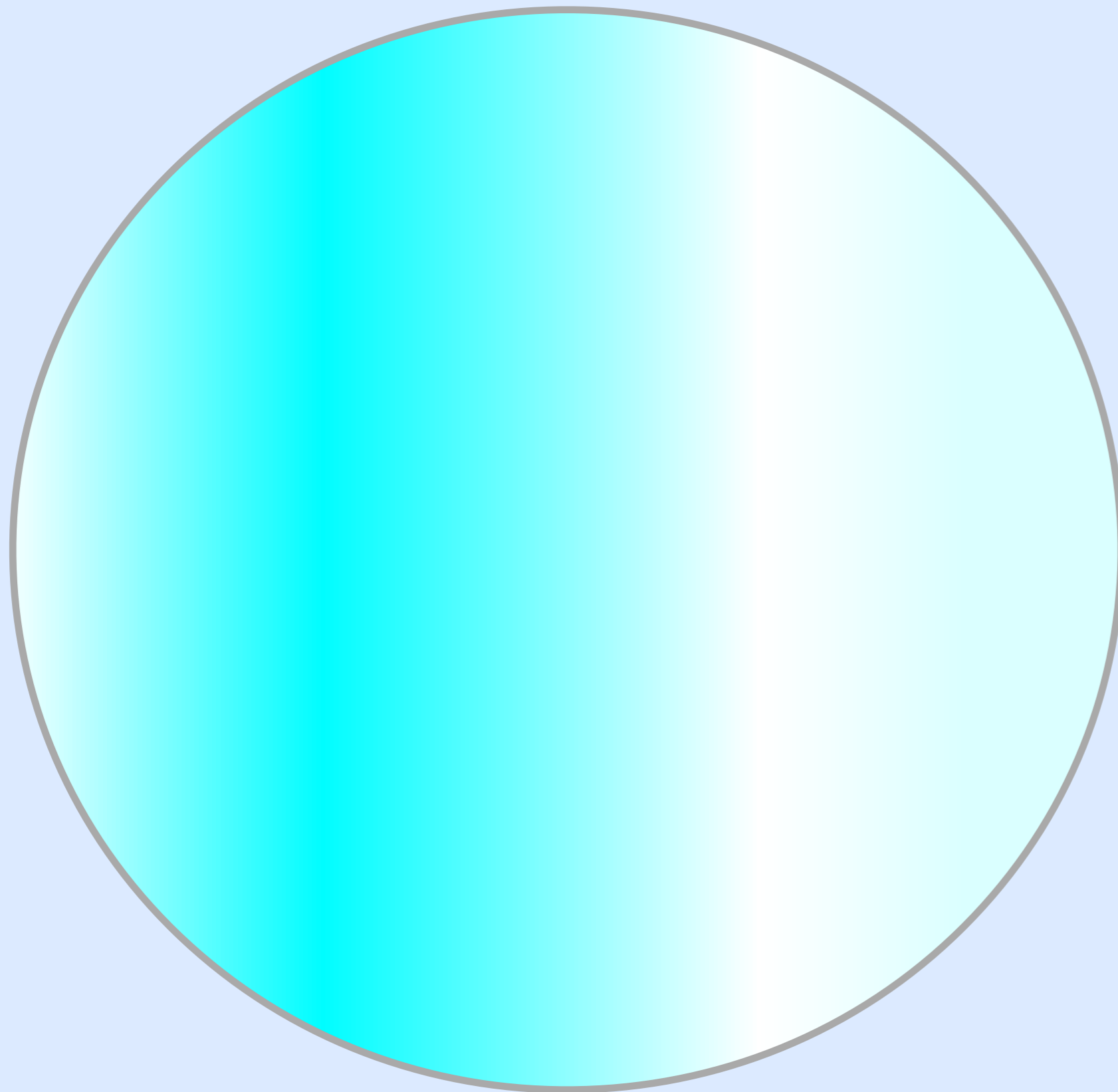
$$S_{\perp} = \frac{b_{\perp} + \gamma B_{\perp}}{i\Gamma + (\gamma B_z - m_a)} S_z + \delta S_{\text{eff}}$$

The transverse spin S_{\perp} is determined by the signal $b_{\perp} + \gamma B_{\perp}$ (Transverse magnetic fields), the decoherence rate $i\Gamma$ (Decoherence Rate), the resonance frequency $\gamma B_z - m_a$ (Resonance Frequency), the spin in the z direction S_z (Spin in the z direction), and the ALP mass m_a (ALP mass). The result is also affected by technical noise δS_{eff} (Technical Noise).

Decoherence Rate:

The decoherence rate determines the width of the atomic response to ALPs. Varies by 10 orders of magnitude depending on the system at hand (in most systems here it is Hz-kHzs). A small decoherence rate can be problematic due to slow response time.

(Co)magnetometer Ingredients List



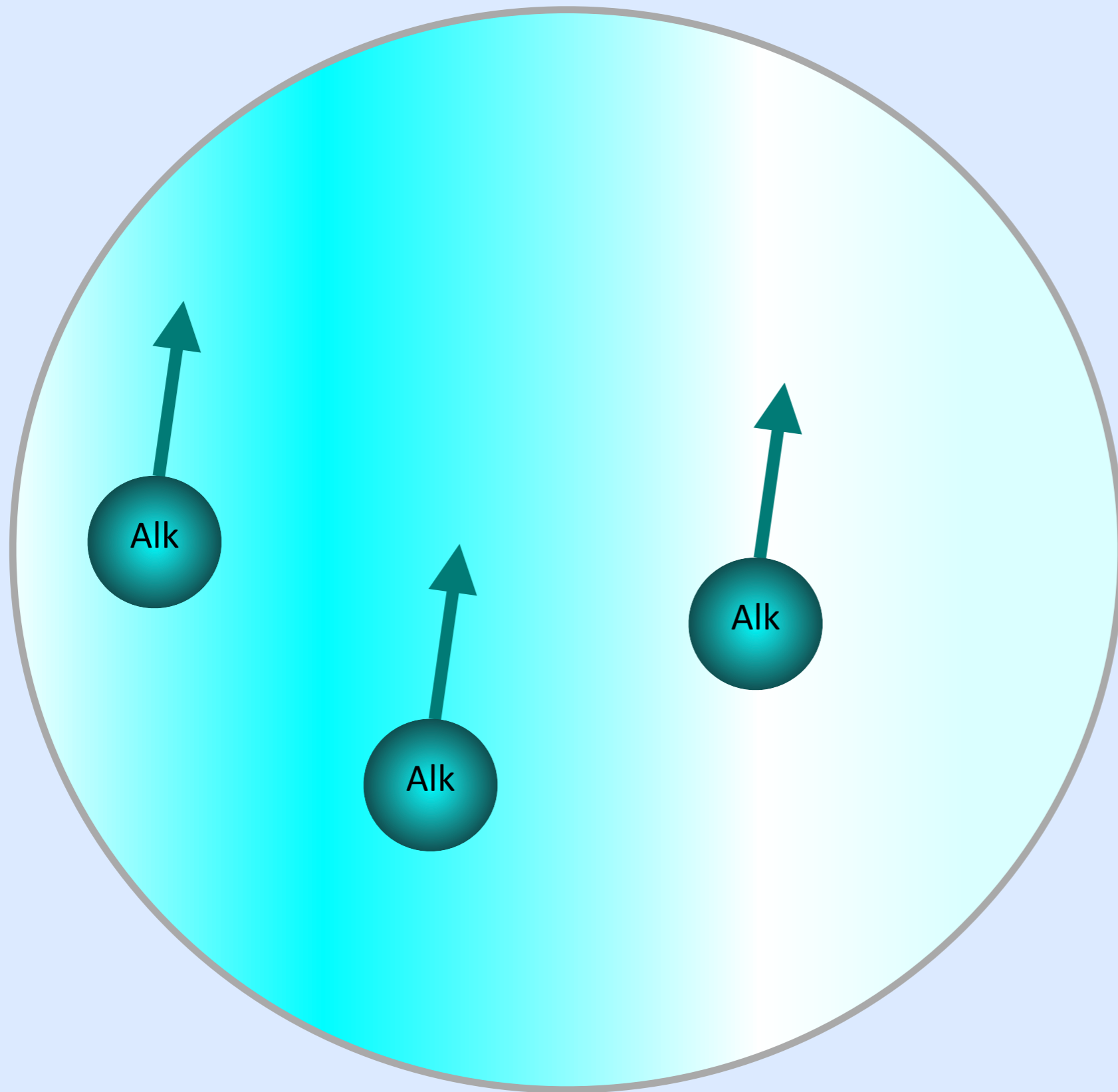
(Co)magnetometer
Ingredients List

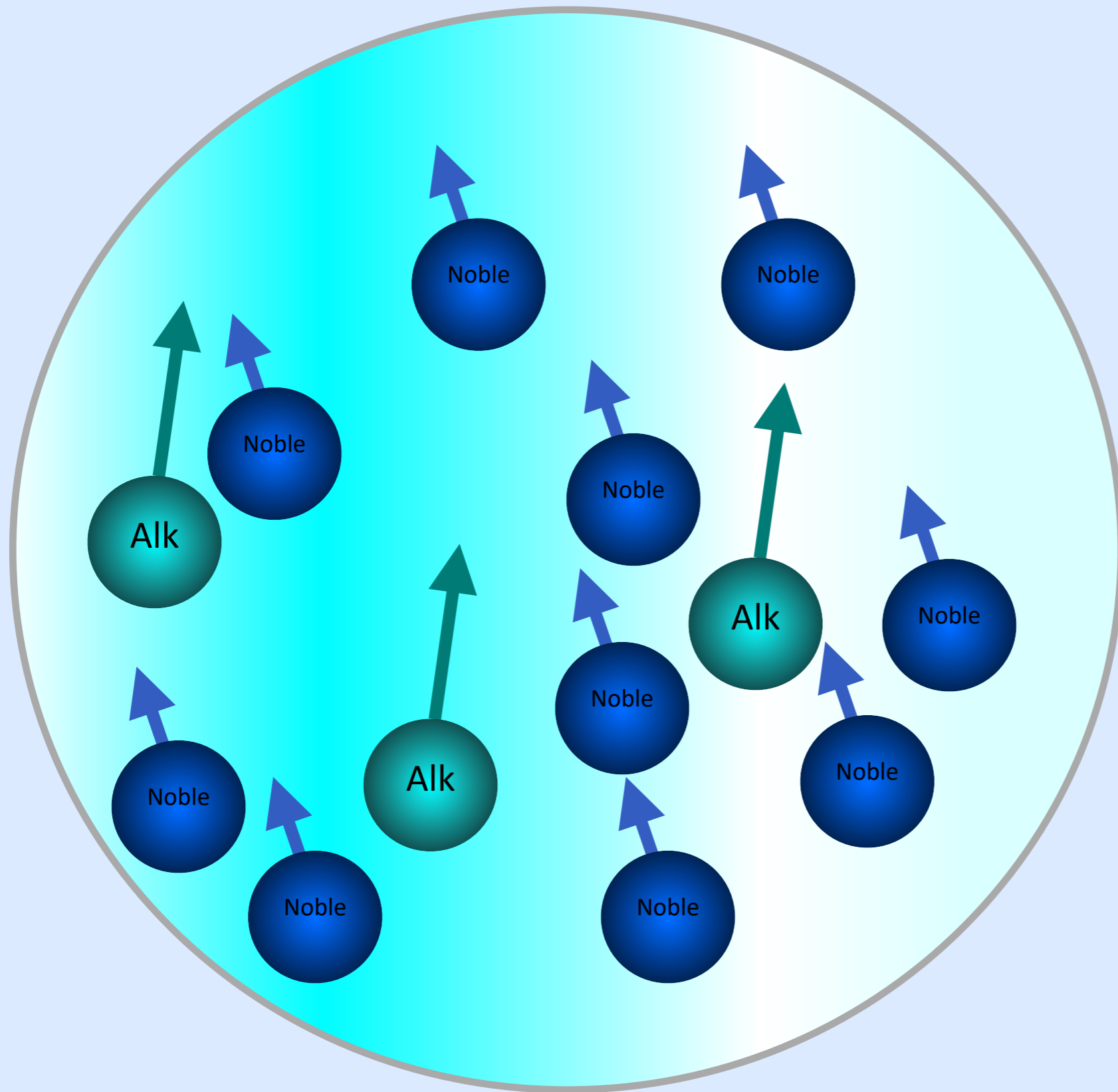
Glass Cell

(Co)magnetometer
Ingredients List

Glass Cell

Alkali Vapor



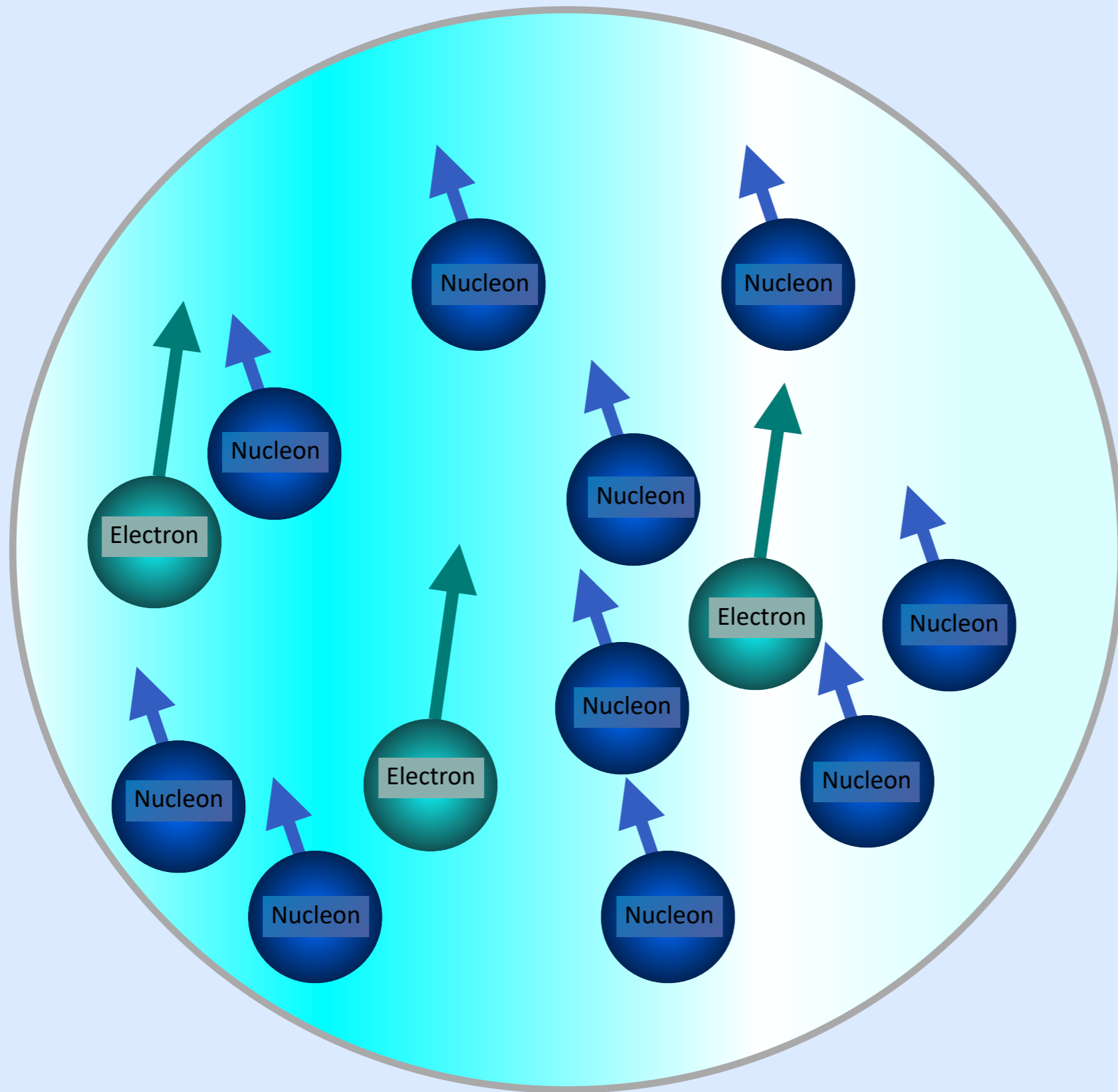


(Co)magnetometer
Ingredients List

Glass Cell

Alkali Vapor

Noble Gas

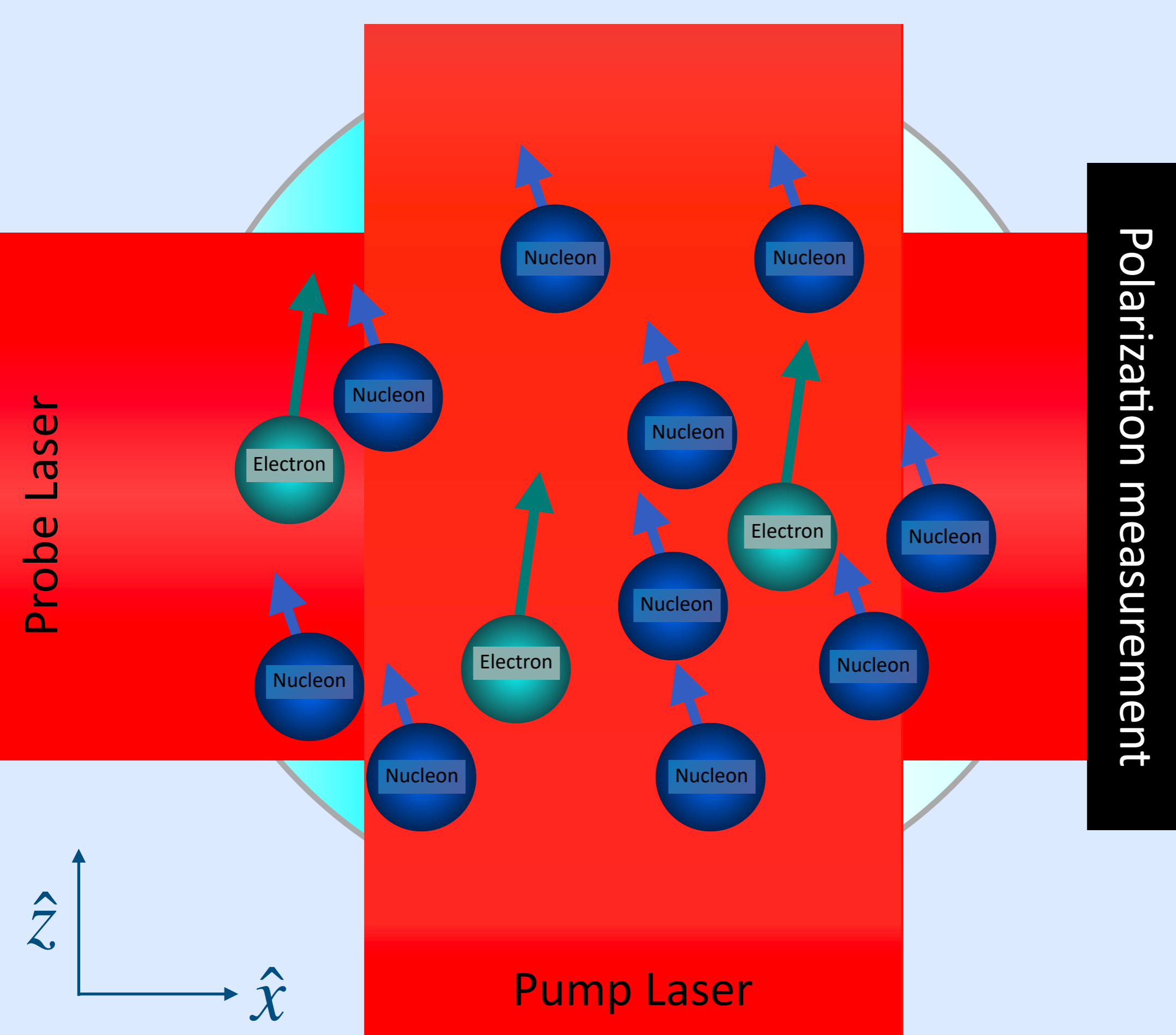


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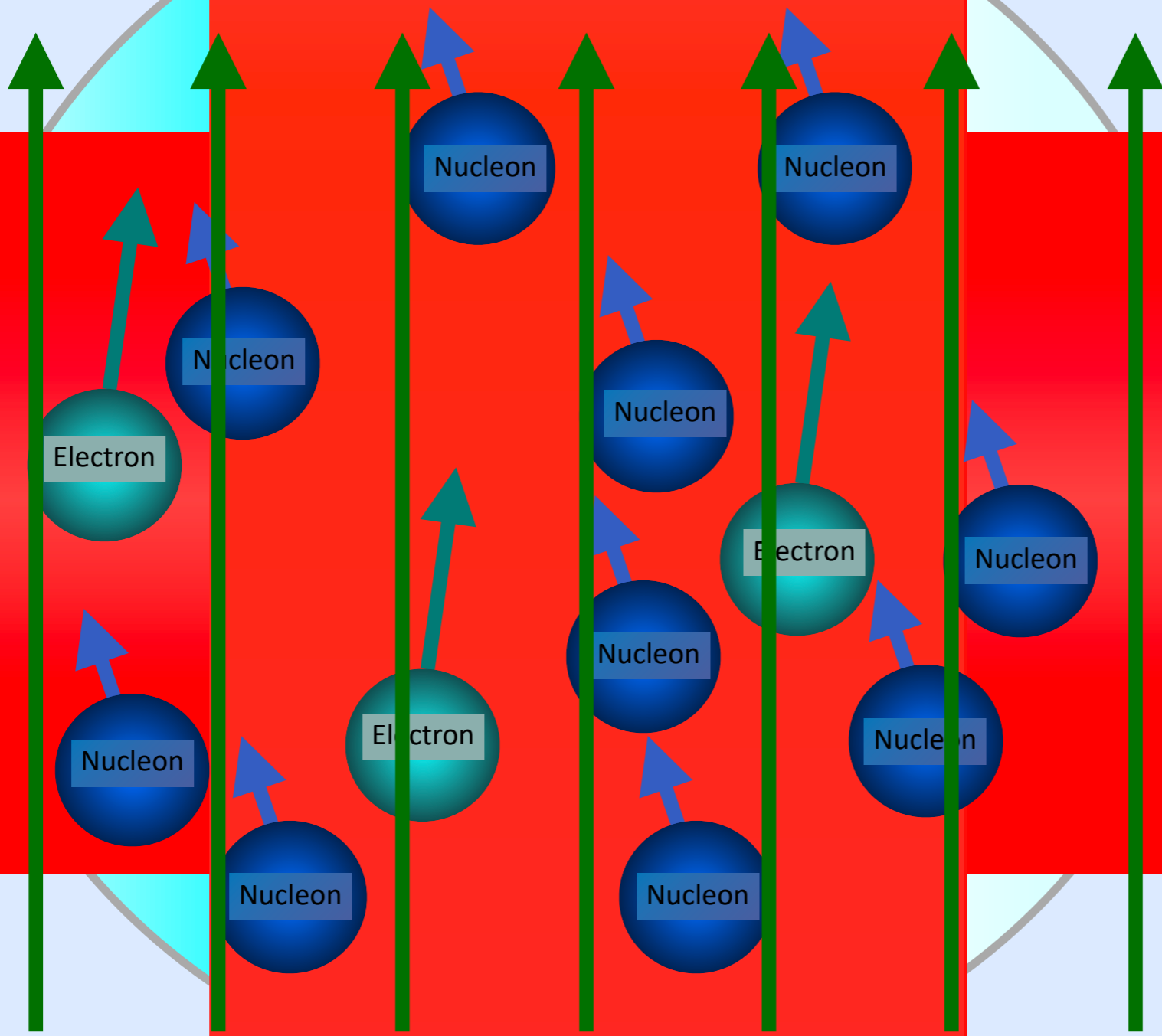
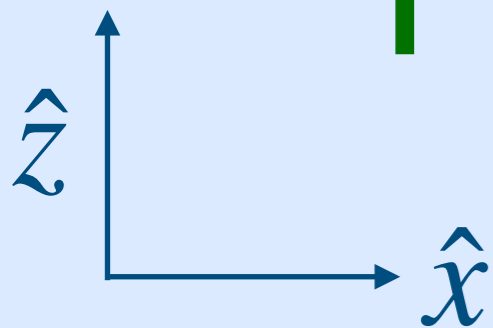


(Co)magnetometer
Ingredients List

- Glass Cell
- Alkali Vapor
- Noble Gas
- Lasers

B_z

Probe Laser



Pump Laser

Polarization measurement

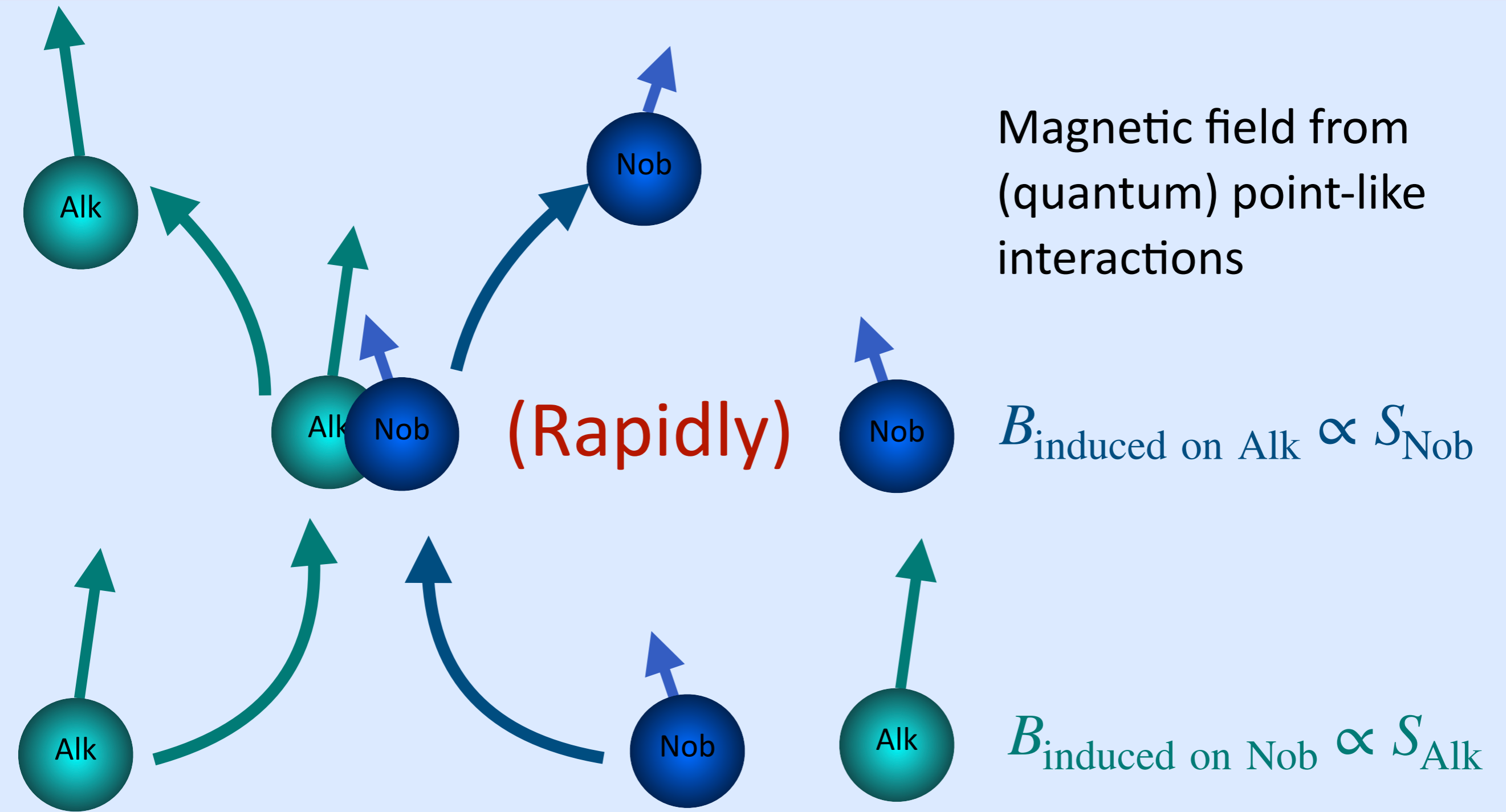
(Co)magnetometer
Ingredients List

- Glass Cell
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- Noble Gas
- Lasers

Misc:

- Oven
- Magnetic Shields
- Magnetic Coils
- Optical Components

Alk-Nob Spin Exchange



Current Summary

- Introduction:

- Axions and ALPs

ALPs create a magnetic-like field that can be measured by spin-based magnetometers.

- Spin-Based (Co)magnetometers

- Established Magnetometry Techniques for DM Research

- ...

“Compensation Point” Comagnetometer

[2020 JHEP: IMB, Hochberg, Kuflik, Volansky]

Response to Magnetic Noise

Response to Magnetic Noise

$$S_{\text{Alk}}(\omega = m_a) = \frac{\text{signal} + \gamma_{\text{Alk}} S_{z,\text{Alk}} B_{\perp,\text{Alk}}}{(\gamma_{\text{Alk}} B_{z,\text{Alk}} - m_a) + i\Gamma_{\text{Alk}}}$$

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$$B_{\perp,\text{Alk}} = B_{\perp,\text{noise}} + 2\lambda M_{\text{Nob}} S_{\perp,\text{Nob}} / S_{\text{Nob},z} = B_{\perp,\text{noise}} + \# S_{\perp,\text{Nob}}$$

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(ignoring backreaction of Alkali on Noble)

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$$\frac{\partial S_{\text{Alk}}}{\partial B_{\perp,\text{noise}}} = \frac{\gamma_{\text{Alk}} S_{z,\text{Alk}}}{(\gamma_{\text{Alk}} B_{z,\text{Alk}} - m_a) + i\Gamma_{\text{Alk}}} \left(1 + \frac{2\gamma_{\text{Nob}} \lambda M_{\text{Nob}}}{(\gamma_{\text{Nob}} B_{z,\text{Nob}} - m_a) + i\Gamma_{\text{Nob}}} \right)$$

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For $\Gamma_{\text{Nob}} \approx 0, m_a \approx 0, B_{z,\text{Nob}}$ is adjustable such that $\partial_{B_{\perp,\text{noise}}} S_{\text{Alk}} = 0$

The Compensation Point

The Compensation Point

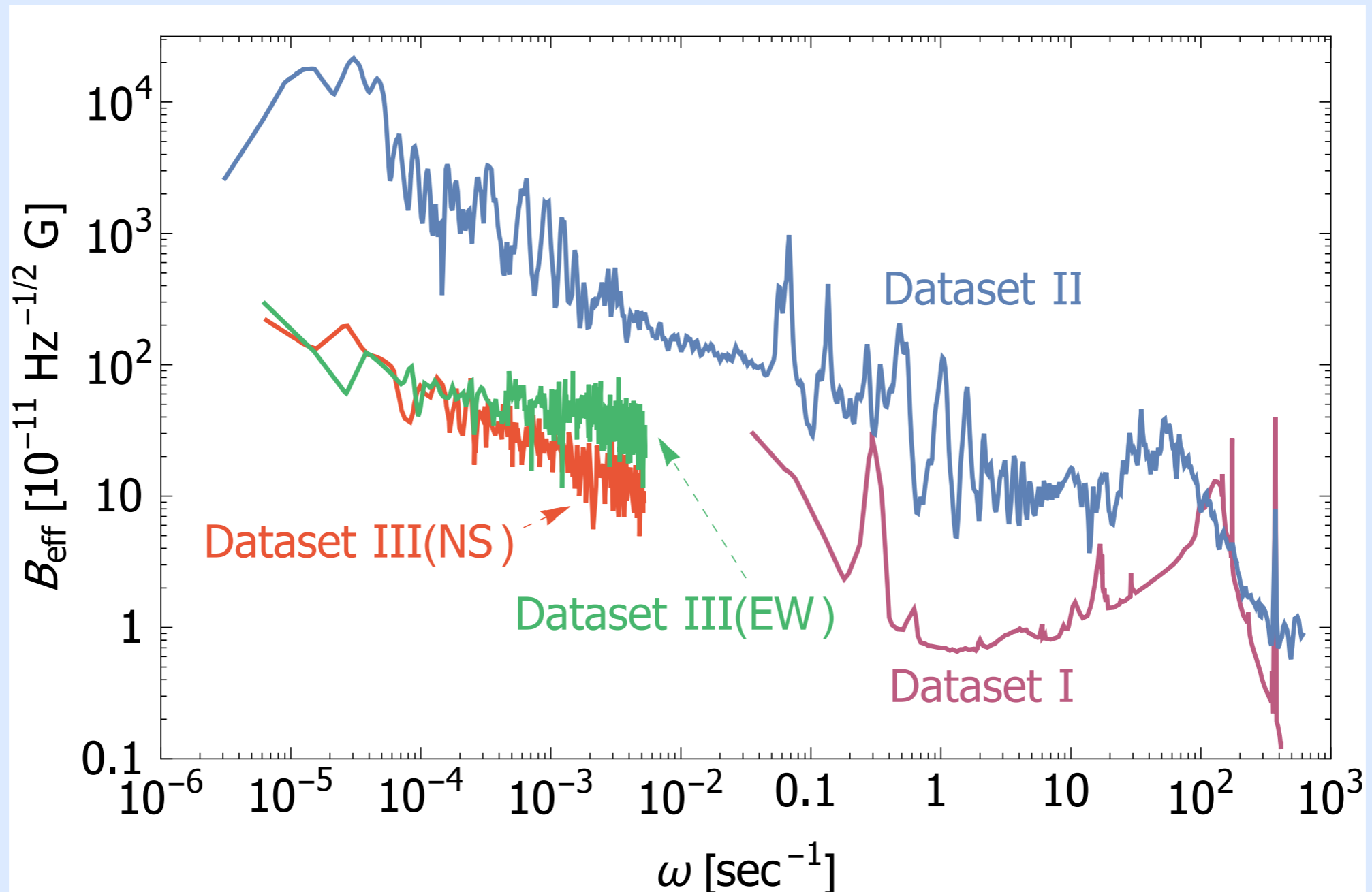
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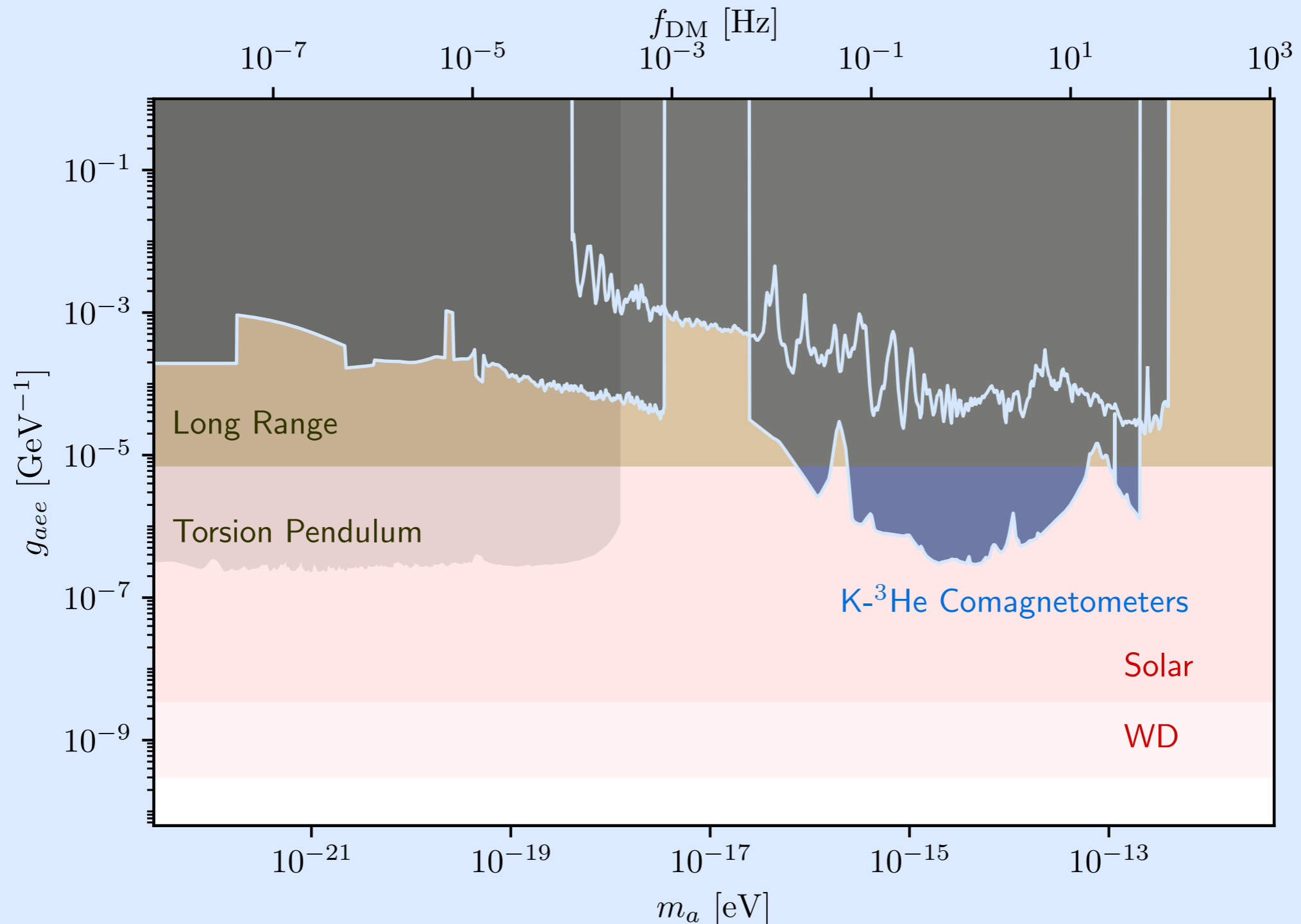
Additionally, the two species are “(near) in resonance”, allowing for a fast response of the system to sudden changes.

Existing Data



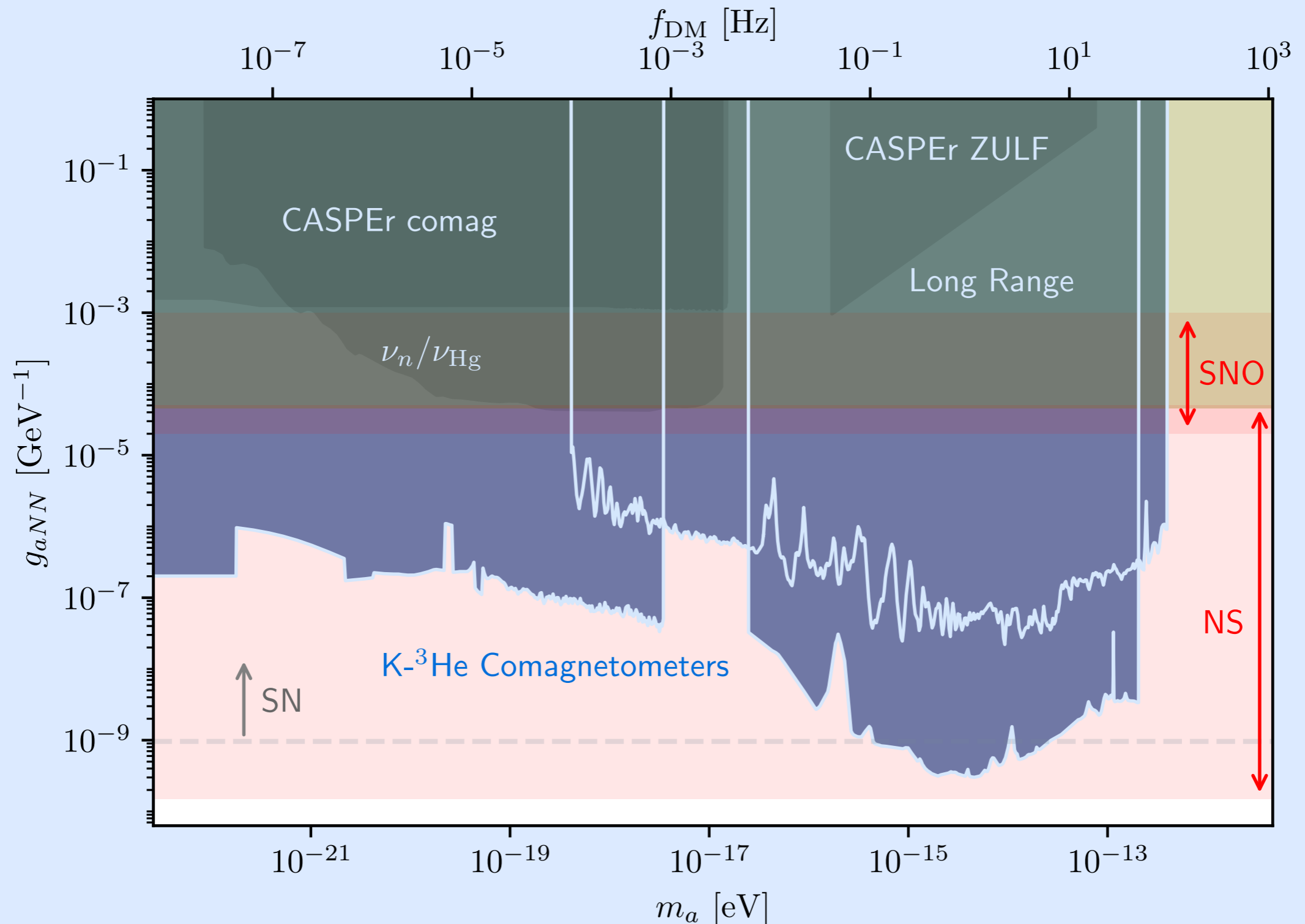
[Gergoios Vasilakis Dissertation 2011], [Justin M. Brown Dissertation 2011], [Thomas W. Kornack Dissertation 2005]

Results (e)

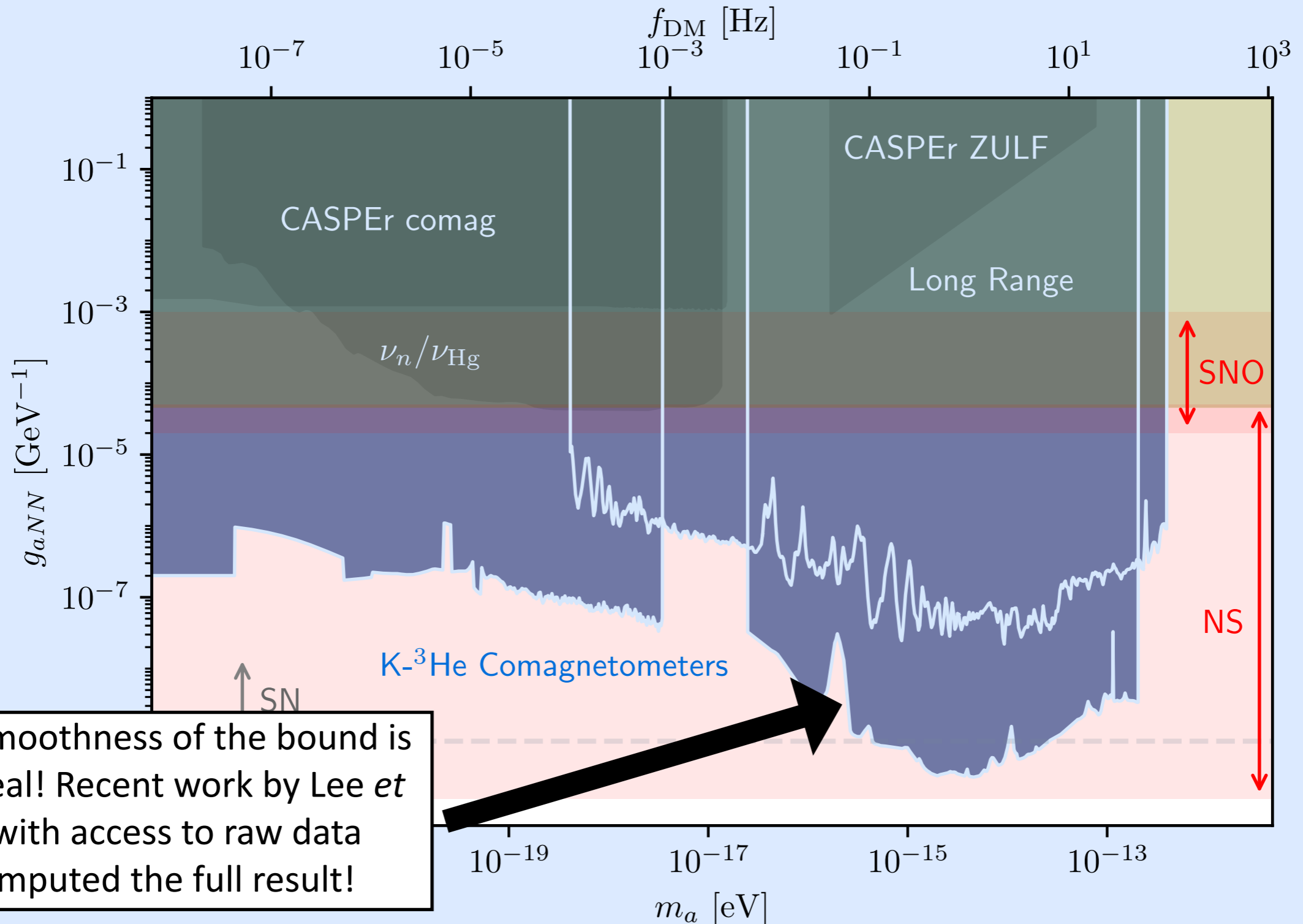


[Y. Hochberg, E. Kuflik, T. Volansky, *IMB 1907.03767*. W. A. Terrano, *et al.*:1508.02463, LUX Collaboration:1704.02297, M. M. M Bertolami, *et al.*:1406.7712, W. A. Terrano, *et al.*: 1902.04246, G. Vasilakis, Dissertation: 2011, J. M. Brown, Dissertation: 2011, T. W. Kornack Dissertation: 2005].

Results (n)



Results (n)



The smoothness of the bound is not real! Recent work by Lee *et al.* with access to raw data computed the full result!

Lessons Learned

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- There's a huge potential for searching for ALP-nucleon interactions with existing techniques.

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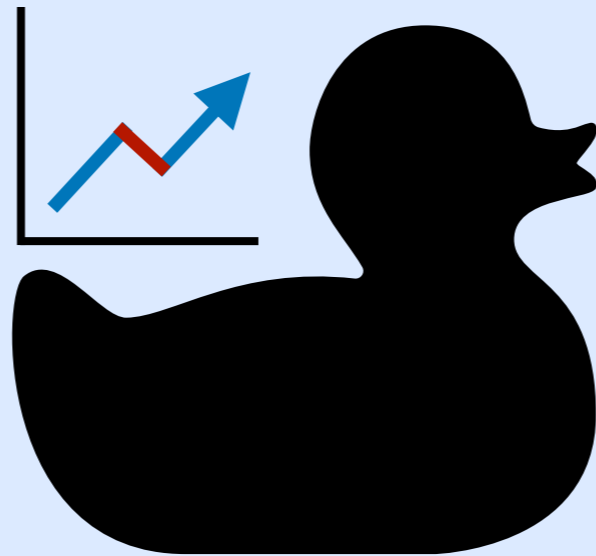
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Lessons Learned

- There's a huge potential for searching for ALP-nucleon interactions with existing techniques.
- Electrons are very hard to work with due to their (i) wide bandwidth and (ii) large response to background magnetic fields.
- We need our own experiment!

Noble and Alkali Spin Detectors for Ultralight Coherent dark matter

Noble and Alkali Spin Detectors for Ultralight Coherent dark matter



NASDUCK

[2022, Science Adv. IMB, Ronen, Shaham, Katz, Volansky, Katz (NASDUCK)], [2023, Nature Comm. IMB, Shaham, Hochberg, Kuflik, Volansky, Katz (NASDUCK)] and [in progress: NASDUCK (incl. IBM)]

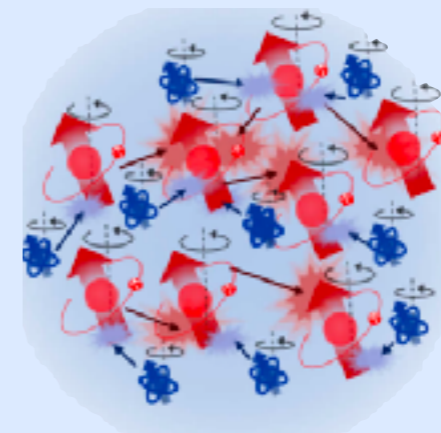
Existing and Upcoming Experiments

NASDUCK Floquet



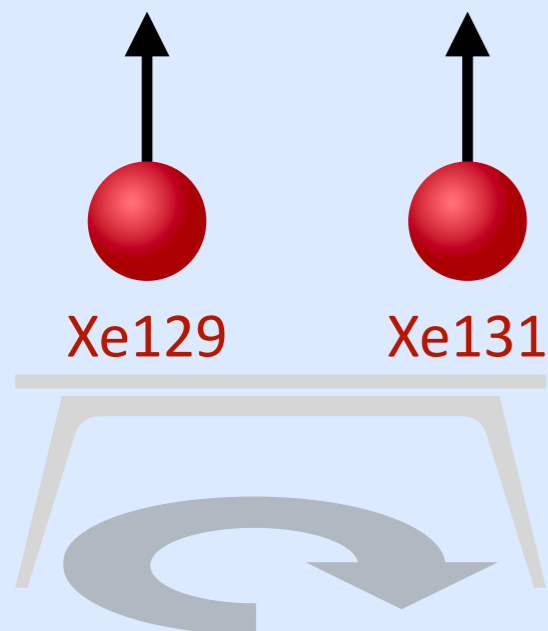
[2022, Science Adv. IMB, Ronen, Shaham, Katz, Volansky, Katz]

NASDUCK SERF



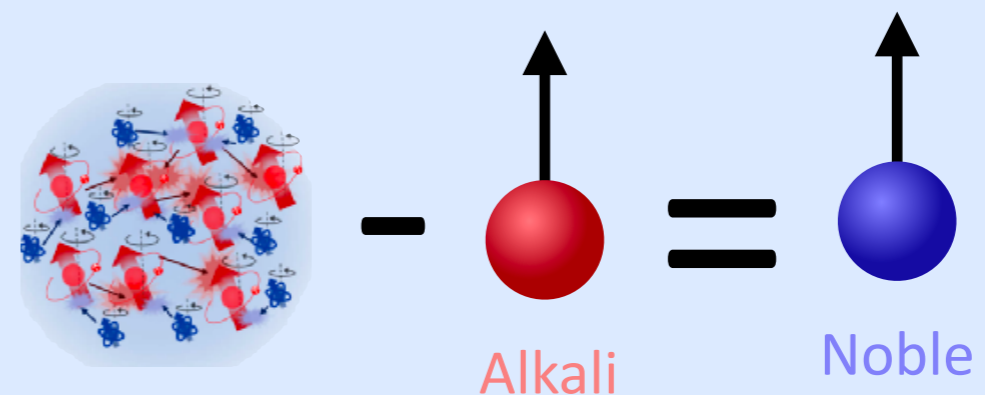
[2023, Nature Comm. IMB, Shaham, Hochberg, Kuflik, Volansky, Katz]

NASDUCK Modulated



(Prototype data exists, redone pre-publication)

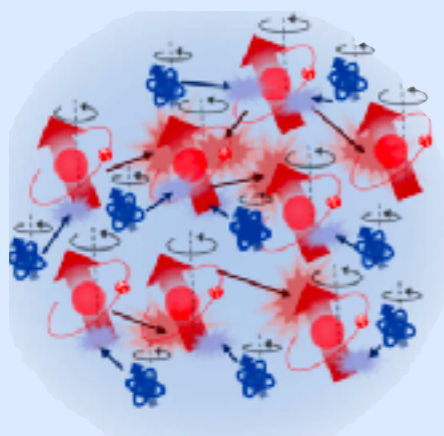
NASDUCK Subtracted(?)



[In progress: NASDUCK (incl. IMB)]

Existing and Upcoming Experiments

NASDUCK SERF



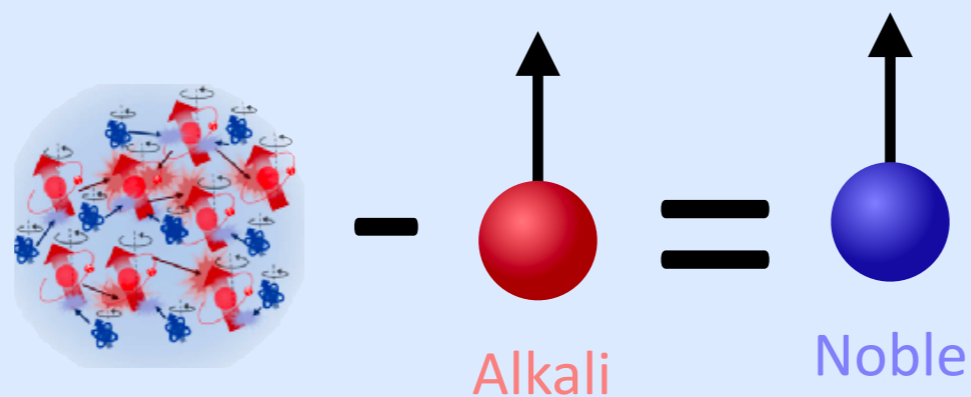
[2023, Nature Comm. IMB, Shaham, Hochberg, Kuflik, Volansky, Katz]

NASDUCK Floquet



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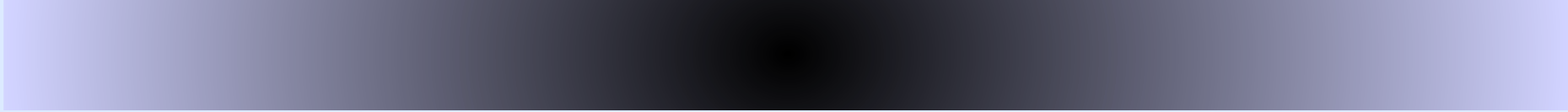
Signal Response of Self-Compensating Comag

* To leading order in relevancy

$$S_{\text{Alk}}(\omega = m_a) = \frac{\gamma_{\text{Alk}} S_{z,\text{Alk}} B_{\perp,\text{Alk}}}{(\gamma_{\text{Alk}} B_{z,\text{Alk}} - m_a) + i\Gamma_{\text{Alk}}} =$$

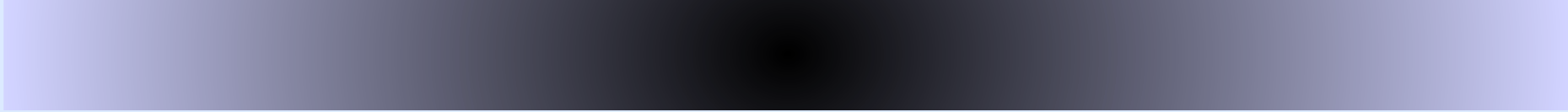
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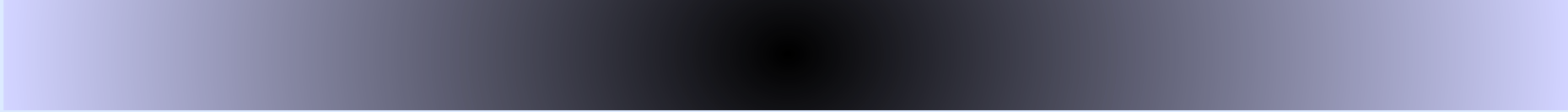
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Tuning $\gamma_{\text{Alk}} B_{z,\text{Alk}} \approx m_a \pm \Gamma_{\text{Alk}}$ gives an enhancement of $\frac{m_a}{\Gamma_{\text{Alk}}}$!



NASDUCK SERF

[2023, Nature Comm. IMB, Shaham, Hochberg, Kuflik, Volansky, Katz]

The Briefest of Explanations on “SERF”

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The enhancement in sensitivity is $\frac{m_a}{\Gamma_{\text{Alk}}}$, so the smaller Γ_{Alk} , the better*!

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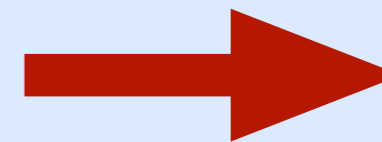
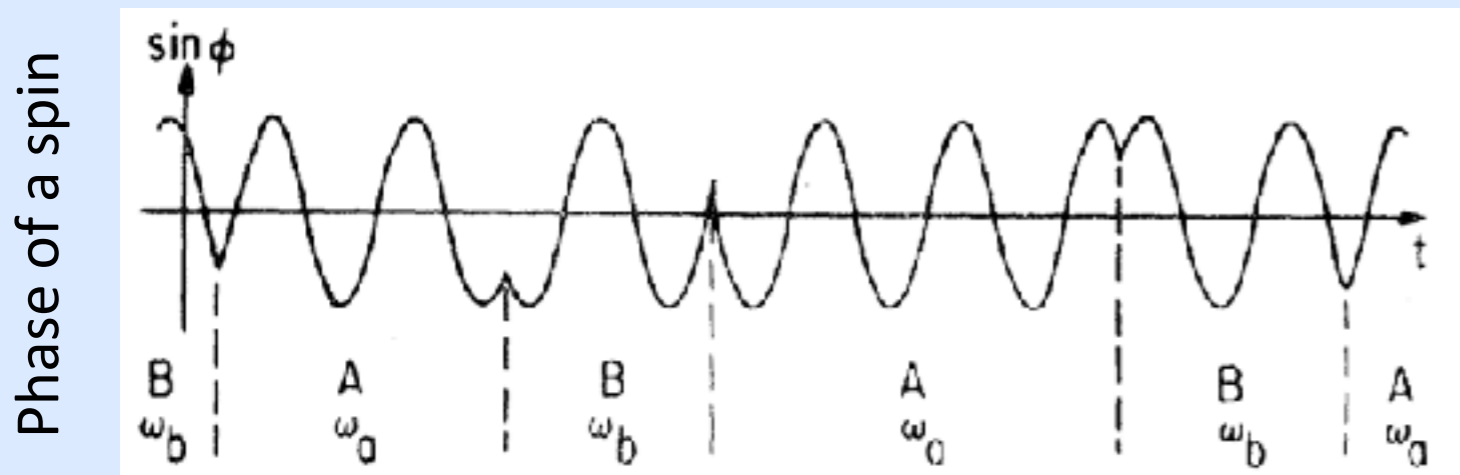
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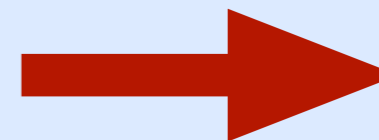
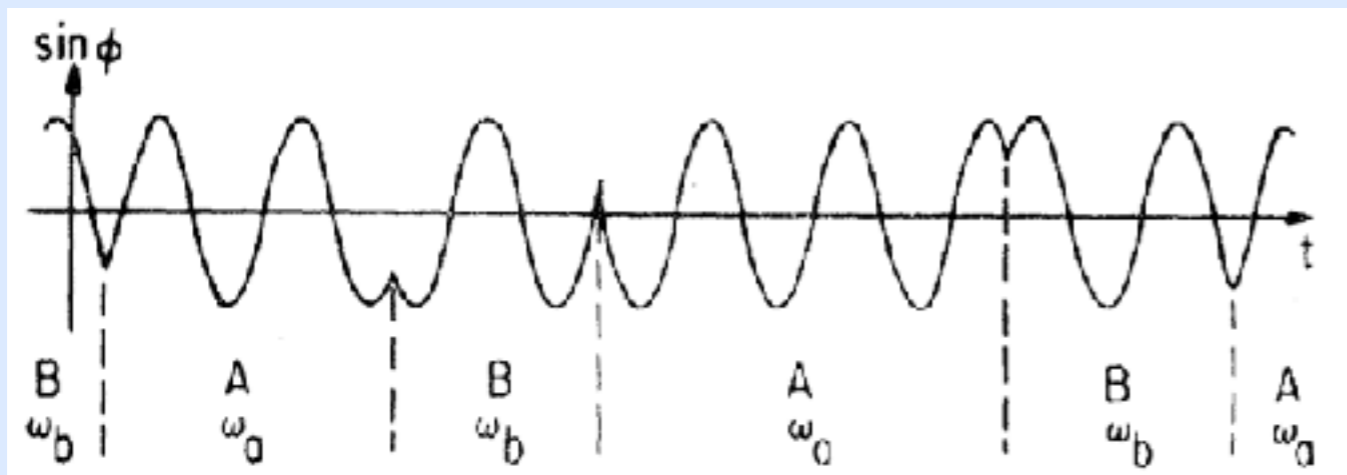
Spin exchange
induces relaxation

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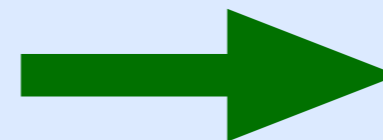
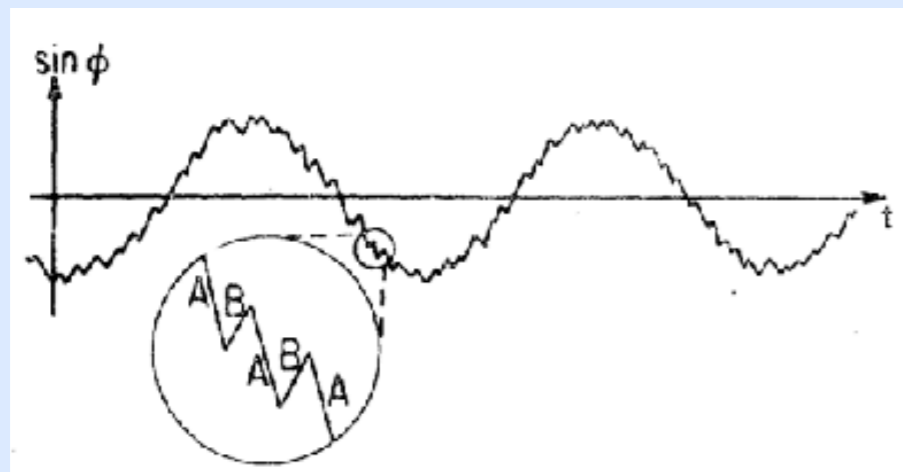
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Phase of a spin

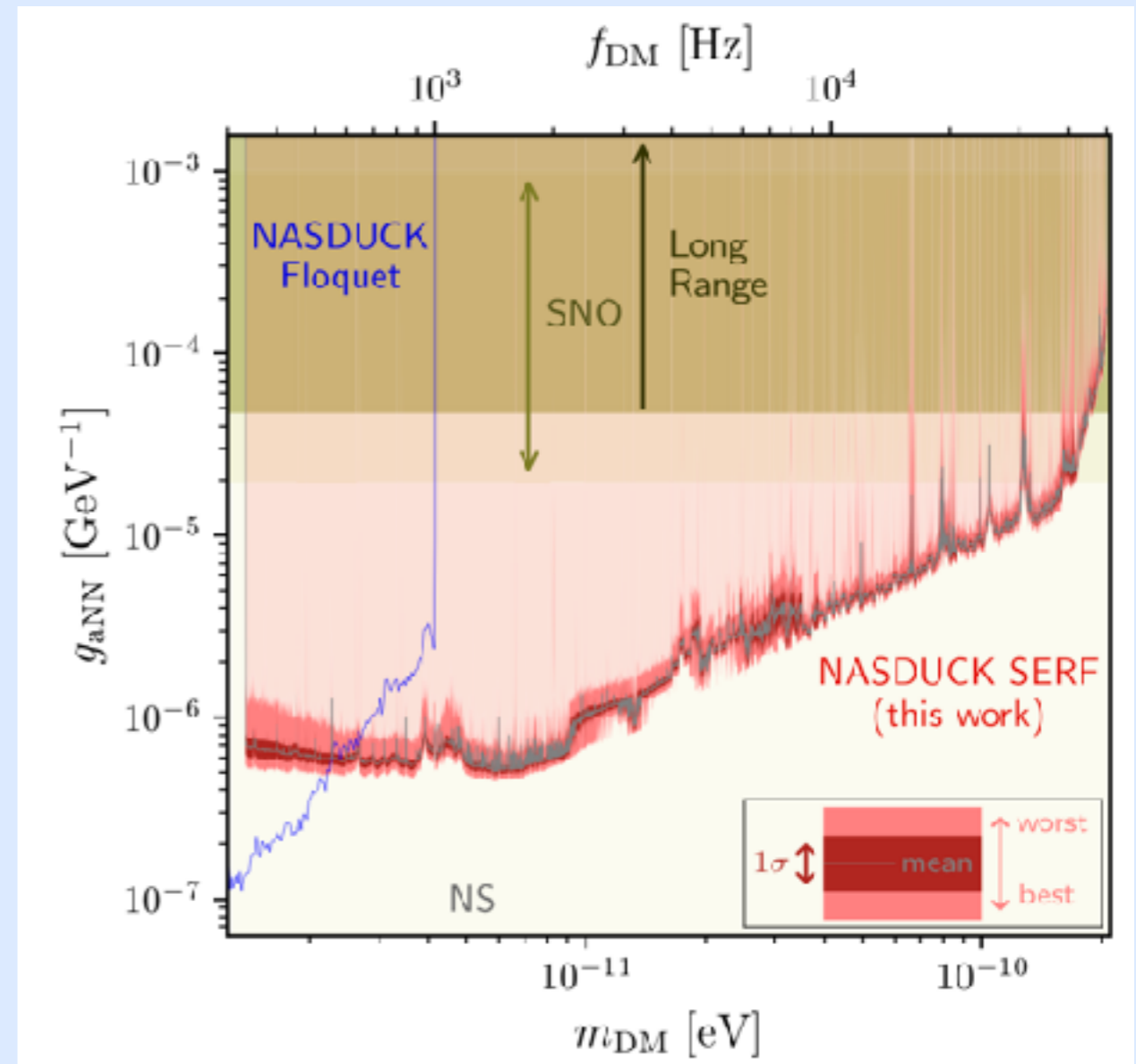
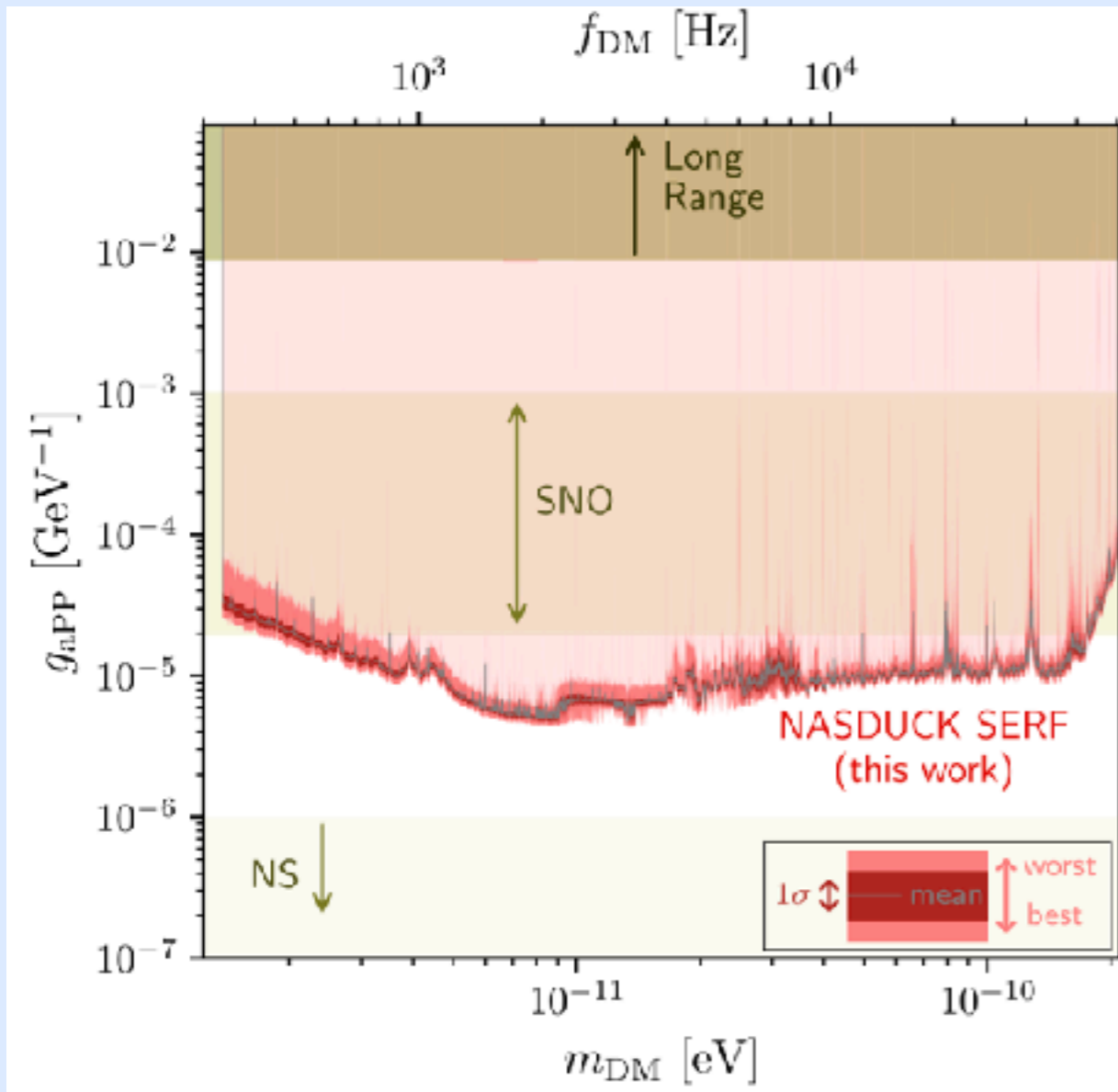


Spin exchange induces relaxation



Rapid spin exchange (from low B fields and high densities) causes no relaxation, **Spin Exchange Relaxation Free (SERF)**

NASDUCK SERF Results





NASDUCK Floquet

[2022, Science Adv. IMB, Ronen, Shaham, Katz, Volansky, Katz]

The Problem at High Frequencies

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$$\text{signal} = \frac{\text{const} \cdot b_{\perp, \text{ALP-Nob}}}{\left((\gamma_{\text{Alk}} B_{z, \text{Alk}} - m_a) + i\Gamma_{\text{Alk}} \right) \left((\gamma_{\text{Nob}} B_{z, \text{Nob}} - m_a) + i\Gamma_{\text{Nob}} \right)}$$

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Alkali response Noble response

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The noble gas for large B fields (large frequencies) is off resonant!

Floquet Fields (Math Slide)

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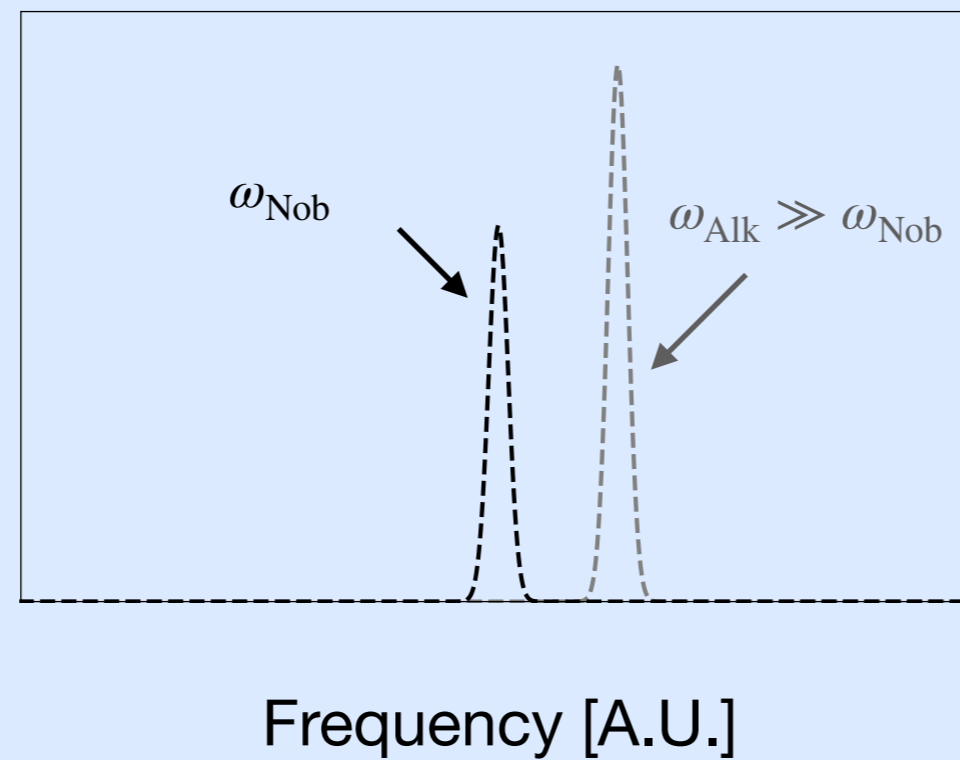
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So that for $m_a = \gamma_{\text{Nob}} B_{z,\text{Nob},0}$, we can now have both the species in resonance!

Floquet Fields (Illustration Slide)

* Plots are not to scale

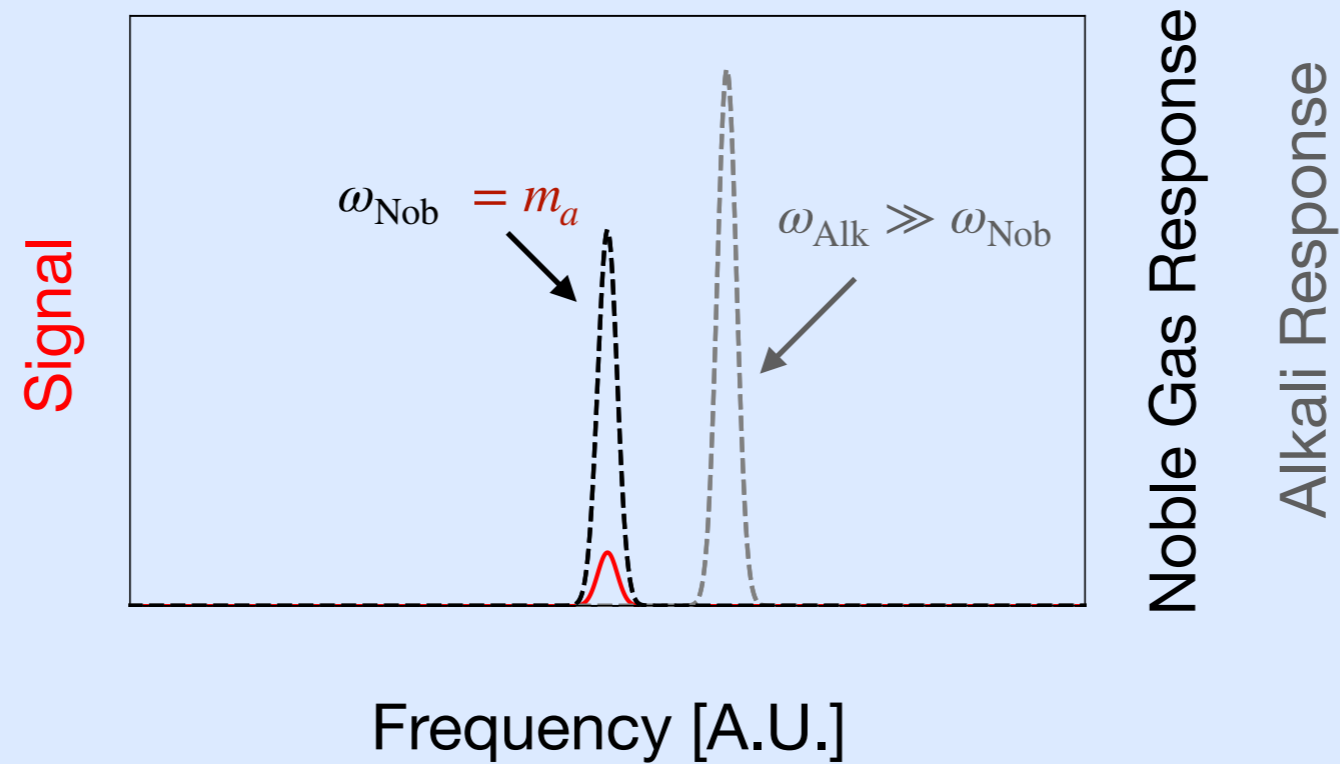


Noble Gas Response

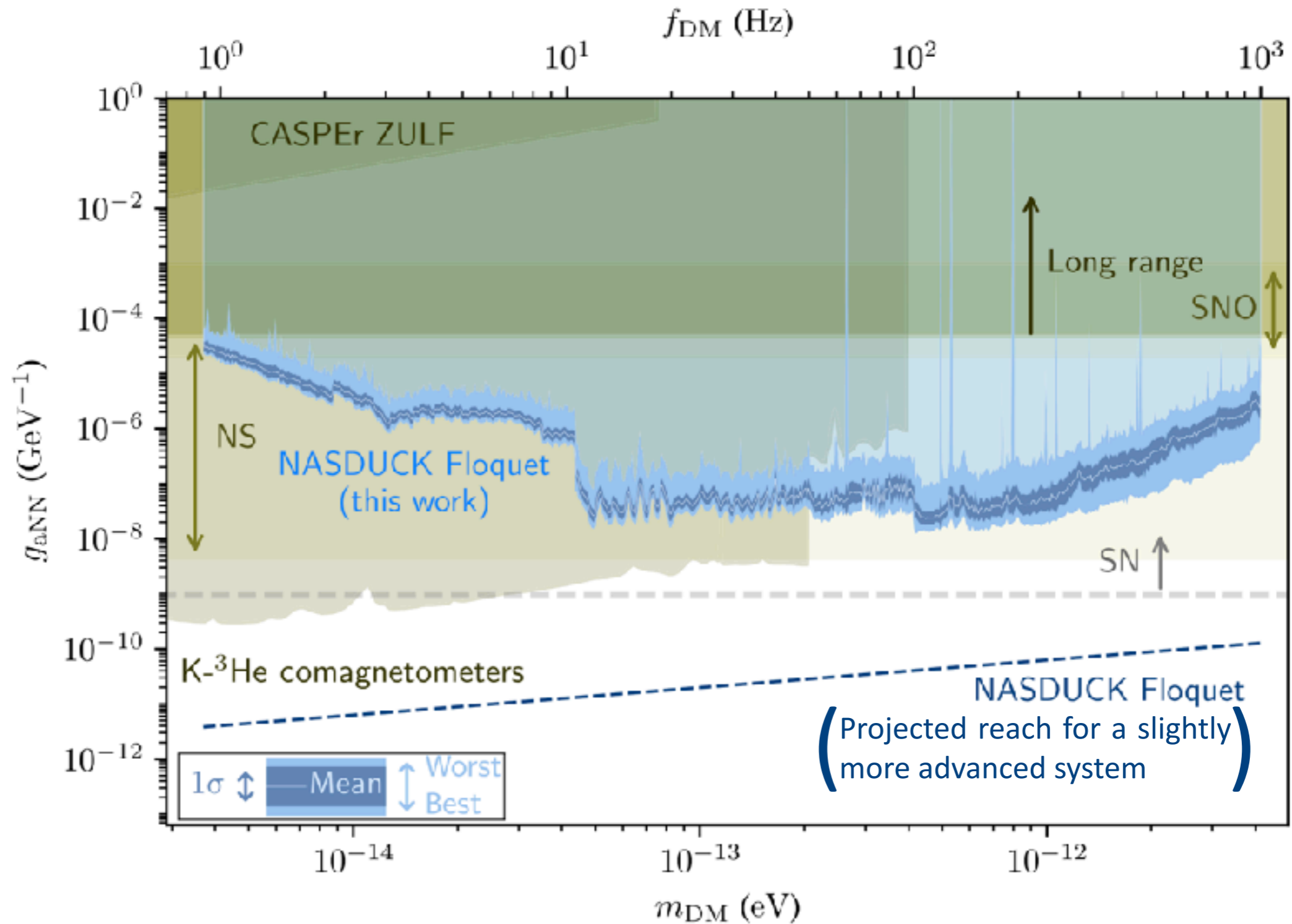
Alkali Response

Floquet Fields (Illustration Slide)

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NASDUCK Floquet Results



NASDUCK Floquet Results Commentary

Sensitivity was limited by noise of probe beam (i.e. OOM larger than magnetic noise)



An improvement by an order of magnitude is fairly easy*

Current Summary

Part 1: ALPs create a magnetic-like field that can be measured by spin-based magnetometers.



- Established Magnetometry Techniques for DM Research

Part 2: NASDUCK opened up new possibilities using existing magnetometry techniques!



- Novel Magnetometry Techniques

Sidenote: what else can be done with these detectors

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- Look for other “Anomalous Fields”:
 - Other DM models/Long Range Forces
 - High Frequency Gravity Waves [IMB et al. in progress]
 - Cosmic Neutrinos (seems too hard)

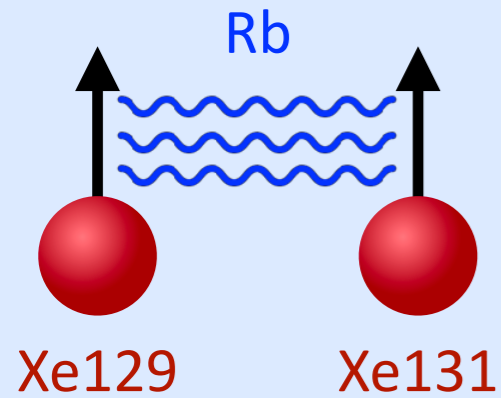
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Ongoing Experiments with new techniques*

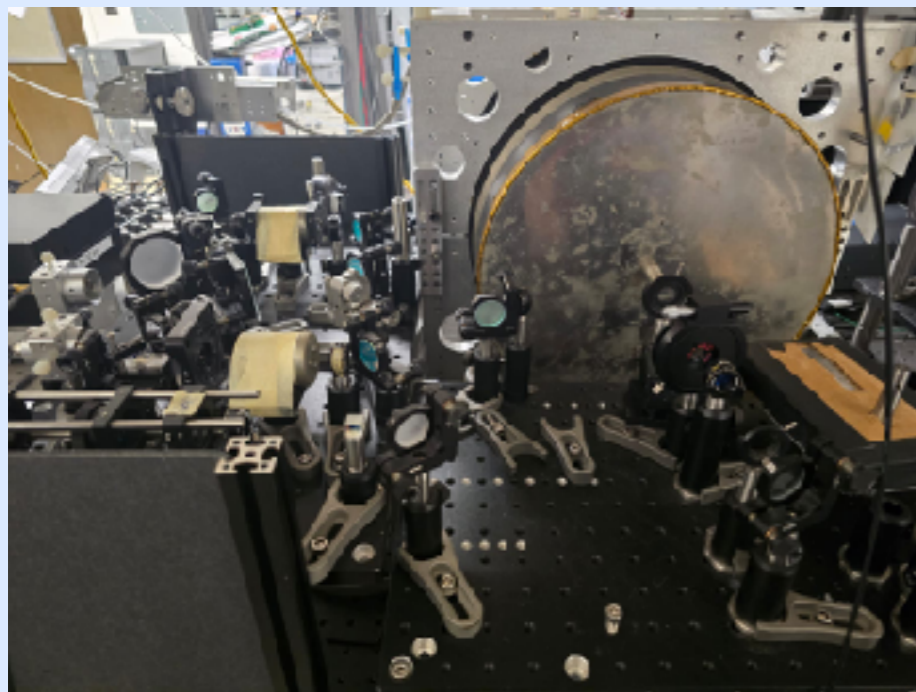
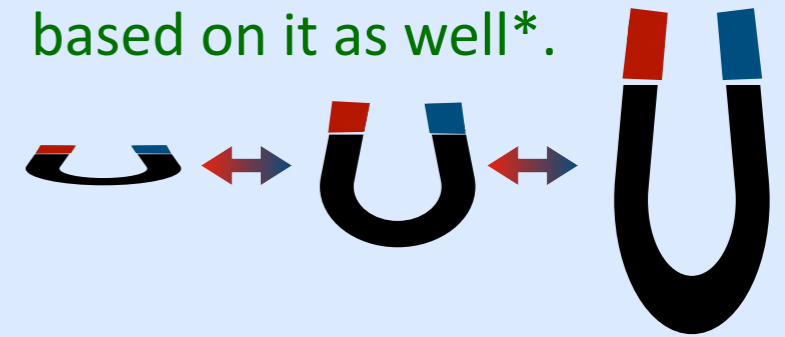


“Cocomag”

Data exists, waiting to be analyzed, this possibly has relevance to QI*.

Longitudinal Measurements

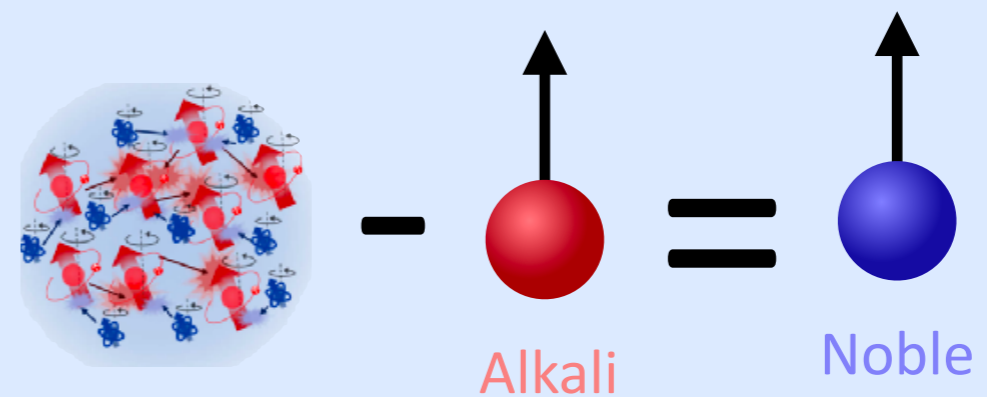
The theory paper is out, and an experiment has already been performed based on it as well*.



Dual Alkali Subtraction

Ongoing calibrations in preparation to data-taking

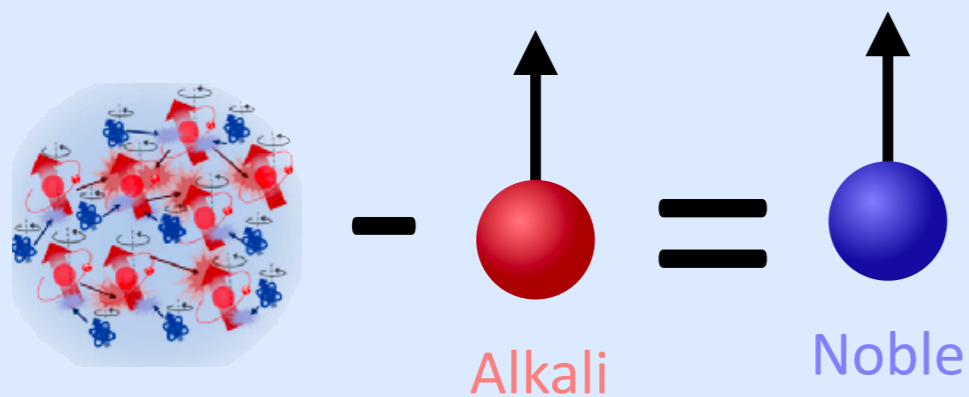
NASDUCK “Subtracted”



At the design stages, optimizing methodologies.

Ongoing Experiments with new techniques*

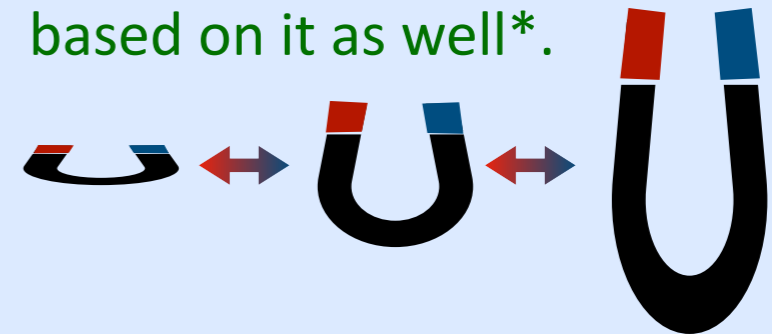
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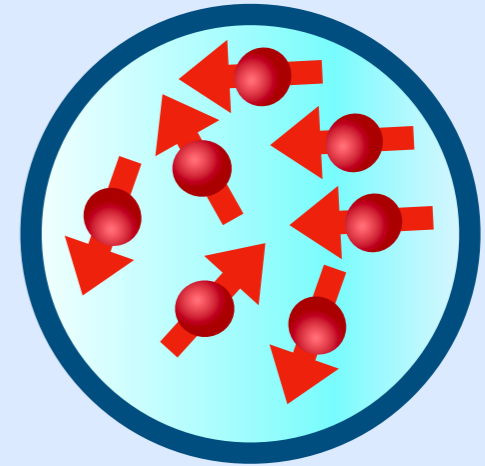
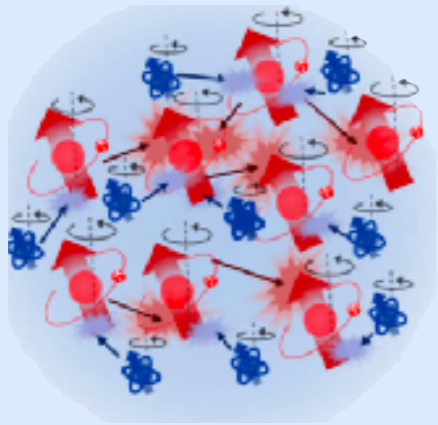
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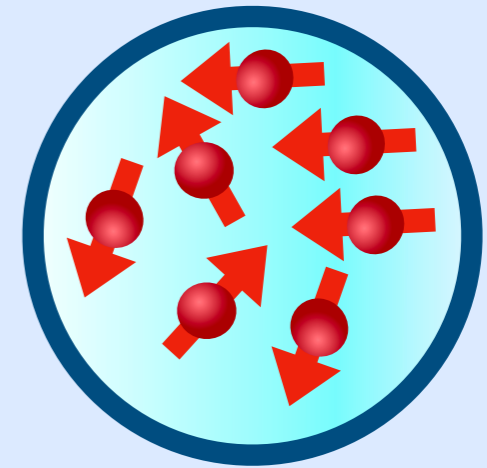
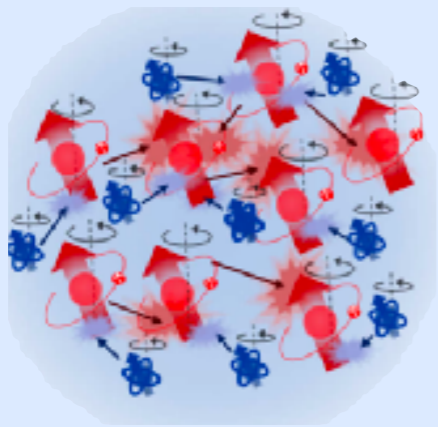
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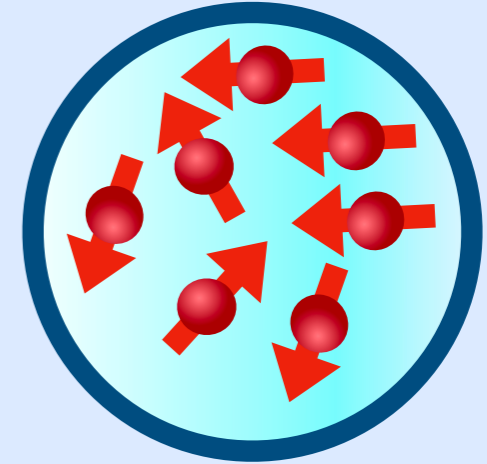
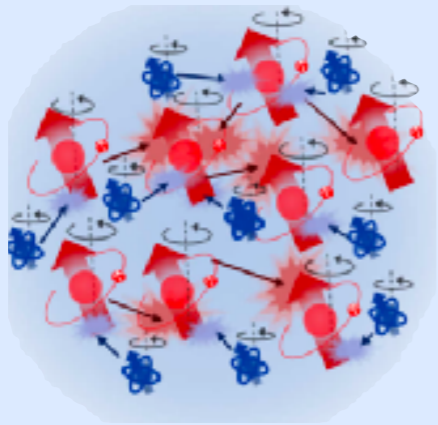


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NASDUCK Subtraction

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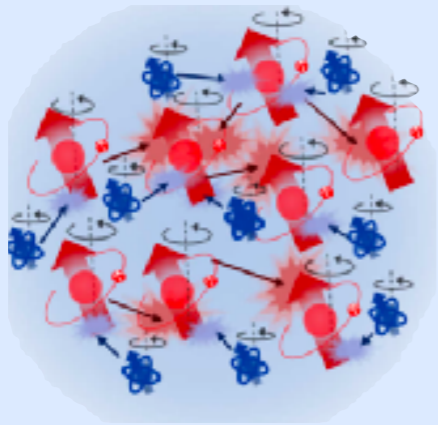
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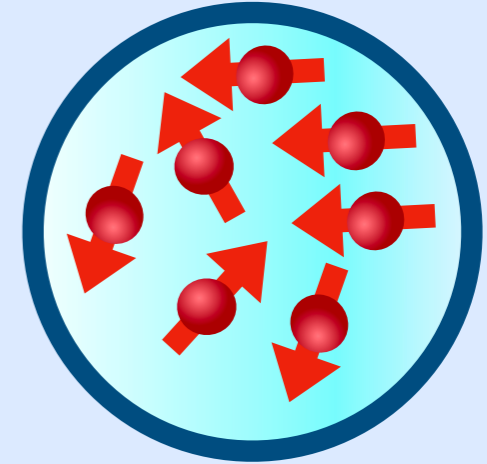
$$\Delta S \equiv S_{\perp,1} - \frac{c_1}{c_3} S_{\perp,2}$$

NASDUCK Subtraction

* To leading order in details



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$$\text{SNR}(\Delta S) = \frac{c_2}{\sqrt{1 + (c_1/c_3)^2}} \cdot \frac{b_{\perp, \text{ALP-Nob}}}{\delta S_{\perp}}$$

Scalar Longitudinal Magnetometry

[2023, PRD. IMB, Budker, Flambaum, Samsonov, Sushkov, Tretiak]

Since coupling constants are scalars, scalar DM (not axions) can mimic variation in fundamental constants.

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We can measure B_z rather than B_{\perp}

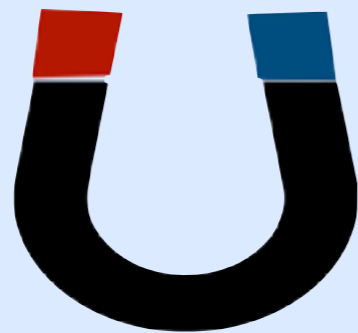
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First experiment is ongoing by Sushkov et al.

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Naive answer:

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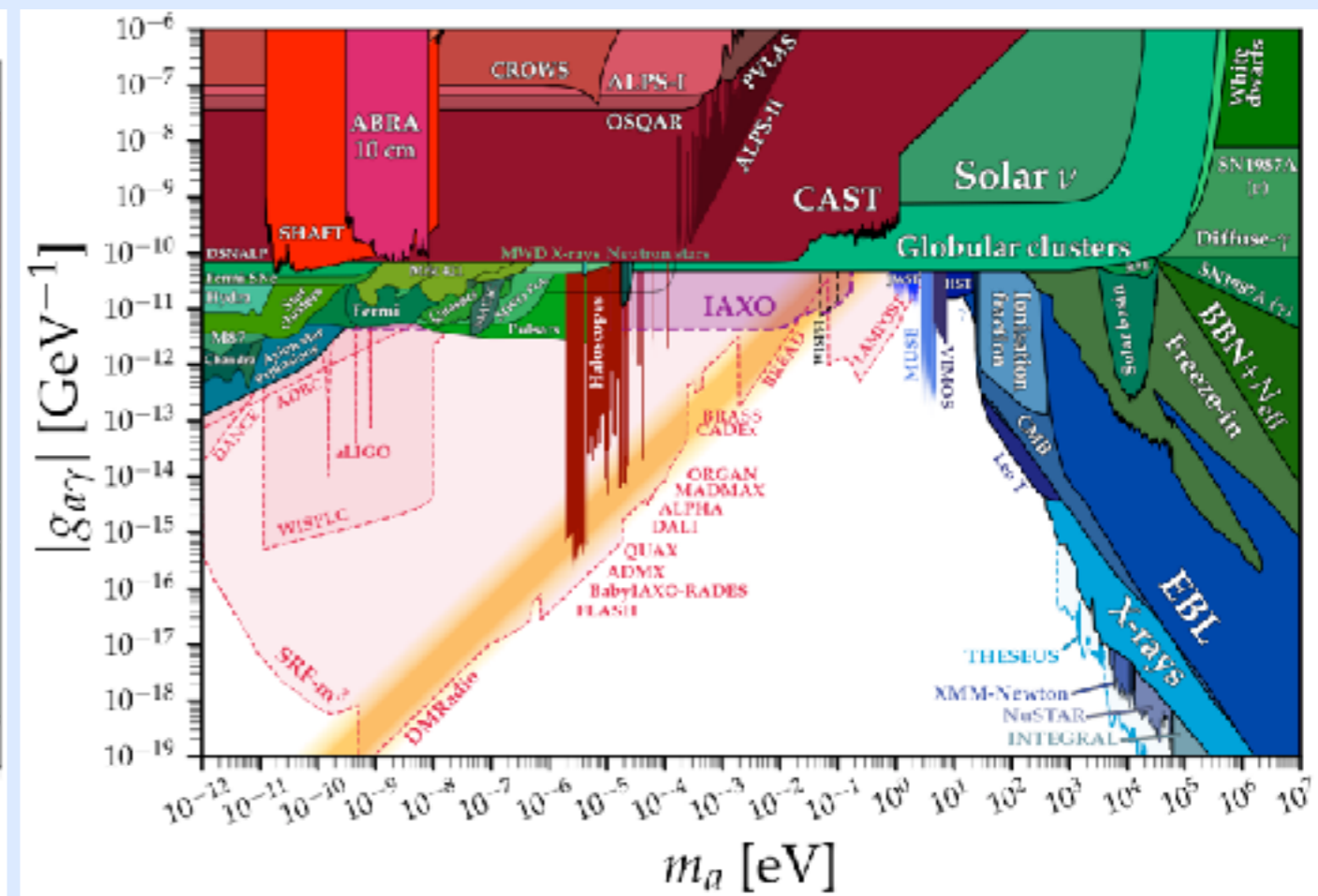
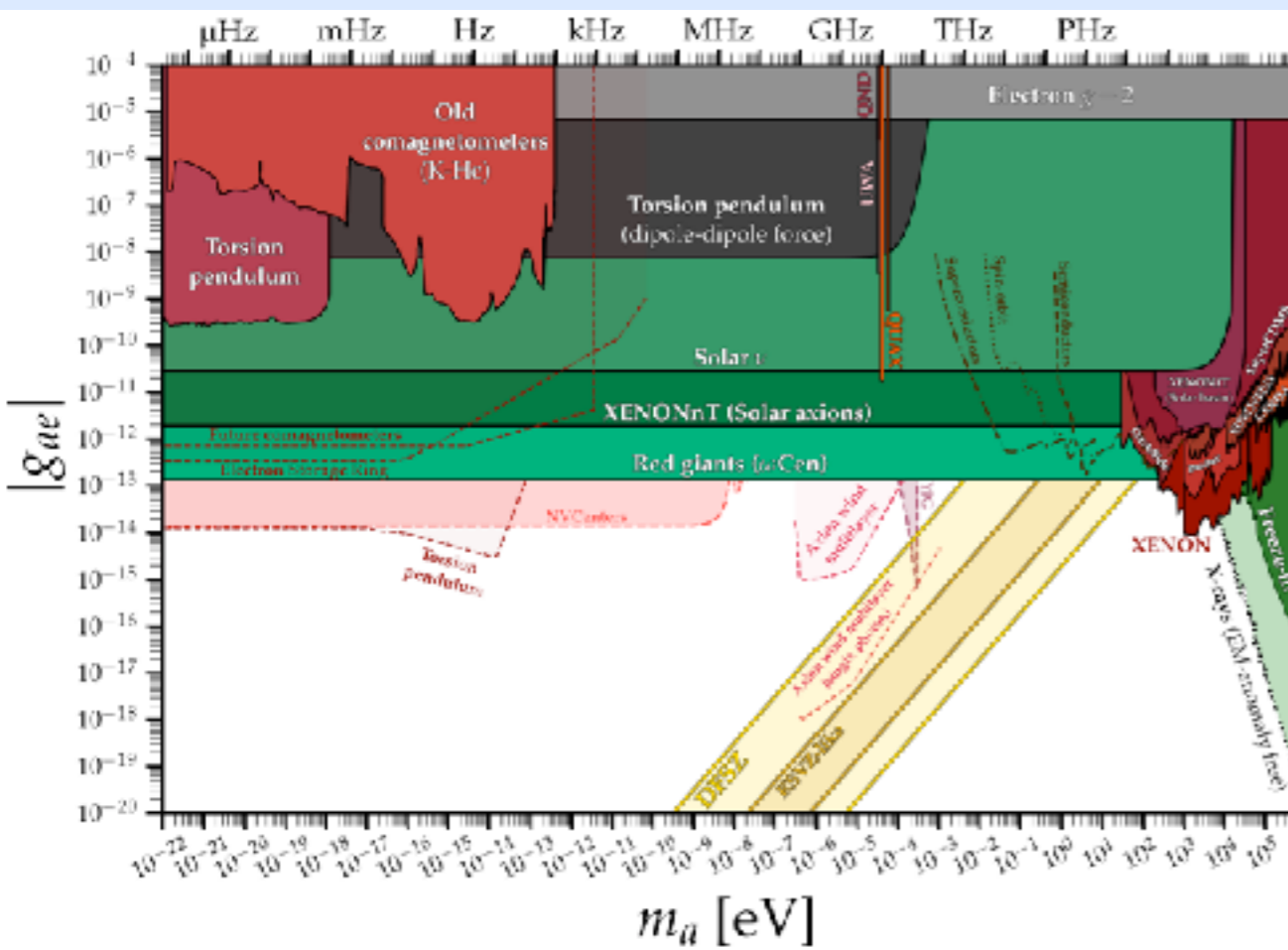
Naive answer:

NO!

$$S_z(t \rightarrow \infty) \propto 1 - \frac{b_{\perp, \text{ALP}}^2 \Gamma}{((m_a - \omega_{\text{res}})^2 + \Gamma^2) \Gamma_L}$$

Second order in the couplings!

Should we try to measure ALPs?



Spin Shot Noise

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At zero temperature, under $\vec{B} = B_z \hat{z}$ (and no axions):

$$\langle \vec{S}(t) \rangle = \frac{N_{\text{spins}} \hat{z}}{2}$$

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This does not exist when measuring S_z ! No Spin Shot Noise*

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Spin Shot Noise as an Observable

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Number of spins, usually one wants this to be big, but here it's not clear

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(Some) Additional Points of Note

- Due to the lack of resonance at the measured signal frequency, one can add a secondary spin/EM amplifier.
- Due to the quantum nature, measuring EMF ($\propto d\mathbf{B}/dt \sim \Gamma_1\mathbf{B}$) can greatly enhance signal (and noise).
- Due to finite B_z stability, a gradiometer is necessary*.
- The “naive observable” isn’t as bad as it seems (given a floquet)
- Many challenges for actual implementation but also many possibilities!

Conclusions

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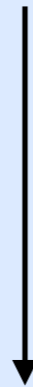
Conclusions

- The use of spin-based sensors to search for DM has bloomed and expanded in the last few years.
- Existing technologies can already enhance the current capabilities, but...
- With creativity, one can think of new ideas, with many promising directions!

DUCK-matter



(Degree in beakness school)



Thanks for listening!

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