



Taus at ATLAS

Davis

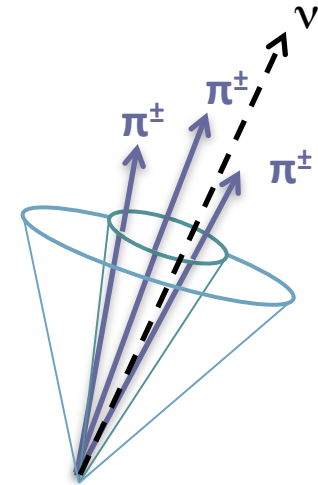
Thursday, April 7, 2011

Sarah Demers

Yale University

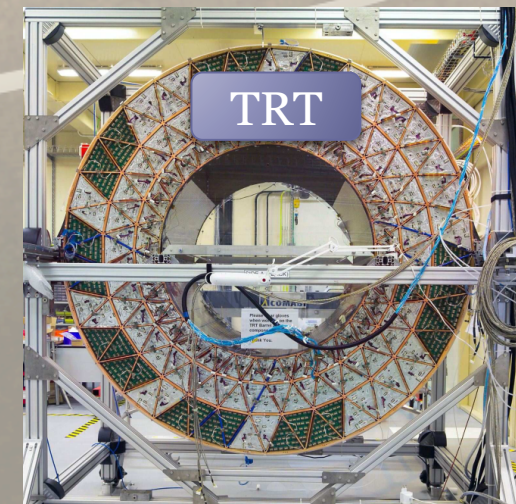
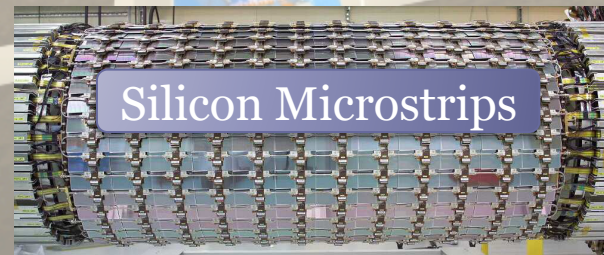
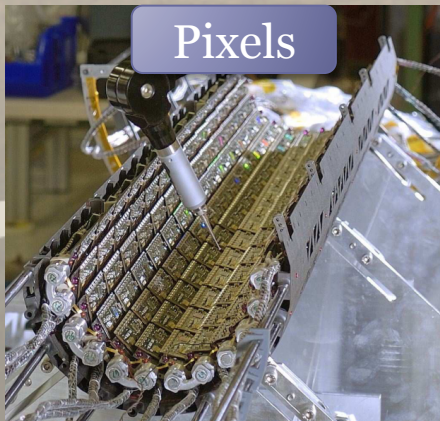
Outline

- ***BREIF ATLAS* Introduction**
- Taus at ATLAS
 - Reconstruction/Identification
 - Trigger
- Channels
 - $W \rightarrow \tau \nu$
 - $Z \rightarrow \tau \tau$
 - $H^+ \rightarrow \tau \nu$
 - $H \rightarrow \tau \tau$
- Long-term outlook



The ATLAS Detector at CERN's LHC

- **Tracking detectors** for momentum and charge (and in the case of the TRT) particle ID
- Sampling Calorimeters
- Trigger and Data Acquisition

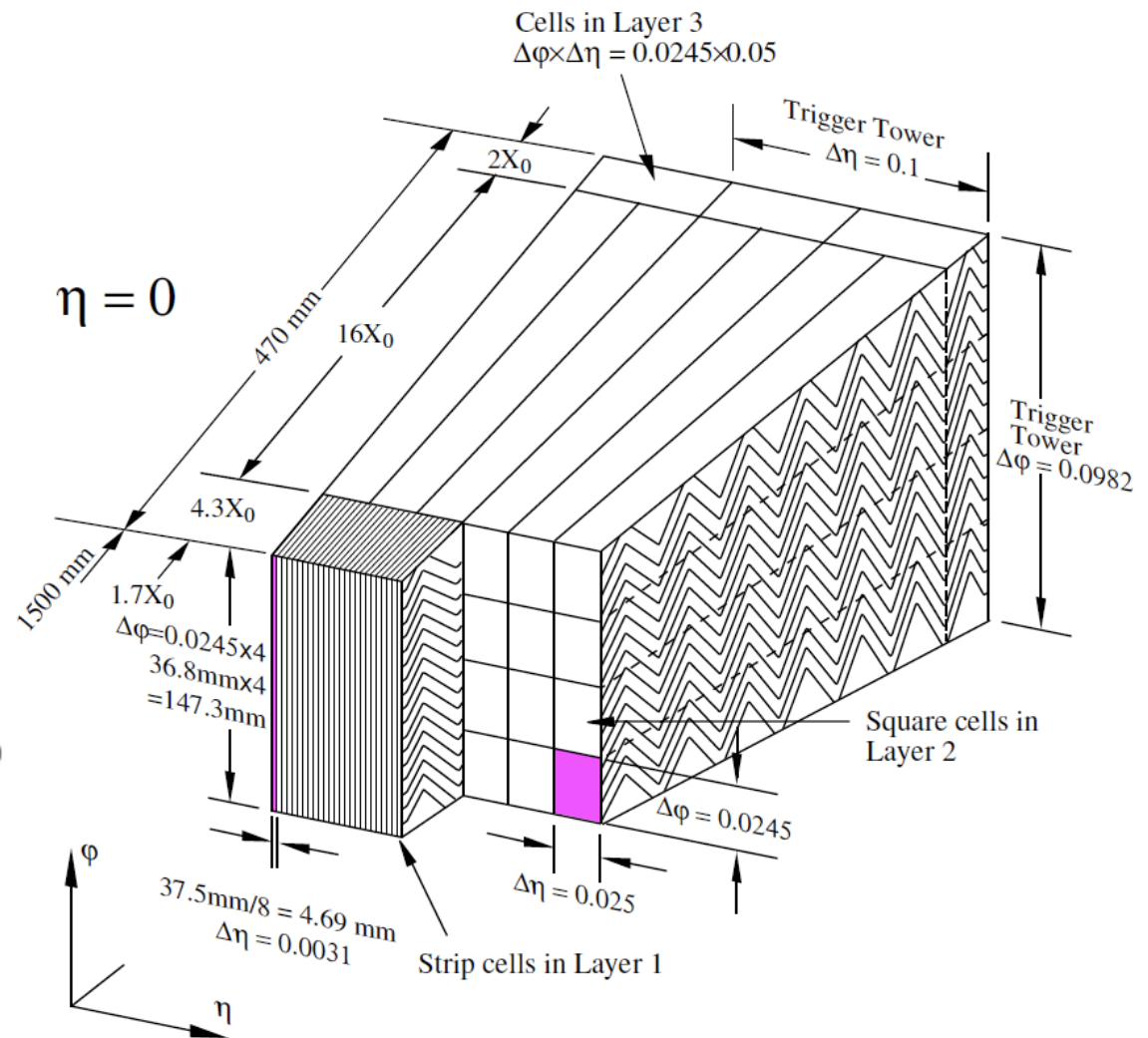
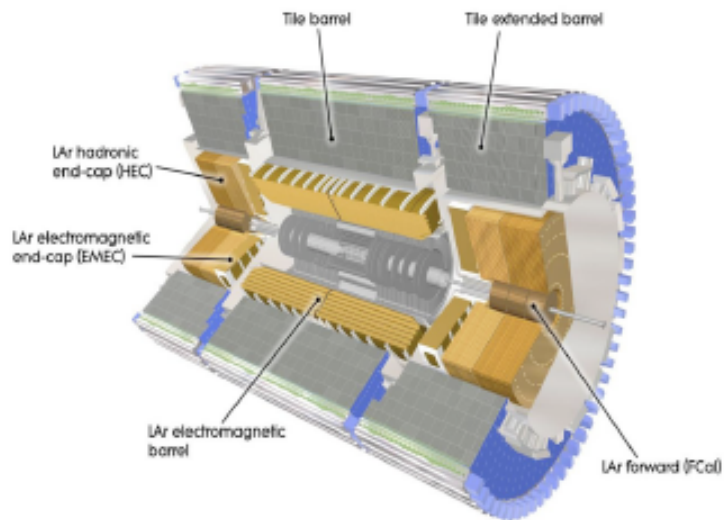


The ATLAS Detector at CERN's LHC

- Tracking detectors
- **Sampling Calorimeters** for energy deposits with fine granularity for shape discrimination
- Trigger and Data Acquisition

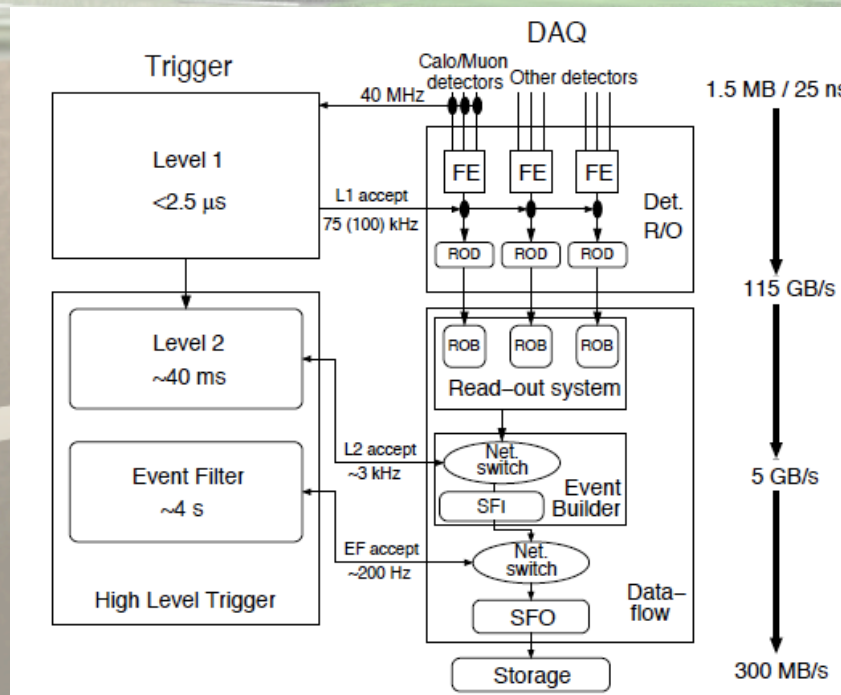


Calorimeters

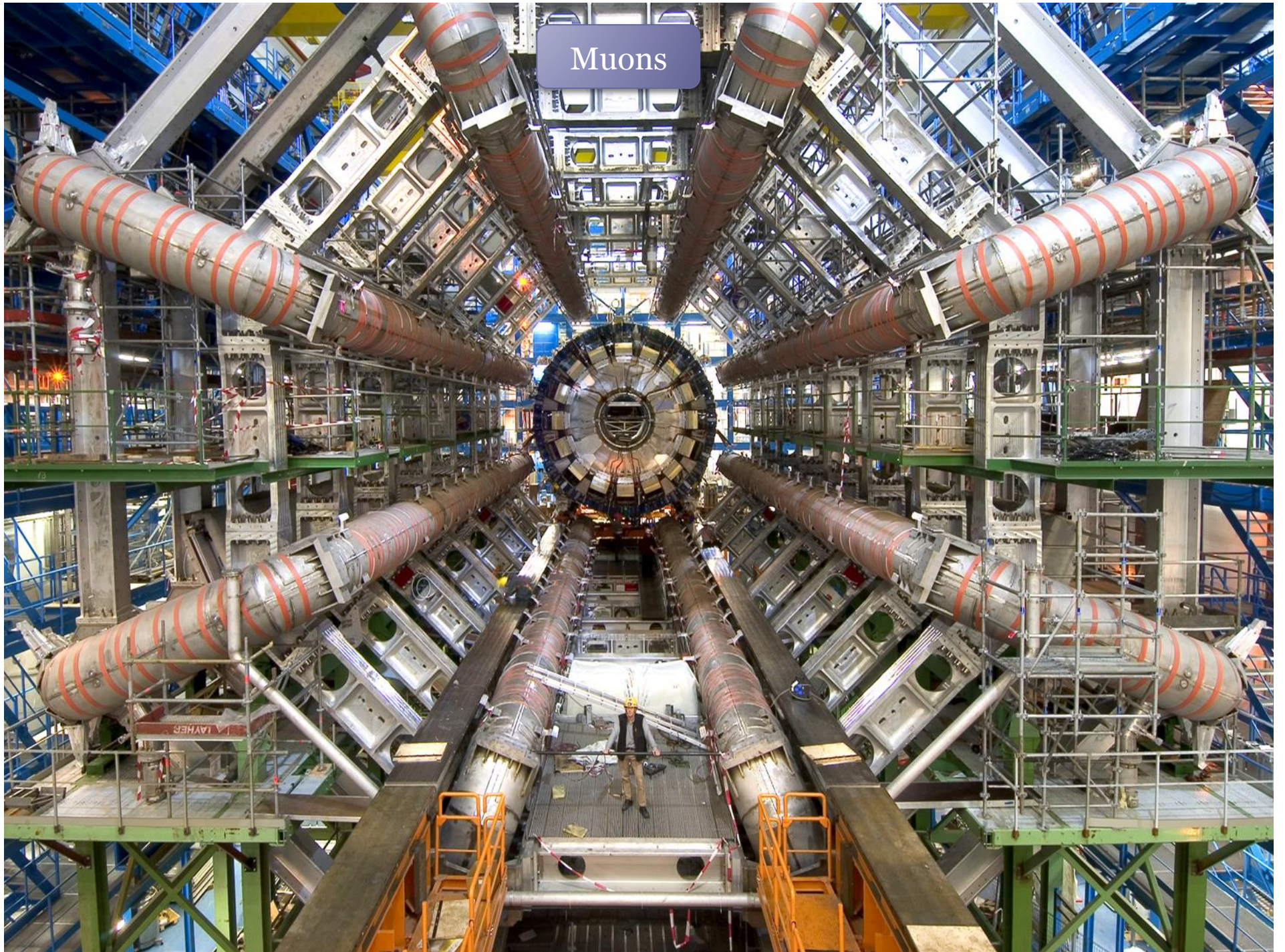


The ATLAS Detector at CERN's LHC

Trigger and Data Acquisition capable of handling 40 MHz interaction rate and writing out events at a rate of $O(100 \text{ Hz})$

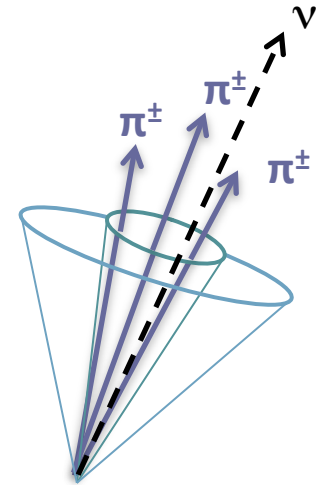


Muons

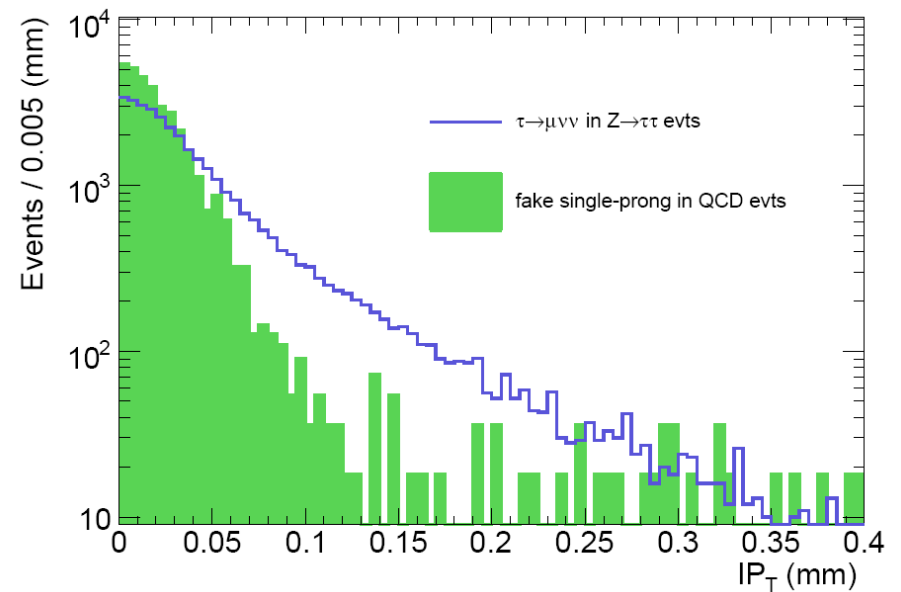
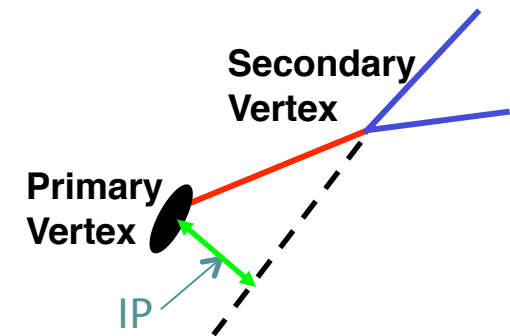
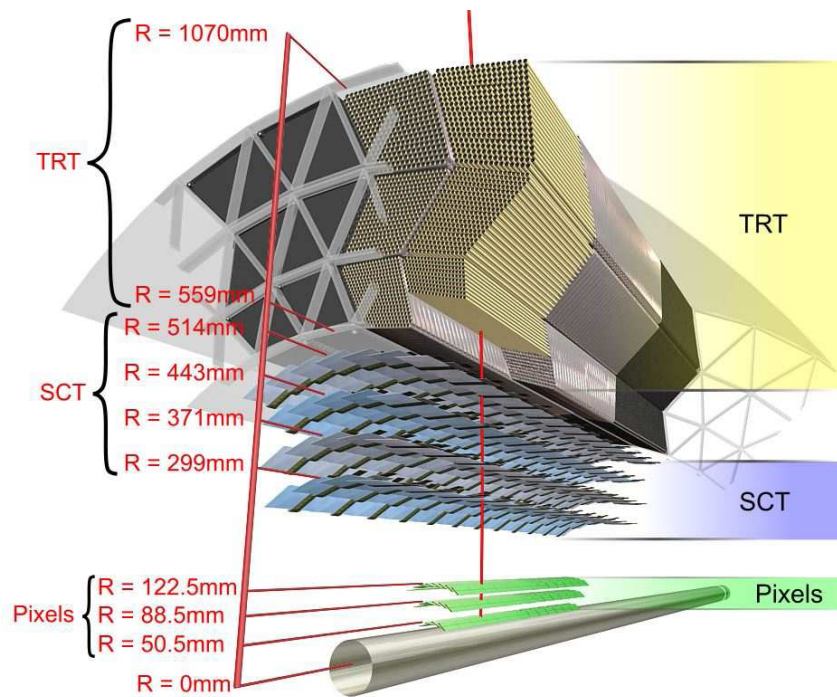


Outline

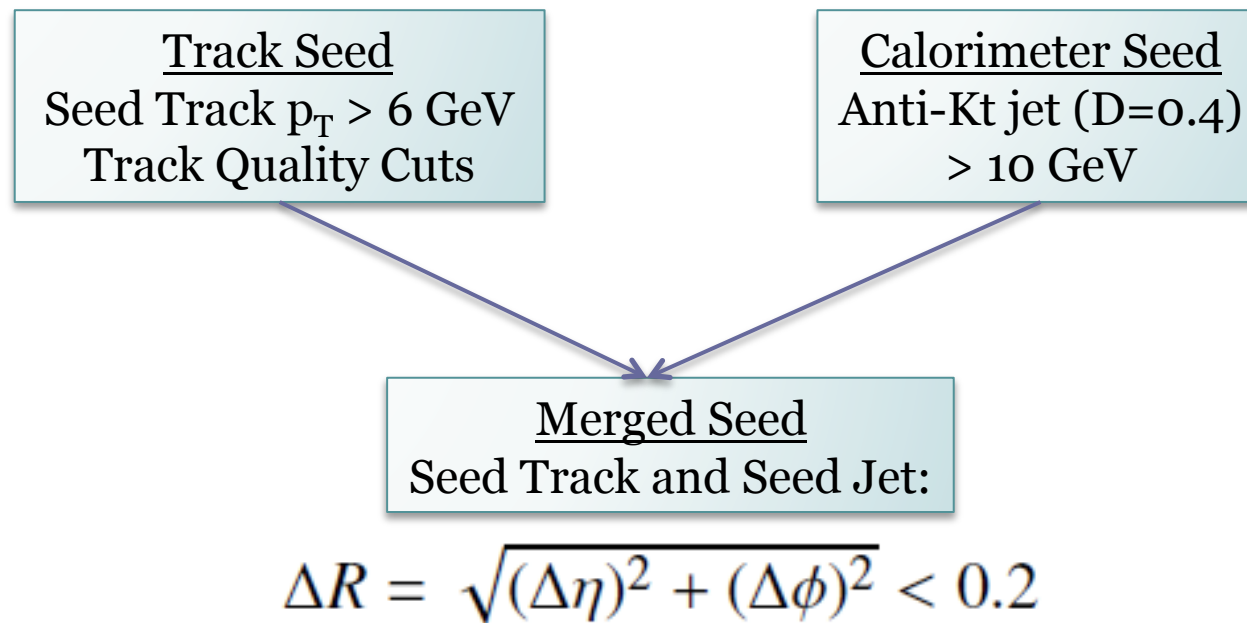
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Using Impact Parameter



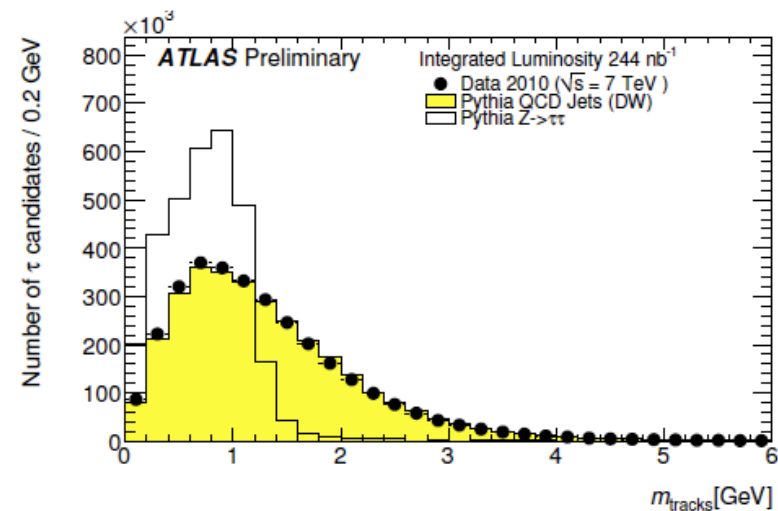
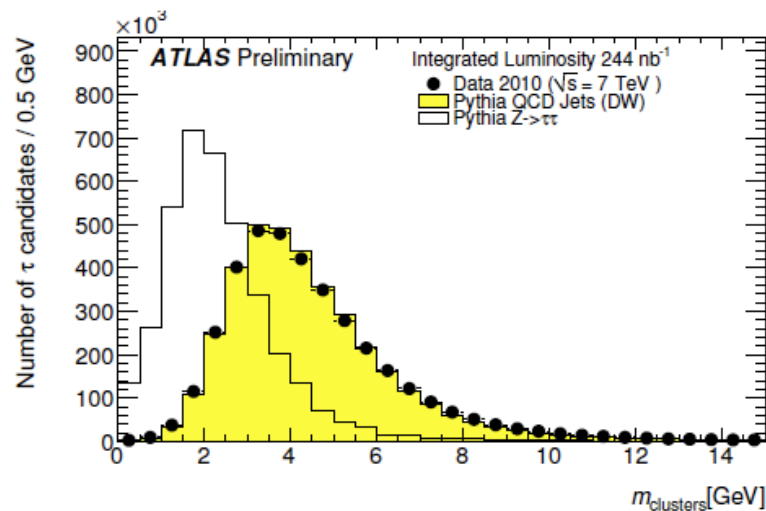
Tau Reconstruction



Tau Identification Variables (I)

- m_{cluster}
 - Invariant Mass from associated topoclusters

- m_{tracks}
 - Invariant Mass of track system

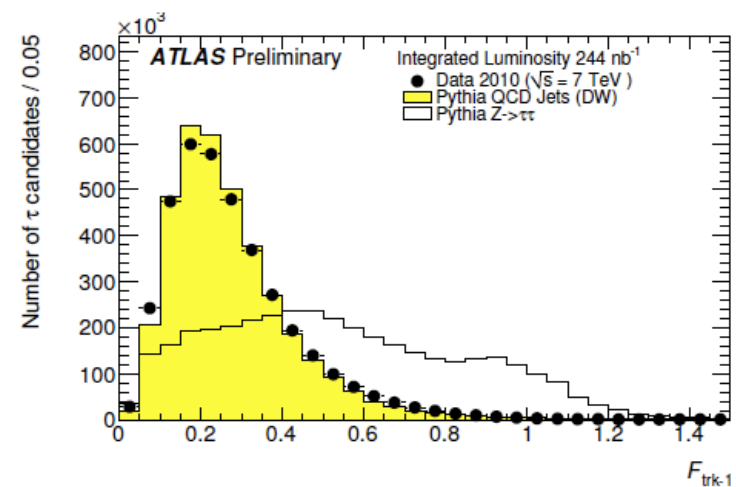
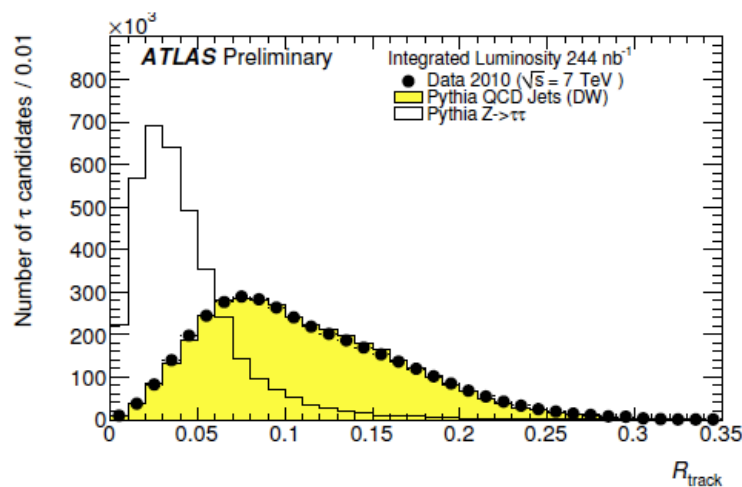


Tau Identification Variables (II)

- R_{track}
 - p_T weighted track width

$$R_{\text{track}} = \frac{\sum_i^{\Delta R_i < 0.2} p_{T,i} \Delta R_i}{\sum_i^{\Delta R_i < 0.2} p_{T,i}}$$

- $F_{\text{trk},l}$
 - Lead track p_T divided by total tau p_T



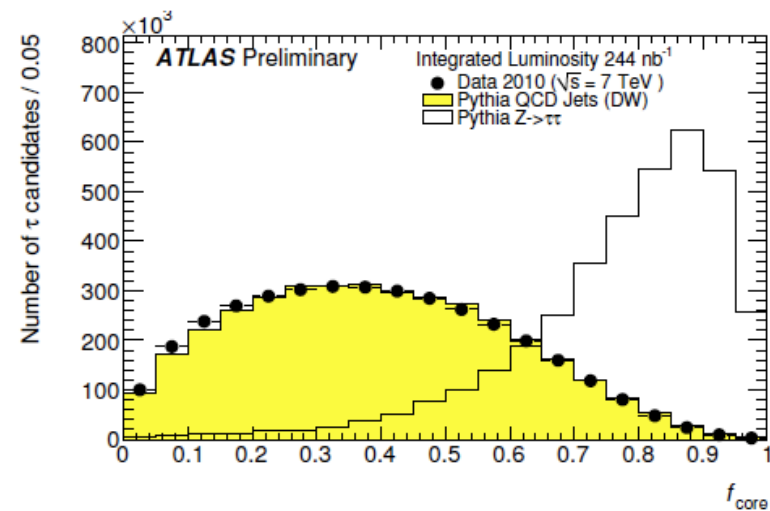
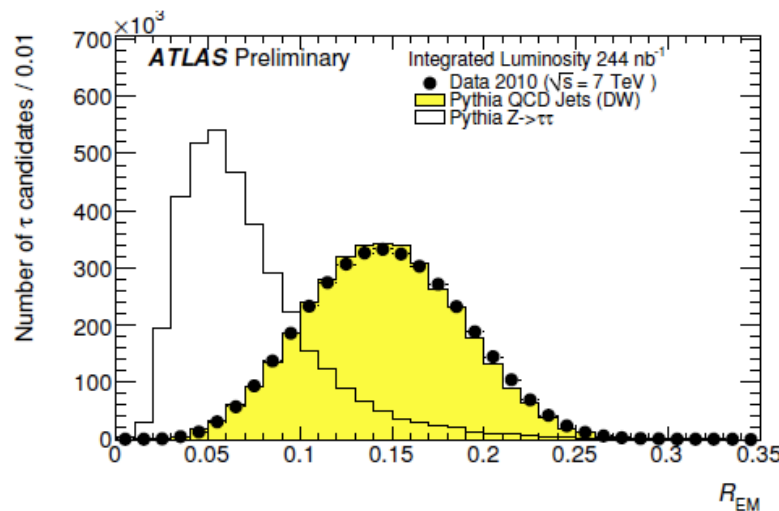
Tau Identification Variables (III)

- R_{EM}
 - Transverse energy weighted width
 - “i” runs over cells in three EM calorimeter layers

$$R_{EM} = \frac{\sum_i^{\Delta R_i < 0.4} E_{T,i}^{EM} \Delta R_i}{\sum_i^{\Delta R_i < 0.4} E_{T,i}^{EM}}$$

- F_{core}
 - Fraction E_T in core region

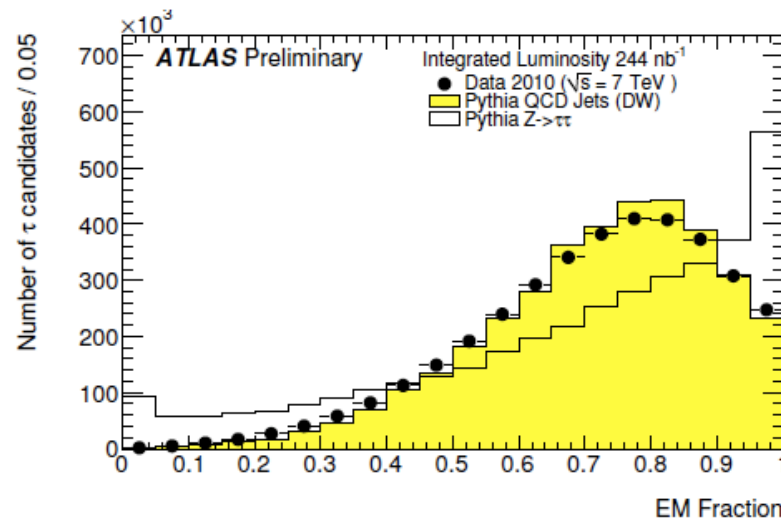
$$f_{core} = \frac{\sum_i^{\Delta R < 0.1} E_{T,i}}{\sum_i^{\Delta R < 0.4} E_{T,i}}$$



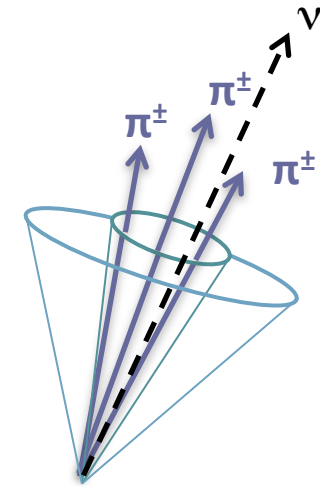
Tau Identification Variables (IV)

- f_{EM}
 - Fraction of energy deposited in the electromagnetic calorimeter
 - “i” runs over cells in EM Cal
 - “j” runs over cells in EM + HAD

$$f_{EM} = \frac{\sum_i^{\Delta R_i < 0.4} E_{T,i}^{GCW}}{\sum_j^{\Delta R_i < 0.4} E_{T,j}^{GCW}}$$



2010 Tau Identification



Cut-Based

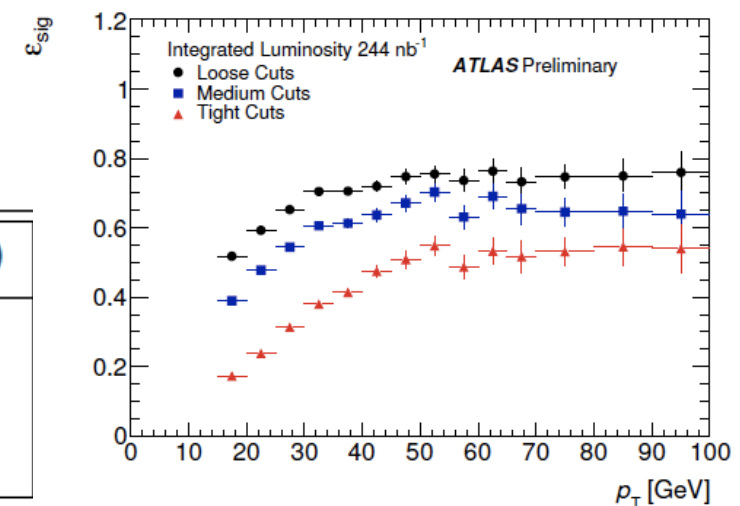
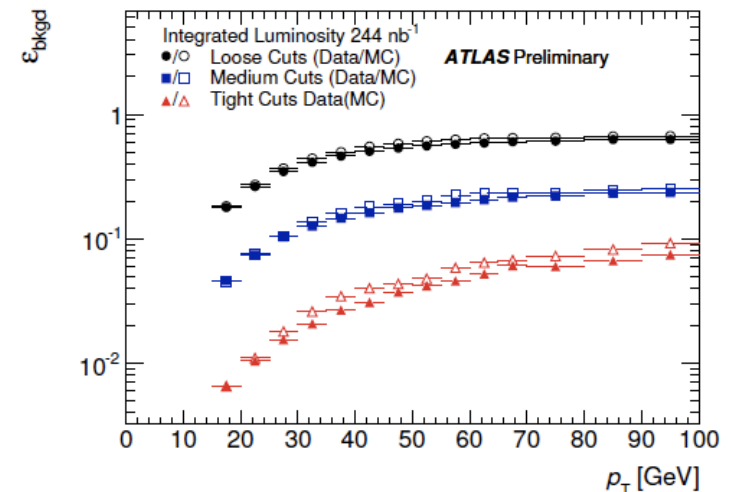
Likelihood

Boosted Decision Tree

Tau Identification: Cut-Based

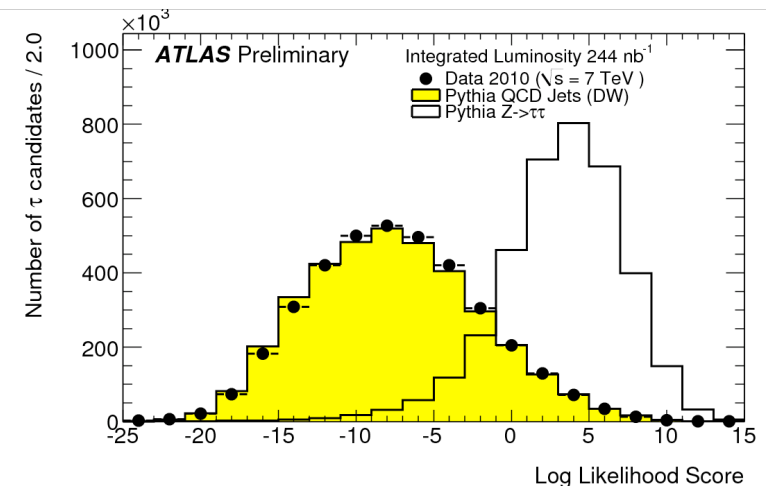
- Use three fairly uncorrelated variables
 - R_{EM} , R_{track} , $f_{trk,1}$
- Three levels
 - Loose: 60% efficiency
 - Medium: 50% efficiency
 - Tight: 30 % efficiency

| Selection | ε_{bkgd} (data) | ε_{bkgd} (MC) |
|-----------|--------------------------------|---------------------------|
| loose | $(3.2 \pm 0.2) \times 10^{-1}$ | 3.4×10^{-1} |
| medium | $(9.5 \pm 1.0) \times 10^{-2}$ | 9.9×10^{-2} |
| tight | $(1.6 \pm 0.3) \times 10^{-2}$ | 1.9×10^{-2} |



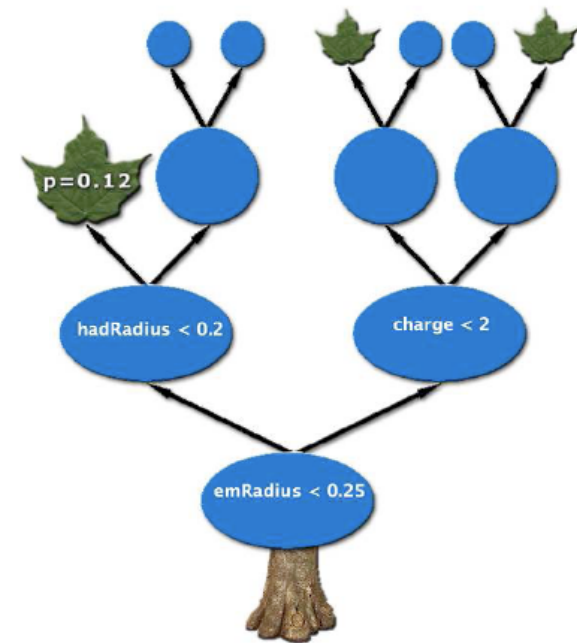
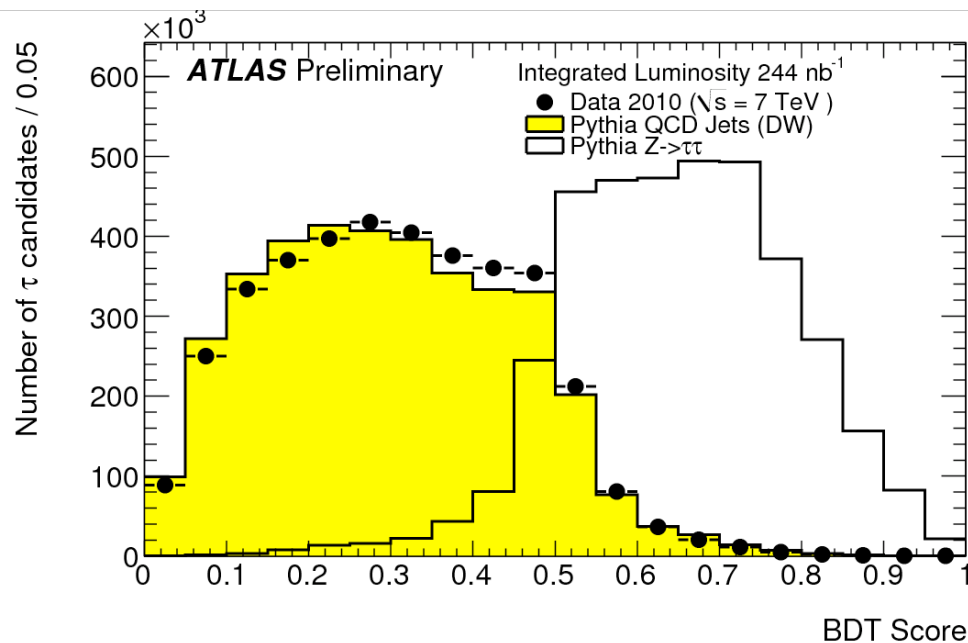
Tau Identification: Log Likelihood

- Uses six of the seven variables:
 - m_{cluster} , m_{track} , R_{track} , $f_{\text{trk,l}}$, R_{EM} , f_{EM}
- F_{core} was not used due to its high correlation with the other variables
- Training done in six p_T bins



Tau Identification: Boosted Decision Tree

- Uses all seven ID variables:
 - m_{cluster} , m_{track} , R_{track} , $f_{\text{trk,l}}$, R_{EM} , f_{core} , f_{EM}



Thanks to J. Godfrey for image!

Performance Comparison

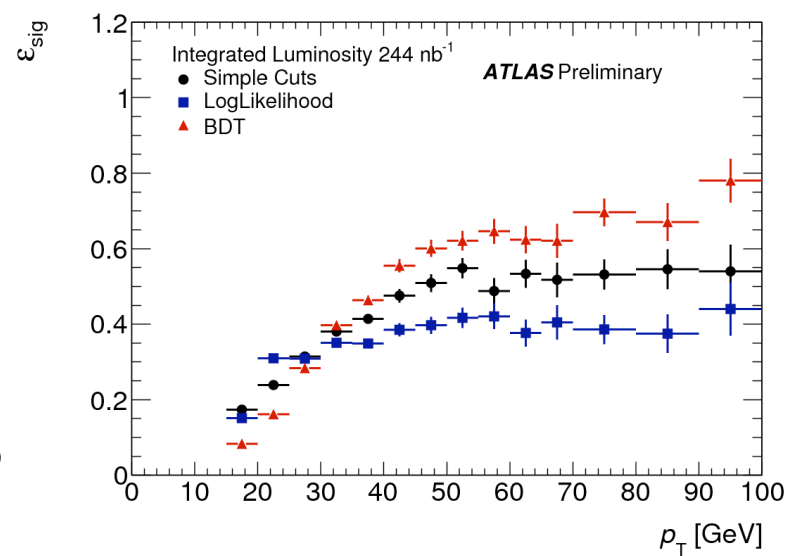
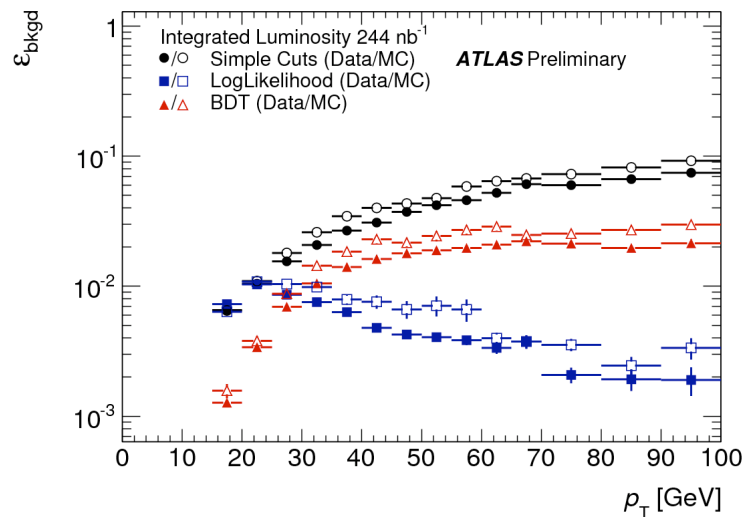
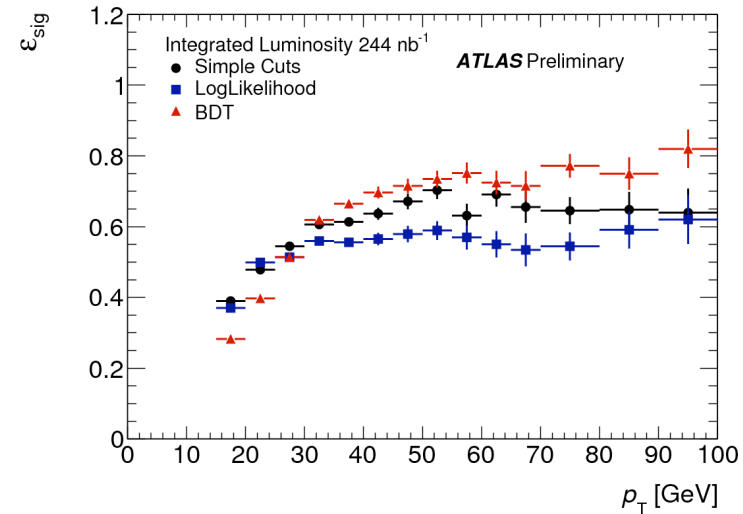
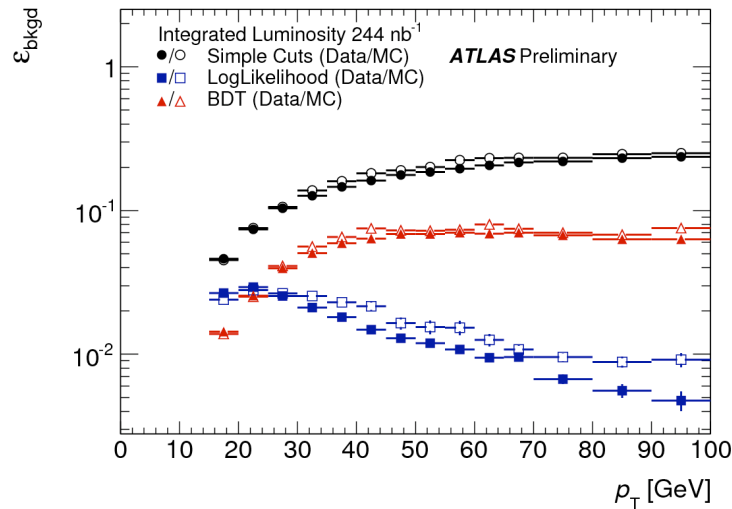
Simple Cut

LL

BDT

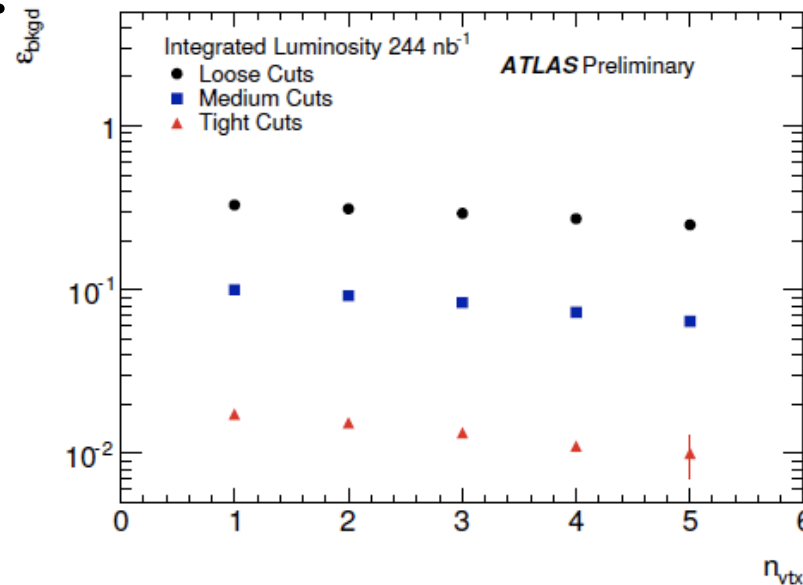
Medium Selection

Tight Selection



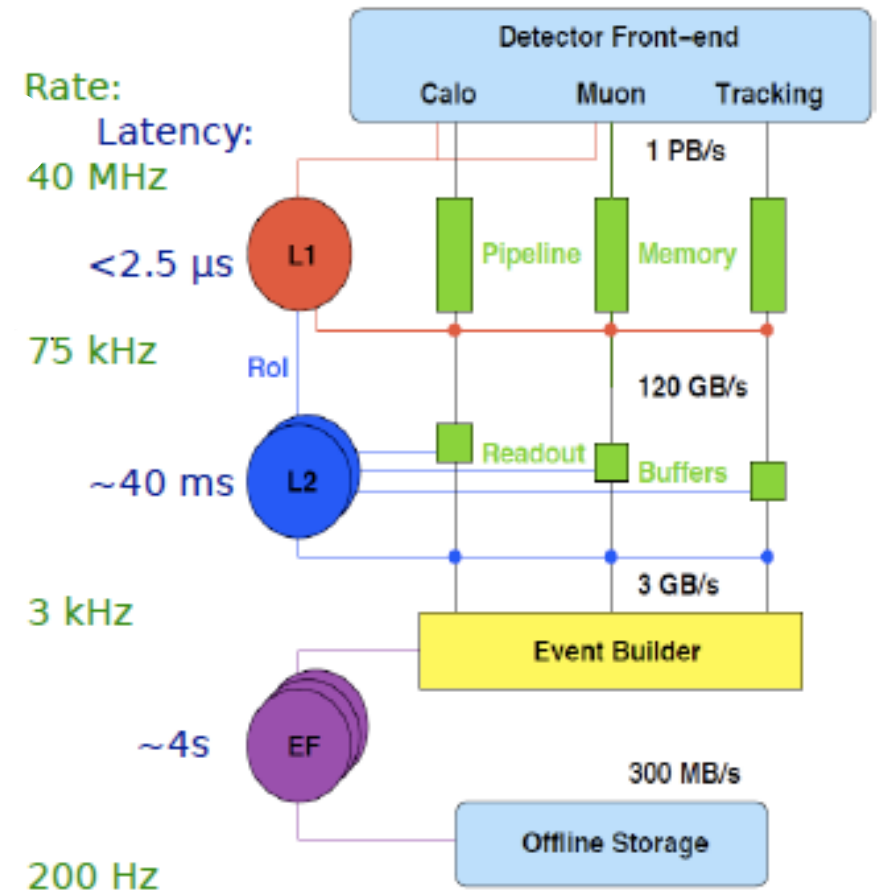
Tau Identification: Future

- Some of the variables relied upon by the 2010 data are sensitive to pile-up so a re-optimization needs to be done as we move from a few pile-up events to ten.

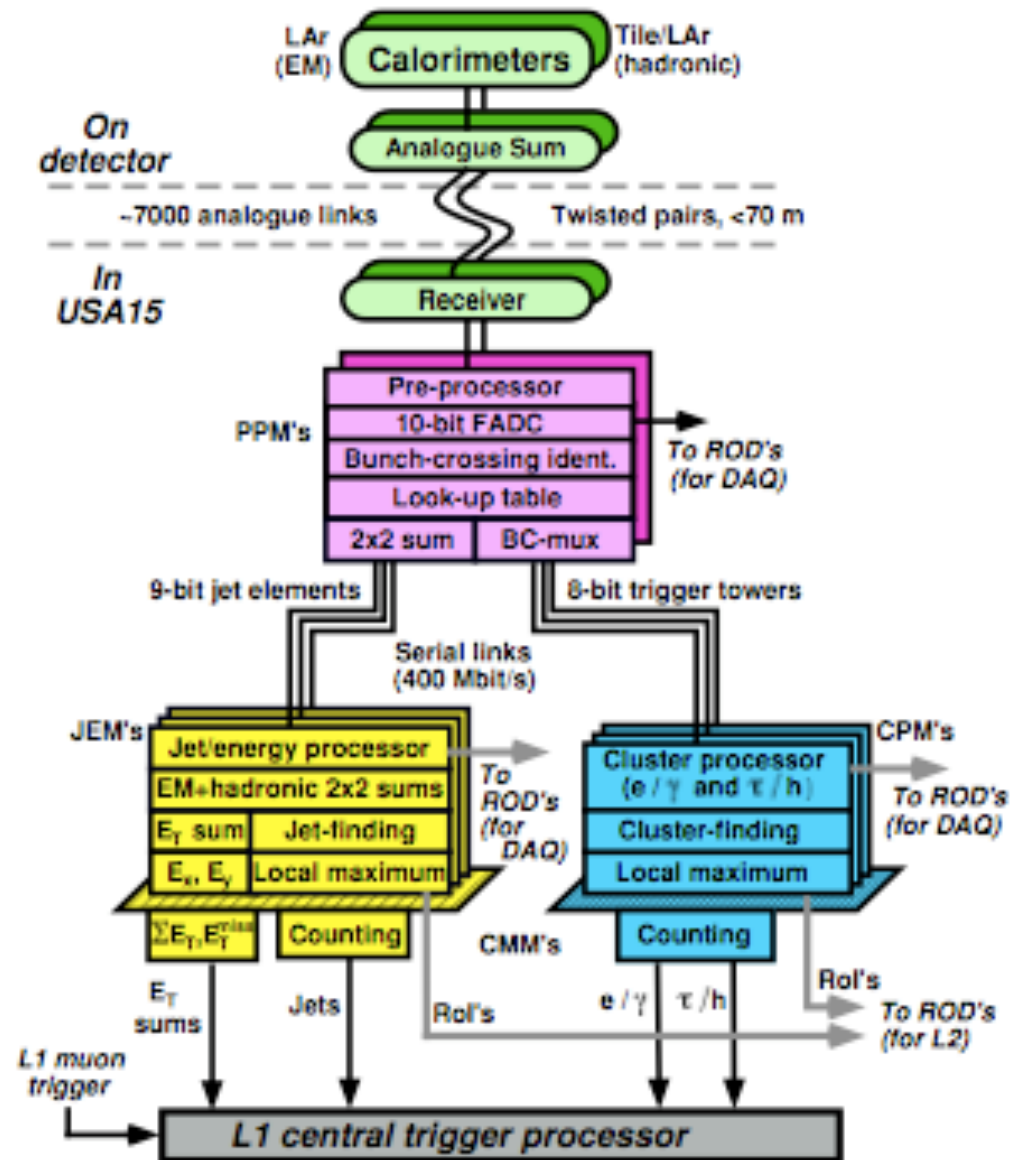


Tau Trigger

- Level 1
 - Hardware calorimeter trigger
 - Limited number of thresholds available
 - Tau energy + eta/phi passed to Level 2 (RoI)
- Level 2
 - Unpacks only the Region of Interest
 - Track and calorimeter variables
- Event Filter
 - Access to full event, but only uses tau RoI
 - Selection similar to offline is available

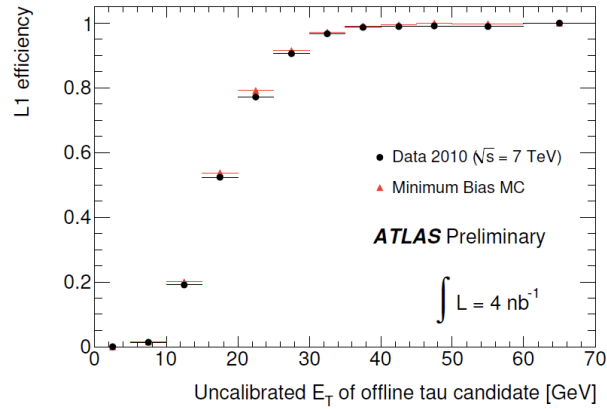


Level 1 Calo Trigger

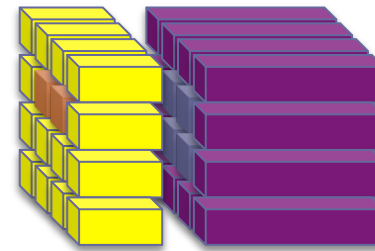


Level 1 Tau Trigger

5 GeV L1 Tau Trigger



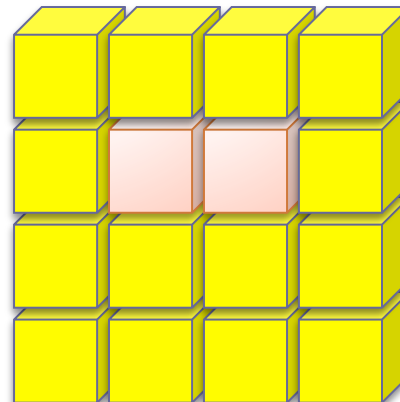
EM
Trigger Towers



HAD
Trigger Towers

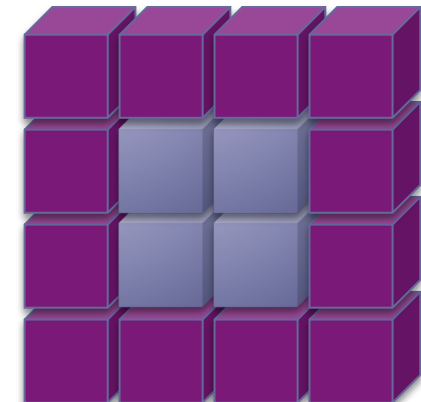
Threshold
Calculation

=



2 Adjacent EM
Trigger Towers

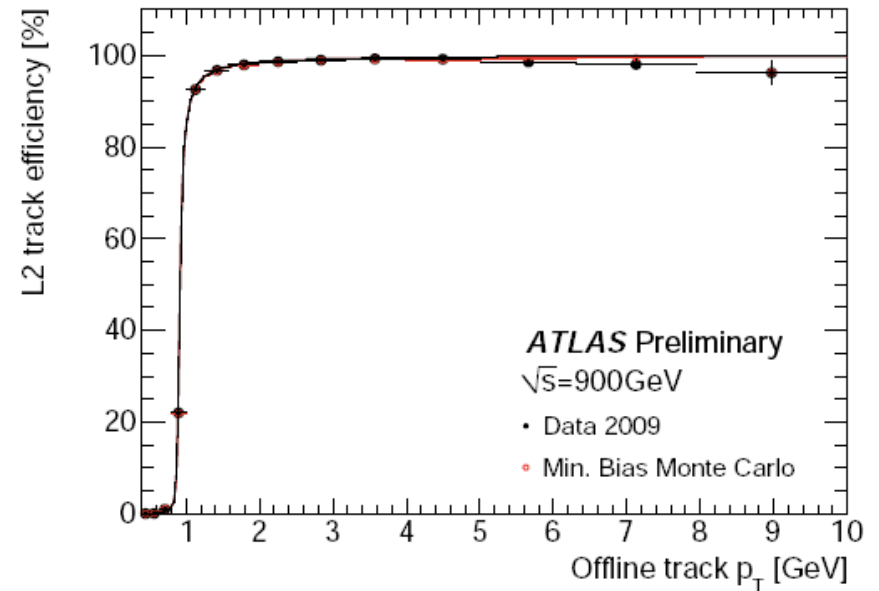
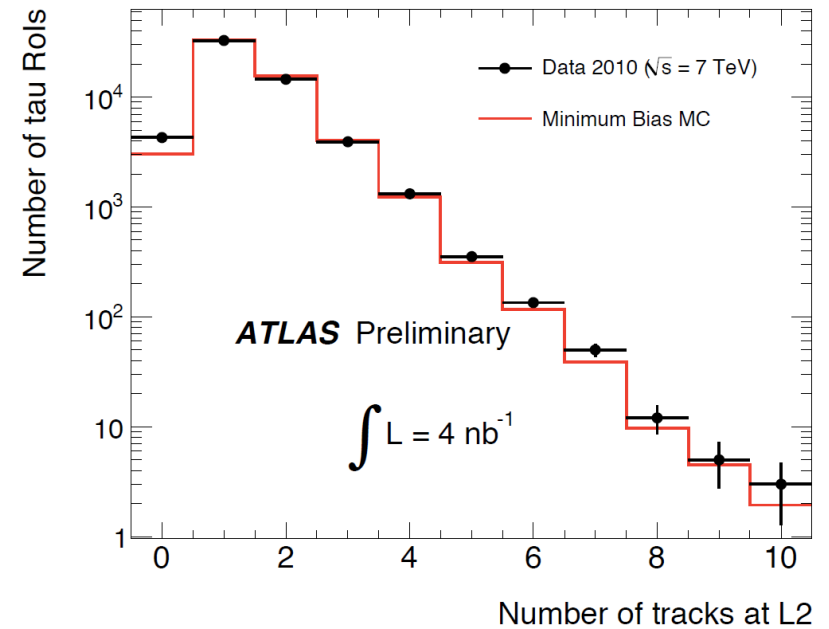
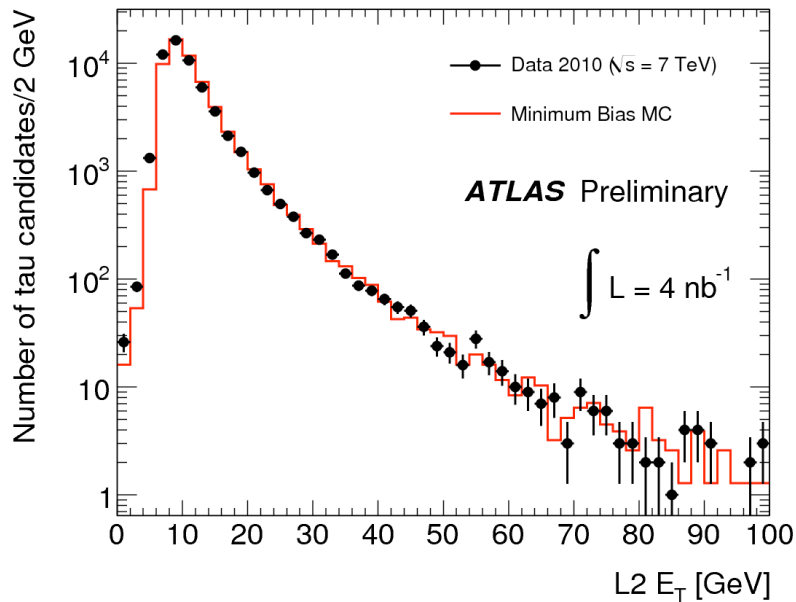
+



2x2 HAD Towers
behind them

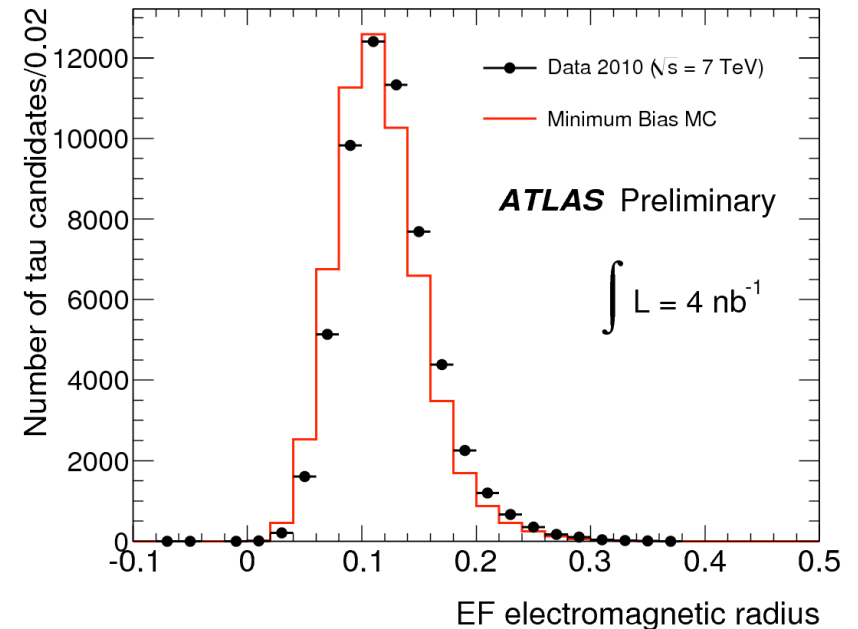
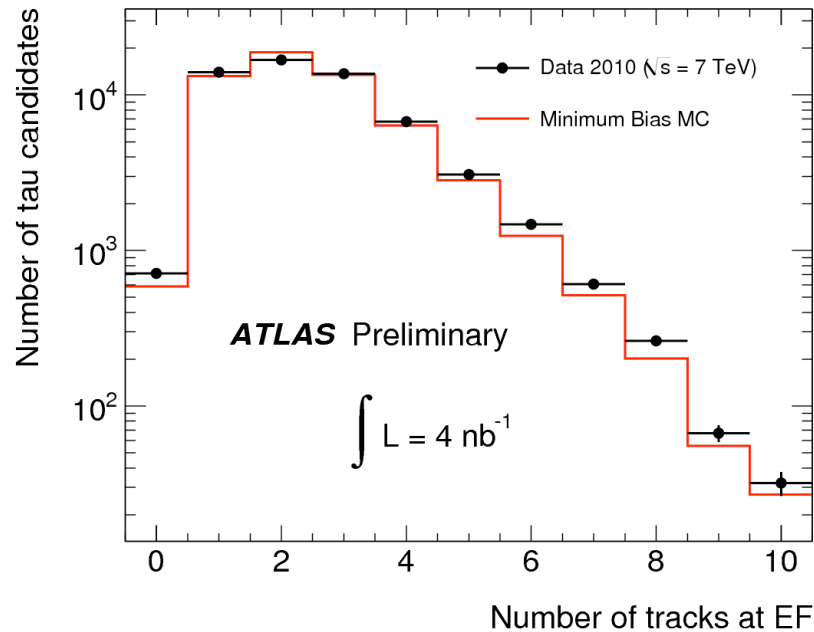
Level2 Trigger

- Only access to small fraction of data is available (a few percent) via L1 tau region of interest (RoI)
- Access to full calorimeter granularity is available

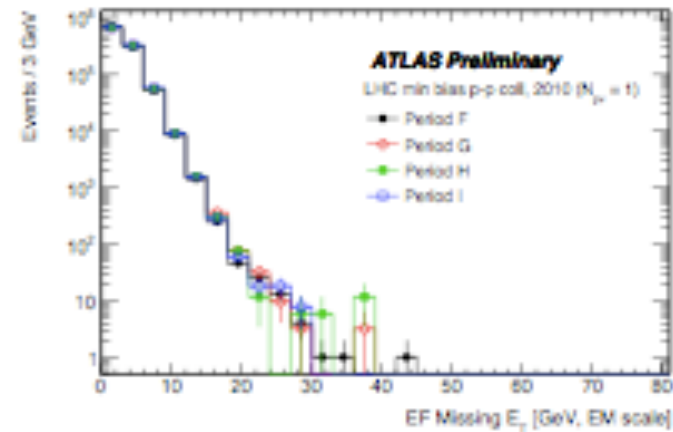
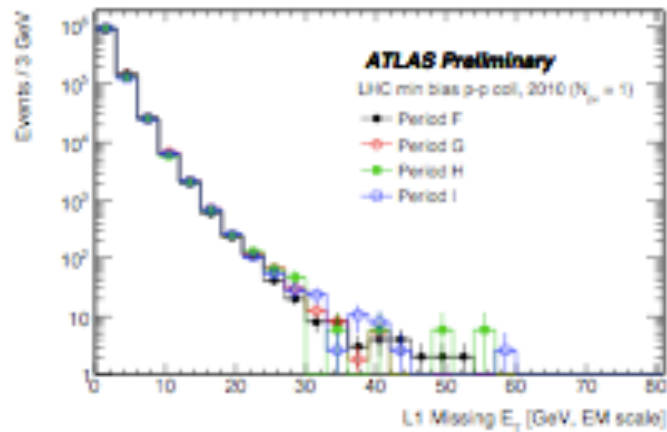


Event Filter (3rd Level Trigger)

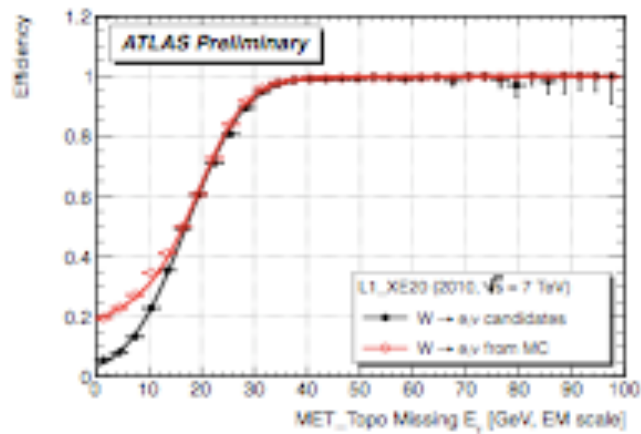
- EF has around 4 seconds per event
- R_{EM} comparison shown below with old MC tune



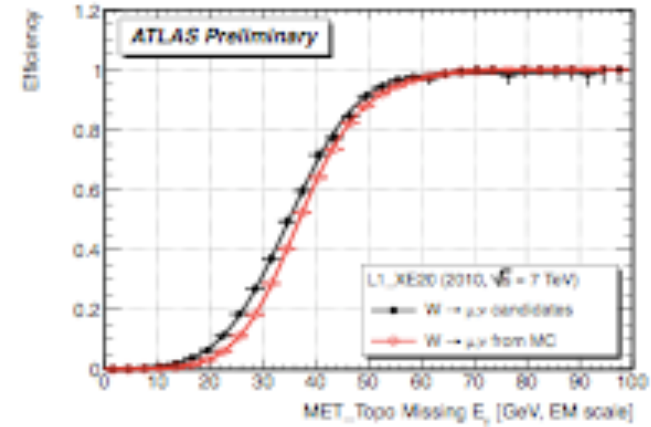
Level 1 Hardware Trigger: Missing E_T



20 GeV Threshold
Efficiency from $W \rightarrow e\nu$ events

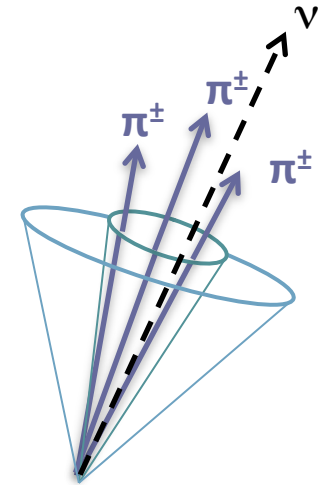


20 GeV Threshold
Efficiency from $W \rightarrow \mu\nu$ events



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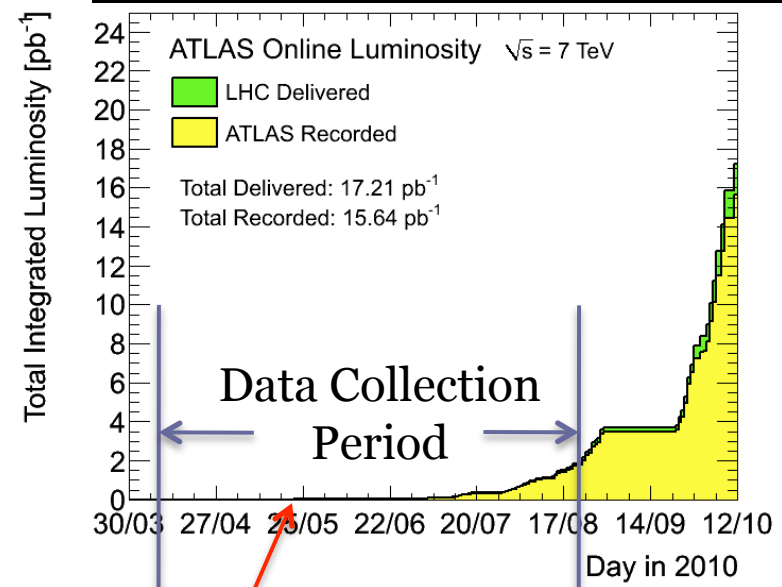
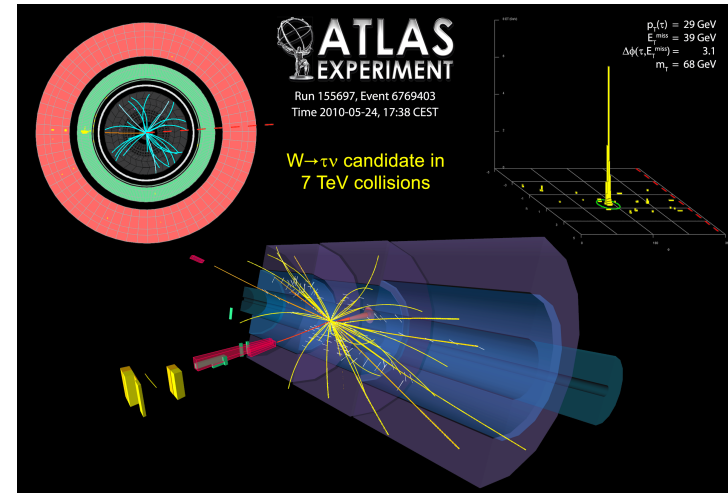


A Few Tau Channels

- $W^- \rightarrow \tau \nu$
 - Exercise the trigger and early tau ID
- $Z \rightarrow \tau \tau$
 - Important benchmark channel
 - Practice for the SM Higgs?
 - Use for efficiency calculations
- $H^+ \rightarrow \tau \nu$
 - Hadronic tau decay mode
- MSSM $H^- \rightarrow \tau \tau$
 - One hadronic, one leptonic tau decay

$W \rightarrow \tau \nu$

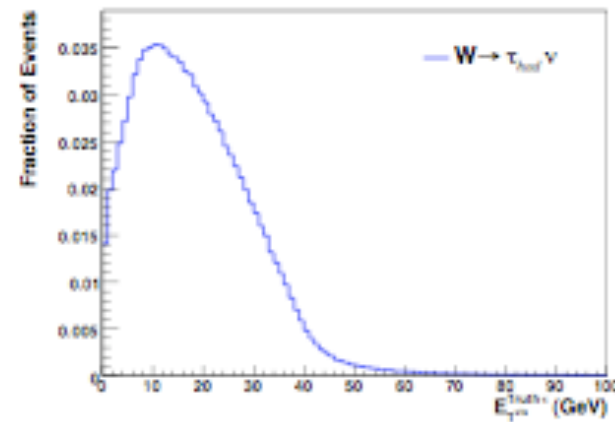
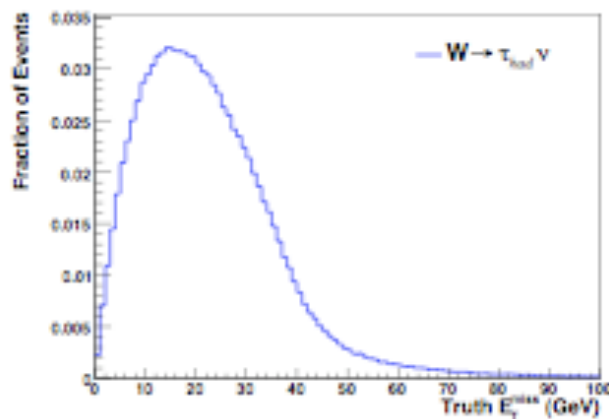
- W - $\tau \nu$ Observation approved by ATLAS Collaboration: Nov 2010
- Dataset: 546 nb⁻¹
- 78 events with excellent signal/background ratio



First $W \rightarrow \tau \nu$ candidate event
May 24, 2010

$W \rightarrow \tau \nu$

- $W \rightarrow \tau \nu$ production cross section at 7 TeV at NNLO is 10.46 nb
 - About ten times higher than the $Z \rightarrow \tau \tau$ production
 - Orders of magnitude lower than QCD di-jet production



Relevant Analysis Cuts: Missing $E_T > 30$ GeV
tau p_T between 20 and 60 GeV

$W \rightarrow \tau \nu$: Trigger

- There are only two objects in these events that we can use to control the trigger rate:
 - Missing transverse energy
 - Tau transverse energy
- Neither provide dramatic enough rate reduction, so the two need to be used in combination
- Keeping the rate low and measuring the trigger efficiency at the end of the day is challenging!
 - Particularly tricky: correlations between objects

>99% efficient after offline selection

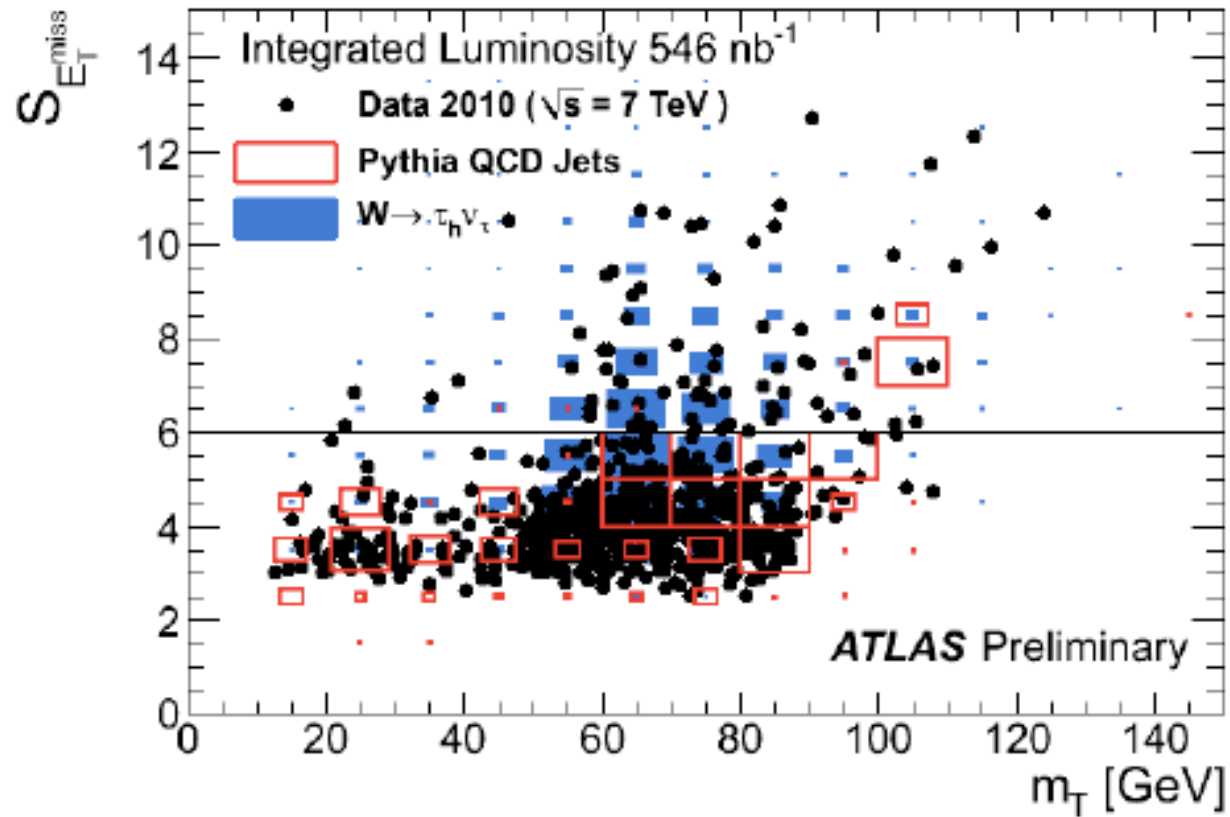
| Object | Cut |
|----------------|--------|
| L1 Missing ET | 5 GeV |
| L1 Tau | 5 GeV |
| L2 Missing ET | 5 GeV |
| L2 Tau (track) | 6 GeV |
| EF Missing ET | 15 GeV |
| EF Tau | - |

W- \rightarrow $\tau\nu$: Offline Selection

- Tight Cut-based tau ID (30% efficient)
- Good data quality and cleaning cuts including
 - Primary vertex w/ 4 tracks $p_T > 100$ MeV
 - Jets cannot point toward Missing E_T
 - Objects cannot point toward overlap calo region (crack)
- Missing $E_T > 30$ GeV
- 20 GeV $>$ tau candidate > 60 GeV
- Electron veto (loose electrons)
- Muon veto (combined muons)
- Missing ET significance > 6

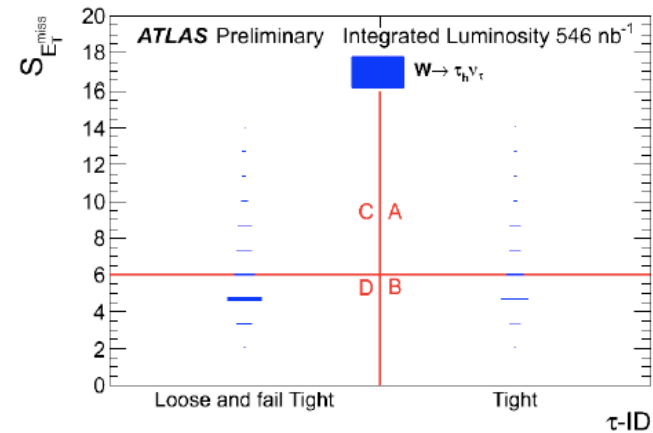
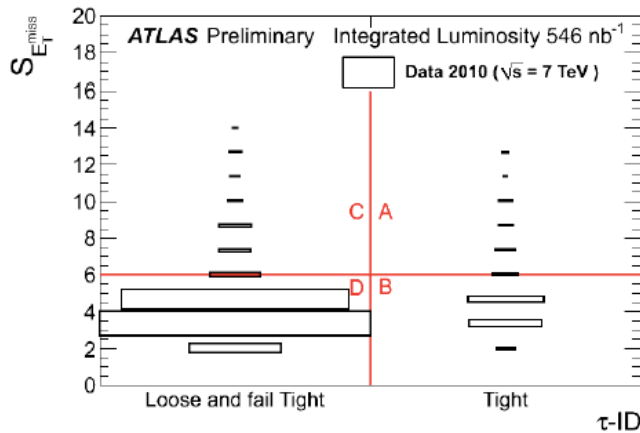
Missing E_T Significance

$$S_{E_T^{\text{miss}}} = \frac{E_T^{\text{miss}}}{0.5 \cdot \sqrt{\sum E_T}}$$



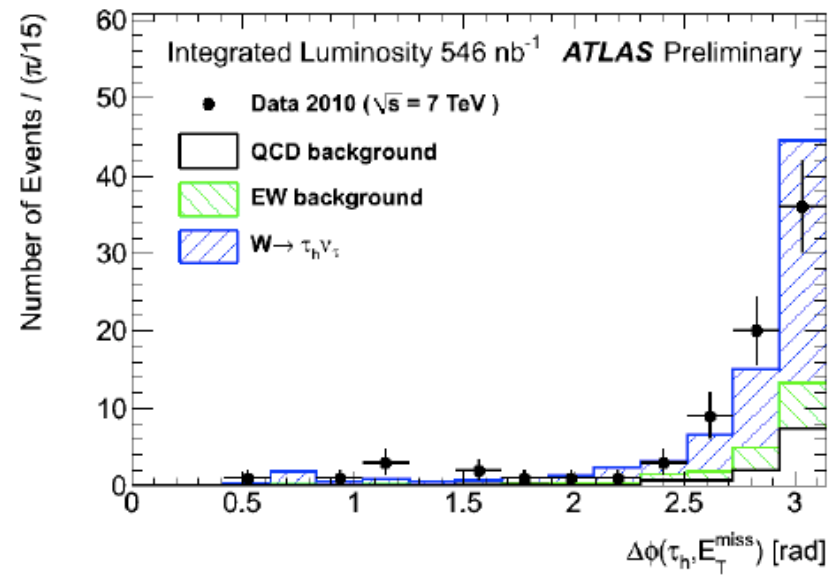
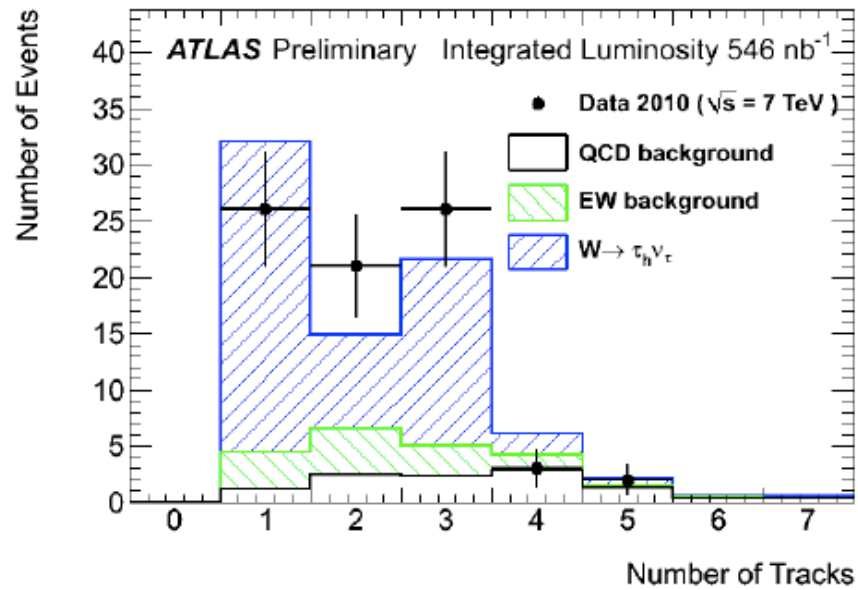
W- $\rightarrow\tau\nu$: Summary

| | Data | $W \rightarrow \tau_h \nu_\tau$ | $W \rightarrow e \nu_e$ | $W \rightarrow \mu \nu_\mu$ | $W \rightarrow \tau_\ell \nu_\tau$ | $Z \rightarrow ee$ | $Z \rightarrow \mu\mu$ | $Z \rightarrow \tau\tau$ |
|------------------------------|--------|---------------------------------|-------------------------|-----------------------------|------------------------------------|--------------------|------------------------|--------------------------|
| Trigger | 986439 | 954.5 ± 5.2 | 3560.7 ± 3.4 | 521.4 ± 1.6 | 296.5 ± 2.8 | 75.3 ± 0.2 | 59.7 ± 0.2 | 115.1 ± 0.7 |
| QCD jets rejection | 415951 | 728.3 ± 4.7 | 2735.3 ± 3.5 | 400.7 ± 1.5 | 229.4 ± 2.6 | 24.5 ± 0.1 | 45.1 ± 0.1 | 71.4 ± 0.6 |
| $E_T^{\text{miss}} > 30$ GeV | 29686 | 411.5 ± 3.8 | 1828.3 ± 3.3 | 317.1 ± 1.3 | 121.9 ± 1.9 | 1.13 ± 0.03 | 34.4 ± 0.1 | 35.4 ± 0.4 |
| τ selection | 2408 | 118.0 ± 2.1 | 1482.0 ± 3.1 | 26.6 ± 0.4 | 34.4 ± 1.0 | 0.59 ± 0.02 | 3.24 ± 0.04 | 11.9 ± 0.3 |
| Lepton rejection | 685 | 94.8 ± 1.9 | 6.7 ± 0.2 | 4.9 ± 0.2 | 2.3 ± 0.3 | < 0.005 | 0.11 ± 0.01 | 4.2 ± 0.2 |
| $S_{E_T^{\text{miss}}} > 6$ | 78 | 55.3 ± 1.4 | 4.2 ± 0.2 | 3.7 ± 0.1 | 1.8 ± 0.2 | | 0.08 ± 0.01 | 2.0 ± 0.1 |



Estimated 11 QCD events in signal region (A)

$W^- \rightarrow \tau \nu$



A Few Tau Channels

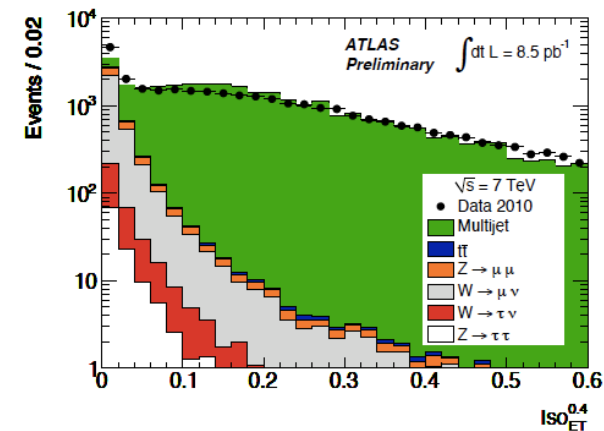
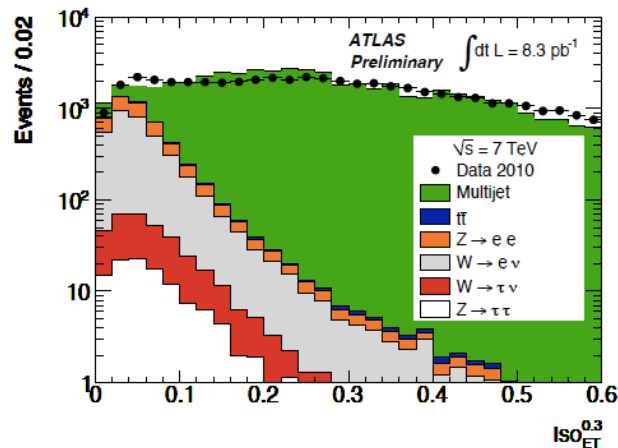
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Z → ττ

Sarah Demers, Yale University Thursday, April 7, 2011

- Electron Channel: 8.3 pb^{-1}
- Trigger: 15 GeV electron (EF)
- Event Selection
 - 15 GeV tight electron
 - Track Isolation
 - Ratio in cone 0.4: < 0.06
 - Calorimeter Isolation
 - Energy in annulus from 0.05 to 0.3 less than 0.1 GeV

- Muon Channel: 8.5 pb^{-1}
- Trigger: 10 GeV muon (EF)
- Event Selection
 - 15 GeV combined muon
 - Track Isolation
 - Ratio in cone 0.4: < 0.06
 - Calorimeter Isolation
 - Energy in annulus from 0.05 to 0.4 less than 0.06 GeV



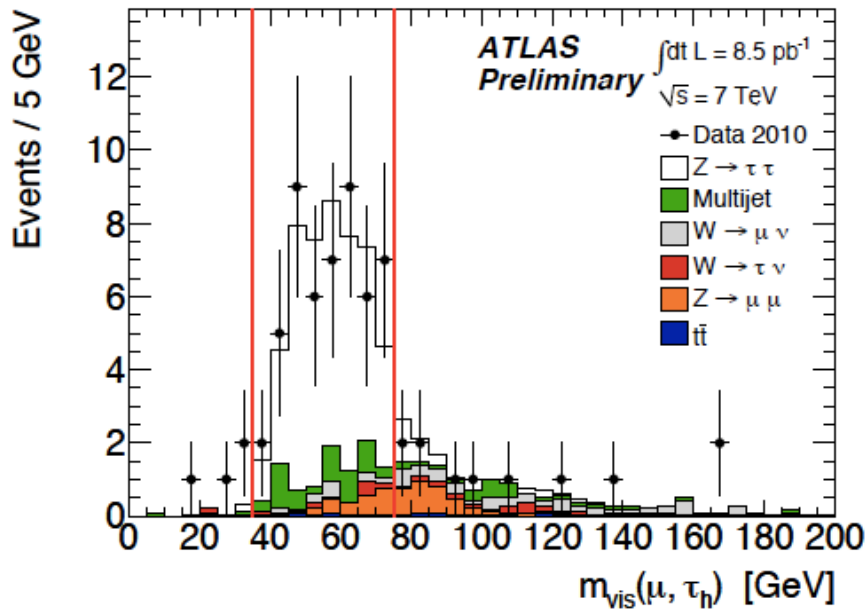
Z- $\rightarrow\tau\tau$: Further event Selection

- Dilepton Veto
- W+jets reduction
- Visible mass between 35 and 75 GeV
- Opposite sign lepton and tau

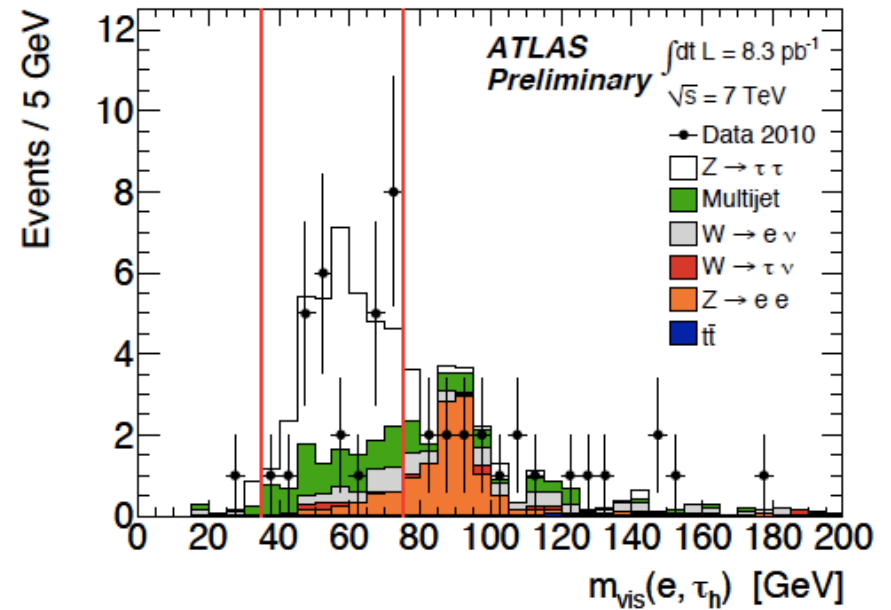
| | Muon Channel (8.5 pb ⁻¹) | Electron Channel (8.3 pb ⁻¹) |
|---|--|--|
| Data (after all selections) | 51 | 29 |
| Total Estimated Background | 9.9 \pm 2.1 | 11.8 \pm 1.7 |
| <i>Estimated Multijet Background</i> | 5.2 \pm 0.7(stat.) \pm 0.7 (syst.) | 6.8 \pm 0.6(stat.) \pm 0.7 (syst.) |
| <i>Estimated W, Z, $t\bar{t}$ Background</i> | 4.7 \pm 0.5(stat.) \pm 1.5(syst.) | 5.0 \pm 0.6 (stat.) \pm 1.4(syst.) |
| Data (after background subtraction) | 41.1 \pm 7.1(stat.) \pm 2.1(bkg. est.) | 17.2 \pm 5.4(stat.) \pm 1.7(bkg. est.) |
| SM Signal Expectation | 39.9 \pm 1.8(stat.) \pm 6.7(syst.) | 24.5 \pm 1.4(stat.) \pm 7.9(syst.) |

Z- $\rightarrow\tau\tau$ Visible Mass

Muon Channel

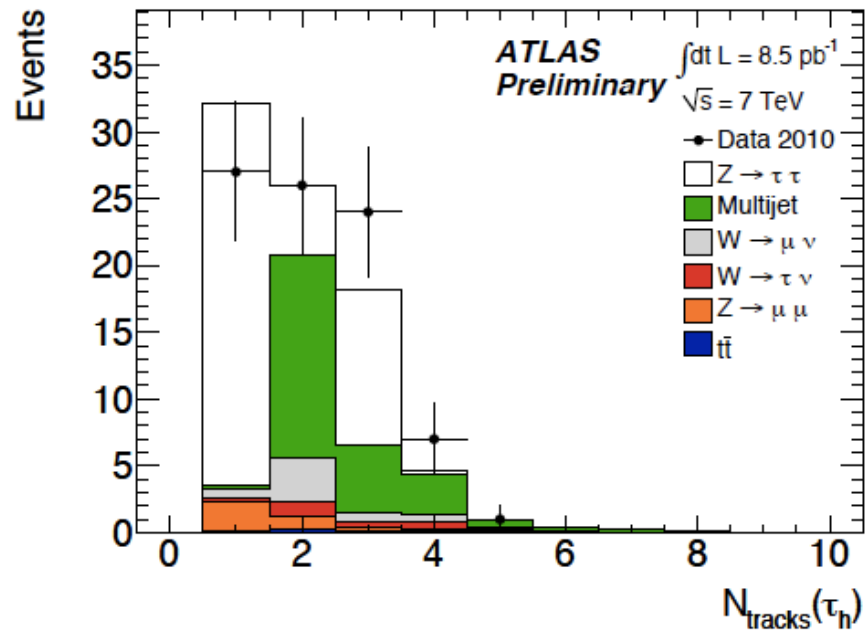


Electron Channel

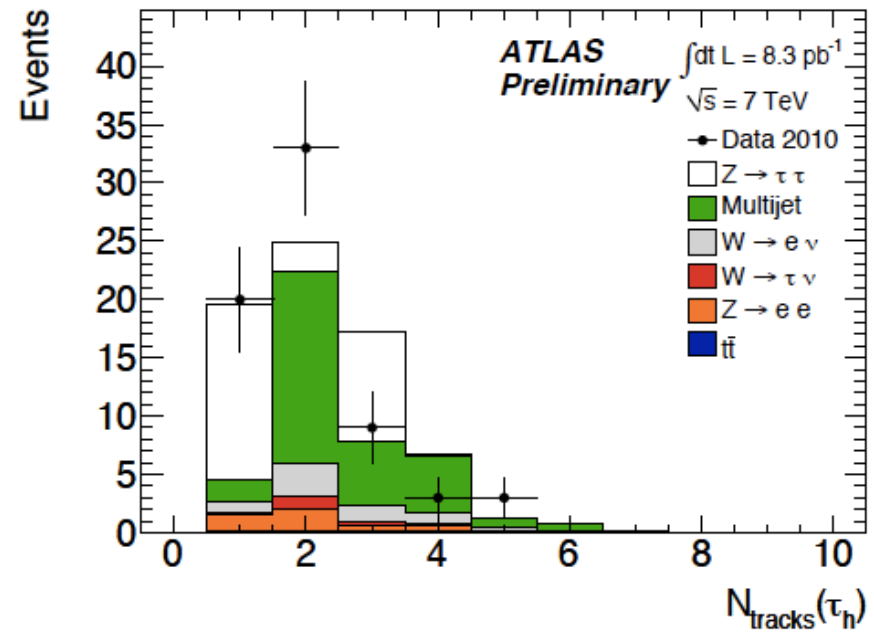


Z- $\rightarrow\tau\tau$ Track Multiplicity

Muon Channel



Electron Channel

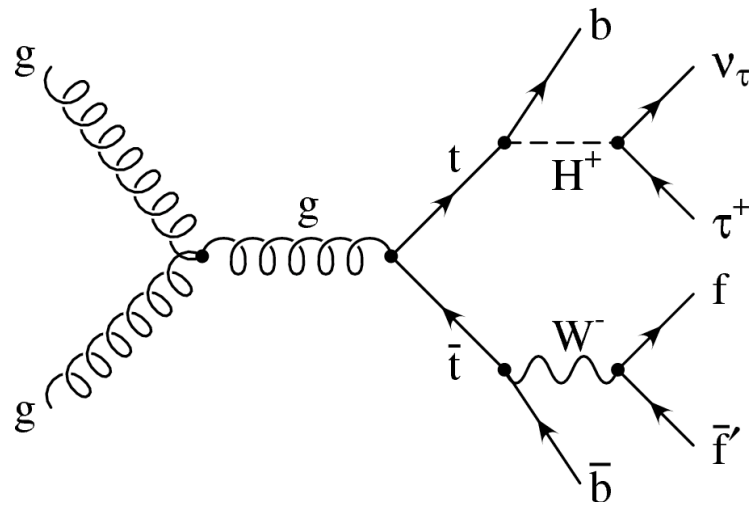


A Few Tau Channels

- $W^- \rightarrow \tau \nu$
 - Exercise the trigger and early tau ID
- $Z \rightarrow \tau \tau$
 - Important benchmark channel
 - Practice for the SM Higgs?
 - Use for efficiency calculations
- $H^\pm \rightarrow \tau \nu$
 - Hadronic tau decay mode
- MSSM $H \rightarrow \tau \tau$
 - One hadronic, one leptonic tau decay

$$H^+ \rightarrow \tau \nu$$

Data-driven estimation of the background to charged Higgs boson searches using hadronically-decaying tau final states in ATLAS

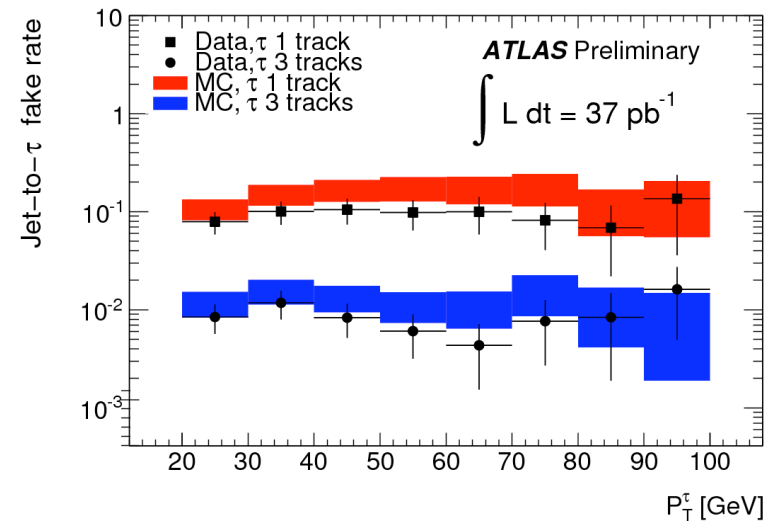
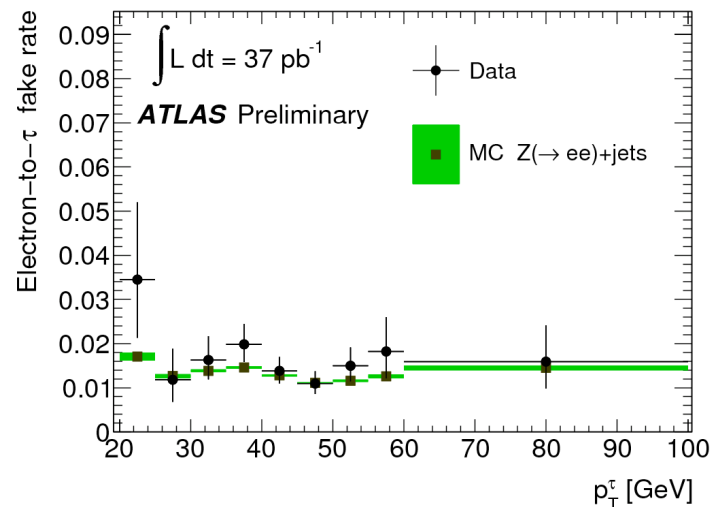


$$H^+ \rightarrow \tau \nu$$

- Event selection:
 - 1 lepton (trigger-matched)
 - 1 τ jet with $p_T > 20$ GeV (opposite charge to lepton)
 - ≥ 2 jets, at least one of them b-tagged
 - $E_T(\text{sum}) > 200$ GeV
 - $E_T(\text{miss}) > 200$ GeV

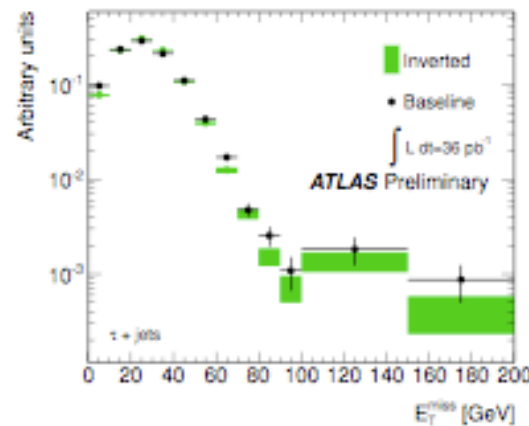
$H^+ \rightarrow \tau \nu$: Fake tau background

- Estimate of electron to tau fakes from $Z \rightarrow ee$ events
- Estimate of jet to tau fakes from $\gamma + \text{jet}$ events

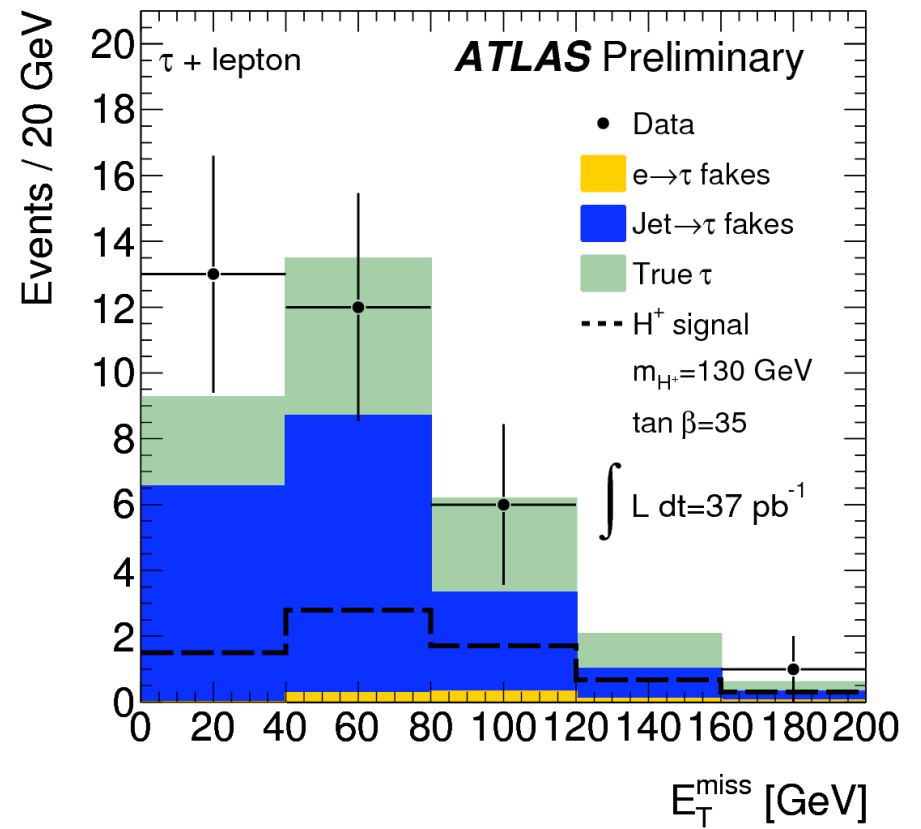
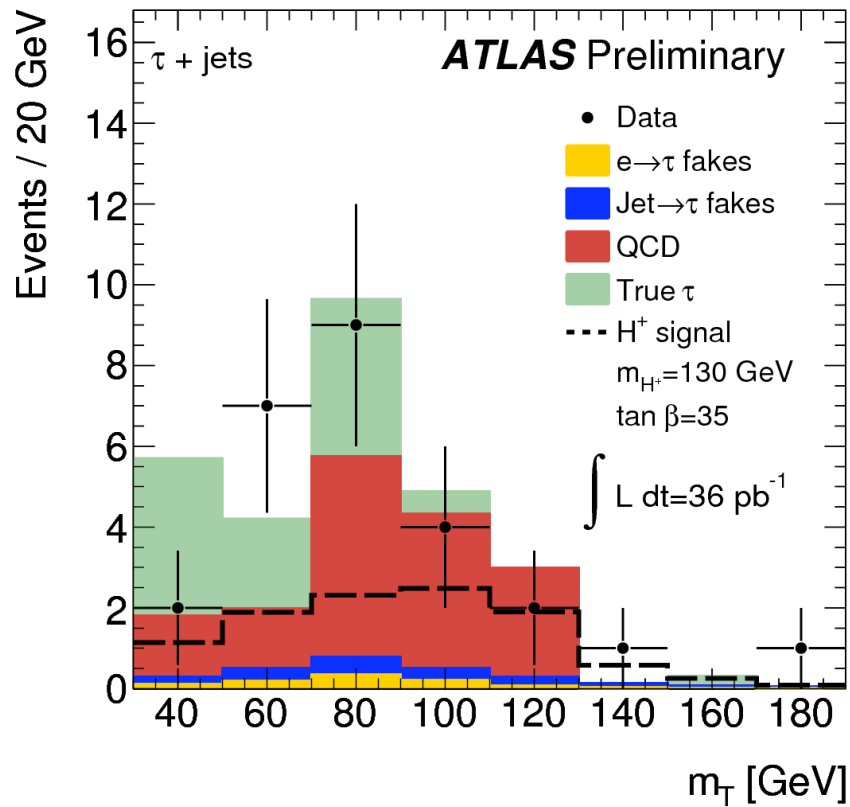


$H^+ \rightarrow \tau\nu$: QCD Background

- Assume the shape of the missing ET is the same in the signal region as it is in the “inverted” region
 - Require a loose tau, reject tight taus



$H^+ \rightarrow \tau \nu$



A Few Tau Channels

- $W^- \rightarrow \tau \nu$
 - Exercise the trigger and early tau ID
- $Z \rightarrow \tau \tau$
 - Important benchmark channel
 - Practice for the SM Higgs?
 - Use for efficiency calculations
- $H^\pm \rightarrow \tau \nu$
 - Hadronic tau decay mode
- **MSSM $H^- \rightarrow \tau \tau$**
 - One hadronic, one leptonic tau decay

MSSM $H \rightarrow \tau\tau$

- Trigger:
 - Electron $> 10 - 15$ GeV (depending on inst lumi)
 - Muon $> 10 - 13$ GeV
- One lepton
 - Electron > 20 GeV
 - Muon > 15 GeV
- Hadronic tau $p_T > 20$ GeV
- Opposite sign lepton and tau
- Missing $E_T > 20$ GeV
- Transverse mass of lepton + MET < 30 GeV

MSSM $H \rightarrow \tau\tau$

- QCD + W+Jets Background determination
 - Assume the shape of the visible mass ($t\bar{t}$) spectrum is the same for SS and OS events
 - The ratio of SS to OS events is the same in the signal region as it is in a QCD-enhanced BG region

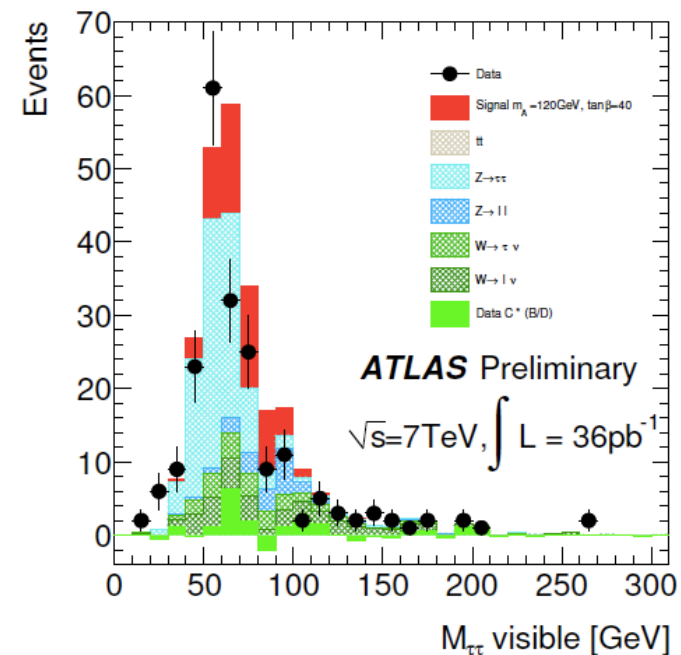
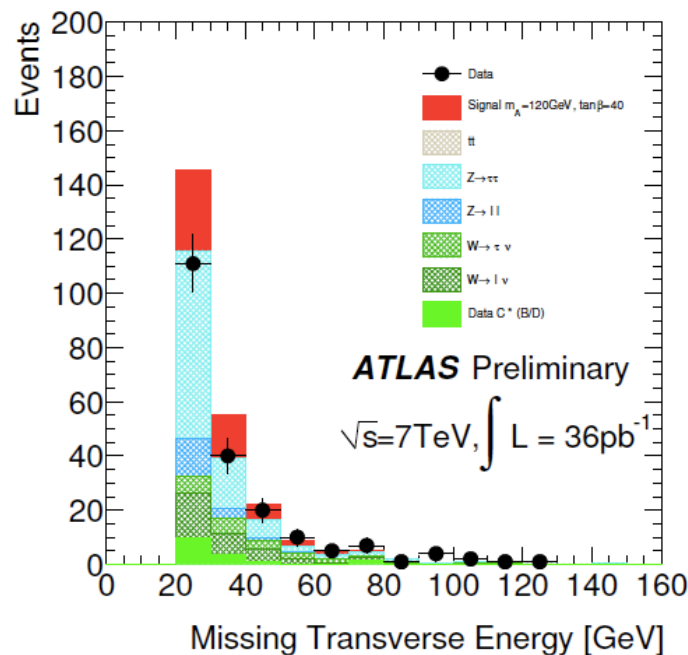
$$n_{OS}^{Bkg}(m_{vis}) = r_{QCD} \cdot n_{SS}^{QCD}(m_{vis}) + r_{W+jets} \cdot n_{SS}^{W+jets}(m_{vis}) + n_{OS}^{Z+jets}(m_{vis}) + n_{OS}^{other}(m_{vis})$$

MSSM $H \rightarrow \tau\tau$

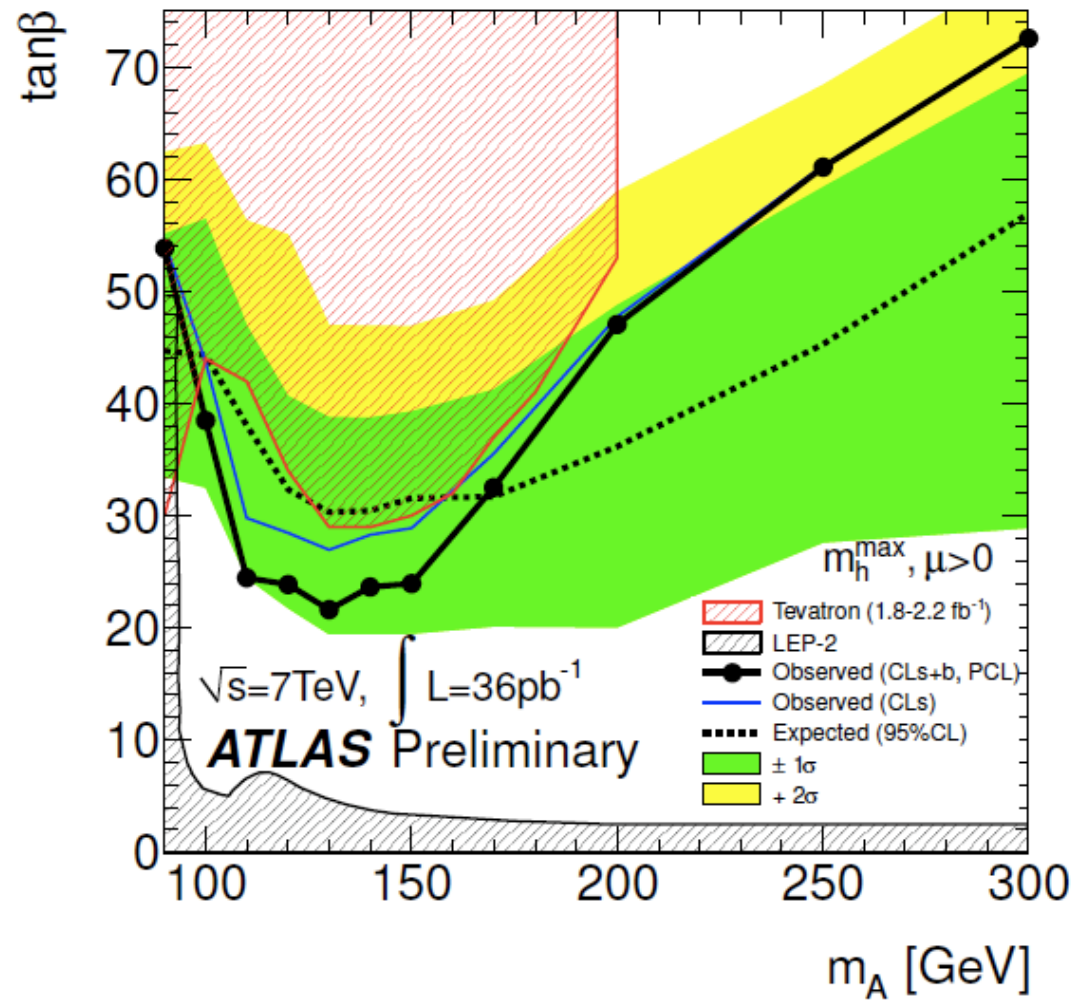
- Alternate QCD Background determination

| | Isolation | Inverted Isolation |
|----|------------------|--------------------|
| OS | Signal region A | Control region B |
| SS | Control region C | Control region D |

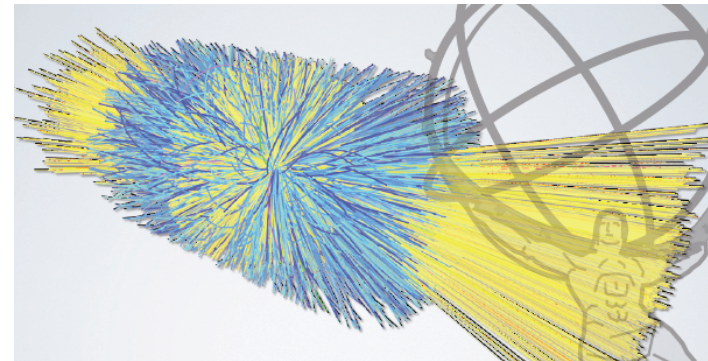
$$n_A^{QCD} = r_{B/D} \times (n_C^{data} - n_C^{non-QCD}) = 12.1 \pm 7.1$$



MSSM $H \rightarrow \tau\tau$



Future Plans



- Phase I possibilities
 - Topology information in the trigger at Level 1?
 - New small FCAL?
- Phase II possibilities
 - New Inner Detector
 - Digital Calorimeter Readout (increased granularity for trigger as well)
 - Track trigger
 - RoI based or self-seeded?
 - maybe with a Level 0 + Level1?
- Simulation studies are ongoing to understand the physics requirements under shifting detector conditions
 - Peak luminosity of $5E34$?
 - 50 ns bunch spacing?

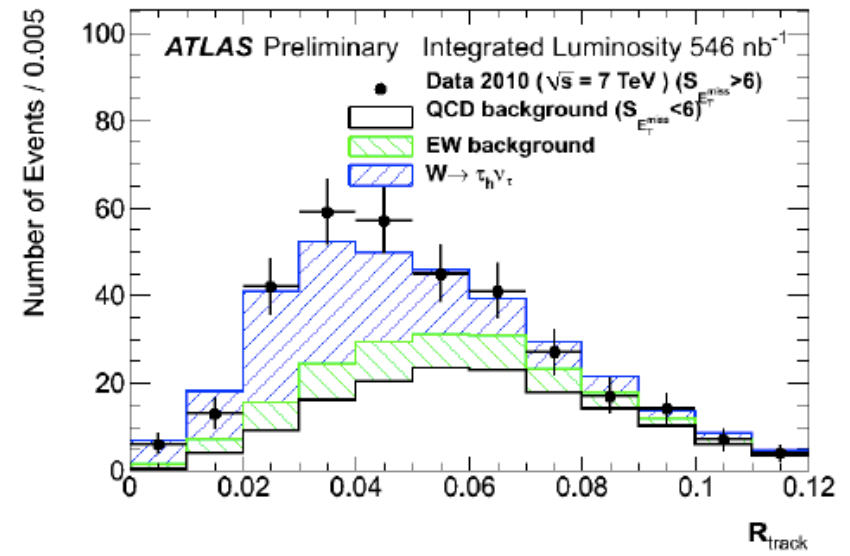
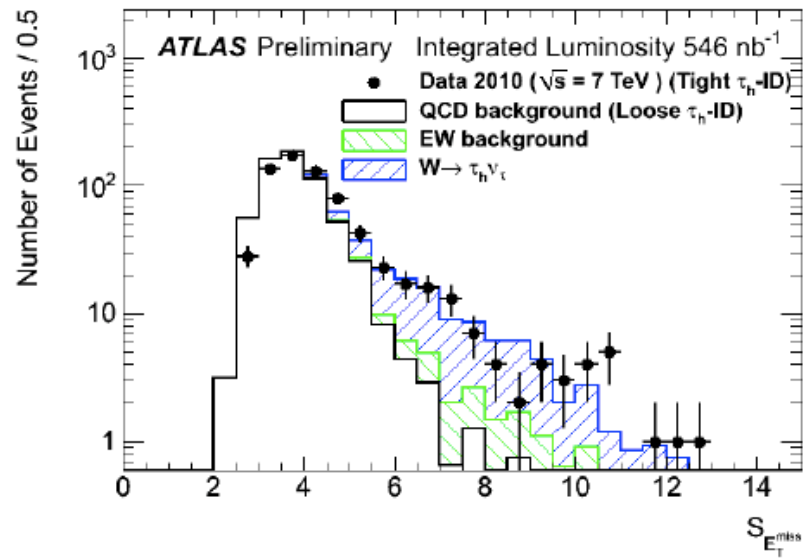
Back-up

Event Selection for tau ID variable

Data-MC Comparisons

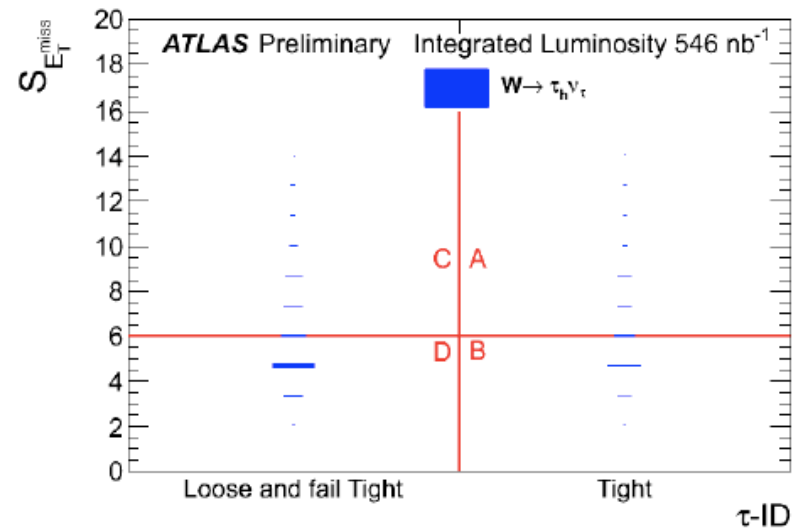
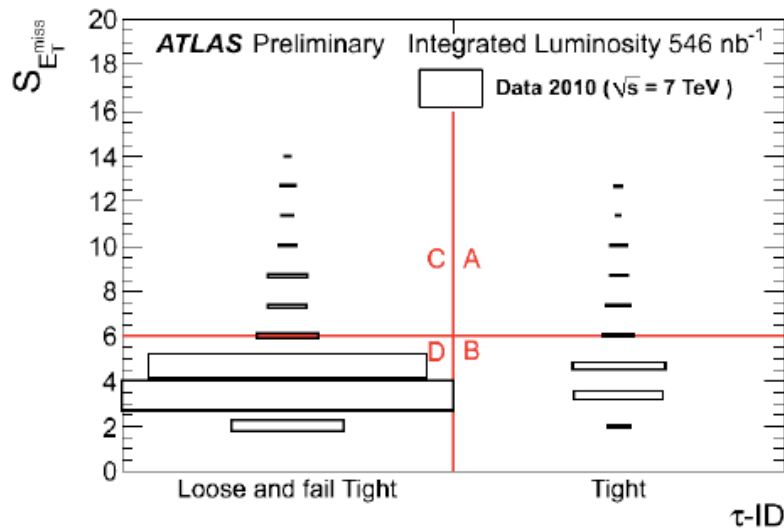
- The leading tau in the event is not included, to remove trigger bias
- the Level 1 trigger requiring a τ trigger object passing a 5 GeV threshold [3] is satisfied,
- there are no “bad” jets in the event [4] caused by out-of-time cosmic events or sporadic noise effects in the calorimeters,
- at least one vertex reconstructed with more than four tracks is present,
- at least one τ candidate with $p_T > 30$ GeV (fully calibrated, as described in Section 3) and $|\eta| < 2.5$, as well as another τ candidate with $p_T > 15$ GeV and $|\eta| < 2.5$ (also fully calibrated). The two candidates are required to be separated by at least 2.7 radians in azimuth (the angle in the plane transverse to the beam pipe).

$W \rightarrow \tau \nu$



W- \rightarrow $\tau\nu$: Estimating QCD Background from Data

$$N_{\text{QCD}}^{\text{A}} = N^{\text{B}} N^{\text{C}} / N^{\text{D}}$$



$$c_i = \frac{N_{\text{sig}}^i + N_{\text{EW}}^i}{N_{\text{sig}}^{\text{A}} + N_{\text{EW}}^{\text{A}}}, \quad i = \text{B, C, D}$$

| Region | A | B | C | D |
|-----------------------------------|----------------|-----------------|-----------------|-----------------|
| Data | 78 | 607 | 254 | 7107 |
| W \rightarrow $\tau_h \nu_\tau$ | 55.3 \pm 1.4 | 39.5 \pm 1.2 | 71.0 \pm 1.6 | 54.2 \pm 1.4 |
| EW | 11.8 \pm 0.4 | 6.5 \pm 0.2 | 44.5 \pm 0.7 | 22.1 \pm 0.5 |
| c_i | | 0.69 \pm 0.02 | 1.72 \pm 0.05 | 1.14 \pm 0.03 |

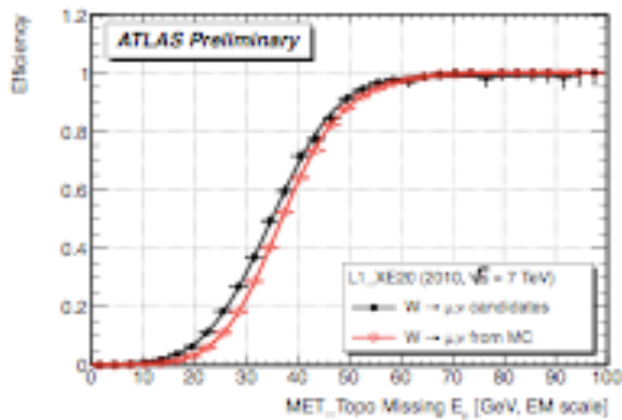
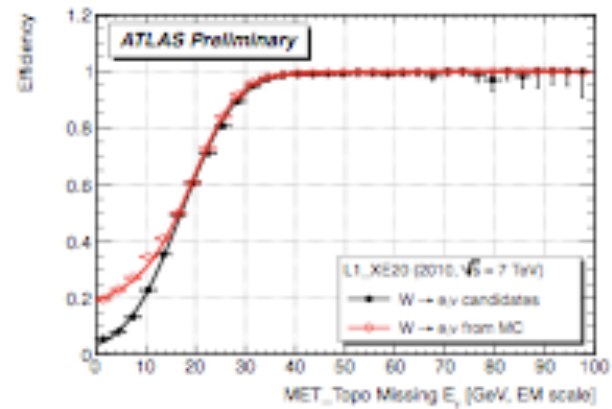
$W \rightarrow \tau \nu$: (Correct for Non-QCD in Control Regions)

$$N_{\text{QCD}}^{\text{A}} = (N^{\text{B}} - c_{\text{B}}(N^{\text{A}} - N_{\text{QCD}}^{\text{A}})) \frac{N^{\text{C}} - c_{\text{C}}(N^{\text{A}} - N_{\text{QCD}}^{\text{A}})}{N^{\text{D}} - c_{\text{D}}(N^{\text{A}} - N_{\text{QCD}}^{\text{A}})}$$

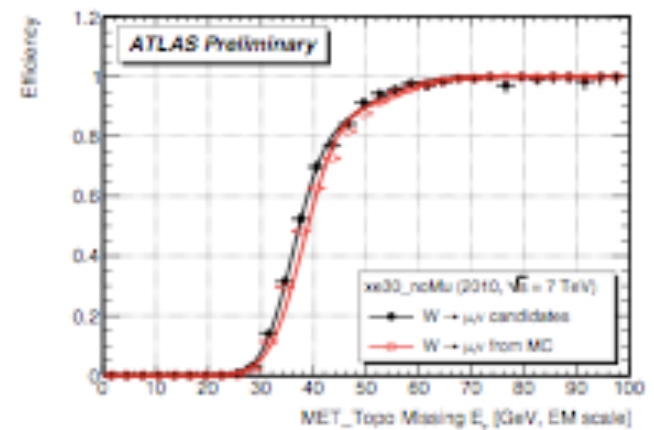
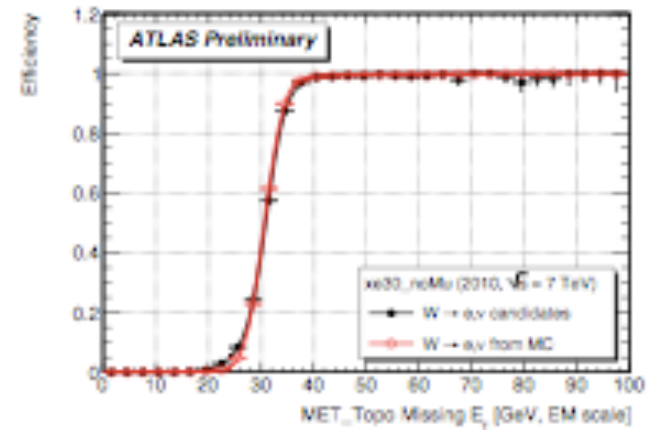
Estimated 11 QCD events in signal region (A)

Trigger Summary

L1 20 GeV threshold
efficiency from $W \rightarrow e\nu$ (top)
 $W \rightarrow \mu\nu$ (bottom) events



Event Filter Missing ET
turn-on curves – very sharp!



Z- \rightarrow $\tau\tau$ Systematics

| Systematic | Uncertainty | Multijets | W+jets | Z & $t\bar{t}$ | Z \rightarrow $\tau\tau$ |
|------------------------------------|--|------------------------------|-----------------|--------------------------|----------------------------|
| μ efficiency | 2.7% | $\pm 0.03^*$ | - | ± 0.07 | ± 1.1 |
| μ trigger efficiency | 2.0% | $\pm 0.01^*$ | - | ± 0.05 | ± 0.8 |
| μ isolation | 1.6% | $\pm 0.01^*$ | - | ± 0.04 | ± 0.7 |
| Jet τ fake rate | 50% | $\pm 0.17^*$ | - | ± 1.34 | - |
| Energy scale | 13% (W \rightarrow $\mu\nu$) / 16% (W \rightarrow $\tau\nu$) 6% (signal) / 13% (Z) / 21% ($t\bar{t}$) | $\pm 0.26^*$ | ± 0.28 | ± 0.40 | ± 2.4 |
| Pile-up re-weighting | 0.5% (signal) / 0.58% ($t\bar{t}$) 3.9% (Z) | $\pm 0.01^*$ | - | ± 0.10 | ± 0.2 |
| MC underlying event model | 7% | $\pm 0.04^*$ | - | - | ± 2.8 |
| MC showering model | 6% | $\pm 0.04^*$ | - | - | ± 2.4 |
| Luminosity | 11% | $\pm 0.07^*$ | - | ± 0.30 | ± 4.4 |
| Theoretical cross section | 5% (Z) 6% ($t\bar{t}$) | $\pm 0.03^*$ $\pm 0.01^*$ | - | ± 0.12 ± 0.02 | ± 2.0 - |
| W rescaling factor | 8.8% in A, B 2.1% in C, D | $\pm 0.04^*$ - | ± 0.17 - | - - | - - |
| Multijet est. (bkg subtraction) | - | ± 0.34 | - | - | - |
| Multijet est. (method systematics) | - | ± 0.56 | - | - | - |
| Total systematics | - | ± 0.66 | ± 0.33 | ± 1.44 | ± 6.7 |

Z- \rightarrow tt W+Jets Reduction

- Angular, sum > -0.15 :

$$\sum \cos \Delta\phi = \cos(\phi(\ell) - \phi(E_T^{\text{miss}})) + \cos(\phi(\tau_h) - \phi(E_T^{\text{miss}}))$$

- Transverse Mass < 50 GeV:

$$m_T(\ell, E_T^{\text{miss}}) = \sqrt{2 p_T(\ell) \cdot E_T^{\text{miss}} \cdot (1 - \cos \Delta\phi(\ell, E_T^{\text{miss}}))}$$